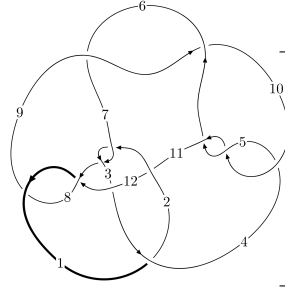
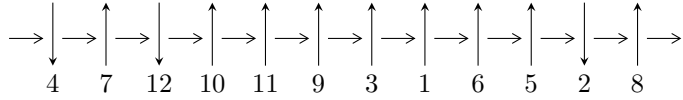


12a<sub>1116</sub> (K12a<sub>1116</sub>)



A knot diagram<sup>1</sup>

**Linearized knot diagram**



**Solving Sequence**

$$1,8 \xrightarrow{c_8} 3,9 \xrightarrow{c_7} 7 \xrightarrow{c_2} 2 \xrightarrow{c_6} 6 \xrightarrow{c_9} 10 \xrightarrow{c_{12}} 12 \xrightarrow{c_3} 4 \xrightarrow{c_{11}} 11 \xrightarrow{c_5} 5 \twoheadrightarrow c_1, c_4, c_{10}$$

**Ideals for irreducible components<sup>2</sup> of  $X_{\text{par}}$**

$$I_1^u = \langle b - u, 1.05217 \times 10^{27} u^{39} + 1.39337 \times 10^{27} u^{38} + \dots + 7.10616 \times 10^{26} a - 1.70682 \times 10^{27}, u^{40} + u^{39} + \dots - 2u + 1 \rangle$$

$$I_2^u = \langle -2.26032 \times 10^{209} u^{71} + 5.90990 \times 10^{209} u^{70} + \dots + 4.11003 \times 10^{210} b - 1.25850 \times 10^{213}, -1.04624 \times 10^{212} u^{71} + 2.60608 \times 10^{212} u^{70} + \dots + 1.55912 \times 10^{213} a - 4.97927 \times 10^{215}, u^{72} - u^{71} + \dots - 10866u + 3667 \rangle$$

$$I_3^u = \langle b + u, 2u^{19} + 2u^{18} + \dots + a - 4, u^{20} + u^{19} + \dots - 4u - 1 \rangle$$

\* 3 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 132 representations.

<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\mathbf{I. } I_1^u = \langle b - u, 1.05 \times 10^{27} u^{39} + 1.39 \times 10^{27} u^{38} + \dots + 7.11 \times 10^{26} a - 1.71 \times 10^{27}, u^{40} + u^{39} + \dots - 2u + 1 \rangle$$

(i) Arc colorings

$$a_1 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -1.48065u^{39} - 1.96079u^{38} + \dots + 1.35762u + 2.40188 \\ u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -0.480143u^{39} - 1.10267u^{38} + \dots - 0.559408u + 2.48065 \\ u^2 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -0.858121u^{39} - 1.37178u^{38} + \dots - 0.162740u + 1.92174 \\ -u^3 + u \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -0.513657u^{39} - 0.937281u^{38} + \dots + 0.205499u + 1.85812 \\ 0.0881220u^{39} - 0.00106714u^{38} + \dots - 0.431317u + 0.198901 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0.170926u^{39} + 0.314539u^{38} + \dots + 0.337548u + 0.372176 \\ -0.269415u^{39} - 0.112280u^{38} + \dots + 1.12121u - 0.412140 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -u \\ u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -0.858121u^{39} - 1.37178u^{38} + \dots + 0.837260u + 1.92174 \\ -0.622525u^{39} - 0.589010u^{38} + \dots + 1.52036u + 0.480143 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1.17203u^{39} + 1.77115u^{38} + \dots - 0.353657u - 2.38079 \\ -0.313912u^{39} - 0.399375u^{38} + \dots + 0.516397u + 0.459050 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -1.61039u^{39} - 2.45419u^{38} + \dots + 0.621411u + 3.20931 \\ 0.249610u^{39} - 0.0431241u^{38} + \dots - 1.08313u + 0.723404 \end{pmatrix}$$

