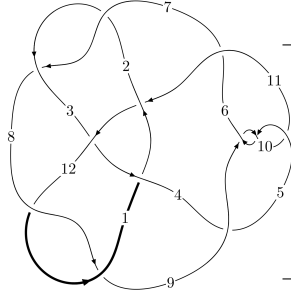
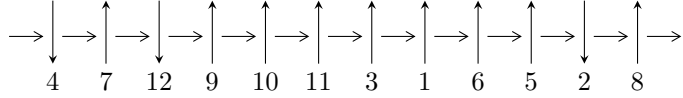


12a<sub>1115</sub> (K12a<sub>1115</sub>)



A knot diagram<sup>1</sup>

**Linearized knot diagram**



**Solving Sequence**

$$6,9 \xrightarrow{c_9} 10 \xrightarrow{c_5} 5 \xrightarrow{c_{10}} 11 \xrightarrow{c_6} 7 \xrightarrow{c_4} 1,4 \xrightarrow{c_1} 2 \xrightarrow{c_8} 8 \xrightarrow{c_{12}} 12 \xrightarrow{c_3} 3 \twoheadrightarrow c_2, c_7, c_{11}$$

**Ideals for irreducible components<sup>2</sup> of  $X_{\text{par}}$**

$$I_1^u = \langle 15u^{35} + 68u^{34} + \dots + 2b - 38, -9u^{35} - 36u^{34} + \dots + 4a + 72, u^{36} + 6u^{35} + \dots - 10u - 4 \rangle$$

$$I_2^u = \langle -415484u^5a^3 + 374659u^5a^2 + \dots + 1141045a + 3493341, u^5a^3 - u^5a^2 + \dots - 62a + 184, u^6 + 3u^4 + u^3 + 2u^2 + 2u - 1 \rangle$$

$$I_3^u = \langle u^{16} + u^{15} + \dots + b + 2, -2u^{17} - 2u^{16} + \dots + a - 2, u^{18} + u^{17} + \dots + 2u + 1 \rangle$$

$$I_4^u = \langle -352079058u^9a^3 - 279641663u^9a^2 + \dots + 597636419a - 889033224, 2u^9a^3 + 3u^9a^2 + \dots + 2a + 4, u^{10} - u^9 + 4u^8 - 4u^7 + 6u^6 - 6u^5 + 3u^4 - 3u^3 + 1 \rangle$$

\* 4 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 118 representations.

<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\mathbf{I. } I_1^u = \langle 15u^{35} + 68u^{34} + \dots + 2b - 38, -9u^{35} - 36u^{34} + \dots + 4a + 72, u^{36} + 6u^{35} + \dots - 10u - 4 \rangle$$

(i) Arc colorings

$$a_6 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -u \\ u^3 + u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} u^2 + 1 \\ -u^4 - 2u^2 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} u^5 + 2u^3 + u \\ -u^7 - 3u^5 - 2u^3 + u \end{pmatrix}$$

