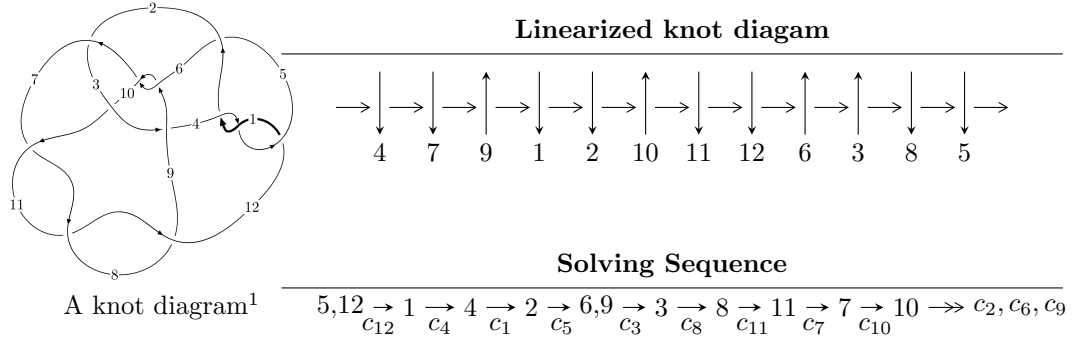


12a<sub>1064</sub> (K12a<sub>1064</sub>)



**Ideals for irreducible components<sup>2</sup> of  $X_{\text{par}}$**

$$I_1^u = \langle -2.52109 \times 10^{85} u^{82} + 8.64634 \times 10^{85} u^{81} + \dots + 1.02529 \times 10^{87} b + 1.52237 \times 10^{87}, \\ -1.47090 \times 10^{87} u^{82} - 1.63708 \times 10^{87} u^{81} + \dots + 1.02529 \times 10^{87} a - 7.79066 \times 10^{86}, u^{83} + u^{82} + \dots - 2u - \dots \rangle$$

\* 1 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 83 representations.

<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

I.

$$I_1^u = \langle -2.52 \times 10^{85} u^{82} + 8.65 \times 10^{85} u^{81} + \dots + 1.03 \times 10^{87} b + 1.52 \times 10^{87}, -1.47 \times 10^{87} u^{82} - 1.64 \times 10^{87} u^{81} + \dots + 1.03 \times 10^{87} a - 7.79 \times 10^{86}, u^{83} + u^{82} + \dots - 2u - 1 \rangle$$