(ii) Obstruction class = -1

$$\text{(iii) Cusp Shapes} = \frac{151015313886743544528267445}{710615561412313479871799093} u^{39} - \frac{543514532737677763668736672}{710615561412313479871799093} u^{38} + \dots - \frac{196468822280070142794468717}{710615561412313479871799093} u + \frac{7938621198965187441158388505}{710615561412313479871799093}$$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_{11}$	$u^{40} + u^{39} + \dots - 14u + 1$
$c_2, c_7, c_8$ $c_{12}$	$u^{40} + u^{39} + \dots - 2u + 1$
$c_3$	$u^{40} + 35u^{39} + \dots + 4063232u + 262144$
$c_4, c_5, c_{10}$	$u^{40} - 6u^{39} + \dots + 14u + 4$
$c_6, c_9$	$u^{40} + 18u^{39} + \dots - 286u - 52$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_{11}$	$y^{40} - 17y^{39} + \dots - 104y + 1$
$c_2, c_7, c_8$ $c_{12}$	$y^{40} - 27y^{39} + \dots - 6y + 1$
$c_3$	$y^{40} - 5y^{39} + \dots - 738734374912y + 68719476736$
$c_4, c_5, c_{10}$	$y^{40} - 34y^{39} + \dots - 76y + 16$
$c_6, c_9$	$y^{40} + 22y^{39} + \dots - 227084y + 2704$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.829708 + 0.582758I$ $a = -0.335057 + 0.593668I$ $b = 0.829708 + 0.582758I$	$0.31185 + 6.62575I$	$5.80735 - 6.70847I$
$u = 0.829708 - 0.582758I$ $a = -0.335057 - 0.593668I$ $b = 0.829708 - 0.582758I$	$0.31185 - 6.62575I$	$5.80735 + 6.70847I$
$u = 0.950467 + 0.117799I$ $a = -2.79305 - 0.18733I$ $b = 0.950467 + 0.117799I$	$0.479393 + 0.290586I$	$9.02412 - 0.47721I$
$u = 0.950467 - 0.117799I$ $a = -2.79305 + 0.18733I$ $b = 0.950467 - 0.117799I$	$0.479393 - 0.290586I$	$9.02412 + 0.47721I$
$u = -1.045880 + 0.174408I$ $a = 2.78432 - 0.39606I$ $b = -1.045880 + 0.174408I$	$-1.95597 - 4.61343I$	$6.17888 + 5.30120I$
$u = -1.045880 - 0.174408I$ $a = 2.78432 + 0.39606I$ $b = -1.045880 - 0.174408I$	$-1.95597 + 4.61343I$	$6.17888 - 5.30120I$
$u = -1.06992$ $a = 3.35821$ $b = -1.06992$	$8.23937$	$8.13250$
$u = -0.709739 + 0.591170I$ $a = 0.136387 + 0.470227I$ $b = -0.709739 + 0.591170I$	$-3.66425 - 2.23553I$	$2.10476 + 3.41235I$
$u = -0.709739 - 0.591170I$ $a = 0.136387 - 0.470227I$ $b = -0.709739 - 0.591170I$	$-3.66425 + 2.23553I$	$2.10476 - 3.41235I$
$u = 1.099650 + 0.175182I$ $a = -2.79566 - 0.50433I$ $b = 1.099650 + 0.175182I$	$3.02582 + 8.81935I$	$10.62324 - 6.97053I$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.099650 - 0.175182I$ $a = -2.79566 + 0.50433I$ $b = 1.099650 - 0.175182I$	$3.02582 - 8.81935I$	$10.62324 + 6.97053I$
$u = -0.301242 + 0.810427I$ $a = 1.231820 - 0.046364I$ $b = -0.301242 + 0.810427I$	$-1.68748 + 6.67297I$	$4.33952 - 4.30566I$
$u = -0.301242 - 0.810427I$ $a = 1.231820 + 0.046364I$ $b = -0.301242 - 0.810427I$	$-1.68748 - 6.67297I$	$4.33952 + 4.30566I$
$u = 0.575167 + 0.621713I$ $a = 0.009634 + 0.324370I$ $b = 0.575167 + 0.621713I$	$0.17012 - 2.02828I$	$6.28682 - 0.18788I$
$u = 0.575167 - 0.621713I$ $a = 0.009634 - 0.324370I$ $b = 0.575167 - 0.621713I$	$0.17012 + 2.02828I$	$6.28682 + 0.18788I$