$$a_1 = \begin{pmatrix} \frac{9}{4}u^{35} + 9u^{34} + \dots - \frac{79}{4}u - 18 \\ -\frac{15}{2}u^{35} - 34u^{34} + \dots + \frac{41}{2}u + 19 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -u^3 - 2u \\ u^3 + u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} \frac{49}{4}u^{35} + 56u^{34} + \dots - \frac{247}{4}u - 66 \\ -\frac{35}{2}u^{35} - 84u^{34} + \dots + \frac{113}{2}u + 49 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -4u^{35} - \frac{43}{2}u^{34} + \dots + 25u + \frac{27}{2} \\ \frac{5}{2}u^{35} + 15u^{34} + \dots - \frac{57}{2}u - 18 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} \frac{7}{2}u^{35} + \frac{33}{2}u^{34} + \dots - \frac{43}{2}u - \frac{45}{2} \\ -\frac{9}{2}u^{35} - 21u^{34} + \dots + \frac{23}{2}u + 14 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} \frac{1}{4}u^{35} + 3u^{34} + \dots - \frac{31}{4}u - 8 \\ \frac{1}{2}u^{35} + u^{34} + \dots - \frac{3}{2}u + 3 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes =  $13u^{35} + 78u^{34} + \dots - 156u - 78$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_{11}$	$u^{36} + 3u^{35} + \dots + 10u - 1$
$c_2, c_7, c_8$ $c_{12}$	$u^{36} + u^{35} + \dots - 4u^2 + 1$
$c_3$	$u^{36} + 36u^{35} + \dots - 851968u - 65536$
$c_4, c_6$	$u^{36} + 6u^{35} + \dots - 3456u - 712$
$c_5, c_9, c_{10}$	$u^{36} - 6u^{35} + \dots + 10u - 4$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_{11}$	$y^{36} + 13y^{35} + \dots - 108y + 1$
$c_2, c_7, c_8$ $c_{12}$	$y^{36} - 31y^{35} + \dots - 8y + 1$
$c_3$	$y^{36} + 8y^{35} + \dots - 81604378624y + 4294967296$
$c_4, c_6$	$y^{36} - 26y^{35} + \dots - 1429120y + 506944$
$c_5, c_9, c_{10}$	$y^{36} + 30y^{35} + \dots - 108y + 16$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.918601 + 0.135473I$ $a = -2.16683 - 0.71703I$ $b = 1.310650 - 0.016930I$	$11.86120 - 2.65850I$	$16.0062 + 3.1622I$
$u = -0.918601 - 0.135473I$ $a = -2.16683 + 0.71703I$ $b = 1.310650 + 0.016930I$	$11.86120 + 2.65850I$	$16.0062 - 3.1622I$
$u = -0.886777 + 0.100899I$ $a = 2.80734 + 0.39802I$ $b = -1.51502 + 0.47144I$	$13.5026 - 12.5111I$	$13.4715 + 6.4902I$
$u = -0.886777 - 0.100899I$ $a = 2.80734 - 0.39802I$ $b = -1.51502 - 0.47144I$	$13.5026 + 12.5111I$	$13.4715 - 6.4902I$
$u = 0.582328 + 0.632591I$ $a = 1.065630 - 0.902416I$ $b = -1.302410 + 0.256154I$	$6.20237 - 3.57524I$	$13.30271 + 2.91674I$
$u = 0.582328 - 0.632591I$ $a = 1.065630 + 0.902416I$ $b = -1.302410 - 0.256154I$	$6.20237 + 3.57524I$	$13.30271 - 2.91674I$
$u = -0.805953 + 0.027041I$ $a = -0.345526 + 0.596121I$ $b = 0.024838 - 0.844400I$	$3.39332 - 2.17431I$	$8.53831 + 3.28500I$
$u = -0.805953 - 0.027041I$ $a = -0.345526 - 0.596121I$ $b = 0.024838 + 0.844400I$	$3.39332 + 2.17431I$	$8.53831 - 3.28500I$
$u = 0.642311 + 0.449784I$ $a = -1.75182 + 0.80743I$ $b = 1.347300 + 0.355724I$	$6.72630 + 7.92579I$	$12.1583 - 8.1491I$
$u = 0.642311 - 0.449784I$ $a = -1.75182 - 0.80743I$ $b = 1.347300 - 0.355724I$	$6.72630 - 7.92579I$	$12.1583 + 8.1491I$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.501660 + 1.136970I$ $a = 1.286290 + 0.341993I$ $b = -1.326480 + 0.043785I$	$8.78940 - 2.36934I$	$14.1647 + 0.I$
$u = -0.501660 - 1.136970I$ $a = 1.286290 - 0.341993I$ $b = -1.326480 - 0.043785I$	$8.78940 + 2.36934I$	$14.1647 + 0.I$
$u = -0.452030 + 1.175710I$ $a = -1.302930 - 0.542898I$ $b = 1.50606 + 0.43598I$	$10.20350 + 7.73445I$	0
$u = -0.452030 - 1.175710I$ $a = -1.302930 + 0.542898I$ $b = 1.50606 - 0.43598I$	$10.20350 - 7.73445I$	0
$u = -0.084827 + 1.288850I$ $a = -0.259022 - 0.468223I$ $b = 0.470070 - 0.345741I$	$-3.34519 - 1.63537I$	0
$u = -0.084827 - 1.288850I$ $a = -0.259022 + 0.468223I$ $b = 0.470070 + 0.345741I$	$-3.34519 + 1.63537I$	0
$u = 0.235443 + 1.273080I$ $a = -1.35454 + 1.10271I$ $b = 0.631652 + 0.250784I$	$-4.21138 + 3.05086I$	0
$u = 0.235443 - 1.273080I$ $a = -1.35454 - 1.10271I$ $b = 0.631652 - 0.250784I$	$-4.21138 - 3.05086I$	0
$u = -0.349327 + 1.249240I$ $a = -0.335653 - 0.135529I$ $b = -0.108783 - 0.819825I$	$-0.38230 - 1.98485I$	0
$u = -0.349327 - 1.249240I$ $a = -0.335653 + 0.135529I$ $b = -0.108783 + 0.819825I$	$-0.38230 + 1.98485I$	0

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.071803 + 1.298360I$ $a = -0.143695 + 1.377620I$ $b = -0.296292 + 0.618271I$	$-5.96094 + 1.93016I$	0
$u = 0.071803 - 1.298360I$ $a = -0.143695 - 1.377620I$ $b = -0.296292 - 0.618271I$	$-5.96094 - 1.93016I$	0
$u = -0.358553 + 1.289720I$ $a = 0.899152 + 0.306766I$ $b = 0.043249 + 0.867682I$	$-0.71095 - 6.36900I$	0
$u = -0.358553 - 1.289720I$ $a = 0.899152 - 0.306766I$ $b = 0.043249 - 0.867682I$	$-0.71095 + 6.36900I$	0
$u = 0.610254$ $a = 2.40590$ $b = -0.572689$	$-0.250744$	18.0910
$u = -0.399118 + 1.345260I$ $a = -1.62048 - 1.69722I$ $b = 1.51341 - 0.49950I$	$8.9652 - 17.1215I$	0
$u = -0.399118 - 1.345260I$ $a = -1.62048 + 1.69722I$ $b = 1.51341 + 0.49950I$	$8.9652 + 17.1215I$	0
$u = 0.18895 + 1.40967I$ $a = 0.307536 - 1.289560I$ $b = -1.319040 - 0.457572I$	$0.76991 + 10.74510I$	0
$u = 0.18895 - 1.40967I$ $a = 0.307536 + 1.289560I$ $b = -1.319040 + 0.457572I$	$0.76991 - 10.74510I$	0
$u = -0.41508 + 1.37015I$ $a = 1.04177 + 1.33272I$ $b = -1.284840 + 0.058721I$	$7.13077 - 7.43744I$	0