(i) Arc colorings

$$a_5 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} u \\ u^3 + u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} u^2 + 1 \\ u^4 + 2u^2 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -u^5 - 2u^3 - u \\ -u^7 - 3u^5 - 2u^3 + u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1.43461u^{82} + 1.59669u^{81} + \dots - 48.1974u + 0.759849 \\ 0.0245891u^{82} - 0.0843305u^{81} + \dots - 0.539171u - 1.48482 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -3.85435u^{82} - 3.70576u^{81} + \dots + 12.1010u - 10.3867 \\ -0.109874u^{82} - 0.158192u^{81} + \dots + 6.49193u + 1.37180 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1.45920u^{82} + 1.51236u^{81} + \dots - 48.7366u - 0.724973 \\ 0.0245891u^{82} - 0.0843305u^{81} + \dots - 0.539171u - 1.48482 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1.57618u^{82} + 0.907236u^{81} + \dots - 69.1885u - 0.00842359 \\ -0.0277634u^{82} - 0.0657480u^{81} + \dots - 1.84911u - 2.19386 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -1.40639u^{82} - 1.36785u^{81} + \dots + 42.0418u - 2.35067 \\ 0.0598792u^{82} - 0.104829u^{81} + \dots + 2.65151u + 1.36301 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1.48382u^{82} + 1.56199u^{81} + \dots - 47.0880u + 0.730578 \\ 0.0160101u^{82} - 0.00198206u^{81} + \dots - 1.69531u - 1.51353 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes =  $3.75821u^{82} + 4.13643u^{81} + \dots - 2.88911u - 1.93224$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_4, c_{12}$	$u^{83} - u^{82} + \dots - 2u + 1$
$c_2$	$u^{83} - 3u^{82} + \dots - 8u - 97$
$c_3$	$u^{83} - u^{82} + \dots - 29240u - 5563$
$c_5$	$u^{83} + u^{82} + \dots + 9630u + 2689$
$c_6, c_9$	$u^{83} - u^{82} + \dots - 7u^2 + 1$
$c_7, c_8, c_{11}$	$u^{83} + 7u^{82} + \dots + 7u^2 - 1$
$c_{10}$	$u^{83} + 3u^{82} + \dots - 4u - 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_4, c_{12}$	$y^{83} + 71y^{82} + \dots - 102y - 1$
$c_2$	$y^{83} - 513y^{82} + \dots + 637742y - 9409$
$c_3$	$y^{83} - 533y^{82} + \dots + 2125110634y - 30946969$
$c_5$	$y^{83} - 29y^{82} + \dots - 827229158y - 7230721$
$c_6, c_9$	$y^{83} - 53y^{82} + \dots + 14y - 1$
$c_7, c_8, c_{11}$	$y^{83} - 85y^{82} + \dots + 14y - 1$
$c_{10}$	$y^{83} + 7y^{82} + \dots + 66y - 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.904665 + 0.431308I$ $a = 0.444111 - 0.833130I$ $b = 1.48483 + 0.03450I$	$-6.93263 - 2.69856I$	0
$u = 0.904665 - 0.431308I$ $a = 0.444111 + 0.833130I$ $b = 1.48483 - 0.03450I$	$-6.93263 + 2.69856I$	0
$u = -0.523171 + 0.935123I$ $a = 0.078517 - 0.193819I$ $b = -1.53601 - 0.20823I$	$-4.33446 - 7.80527I$	0
$u = -0.523171 - 0.935123I$ $a = 0.078517 + 0.193819I$ $b = -1.53601 + 0.20823I$	$-4.33446 + 7.80527I$	0
$u = 0.926387 + 0.043053I$ $a = -1.253500 + 0.168894I$ $b = -1.47810 - 0.00383I$	$-7.59406 - 0.00917I$	$-13.41457 + 0.I$
$u = 0.926387 - 0.043053I$ $a = -1.253500 - 0.168894I$ $b = -1.47810 + 0.00383I$	$-7.59406 + 0.00917I$	$-13.41457 + 0.I$
$u = -0.387244 + 0.823860I$ $a = -0.565051 - 0.405945I$ $b = 0.547345 + 0.608594I$	$2.54832 - 4.77196I$	$0. + 4.88934I$
$u = -0.387244 - 0.823860I$ $a = -0.565051 + 0.405945I$ $b = 0.547345 - 0.608594I$	$2.54832 + 4.77196I$	$0. - 4.88934I$
$u = -0.371273 + 1.048980I$ $a = -0.208988 + 0.342891I$ $b = 1.56520 + 0.18830I$	$-7.61151 - 2.62136I$	0
$u = -0.371273 - 1.048980I$ $a = -0.208988 - 0.342891I$ $b = 1.56520 - 0.18830I$	$-7.61151 + 2.62136I$	0