$u = 0.347115 + 0.764028I$ $a = -1.348860 + 0.000533I$ $b = 0.347115 + 0.764028I$	$-5.94604 - 2.55676I$	$-0.337170 + 1.059387I$
$u = 0.347115 - 0.764028I$ $a = -1.348860 - 0.000533I$ $b = 0.347115 - 0.764028I$	$-5.94604 + 2.55676I$	$-0.337170 - 1.059387I$
$u = -0.408843 + 0.706524I$ $a = 1.51264 + 0.04027I$ $b = -0.408843 + 0.706524I$	$-2.38796 - 1.54380I$	$3.59940 + 3.55875I$
$u = -0.408843 - 0.706524I$ $a = 1.51264 - 0.04027I$ $b = -0.408843 - 0.706524I$	$-2.38796 + 1.54380I$	$3.59940 - 3.55875I$
$u = -0.744235$ $a = -1.54163$ $b = -0.744235$	$7.13720$	$26.0990$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.233550 + 0.336291I$ $a = 1.58613 + 1.22068I$ $b = -1.233550 + 0.336291I$	$10.81870 - 1.65128I$	$14.7327 + 4.5795I$
$u = -1.233550 - 0.336291I$ $a = 1.58613 - 1.22068I$ $b = -1.233550 - 0.336291I$	$10.81870 + 1.65128I$	$14.7327 - 4.5795I$
$u = 1.230890 + 0.434304I$ $a = -1.40654 + 0.97624I$ $b = 1.230890 + 0.434304I$	$4.92417 + 4.68998I$	$8.58815 - 3.67892I$
$u = 1.230890 - 0.434304I$ $a = -1.40654 - 0.97624I$ $b = 1.230890 - 0.434304I$	$4.92417 - 4.68998I$	$8.58815 + 3.67892I$
$u = -0.008320 + 0.688792I$ $a = -0.644264 + 0.267316I$ $b = -0.008320 + 0.688792I$	$3.24536 - 1.80566I$	$7.66277 + 3.84341I$
$u = -0.008320 - 0.688792I$ $a = -0.644264 - 0.267316I$ $b = -0.008320 - 0.688792I$	$3.24536 + 1.80566I$	$7.66277 - 3.84341I$
$u = 0.619486$ $a = -2.75105$ $b = 0.619486$	$0.329159$	$14.0190$
$u = -1.306240 + 0.490977I$ $a = 1.50397 + 0.75841I$ $b = -1.306240 + 0.490977I$	$5.64753 - 8.73681I$	$9.75964 + 8.45348I$
$u = -1.306240 - 0.490977I$ $a = 1.50397 - 0.75841I$ $b = -1.306240 - 0.490977I$	$5.64753 + 8.73681I$	$9.75964 - 8.45348I$
$u = 1.39043 + 0.46049I$ $a = -1.69234 + 0.71463I$ $b = 1.39043 + 0.46049I$	$12.1702 + 10.4927I$	$0$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.39043 - 0.46049I$ $a = -1.69234 - 0.71463I$ $b = 1.39043 - 0.46049I$	$12.1702 - 10.4927I$	0
$u = -1.37616 + 0.58894I$ $a = 1.53982 + 0.51187I$ $b = -1.37616 + 0.58894I$	$3.95118 - 8.98770I$	0
$u = -1.37616 - 0.58894I$ $a = 1.53982 - 0.51187I$ $b = -1.37616 - 0.58894I$	$3.95118 + 8.98770I$	0
$u = -0.114437 + 0.486204I$ $a = 0.910358 + 0.962474I$ $b = -0.114437 + 0.486204I$	$-1.35206 + 0.83491I$	$-2.58594 - 2.82924I$
$u = -0.114437 - 0.486204I$ $a = 0.910358 - 0.962474I$ $b = -0.114437 - 0.486204I$	$-1.35206 - 0.83491I$	$-2.58594 + 2.82924I$
$u = 1.41567 + 0.59218I$ $a = -1.60292 + 0.47452I$ $b = 1.41567 + 0.59218I$	$1.03205 + 13.48300I$	0
$u = 1.41567 - 0.59218I$ $a = -1.60292 - 0.47452I$ $b = 1.41567 - 0.59218I$	$1.03205 - 13.48300I$	0
$u = -1.44142 + 0.58645I$ $a = 1.64842 + 0.46268I$ $b = -1.44142 + 0.58645I$	$5.7710 - 17.8215I$	0
$u = -1.44142 - 0.58645I$ $a = 1.64842 - 0.46268I$ $b = -1.44142 - 0.58645I$	$5.7710 + 17.8215I$	0
$u = 0.408146$ $a = 0.444839$ $b = 0.408146$	0.723836	14.2940