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.41508 - 1.37015I$ $a = 1.04177 - 1.33272I$ $b = -1.284840 - 0.058721I$	$7.13077 + 7.43744I$	0
$u = 0.09158 + 1.50603I$ $a = 0.067556 + 0.267829I$ $b = 1.171500 - 0.194024I$	$-0.95947 - 1.45291I$	0
$u = 0.09158 - 1.50603I$ $a = 0.067556 - 0.267829I$ $b = 1.171500 + 0.194024I$	$-0.95947 + 1.45291I$	0
$u = -0.389978$ $a = 0.839038$ $b = -0.338534$	0.631815	16.0810
$u = 0.249379 + 0.255614I$ $a = 0.432749 - 1.105430I$ $b = 0.089749 - 0.497899I$	$-1.30214 + 0.83943I$	$-2.00109 - 3.97156I$
$u = 0.249379 - 0.255614I$ $a = 0.432749 + 1.105430I$ $b = 0.089749 + 0.497899I$	$-1.30214 - 0.83943I$	$-2.00109 + 3.97156I$



$$\text{II. } I_2^u = \langle -4.15 \times 10^5 a^3 u^5 + 3.75 \times 10^5 a^2 u^5 + \cdots + 1.14 \times 10^6 a + 3.49 \times 10^6, u^5 a^3 - u^5 a^2 + \cdots - 62a + 184, u^6 + 3u^4 + u^3 + 2u^2 + 2u - 1 \rangle$$

(i) Arc colorings

$$a_6 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -u \\ u^3 + u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} u^2 + 1 \\ -u^4 - 2u^2 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} u^5 + 2u^3 + u \\ u^4 + 2u^2 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} a \\ 0.126898a^3 u^5 - 0.114429a^2 u^5 + \cdots - 0.348501a - 1.06694 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -u^3 - 2u \\ u^3 + u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -0.00312508a^3 u^5 + 0.0678169a^2 u^5 + \cdots + 0.727219a + 1.00927 \\ 0.190720a^3 u^5 - 0.341686a^2 u^5 + \cdots + 0.335179a - 1.84361 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -0.140638a^3 u^5 - 0.166994a^2 u^5 + \cdots + 0.0966799a - 1.53356 \\ -0.221029a^3 u^5 - 0.473050a^2 u^5 + \cdots - 0.397307a + 1.62574 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 0.250573a^3 u^5 + 0.178839a^2 u^5 + \cdots + 0.777234a - 3.90996 \\ 0.447730a^3 u^5 - 0.0123159a^2 u^5 + \cdots - 0.381117a + 2.65314 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -0.423110a^3 u^5 - 0.178982a^2 u^5 + \cdots - 0.0812311a + 1.15365 \\ 0.0741663a^3 u^5 - 0.382732a^2 u^5 + \cdots + 0.0906915a - 1.83998 \end{pmatrix}$$

(ii) Obstruction class = -1

$$\text{(iii) Cusp Shapes} = -\frac{117036}{125929}u^5 a^3 - \frac{112360}{125929}u^5 a^2 + \cdots + \frac{188412}{125929}a + \frac{1819422}{125929}$$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_{11}$	$u^{24} - 6u^{23} + \dots - 40u + 13$
$c_2, c_7, c_8$ $c_{12}$	$u^{24} - 9u^{22} + \dots - 4u + 1$
$c_3$	$(u^2 - u + 1)^{12}$
$c_4, c_6$	$(u^6 - 3u^5 + 2u^4 - u^3 + 5u^2 - 3u - 2)^4$
$c_5, c_9, c_{10}$	$(u^6 + 3u^4 - u^3 + 2u^2 - 2u - 1)^4$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_{11}$	$y^{24} + 6y^{23} + \dots + 1260y + 169$
$c_2, c_7, c_8$ $c_{12}$	$y^{24} - 18y^{23} + \dots + 108y + 1$
$c_3$	$(y^2 + y + 1)^{12}$
$c_4, c_6$	$(y^6 - 5y^5 + 8y^4 - 3y^3 + 11y^2 - 29y + 4)^4$
$c_5, c_9, c_{10}$	$(y^6 + 6y^5 + 13y^4 + 9y^3 - 6y^2 - 8y + 1)^4$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.841864$ $a = -3.10867 + 0.50234I$ $b = 1.70590 - 0.70540I$	$11.46240 - 2.02988I$	$16.6818 + 3.4641I$
$u = -0.841864$ $a = -3.10867 - 0.50234I$ $b = 1.70590 + 0.70540I$	$11.46240 + 2.02988I$	$16.6818 - 3.4641I$
$u = -0.841864$ $a = 3.38289 + 0.97731I$ $b = -1.284970 + 0.023677I$	$11.46240 + 2.02988I$	$16.6818 - 3.4641I$
$u = -0.841864$ $a = 3.38289 - 0.97731I$ $b = -1.284970 - 0.023677I$	$11.46240 - 2.02988I$	$16.6818 + 3.4641I$
$u = -0.126468 + 1.352400I$ $a = -0.275034 - 0.878182I$ $b = 0.006754 - 1.081960I$	$-3.42893 - 5.42362I$	$3.63982 + 6.98172I$
$u = -0.126468 + 1.352400I$ $a = -0.756293 - 0.508483I$ $b = 0.332337 - 0.589055I$	$-3.42893 - 1.36386I$	$3.63982 + 0.05352I$
$u = -0.126468 + 1.352400I$ $a = 0.402484 - 0.343050I$ $b = 0.902109 + 0.022381I$	$-3.42893 - 1.36386I$	$3.63982 + 0.05352I$
$u = -0.126468 + 1.352400I$ $a = -0.28551 + 1.61036I$ $b = -1.114730 + 0.296237I$	$-3.42893 - 5.42362I$	$3.63982 + 6.98172I$
$u = -0.126468 - 1.352400I$ $a = -0.275034 + 0.878182I$ $b = 0.006754 + 1.081960I$	$-3.42893 + 5.42362I$	$3.63982 - 6.98172I$
$u = -0.126468 - 1.352400I$ $a = -0.756293 + 0.508483I$ $b = 0.332337 + 0.589055I$	$-3.42893 + 1.36386I$	$3.63982 - 0.05352I$