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.849324 + 0.250360I$ $a = -1.03559 - 1.28238I$ $b = -1.55846 + 0.25137I$	$-6.4541 + 12.6262I$	$-7.38891 - 7.59104I$
$u = -0.849324 - 0.250360I$ $a = -1.03559 + 1.28238I$ $b = -1.55846 - 0.25137I$	$-6.4541 - 12.6262I$	$-7.38891 + 7.59104I$
$u = 0.349735 + 1.067780I$ $a = -0.248736 - 0.432337I$ $b = 0.508066 + 0.276673I$	$1.92187 - 4.22604I$	0
$u = 0.349735 - 1.067780I$ $a = -0.248736 + 0.432337I$ $b = 0.508066 - 0.276673I$	$1.92187 + 4.22604I$	0
$u = -0.801322 + 0.161892I$ $a = 1.19606 + 1.08916I$ $b = 1.57257 - 0.25982I$	$-10.32350 + 6.88913I$	$-11.30755 - 5.10720I$
$u = -0.801322 - 0.161892I$ $a = 1.19606 - 1.08916I$ $b = 1.57257 + 0.25982I$	$-10.32350 - 6.88913I$	$-11.30755 + 5.10720I$
$u = 0.527206 + 0.622474I$ $a = -0.213152 - 0.852381I$ $b = 1.47354 + 0.06068I$	$-6.26479 - 2.24210I$	$-10.47377 + 2.86125I$
$u = 0.527206 - 0.622474I$ $a = -0.213152 + 0.852381I$ $b = 1.47354 - 0.06068I$	$-6.26479 + 2.24210I$	$-10.47377 - 2.86125I$
$u = 0.811237$ $a = 0.122702$ $b = 0.422769$	$-1.35401$	$-13.8280$
$u = -0.768502 + 0.243547I$ $a = 0.659044 + 0.689542I$ $b = 0.601985 - 0.744053I$	$0.63414 + 8.95004I$	$-4.61101 - 8.69193I$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.768502 - 0.243547I$		
$a = 0.659044 - 0.689542I$	$0.63414 - 8.95004I$	$-4.61101 + 8.69193I$
$b = 0.601985 + 0.744053I$		
$u = 0.609295 + 1.049720I$		
$a = -0.073062 + 0.756246I$	$-4.55776 - 5.42713I$	0
$b = -1.48758 - 0.06918I$		
$u = 0.609295 - 1.049720I$		
$a = -0.073062 - 0.756246I$	$-4.55776 + 5.42713I$	0
$b = -1.48758 + 0.06918I$		
$u = 0.699140 + 0.354524I$		
$a = 0.157935 + 0.565146I$	$-0.61000 - 2.03869I$	$-10.08458 + 9.40265I$
$b = -0.436838 - 0.172780I$		
$u = 0.699140 - 0.354524I$		
$a = 0.157935 - 0.565146I$	$-0.61000 + 2.03869I$	$-10.08458 - 9.40265I$
$b = -0.436838 + 0.172780I$		
$u = -0.193772 + 1.213450I$		
$a = 1.038160 + 0.359525I$	$0.236787 + 0.202779I$	0
$b = -0.911881 - 0.647788I$		
$u = -0.193772 - 1.213450I$		
$a = 1.038160 - 0.359525I$	$0.236787 - 0.202779I$	0
$b = -0.911881 + 0.647788I$		
$u = -0.110659 + 1.233990I$		
$a = 0.64968 + 1.57490I$	$3.83261 - 1.11879I$	0
$b = 0.062828 - 0.831522I$		
$u = -0.110659 - 1.233990I$		
$a = 0.64968 - 1.57490I$	$3.83261 + 1.11879I$	0
$b = 0.062828 + 0.831522I$		
$u = 0.027460 + 1.239750I$		
$a = 1.23418 - 1.00702I$	$0.784753 + 0.015689I$	0
$b = -1.077100 + 0.037871I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.027460 - 1.239750I$ $a = 1.23418 + 1.00702I$ $b = -1.077100 - 0.037871I$	$0.784753 - 0.015689I$	0
$u = 0.162835 + 1.275350I$ $a = 0.33304 + 1.70965I$ $b = -0.007261 - 0.443486I$	$3.90089 - 2.03788I$	0
$u = 0.162835 - 1.275350I$ $a = 0.33304 - 1.70965I$ $b = -0.007261 + 0.443486I$	$3.90089 + 2.03788I$	0
$u = -0.235341 + 1.264360I$ $a = 0.743300 - 0.777633I$ $b = -1.74342 - 0.20507I$	$-1.71143 + 2.17576I$	0
$u = -0.235341 - 1.264360I$ $a = 0.743300 + 0.777633I$ $b = -1.74342 + 0.20507I$	$-1.71143 - 2.17576I$	0
$u = -0.679568 + 0.099033I$ $a = -0.715170 - 0.353529I$ $b = -0.663430 + 0.819395I$	$-3.02457 + 2.97739I$	$-11.4522 - 8.4957I$
$u = -0.679568 - 0.099033I$ $a = -0.715170 + 0.353529I$ $b = -0.663430 - 0.819395I$	$-3.02457 - 2.97739I$	$-11.4522 + 8.4957I$
$u = -0.660019 + 0.182223I$ $a = 0.061412 - 0.133999I$ $b = 0.437248 + 0.838716I$	$1.14107 + 3.77675I$	$-4.42430 - 6.83951I$
$u = -0.660019 - 0.182223I$ $a = 0.061412 + 0.133999I$ $b = 0.437248 - 0.838716I$	$1.14107 - 3.77675I$	$-4.42430 + 6.83951I$
$u = -0.261761 + 1.299130I$ $a = 0.45969 - 2.13143I$ $b = -1.59789 + 0.43691I$	$-1.29190 + 4.37029I$	0



Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.261761 - 1.299130I$ $a = 0.45969 + 2.13143I$ $b = -1.59789 - 0.43691I$	$-1.29190 - 4.37029I$	0
$u = 0.219448 + 1.308160I$ $a = 2.73510 - 11.43200I$ $b = 1.41994 + 0.01827I$	$-0.27613 - 2.86489I$	0
$u = 0.219448 - 1.308160I$ $a = 2.73510 + 11.43200I$ $b = 1.41994 - 0.01827I$	$-0.27613 + 2.86489I$	0
$u = 0.259628 + 1.304990I$ $a = 0.360641 - 0.794383I$ $b = 0.334600 + 0.235718I$	$2.59124 - 3.33493I$	0
$u = 0.259628 - 1.304990I$ $a = 0.360641 + 0.794383I$ $b = 0.334600 - 0.235718I$	$2.59124 + 3.33493I$	0
$u = 0.665599$ $a = 0.644909$ $b = 0.324269$	$-1.54000$	$-7.43950$
$u = -0.658981 + 0.038729I$ $a = -1.62674 - 0.57595I$ $b = -1.64085 + 0.31051I$	$-5.47873 + 1.02972I$	$-17.8027 - 5.9458I$
$u = -0.658981 - 0.038729I$ $a = -1.62674 + 0.57595I$ $b = -1.64085 - 0.31051I$	$-5.47873 - 1.02972I$	$-17.8027 + 5.9458I$
$u = -0.276913 + 1.324360I$ $a = -0.40863 - 1.80806I$ $b = -0.573341 + 0.956974I$	$1.44716 + 6.45467I$	0
$u = -0.276913 - 1.324360I$ $a = -0.40863 + 1.80806I$ $b = -0.573341 - 0.956974I$	$1.44716 - 6.45467I$	0

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.364043 + 1.314560I$ $a = -0.16640 + 1.51924I$ $b = -1.46030 - 0.07333I$	$-3.32542 - 4.47511I$	0
$u = 0.364043 - 1.314560I$ $a = -0.16640 - 1.51924I$ $b = -1.46030 + 0.07333I$	$-3.32542 + 4.47511I$	0
$u = 0.227692 + 1.349670I$ $a = -0.67339 - 1.41304I$ $b = -0.310421 + 0.278426I$	$5.03483 - 3.41427I$	0
$u = 0.227692 - 1.349670I$ $a = -0.67339 + 1.41304I$ $b = -0.310421 - 0.278426I$	$5.03483 + 3.41427I$	0
$u = -0.272805 + 1.364300I$ $a = -0.911810 - 0.993141I$ $b = 0.551748 + 0.917797I$	$6.03553 + 7.19350I$	0
$u = -0.272805 - 1.364300I$ $a = -0.911810 + 0.993141I$ $b = 0.551748 - 0.917797I$	$6.03553 - 7.19350I$	0
$u = -0.092196 + 1.389330I$ $a = -0.06722 + 1.61828I$ $b = 0.803073 - 0.549130I$	$8.45681 + 0.24363I$	0
$u = -0.092196 - 1.389330I$ $a = -0.06722 - 1.61828I$ $b = 0.803073 + 0.549130I$	$8.45681 - 0.24363I$	0
$u = 0.101162 + 1.394370I$ $a = -1.84470 - 0.66191I$ $b = 1.340300 + 0.132764I$	$0.07406 - 4.01812I$	0
$u = 0.101162 - 1.394370I$ $a = -1.84470 + 0.66191I$ $b = 1.340300 - 0.132764I$	$0.07406 + 4.01812I$	0

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.337682 + 1.362540I$ $a = -0.37629 + 2.05946I$ $b = 1.56580 - 0.31162I$	$-5.51432 + 10.99590I$	0
$u = -0.337682 - 1.362540I$ $a = -0.37629 - 2.05946I$ $b = 1.56580 + 0.31162I$	$-5.51432 - 10.99590I$	0
$u = 0.574728 + 0.106362I$ $a = -0.33938 - 2.36609I$ $b = -0.116893 + 0.292931I$	$0.395479 - 0.483381I$	$4.40966 - 13.36233I$
$u = 0.574728 - 0.106362I$ $a = -0.33938 + 2.36609I$ $b = -0.116893 - 0.292931I$	$0.395479 + 0.483381I$	$4.40966 + 13.36233I$
$u = 0.575433$ $a = 27.0401$ $b = 1.42241$	$-4.41961$	257.880
$u = -0.31415 + 1.39980I$ $a = 0.30356 + 1.69619I$ $b = 0.589076 - 0.824484I$	$5.85194 + 12.87300I$	0
$u = -0.31415 - 1.39980I$ $a = 0.30356 - 1.69619I$ $b = 0.589076 + 0.824484I$	$5.85194 - 12.87300I$	0
$u = -0.35115 + 1.41539I$ $a = 0.36276 - 2.03460I$ $b = -1.56117 + 0.28469I$	$-1.1644 + 16.9553I$	0
$u = -0.35115 - 1.41539I$ $a = 0.36276 + 2.03460I$ $b = -1.56117 - 0.28469I$	$-1.1644 - 16.9553I$	0
$u = 0.30034 + 1.43004I$ $a = 0.126466 + 0.985341I$ $b = -0.369330 - 0.393419I$	$5.05592 - 5.76330I$	0