$$\text{II. } I_2^u = \langle -2.26 \times 10^{209} u^{71} + 5.91 \times 10^{209} u^{70} + \dots + 4.11 \times 10^{210} b - 1.26 \times 10^{213}, -1.05 \times 10^{212} u^{71} + 2.61 \times 10^{212} u^{70} + \dots + 1.56 \times 10^{213} a - 4.98 \times 10^{215}, u^{72} - u^{71} + \dots - 10866u + 3667 \rangle$$

(i) Arc colorings

$$a_1 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 0.0671046u^{71} - 0.167151u^{70} + \dots - 1109.95u + 319.364 \\ 0.0549952u^{71} - 0.143792u^{70} + \dots - 1113.13u + 306.203 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -0.0301419u^{71} + 0.0293224u^{70} + \dots + 395.244u - 87.4100 \\ 0.328648u^{71} - 0.521975u^{70} + \dots - 3059.47u + 668.529 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 0.278968u^{71} - 0.729274u^{70} + \dots - 5396.58u + 1506.02 \\ -0.454216u^{71} + 1.22463u^{70} + \dots + 8943.08u - 2530.76 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -0.339538u^{71} + 0.567129u^{70} + \dots + 3353.09u - 758.945 \\ 0.688383u^{71} - 1.16484u^{70} + \dots - 6675.94u + 1506.11 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0.541344u^{71} - 0.890028u^{70} + \dots - 4490.24u + 952.255 \\ -0.342960u^{71} + 0.537379u^{70} + \dots + 2175.57u - 399.573 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -u \\ u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -0.0741667u^{71} + 0.182756u^{70} + \dots + 1389.76u - 373.122 \\ 0.196267u^{71} - 0.493699u^{70} + \dots - 3612.84u + 998.690 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0.447909u^{71} - 1.21674u^{70} + \dots - 8536.05u + 2445.31 \\ -0.367683u^{71} + 1.02998u^{70} + \dots + 7199.69u - 2091.60 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 0.621670u^{71} - 1.32742u^{70} + \dots - 8696.78u + 2258.81 \\ -0.208971u^{71} + 0.514036u^{70} + \dots + 3370.06u - 922.984 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes =  $0.552929u^{71} - 1.11719u^{70} + \dots - 7329.04u + 1860.11$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_{11}$	$u^{72} - 19u^{71} + \dots + 178u + 13$
$c_2, c_7, c_8$ $c_{12}$	$u^{72} - u^{71} + \dots - 10866u + 3667$
$c_3$	$(u^2 - u + 1)^{36}$
$c_4, c_5, c_{10}$	$(u^{18} + u^{17} + \dots - u - 1)^4$
$c_6, c_9$	$(u^{18} - 3u^{17} + \dots - 3u + 3)^4$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_{11}$	$y^{72} + 11y^{71} + \dots - 11560y + 169$
$c_2, c_7, c_8$ $c_{12}$	$y^{72} - 57y^{71} + \dots - 103020588y + 13446889$
$c_3$	$(y^2 + y + 1)^{36}$
$c_4, c_5, c_{10}$	$(y^{18} - 15y^{17} + \dots - 7y + 1)^4$
$c_6, c_9$	$(y^{18} + 13y^{17} + \dots - 75y + 9)^4$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.017220 + 0.027464I$ $a = 2.13206 - 0.52858I$ $b = -1.66385 - 0.33543I$	$2.50861 + 0.14420I$	0
$u = 1.017220 - 0.027464I$ $a = 2.13206 + 0.52858I$ $b = -1.66385 + 0.33543I$	$2.50861 - 0.14420I$	0
$u = 0.693662 + 0.751370I$ $a = 0.303778 + 0.388548I$ $b = 0.650141 - 0.173344I$	$-0.21034 - 1.47092I$	0
$u = 0.693662 - 0.751370I$ $a = 0.303778 - 0.388548I$ $b = 0.650141 + 0.173344I$	$-0.21034 + 1.47092I$	0
$u = 1.033500 + 0.072324I$ $a = 0.293773 - 0.211699I$ $b = 0.129307 - 0.655859I$	$1.58118 + 0.45801I$	0
$u = 1.033500 - 0.072324I$ $a = 0.293773 + 0.211699I$ $b = 0.129307 + 0.655859I$	$1.58118 - 0.45801I$	0
$u = 0.031660 + 0.944468I$ $a = 0.220232 - 0.330295I$ $b = -1.118420 - 0.229212I$	$1.58118 + 3.60176I$	$0. - 7.68480I$
$u = 0.031660 - 0.944468I$ $a = 0.220232 + 0.330295I$ $b = -1.118420 + 0.229212I$	$1.58118 - 3.60176I$	$0. + 7.68480I$
$u = -1.066340 + 0.019440I$ $a = -2.19706 + 0.41240I$ $b = 1.71352 + 0.39093I$	$6.82360 - 3.68439I$	0
$u = -1.066340 - 0.019440I$ $a = -2.19706 - 0.41240I$ $b = 1.71352 - 0.39093I$	$6.82360 + 3.68439I$	0

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.913482 + 0.085334I$ $a = -2.06764 - 0.75190I$ $b = 1.61282 - 0.23864I$	$6.06357 - 3.81683I$	$11.23943 + 0.I$
$u = -0.913482 - 0.085334I$ $a = -2.06764 + 0.75190I$ $b = 1.61282 + 0.23864I$	$6.06357 + 3.81683I$	$11.23943 + 0.I$
$u = -0.846987 + 0.697488I$ $a = -0.333673 + 0.483654I$ $b = -0.519849 - 0.164047I$	$-3.45249 - 2.84406I$	0
$u = -0.846987 - 0.697488I$ $a = -0.333673 - 0.483654I$ $b = -0.519849 + 0.164047I$	$-3.45249 + 2.84406I$	0
$u = -0.289505 + 1.062300I$ $a = -0.594187 - 0.376086I$ $b = 1.233660 - 0.268864I$	$7.08808 - 5.25662I$	0
$u = -0.289505 - 1.062300I$ $a = -0.594187 + 0.376086I$ $b = 1.233660 + 0.268864I$	$7.08808 + 5.25662I$	0
$u = -1.118420 + 0.229212I$ $a = -0.308403 + 0.113424I$ $b = 0.031660 - 0.944468I$	$1.58118 - 3.60176I$	0
$u = -1.118420 - 0.229212I$ $a = -0.308403 - 0.113424I$ $b = 0.031660 + 0.944468I$	$1.58118 + 3.60176I$	0
$u = 0.955436 + 0.668372I$ $a = 0.353081 + 0.532513I$ $b = 0.424031 - 0.169720I$	$1.04456 + 7.10521I$	0
$u = 0.955436 - 0.668372I$ $a = 0.353081 - 0.532513I$ $b = 0.424031 + 0.169720I$	$1.04456 - 7.10521I$	0