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.126468 - 1.352400I$ $a = 0.402484 + 0.343050I$ $b = 0.902109 - 0.022381I$	$-3.42893 + 1.36386I$	$3.63982 - 0.05352I$
$u = -0.126468 - 1.352400I$ $a = -0.28551 - 1.61036I$ $b = -1.114730 - 0.296237I$	$-3.42893 + 5.42362I$	$3.63982 - 6.98172I$
$u = 0.376468 + 1.319680I$ $a = 1.337000 - 0.149230I$ $b = -0.322326 - 1.361500I$	$3.16668 + 10.80330I$	$8.43784 - 9.36504I$
$u = 0.376468 + 1.319680I$ $a = 0.345851 + 0.454309I$ $b = -0.0385806 + 0.1120340I$	$3.16668 + 6.74357I$	$8.43784 - 2.43684I$
$u = 0.376468 + 1.319680I$ $a = 1.30610 - 1.33449I$ $b = -1.292530 - 0.445841I$	$3.16668 + 6.74357I$	$8.43784 - 2.43684I$
$u = 0.376468 + 1.319680I$ $a = -1.40072 + 2.01996I$ $b = 1.276970 + 0.375627I$	$3.16668 + 10.80330I$	$8.43784 - 9.36504I$
$u = 0.376468 - 1.319680I$ $a = 1.337000 + 0.149230I$ $b = -0.322326 + 1.361500I$	$3.16668 - 10.80330I$	$8.43784 + 9.36504I$
$u = 0.376468 - 1.319680I$ $a = 0.345851 - 0.454309I$ $b = -0.0385806 - 0.1120340I$	$3.16668 - 6.74357I$	$8.43784 + 2.43684I$
$u = 0.376468 - 1.319680I$ $a = 1.30610 + 1.33449I$ $b = -1.292530 + 0.445841I$	$3.16668 - 6.74357I$	$8.43784 + 2.43684I$
$u = 0.376468 - 1.319680I$ $a = -1.40072 - 2.01996I$ $b = 1.276970 - 0.375627I$	$3.16668 - 10.80330I$	$8.43784 + 9.36504I$

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.341865$ $a = 2.43368 + 1.17121I$ $b = -1.39615 + 0.48806I$	$5.51139 - 2.02988I$	$19.1629 + 3.4641I$
$u = 0.341865$ $a = 2.43368 - 1.17121I$ $b = -1.39615 - 0.48806I$	$5.51139 + 2.02988I$	$19.1629 - 3.4641I$
$u = 0.341865$ $a = -4.88179 + 3.06904I$ $b = 1.225210 - 0.191994I$	$5.51139 - 2.02988I$	$19.1629 + 3.4641I$
$u = 0.341865$ $a = -4.88179 - 3.06904I$ $b = 1.225210 + 0.191994I$	$5.51139 + 2.02988I$	$19.1629 - 3.4641I$

**III.**

$$I_3^u = \langle u^{16} + u^{15} + \dots + b + 2, -2u^{17} - 2u^{16} + \dots + a - 2, u^{18} + u^{17} + \dots + 2u + 1 \rangle$$

**(i) Arc colorings**

$$a_6 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -u \\ u^3 + u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} u^2 + 1 \\ -u^4 - 2u^2 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} u^5 + 2u^3 + u \\ -u^7 - 3u^5 - 2u^3 + u \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 2u^{17} + 2u^{16} + \dots + 9u + 2 \\ -u^{16} - u^{15} + \dots - 2u - 2 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -u^3 - 2u \\ u^3 + u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 2u^{17} + u^{16} + \dots + 8u + 1 \\ -u^{17} - 2u^{16} + \dots - 3u - 2 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} u^{16} - u^{15} + \dots + 10u^2 - 8u \\ u^{17} + 7u^{15} + \dots + u + 1 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -u^{17} - u^{16} + \dots - 5u + 2 \\ u^{15} + u^{14} + \dots + 3u + 1 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 2u^{17} + u^{16} + \dots + 9u + 1 \\ -u^{16} - u^{15} + \dots - u - 2 \end{pmatrix}$$