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.30034 - 1.43004I$ $a = 0.126466 - 0.985341I$ $b = -0.369330 + 0.393419I$	$5.05592 + 5.76330I$	0
$u = -0.02030 + 1.47331I$ $a = -0.512899 - 1.238070I$ $b = 0.295028 + 0.672756I$	$9.93674 - 3.97534I$	0
$u = -0.02030 - 1.47331I$ $a = -0.512899 + 1.238070I$ $b = 0.295028 - 0.672756I$	$9.93674 + 3.97534I$	0
$u = -0.199566 + 0.452923I$ $a = 1.24239 + 1.62287I$ $b = 0.461828 - 0.484933I$	$2.79973 - 0.93314I$	$1.18279 - 2.17360I$
$u = -0.199566 - 0.452923I$ $a = 1.24239 - 1.62287I$ $b = 0.461828 + 0.484933I$	$2.79973 + 0.93314I$	$1.18279 + 2.17360I$
$u = 0.39359 + 1.47783I$ $a = -0.439946 - 1.227010I$ $b = 1.46110 + 0.10369I$	$-0.91436 - 7.48576I$	0
$u = 0.39359 - 1.47783I$ $a = -0.439946 + 1.227010I$ $b = 1.46110 - 0.10369I$	$-0.91436 + 7.48576I$	0
$u = 0.04543 + 1.54868I$ $a = 1.134650 + 0.625371I$ $b = -1.41362 - 0.19449I$	$4.49350 - 7.02190I$	0
$u = 0.04543 - 1.54868I$ $a = 1.134650 - 0.625371I$ $b = -1.41362 + 0.19449I$	$4.49350 + 7.02190I$	0
$u = 0.158913 + 0.328968I$ $a = 0.938978 + 0.786692I$ $b = -0.332746 - 0.347602I$	$-0.233005 - 0.980237I$	$-4.40622 + 6.53050I$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.158913 - 0.328968I$		
$a = 0.938978 - 0.786692I$	$-0.233005 + 0.980237I$	$-4.40622 - 6.53050I$
$b = -0.332746 + 0.347602I$		
$u = -0.012139 + 0.141810I$		
$a = 2.01713 - 6.48316I$	$-3.17129 - 0.11870I$	$-1.99127 - 1.49453I$
$b = -1.384180 - 0.065251I$		
$u = -0.012139 - 0.141810I$		
$a = 2.01713 + 6.48316I$	$-3.17129 + 0.11870I$	$-1.99127 + 1.49453I$
$b = -1.384180 + 0.065251I$		

## II. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1, c_4, c_{12}$	$u^{83} - u^{82} + \dots - 2u + 1$
$c_2$	$u^{83} - 3u^{82} + \dots - 8u - 97$
$c_3$	$u^{83} - u^{82} + \dots - 29240u - 5563$
$c_5$	$u^{83} + u^{82} + \dots + 9630u + 2689$
$c_6, c_9$	$u^{83} - u^{82} + \dots - 7u^2 + 1$
$c_7, c_8, c_{11}$	$u^{83} + 7u^{82} + \dots + 7u^2 - 1$
$c_{10}$	$u^{83} + 3u^{82} + \dots - 4u - 1$

### III. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1, c_4, c_{12}$	$y^{83} + 71y^{82} + \dots - 102y - 1$
$c_2$	$y^{83} - 513y^{82} + \dots + 637742y - 9409$
$c_3$	$y^{83} - 533y^{82} + \dots + 2125110634y - 30946969$
$c_5$	$y^{83} - 29y^{82} + \dots - 827229158y - 7230721$
$c_6, c_9$	$y^{83} - 53y^{82} + \dots + 14y - 1$
$c_7, c_8, c_{11}$	$y^{83} - 85y^{82} + \dots + 14y - 1$
$c_{10}$	$y^{83} + 7y^{82} + \dots + 66y - 1$