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.098140 + 0.393816I$		
$a = -0.078496 + 0.425133I$	$-0.21034 - 2.58885I$	0
$b = -0.074344 - 1.268570I$		
$u = -1.098140 - 0.393816I$		
$a = -0.078496 - 0.425133I$	$-0.21034 + 2.58885I$	0
$b = -0.074344 + 1.268570I$		
$u = -1.187800 + 0.128492I$		
$a = -0.522626 + 0.383206I$	$7.08808 - 1.19685I$	0
$b = 0.028590 + 0.292450I$		
$u = -1.187800 - 0.128492I$		
$a = -0.522626 - 0.383206I$	$7.08808 + 1.19685I$	0
$b = 0.028590 - 0.292450I$		
$u = 1.137940 + 0.411255I$		
$a = 0.137911 + 0.514671I$	$-3.45249 + 6.90382I$	0
$b = 0.007450 - 1.328250I$		
$u = 1.137940 - 0.411255I$		
$a = 0.137911 - 0.514671I$	$-3.45249 - 6.90382I$	0
$b = 0.007450 + 1.328250I$		
$u = -1.224820 + 0.174181I$		
$a = -1.71777 - 0.24428I$	$5.55672 - 2.02988I$	0
$b = 1.41620 - 0.50567I$		
$u = -1.224820 - 0.174181I$		
$a = -1.71777 + 0.24428I$	$5.55672 + 2.02988I$	0
$b = 1.41620 + 0.50567I$		
$u = -1.166860 + 0.418865I$		
$a = -0.188865 + 0.570472I$	$1.04456 - 11.16500I$	0
$b = 0.045286 - 1.364190I$		
$u = -1.166860 - 0.418865I$		
$a = -0.188865 - 0.570472I$	$1.04456 + 11.16500I$	0
$b = 0.045286 + 1.364190I$		

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.248510 + 0.052716I$ $a = 1.95056 - 0.08236I$ $b = -1.58003 - 0.62693I$	$10.76740 + 2.02988I$	0
$u = 1.248510 - 0.052716I$ $a = 1.95056 + 0.08236I$ $b = -1.58003 + 0.62693I$	$10.76740 - 2.02988I$	0
$u = 1.233660 + 0.268864I$ $a = 0.530370 + 0.307807I$ $b = -0.289505 - 1.062300I$	$7.08808 + 5.25662I$	0
$u = 1.233660 - 0.268864I$ $a = 0.530370 - 0.307807I$ $b = -0.289505 + 1.062300I$	$7.08808 - 5.25662I$	0
$u = -0.074344 + 1.268570I$ $a = 0.394783 + 0.040892I$ $b = -1.098140 - 0.393816I$	$-0.21034 + 2.58885I$	0
$u = -0.074344 - 1.268570I$ $a = 0.394783 - 0.040892I$ $b = -1.098140 + 0.393816I$	$-0.21034 - 2.58885I$	0
$u = 0.650141 + 0.173344I$ $a = -0.307229 - 0.683719I$ $b = 0.693662 - 0.751370I$	$-0.21034 + 1.47092I$	$7.51114 - 3.72400I$
$u = 0.650141 - 0.173344I$ $a = -0.307229 + 0.683719I$ $b = 0.693662 + 0.751370I$	$-0.21034 - 1.47092I$	$7.51114 + 3.72400I$
$u = 0.007450 + 1.328250I$ $a = -0.483846 + 0.038488I$ $b = 1.137940 - 0.411255I$	$-3.45249 - 6.90382I$	0
$u = 0.007450 - 1.328250I$ $a = -0.483846 - 0.038488I$ $b = 1.137940 + 0.411255I$	$-3.45249 + 6.90382I$	0

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.129307 + 0.655859I$ $a = 0.382215 - 0.410916I$ $b = 1.033500 - 0.072324I$	$1.58118 - 0.45801I$	$7.80878 - 0.75660I$
$u = 0.129307 - 0.655859I$ $a = 0.382215 + 0.410916I$ $b = 1.033500 + 0.072324I$	$1.58118 + 0.45801I$	$7.80878 + 0.75660I$
$u = 0.045286 + 1.364190I$ $a = 0.544891 + 0.031701I$ $b = -1.166860 - 0.418865I$	$1.04456 + 11.16500I$	0
$u = 0.045286 - 1.364190I$ $a = 0.544891 - 0.031701I$ $b = -1.166860 + 0.418865I$	$1.04456 - 11.16500I$	0
$u = 1.370090 + 0.136727I$ $a = 1.61237 + 0.18879I$ $b = -1.31349 - 0.85071I$	$2.50861 + 3.91557I$	0
$u = 1.370090 - 0.136727I$ $a = 1.61237 - 0.18879I$ $b = -1.31349 + 0.85071I$	$2.50861 - 3.91557I$	0
$u = -1.372800 + 0.107076I$ $a = -1.71771 + 0.21747I$ $b = 1.40460 - 0.87274I$	$6.82360 - 7.74416I$	0
$u = -1.372800 - 0.107076I$ $a = -1.71771 - 0.21747I$ $b = 1.40460 + 0.87274I$	$6.82360 + 7.74416I$	0
$u = -1.377880 + 0.171851I$ $a = -1.44111 + 0.19069I$ $b = 1.16098 - 0.85415I$	$6.06357 - 0.24294I$	0
$u = -1.377880 - 0.171851I$ $a = -1.44111 - 0.19069I$ $b = 1.16098 + 0.85415I$	$6.06357 + 0.24294I$	0



Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.16098 + 0.85415I$ $a = 1.301240 - 0.517704I$ $b = -1.377880 - 0.171851I$	$6.06357 + 0.24294I$	0
$u = 1.16098 - 0.85415I$ $a = 1.301240 + 0.517704I$ $b = -1.377880 + 0.171851I$	$6.06357 - 0.24294I$	0
$u = -0.519849 + 0.164047I$ $a = 0.450371 - 1.093590I$ $b = -0.846987 - 0.697488I$	$-3.45249 + 2.84406I$	$4.47320 - 0.13726I$
$u = -0.519849 - 0.164047I$ $a = 0.450371 + 1.093590I$ $b = -0.846987 + 0.697488I$	$-3.45249 - 2.84406I$	$4.47320 + 0.13726I$
$u = 1.41620 + 0.50567I$ $a = 1.34430 - 0.47999I$ $b = -1.224820 - 0.174181I$	$5.55672 + 2.02988I$	0
$u = 1.41620 - 0.50567I$ $a = 1.34430 + 0.47999I$ $b = -1.224820 + 0.174181I$	$5.55672 - 2.02988I$	0
$u = 0.424031 + 0.169720I$ $a = -0.64369 - 1.49877I$ $b = 0.955436 - 0.668372I$	$1.04456 - 7.10521I$	$8.98695 + 2.40068I$
$u = 0.424031 - 0.169720I$ $a = -0.64369 + 1.49877I$ $b = 0.955436 + 0.668372I$	$1.04456 + 7.10521I$	$8.98695 - 2.40068I$
$u = -1.31349 + 0.85071I$ $a = -1.33743 - 0.50145I$ $b = 1.370090 - 0.136727I$	$2.50861 - 3.91557I$	0
$u = -1.31349 - 0.85071I$ $a = -1.33743 + 0.50145I$ $b = 1.370090 + 0.136727I$	$2.50861 + 3.91557I$	0

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.61282 + 0.23864I$ $a = 1.139110 - 0.485015I$ $b = -0.913482 - 0.085334I$	$6.06357 + 3.81683I$	0
$u = 1.61282 - 0.23864I$ $a = 1.139110 + 0.485015I$ $b = -0.913482 + 0.085334I$	$6.06357 - 3.81683I$	0
$u = 1.40460 + 0.87274I$ $a = 1.35323 - 0.49733I$ $b = -1.372800 - 0.107076I$	$6.82360 + 7.74416I$	0
$u = 1.40460 - 0.87274I$ $a = 1.35323 + 0.49733I$ $b = -1.372800 + 0.107076I$	$6.82360 - 7.74416I$	0
$u = -1.66385 + 0.33543I$ $a = -1.205150 - 0.530920I$ $b = 1.017220 - 0.027464I$	$2.50861 - 0.14420I$	0
$u = -1.66385 - 0.33543I$ $a = -1.205150 + 0.530920I$ $b = 1.017220 + 0.027464I$	$2.50861 + 0.14420I$	0
$u = -1.58003 + 0.62693I$ $a = -1.33401 - 0.52932I$ $b = 1.248510 - 0.052716I$	$10.76740 - 2.02988I$	0
$u = -1.58003 - 0.62693I$ $a = -1.33401 + 0.52932I$ $b = 1.248510 + 0.052716I$	$10.76740 + 2.02988I$	0
$u = 0.028590 + 0.292450I$ $a = -1.57989 - 2.10875I$ $b = -1.187800 + 0.128492I$	$7.08808 - 1.19685I$	$13.05526 + 0.16546I$
$u = 0.028590 - 0.292450I$ $a = -1.57989 + 2.10875I$ $b = -1.187800 - 0.128492I$	$7.08808 + 1.19685I$	$13.05526 - 0.16546I$

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.71352 + 0.39093I$	$6.82360 - 3.68439I$	0
$a = 1.234100 - 0.563121I$		
$b = -1.066340 + 0.019440I$		
$u = 1.71352 - 0.39093I$	$6.82360 + 3.68439I$	0
$a = 1.234100 + 0.563121I$		
$b = -1.066340 - 0.019440I$		

$$\text{III. } I_3^u = \langle b + u, 2u^{19} + 2u^{18} + \dots + a - 4, u^{20} + u^{19} + \dots - 4u - 1 \rangle$$