**(ii) Obstruction class = 1**

**(iii) Cusp Shapes**  $= -u^{16} - u^{15} - 7u^{14} - 2u^{13} - 17u^{12} + 10u^{11} - 12u^{10} + 39u^9 + 16u^8 + 42u^7 + 27u^6 - 4u^5 + 2u^4 - 26u^3 - 10u^2 - 4u + 7$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_{11}$	$u^{18} + 3u^{17} + \dots - 3u - 1$
$c_2, c_8$	$u^{18} + u^{17} + \dots - u - 1$
$c_3$	$u^{18} - 3u^{17} + \dots + 3u - 1$
$c_4, c_6$	$u^{18} + u^{17} + \dots + 7u^2 + 1$
$c_5$	$u^{18} - u^{17} + \dots - 2u + 1$
$c_7, c_{12}$	$u^{18} - u^{17} + \dots + u - 1$
$c_9, c_{10}$	$u^{18} + u^{17} + \dots + 2u + 1$



(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_{11}$	$y^{18} + 3y^{17} + \cdots + 7y + 1$
$c_2, c_7, c_8$ $c_{12}$	$y^{18} - 21y^{17} + \cdots - 29y + 1$
$c_3$	$y^{18} + 7y^{17} + \cdots + 3y + 1$
$c_4, c_6$	$y^{18} - 11y^{17} + \cdots + 14y + 1$
$c_5, c_9, c_{10}$	$y^{18} + 17y^{17} + \cdots + 8y + 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.863058$ $a = -3.08851$ $b = 1.47146$	10.9241	14.9390
$u = -0.811794 + 0.086746I$ $a = -1.66812 - 0.06489I$ $b = 1.106420 - 0.516453I$	$8.19254 - 4.11062I$	$15.0302 + 4.4552I$
$u = -0.811794 - 0.086746I$ $a = -1.66812 + 0.06489I$ $b = 1.106420 + 0.516453I$	$8.19254 + 4.11062I$	$15.0302 - 4.4552I$
$u = -0.037936 + 1.201190I$ $a = -0.67412 - 1.88976I$ $b = 1.359340 - 0.368138I$	$1.99280 - 2.42184I$	$8.62527 + 0.56589I$
$u = -0.037936 - 1.201190I$ $a = -0.67412 + 1.88976I$ $b = 1.359340 + 0.368138I$	$1.99280 + 2.42184I$	$8.62527 - 0.56589I$
$u = -0.346661 + 1.200250I$ $a = 0.135968 + 0.447764I$ $b = -1.186850 - 0.513231I$	$4.79445 - 0.07036I$	$11.73338 - 0.07459I$
$u = -0.346661 - 1.200250I$ $a = 0.135968 - 0.447764I$ $b = -1.186850 + 0.513231I$	$4.79445 + 0.07036I$	$11.73338 + 0.07459I$
$u = 0.175966 + 1.280820I$ $a = -0.806426 + 1.002530I$ $b = 0.228924 + 0.234817I$	$-4.68984 + 2.45101I$	$0.705670 - 1.175054I$
$u = 0.175966 - 1.280820I$ $a = -0.806426 - 1.002530I$ $b = 0.228924 - 0.234817I$	$-4.68984 - 2.45101I$	$0.705670 + 1.175054I$
$u = 0.400557 + 1.266130I$ $a = 1.79737 - 1.11786I$ $b = -1.47149 - 0.06981I$	$6.99702 + 4.52950I$	$11.21141 - 3.10762I$

Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.400557 - 1.266130I$ $a = 1.79737 + 1.11786I$ $b = -1.47149 + 0.06981I$	$6.99702 - 4.52950I$	$11.21141 + 3.10762I$
$u = -0.361990 + 1.332230I$ $a = 0.81927 + 1.15450I$ $b = -1.037050 + 0.524649I$	$3.73552 - 8.34686I$	$10.33759 + 7.17460I$
$u = -0.361990 - 1.332230I$ $a = 0.81927 - 1.15450I$ $b = -1.037050 - 0.524649I$	$3.73552 + 8.34686I$	$10.33759 - 7.17460I$
$u = -0.04839 + 1.45535I$ $a = 0.145310 - 0.301991I$ $b = 1.107200 + 0.202918I$	$-1.25223 + 1.02332I$	$5.08940 + 3.59240I$
$u = -0.04839 - 1.45535I$ $a = 0.145310 + 0.301991I$ $b = 1.107200 - 0.202918I$	$-1.25223 - 1.02332I$	$5.08940 - 3.59240I$
$u = 0.507807$ $a = 1.87659$ $b = -0.212766$	$-0.692851$	$-0.0433770$
$u = -0.155186 + 0.321559I$ $a = 0.85670 + 2.76375I$ $b = -1.235840 - 0.300145I$	$4.72294 + 1.80776I$	$7.31942 + 0.02100I$
$u = -0.155186 - 0.321559I$ $a = 0.85670 - 2.76375I$ $b = -1.235840 + 0.300145I$	$4.72294 - 1.80776I$	$7.31942 - 0.02100I$

$$\text{IV. } I_4^u = \langle -3.52 \times 10^8 a^3 u^9 - 2.80 \times 10^8 a^2 u^9 + \dots + 5.98 \times 10^8 a - 8.89 \times 10^8, 2u^9 a^3 + 3u^9 a^2 + \dots + 2a + 4, u^{10} - u^9 + \dots - 3u^3 + 1 \rangle$$