(i) Arc colorings

$$\begin{aligned} a_1 &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_8 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_3 &= \begin{pmatrix} -2u^{19} - 2u^{18} + \dots - 3u + 4 \\ -u \end{pmatrix} \\ a_9 &= \begin{pmatrix} 1 \\ -u^2 \end{pmatrix} \\ a_7 &= \begin{pmatrix} u^{18} + u^{17} + \dots + 4u + 3 \\ u^2 \end{pmatrix} \\ a_2 &= \begin{pmatrix} -u^{19} - u^{18} + \dots - 23u^2 + 4 \\ u^3 - u \end{pmatrix} \\ a_6 &= \begin{pmatrix} u^4 - 3u^2 + 2 \\ u^{18} + u^{17} + \dots + 4u + 1 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} u^8 - 5u^6 + 9u^4 - 6u^2 + 1 \\ -u^{18} - u^{17} + \dots - 8u - 2 \end{pmatrix} \\ a_{12} &= \begin{pmatrix} -u \\ u \end{pmatrix} \\ a_4 &= \begin{pmatrix} -u^{19} - u^{18} + \dots - u + 4 \\ -u^{19} - u^{18} + \dots - 4u^2 - 3u \end{pmatrix} \\ a_{11} &= \begin{pmatrix} u^{19} + u^{18} + \dots - 2u - 4 \\ u^5 - 2u^3 + 2u \end{pmatrix} \\ a_5 &= \begin{pmatrix} -u^{18} - u^{17} + \dots - 4u + 4 \\ 2u^{18} + 2u^{17} + \dots + 8u + 2 \end{pmatrix} \end{aligned}$$

(ii) Obstruction class = 1

$$\text{(iii) Cusp Shapes} = -u^{19} - 7u^{18} + 3u^{17} + 65u^{16} + 20u^{15} - 268u^{14} - 151u^{13} + 623u^{12} + 438u^{11} - 868u^{10} - 705u^9 + 708u^8 + 674u^7 - 305u^6 - 385u^5 + 57u^4 + 140u^3 - 34u - 7$$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_{11}$	$u^{20} + u^{19} + \dots - 2u + 1$
$c_2, c_8$	$u^{20} + u^{19} + \dots - 4u - 1$
$c_3$	$u^{20} + 2u^{19} + \dots - u + 1$
$c_4, c_5$	$u^{20} - u^{19} + \dots + u - 1$
$c_6$	$u^{20} + 3u^{19} + \dots + 3u + 1$
$c_7, c_{12}$	$u^{20} - u^{19} + \dots + 4u - 1$
$c_9$	$u^{20} - 3u^{19} + \dots - 3u + 1$
$c_{10}$	$u^{20} + u^{19} + \dots - u - 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_{11}$	$y^{20} + y^{19} + \dots - 6y + 1$
$c_2, c_7, c_8$ $c_{12}$	$y^{20} - 21y^{19} + \dots - 20y + 1$
$c_3$	$y^{20} - 6y^{19} + \dots + y + 1$
$c_4, c_5, c_{10}$	$y^{20} - 19y^{19} + \dots + 13y + 1$
$c_6, c_9$	$y^{20} + 9y^{19} + \dots + 7y + 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.668831 + 0.463717I$ $a = 0.572743 + 0.372465I$ $b = 0.668831 - 0.463717I$	$0.99019 - 8.34686I$	$8.11381 + 8.96345I$
$u = -0.668831 - 0.463717I$ $a = 0.572743 - 0.372465I$ $b = 0.668831 + 0.463717I$	$0.99019 + 8.34686I$	$8.11381 - 8.96345I$
$u = 1.258910 + 0.181820I$ $a = 1.99407 - 0.63175I$ $b = -1.258910 - 0.181820I$	$9.55967 + 0.46214I$	$14.09005 - 0.25844I$
$u = 1.258910 - 0.181820I$ $a = 1.99407 + 0.63175I$ $b = -1.258910 + 0.181820I$	$9.55967 - 0.46214I$	$14.09005 + 0.25844I$
$u = 0.725943$ $a = -2.18632$ $b = -0.725943$	$6.91929$	$-11.6540$
$u = -1.236350 + 0.313248I$ $a = -1.46303 - 0.54202I$ $b = 1.236350 - 0.313248I$	$4.72409 - 1.84698I$	$6.40432 + 0.80024I$
$u = -1.236350 - 0.313248I$ $a = -1.46303 + 0.54202I$ $b = 1.236350 + 0.313248I$	$4.72409 + 1.84698I$	$6.40432 - 0.80024I$
$u = 1.204020 + 0.427966I$ $a = 1.139070 - 0.304352I$ $b = -1.204020 - 0.427966I$	$8.43027 + 3.23489I$	$15.8353 - 3.8708I$
$u = 1.204020 - 0.427966I$ $a = 1.139070 + 0.304352I$ $b = -1.204020 + 0.427966I$	$8.43027 - 3.23489I$	$15.8353 + 3.8708I$
$u = 0.578178 + 0.423999I$ $a = -0.840664 + 0.576748I$ $b = -0.578178 - 0.423999I$	$-3.69104 + 4.05229I$	$2.53314 - 6.60174I$

Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.578178 - 0.423999I$ $a = -0.840664 - 0.576748I$ $b = -0.578178 + 0.423999I$	$-3.69104 - 4.05229I$	$2.53314 + 6.60174I$
$u = -1.38058 + 0.41854I$ $a = -1.51557 - 0.07010I$ $b = 1.38058 - 0.41854I$	$6.22565 + 1.09815I$	$12.16495 - 2.52978I$
$u = -1.38058 - 0.41854I$ $a = -1.51557 + 0.07010I$ $b = 1.38058 + 0.41854I$	$6.22565 - 1.09815I$	$12.16495 + 2.52978I$
$u = 1.39961 + 0.36809I$ $a = 1.61183 - 0.11089I$ $b = -1.39961 - 0.36809I$	$2.44488 + 2.56909I$	$7.07712 - 1.16744I$
$u = 1.39961 - 0.36809I$ $a = 1.61183 + 0.11089I$ $b = -1.39961 + 0.36809I$	$2.44488 - 2.56909I$	$7.07712 + 1.16744I$
$u = -0.421666 + 0.351150I$ $a = 1.27891 + 1.05193I$ $b = 0.421666 - 0.351150I$	$-0.757748 + 0.237341I$	$4.04858 + 0.92208I$
$u = -0.421666 - 0.351150I$ $a = 1.27891 - 1.05193I$ $b = 0.421666 + 0.351150I$	$-0.757748 - 0.237341I$	$4.04858 - 0.92208I$
$u = -1.42948 + 0.32689I$ $a = -1.70399 - 0.10936I$ $b = 1.42948 - 0.32689I$	$6.63079 - 6.29581I$	$12.13979 + 4.17305I$
$u = -1.42948 - 0.32689I$ $a = -1.70399 + 0.10936I$ $b = 1.42948 + 0.32689I$	$6.63079 + 6.29581I$	$12.13979 - 4.17305I$
$u = -0.333578$ $a = 3.03956$ $b = 0.333578$	$-0.365832$	$0.839520$



#### IV. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1, c_{11}$	$(u^{20} + u^{19} + \dots - 2u + 1)(u^{40} + u^{39} + \dots - 14u + 1)$ $\cdot (u^{72} - 19u^{71} + \dots + 178u + 13)$
$c_2, c_8$	$(u^{20} + u^{19} + \dots - 4u - 1)(u^{40} + u^{39} + \dots - 2u + 1)$ $\cdot (u^{72} - u^{71} + \dots - 10866u + 3667)$
$c_3$	$((u^2 - u + 1)^{36})(u^{20} + 2u^{19} + \dots - u + 1)$ $\cdot (u^{40} + 35u^{39} + \dots + 4063232u + 262144)$
$c_4, c_5$	$((u^{18} + u^{17} + \dots - u - 1)^4)(u^{20} - u^{19} + \dots + u - 1)$ $\cdot (u^{40} - 6u^{39} + \dots + 14u + 4)$
$c_6$	$((u^{18} - 3u^{17} + \dots - 3u + 3)^4)(u^{20} + 3u^{19} + \dots + 3u + 1)$ $\cdot (u^{40} + 18u^{39} + \dots - 286u - 52)$
$c_7, c_{12}$	$(u^{20} - u^{19} + \dots + 4u - 1)(u^{40} + u^{39} + \dots - 2u + 1)$ $\cdot (u^{72} - u^{71} + \dots - 10866u + 3667)$
$c_9$	$((u^{18} - 3u^{17} + \dots - 3u + 3)^4)(u^{20} - 3u^{19} + \dots - 3u + 1)$ $\cdot (u^{40} + 18u^{39} + \dots - 286u - 52)$
$c_{10}$	$((u^{18} + u^{17} + \dots - u - 1)^4)(u^{20} + u^{19} + \dots - u - 1)$ $\cdot (u^{40} - 6u^{39} + \dots + 14u + 4)$

### V. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1, c_{11}$	$(y^{20} + y^{19} + \dots - 6y + 1)(y^{40} - 17y^{39} + \dots - 104y + 1)$ $\cdot (y^{72} + 11y^{71} + \dots - 11560y + 169)$
$c_2, c_7, c_8$ $c_{12}$	$(y^{20} - 21y^{19} + \dots - 20y + 1)(y^{40} - 27y^{39} + \dots - 6y + 1)$ $\cdot (y^{72} - 57y^{71} + \dots - 103020588y + 13446889)$
$c_3$	$((y^2 + y + 1)^{36})(y^{20} - 6y^{19} + \dots + y + 1)$ $\cdot (y^{40} - 5y^{39} + \dots - 738734374912y + 68719476736)$
$c_4, c_5, c_{10}$	$((y^{18} - 15y^{17} + \dots - 7y + 1)^4)(y^{20} - 19y^{19} + \dots + 13y + 1)$ $\cdot (y^{40} - 34y^{39} + \dots - 76y + 16)$
$c_6, c_9$	$((y^{18} + 13y^{17} + \dots - 75y + 9)^4)(y^{20} + 9y^{19} + \dots + 7y + 1)$ $\cdot (y^{40} + 22y^{39} + \dots - 227084y + 2704)$