(i) Arc colorings

$$a_6 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -u \\ u^3 + u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} u^2 + 1 \\ -u^4 - 2u^2 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} u^5 + 2u^3 + u \\ -u^7 - 3u^5 - 2u^3 + u \end{pmatrix}$$

$$a_1 = \begin{pmatrix} a \\ 0.394132a^3 u^9 + 0.313043a^2 u^9 + \dots - 0.669019a + 0.995221 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -u^3 - 2u \\ u^3 + u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 0.198848a^3 u^9 - 1.61597a^2 u^9 + \dots + 0.322034a - 4.36671 \\ 0.624336a^3 u^9 + 1.68297a^2 u^9 + \dots - 0.641178a + 4.12350 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -0.139537a^3 u^9 + 0.126621a^2 u^9 + \dots - 1.16026a + 0.198975 \\ 0.137288a^3 u^9 - 0.949133a^2 u^9 + \dots + 2.17072a + 0.562076 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -0.176443a^3 u^9 - 0.622692a^2 u^9 + \dots + 2.44767a - 0.594951 \\ 0.512002a^3 u^9 + 0.204390a^2 u^9 + \dots - 0.220227a + 0.220345 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -0.144321a^3 u^9 - 0.0728304a^2 u^9 + \dots - 4.82417a - 3.30781 \\ -0.228457a^3 u^9 + 0.463402a^2 u^9 + \dots + 1.58033a + 2.20288 \end{pmatrix}$$

(ii) Obstruction class = -1

$$\text{(iii) Cusp Shapes} = -\frac{23189728}{893302351} u^9 a^3 - \frac{17608364}{893302351} u^9 a^2 + \dots - \frac{2297249516}{893302351} a + \frac{5202904734}{893302351}$$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_{11}$	$u^{40} - 13u^{39} + \dots - 5772u + 757$
$c_2, c_7, c_8$ $c_{12}$	$u^{40} - u^{39} + \dots + 18u^2 + 1$
$c_3$	$(u^2 - u + 1)^{20}$
$c_4, c_6$	$(u^5 + u^4 - 2u^3 - u^2 + u - 1)^8$
$c_5, c_9, c_{10}$	$(u^{10} + u^9 + 4u^8 + 4u^7 + 6u^6 + 6u^5 + 3u^4 + 3u^3 + 1)^4$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_{11}$	$y^{40} + 21y^{39} + \cdots + 22553644y + 573049$
$c_2, c_7, c_8$ $c_{12}$	$y^{40} - 39y^{39} + \cdots + 36y + 1$
$c_3$	$(y^2 + y + 1)^{20}$
$c_4, c_6$	$(y^5 - 5y^4 + 8y^3 - 3y^2 - y - 1)^8$
$c_5, c_9, c_{10}$	$(y^{10} + 7y^9 + 20y^8 + 26y^7 + 6y^6 - 22y^5 - 19y^4 + 3y^3 + 6y^2 + 1)^4$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_4^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.839548 + 0.070481I$ $a = -0.402562 - 0.505149I$ $b = -0.0439825 - 0.0696372I$	$7.51750 + 2.37095I$	$12.74431 - 0.03448I$
$u = 0.839548 + 0.070481I$ $a = -0.87672 - 1.40077I$ $b = 0.384497 + 1.319600I$	$7.51750 + 6.43072I$	$12.7443 - 6.9627I$
$u = 0.839548 + 0.070481I$ $a = -2.42644 + 0.17767I$ $b = 1.336310 + 0.372529I$	$7.51750 + 2.37095I$	$12.74431 - 0.03448I$
$u = 0.839548 + 0.070481I$ $a = 2.57482 - 0.88548I$ $b = -1.292970 - 0.351858I$	$7.51750 + 6.43072I$	$12.7443 - 6.9627I$
$u = 0.839548 - 0.070481I$ $a = -0.402562 + 0.505149I$ $b = -0.0439825 + 0.0696372I$	$7.51750 - 2.37095I$	$12.74431 + 0.03448I$
$u = 0.839548 - 0.070481I$ $a = -0.87672 + 1.40077I$ $b = 0.384497 - 1.319600I$	$7.51750 - 6.43072I$	$12.7443 + 6.9627I$
$u = 0.839548 - 0.070481I$ $a = -2.42644 - 0.17767I$ $b = 1.336310 - 0.372529I$	$7.51750 - 2.37095I$	$12.74431 + 0.03448I$
$u = 0.839548 - 0.070481I$ $a = 2.57482 + 0.88548I$ $b = -1.292970 + 0.351858I$	$7.51750 - 6.43072I$	$12.7443 + 6.9627I$
$u = 0.090539 + 1.215350I$ $a = -0.225264 + 0.093412I$ $b = 1.56209 - 0.31243I$	$1.97403 - 0.49930I$	$8.51511 - 0.96655I$
$u = 0.090539 + 1.215350I$ $a = 0.66256 + 1.78010I$ $b = 1.22523 + 0.73772I$	$1.97403 + 3.56046I$	$8.51511 - 7.89475I$

Solutions to $I_4^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.090539 + 1.215350I$ $a = 1.99879 - 0.95641I$ $b = -1.350730 - 0.169147I$	$1.97403 + 3.56046I$	$8.51511 - 7.89475I$
$u = 0.090539 + 1.215350I$ $a = -0.39206 - 2.81005I$ $b = -1.006940 + 0.136833I$	$1.97403 - 0.49930I$	$8.51511 - 0.96655I$
$u = 0.090539 - 1.215350I$ $a = -0.225264 - 0.093412I$ $b = 1.56209 + 0.31243I$	$1.97403 + 0.49930I$	$8.51511 + 0.96655I$
$u = 0.090539 - 1.215350I$ $a = 0.66256 - 1.78010I$ $b = 1.22523 - 0.73772I$	$1.97403 - 3.56046I$	$8.51511 + 7.89475I$
$u = 0.090539 - 1.215350I$ $a = 1.99879 + 0.95641I$ $b = -1.350730 + 0.169147I$	$1.97403 - 3.56046I$	$8.51511 + 7.89475I$
$u = 0.090539 - 1.215350I$ $a = -0.39206 + 2.81005I$ $b = -1.006940 - 0.136833I$	$1.97403 + 0.49930I$	$8.51511 + 0.96655I$
$u = 0.383413 + 1.200420I$ $a = -0.604285 - 0.632212I$ $b = -0.462034 + 1.251310I$	$4.04602 - 2.02988I$	$9.48114 + 3.46410I$
$u = 0.383413 + 1.200420I$ $a = 0.478064 - 0.583666I$ $b = 0.150869 - 0.009153I$	$4.04602 + 2.02988I$	$9.48114 - 3.46410I$
$u = 0.383413 + 1.200420I$ $a = 1.045730 - 0.689743I$ $b = -1.382170 + 0.277320I$	$4.04602 + 2.02988I$	$9.48114 - 3.46410I$
$u = 0.383413 + 1.200420I$ $a = -1.260420 - 0.050726I$ $b = 1.309920 - 0.319057I$	$4.04602 - 2.02988I$	$9.48114 + 3.46410I$



Solutions to $I_4^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.383413 - 1.200420I$ $a = -0.604285 + 0.632212I$ $b = -0.462034 - 1.251310I$	$4.04602 + 2.02988I$	$9.48114 - 3.46410I$
$u = 0.383413 - 1.200420I$ $a = 0.478064 + 0.583666I$ $b = 0.150869 + 0.009153I$	$4.04602 - 2.02988I$	$9.48114 + 3.46410I$
$u = 0.383413 - 1.200420I$ $a = 1.045730 + 0.689743I$ $b = -1.382170 - 0.277320I$	$4.04602 - 2.02988I$	$9.48114 + 3.46410I$
$u = 0.383413 - 1.200420I$ $a = -1.260420 + 0.050726I$ $b = 1.309920 + 0.319057I$	$4.04602 + 2.02988I$	$9.48114 - 3.46410I$
$u = -0.383851 + 1.270630I$ $a = 0.98145 + 1.21602I$ $b = -1.73426 - 0.65183I$	$7.51750 - 2.37095I$	$12.74431 + 0.03448I$
$u = -0.383851 + 1.270630I$ $a = -2.23007 - 0.18057I$ $b = 1.313220 + 0.005597I$	$7.51750 - 6.43072I$	$12.7443 + 6.9627I$
$u = -0.383851 + 1.270630I$ $a = 1.96754 + 1.53952I$ $b = -1.67195 + 0.75671I$	$7.51750 - 6.43072I$	$12.7443 + 6.9627I$
$u = -0.383851 + 1.270630I$ $a = -2.02707 - 2.12285I$ $b = 1.253450 - 0.039994I$	$7.51750 - 2.37095I$	$12.74431 + 0.03448I$
$u = -0.383851 - 1.270630I$ $a = 0.98145 - 1.21602I$ $b = -1.73426 + 0.65183I$	$7.51750 + 2.37095I$	$12.74431 - 0.03448I$
$u = -0.383851 - 1.270630I$ $a = -2.23007 + 0.18057I$ $b = 1.313220 - 0.005597I$	$7.51750 + 6.43072I$	$12.7443 - 6.9627I$

Solutions to $I_4^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.383851 - 1.270630I$ $a = 1.96754 - 1.53952I$ $b = -1.67195 - 0.75671I$	$7.51750 + 6.43072I$	$12.7443 - 6.9627I$
$u = -0.383851 - 1.270630I$ $a = -2.02707 + 2.12285I$ $b = 1.253450 + 0.039994I$	$7.51750 + 2.37095I$	$12.74431 - 0.03448I$
$u = -0.429649 + 0.392970I$ $a = 0.786631 + 0.807814I$ $b = -1.142270 - 0.034877I$	$1.97403 + 0.49930I$	$8.51511 + 0.96655I$
$u = -0.429649 + 0.392970I$ $a = 1.29731 - 0.58385I$ $b = 0.044480 + 0.564141I$	$1.97403 + 0.49930I$	$8.51511 + 0.96655I$
$u = -0.429649 + 0.392970I$ $a = 0.266316 - 0.274622I$ $b = -0.176919 + 0.887142I$	$1.97403 - 3.56046I$	$8.51511 + 7.89475I$
$u = -0.429649 + 0.392970I$ $a = -1.11432 - 1.64211I$ $b = 1.184170 - 0.201060I$	$1.97403 - 3.56046I$	$8.51511 + 7.89475I$
$u = -0.429649 - 0.392970I$ $a = 0.786631 - 0.807814I$ $b = -1.142270 + 0.034877I$	$1.97403 - 0.49930I$	$8.51511 - 0.96655I$
$u = -0.429649 - 0.392970I$ $a = 1.29731 + 0.58385I$ $b = 0.044480 - 0.564141I$	$1.97403 - 0.49930I$	$8.51511 - 0.96655I$
$u = -0.429649 - 0.392970I$ $a = 0.266316 + 0.274622I$ $b = -0.176919 - 0.887142I$	$1.97403 + 3.56046I$	$8.51511 - 7.89475I$
$u = -0.429649 - 0.392970I$ $a = -1.11432 + 1.64211I$ $b = 1.184170 + 0.201060I$	$1.97403 + 3.56046I$	$8.51511 - 7.89475I$

## V. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1, c_{11}$	$(u^{18} + 3u^{17} + \dots - 3u - 1)(u^{24} - 6u^{23} + \dots - 40u + 13)$ $\cdot (u^{36} + 3u^{35} + \dots + 10u - 1)(u^{40} - 13u^{39} + \dots - 5772u + 757)$
$c_2, c_8$	$(u^{18} + u^{17} + \dots - u - 1)(u^{24} - 9u^{22} + \dots - 4u + 1)$ $\cdot (u^{36} + u^{35} + \dots - 4u^2 + 1)(u^{40} - u^{39} + \dots + 18u^2 + 1)$
$c_3$	$((u^2 - u + 1)^{32})(u^{18} - 3u^{17} + \dots + 3u - 1)$ $\cdot (u^{36} + 36u^{35} + \dots - 851968u - 65536)$
$c_4, c_6$	$(u^5 + u^4 - 2u^3 - u^2 + u - 1)^8(u^6 - 3u^5 + 2u^4 - u^3 + 5u^2 - 3u - 2)^4$ $\cdot (u^{18} + u^{17} + \dots + 7u^2 + 1)(u^{36} + 6u^{35} + \dots - 3456u - 712)$
$c_5$	$(u^6 + 3u^4 - u^3 + 2u^2 - 2u - 1)^4$ $\cdot (u^{10} + u^9 + 4u^8 + 4u^7 + 6u^6 + 6u^5 + 3u^4 + 3u^3 + 1)^4$ $\cdot (u^{18} - u^{17} + \dots - 2u + 1)(u^{36} - 6u^{35} + \dots + 10u - 4)$
$c_7, c_{12}$	$(u^{18} - u^{17} + \dots + u - 1)(u^{24} - 9u^{22} + \dots - 4u + 1)$ $\cdot (u^{36} + u^{35} + \dots - 4u^2 + 1)(u^{40} - u^{39} + \dots + 18u^2 + 1)$
$c_9, c_{10}$	$(u^6 + 3u^4 - u^3 + 2u^2 - 2u - 1)^4$ $\cdot (u^{10} + u^9 + 4u^8 + 4u^7 + 6u^6 + 6u^5 + 3u^4 + 3u^3 + 1)^4$ $\cdot (u^{18} + u^{17} + \dots + 2u + 1)(u^{36} - 6u^{35} + \dots + 10u - 4)$

## VI. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1, c_{11}$	$(y^{18} + 3y^{17} + \dots + 7y + 1)(y^{24} + 6y^{23} + \dots + 1260y + 169)$ $\cdot (y^{36} + 13y^{35} + \dots - 108y + 1)$ $\cdot (y^{40} + 21y^{39} + \dots + 22553644y + 573049)$
$c_2, c_7, c_8$ $c_{12}$	$(y^{18} - 21y^{17} + \dots - 29y + 1)(y^{24} - 18y^{23} + \dots + 108y + 1)$ $\cdot (y^{36} - 31y^{35} + \dots - 8y + 1)(y^{40} - 39y^{39} + \dots + 36y + 1)$
$c_3$	$((y^2 + y + 1)^{32})(y^{18} + 7y^{17} + \dots + 3y + 1)$ $\cdot (y^{36} + 8y^{35} + \dots - 81604378624y + 4294967296)$
$c_4, c_6$	$(y^5 - 5y^4 + 8y^3 - 3y^2 - y - 1)^8$ $\cdot (y^6 - 5y^5 + 8y^4 - 3y^3 + 11y^2 - 29y + 4)^4$ $\cdot (y^{18} - 11y^{17} + \dots + 14y + 1)$ $\cdot (y^{36} - 26y^{35} + \dots - 1429120y + 506944)$
$c_5, c_9, c_{10}$	$(y^6 + 6y^5 + 13y^4 + 9y^3 - 6y^2 - 8y + 1)^4$ $\cdot (y^{10} + 7y^9 + 20y^8 + 26y^7 + 6y^6 - 22y^5 - 19y^4 + 3y^3 + 6y^2 + 1)^4$ $\cdot (y^{18} + 17y^{17} + \dots + 8y + 1)(y^{36} + 30y^{35} + \dots - 108y + 16)$