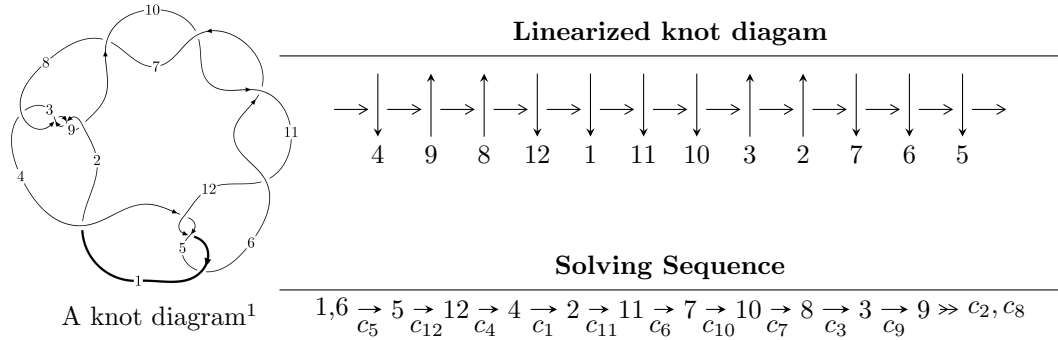


12a<sub>1165</sub> (K12a<sub>1165</sub>)



**Ideals for irreducible components<sup>2</sup> of  $X_{\text{par}}$**

$$I_1^u = \langle u^{33} + u^{32} + \dots + u + 1 \rangle$$

\* 1 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 33 representations.

<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\text{I. } I_1^u = \langle u^{33} + u^{32} + \dots + u + 1 \rangle$$

(i) Arc colorings

$$\begin{aligned} a_1 &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_6 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_5 &= \begin{pmatrix} 1 \\ -u^2 \end{pmatrix} \\ a_{12} &= \begin{pmatrix} u \\ -u^3 + u \end{pmatrix} \\ a_4 &= \begin{pmatrix} -u^2 + 1 \\ u^4 - 2u^2 \end{pmatrix} \\ a_2 &= \begin{pmatrix} -u^5 + 2u^3 - u \\ u^7 - 3u^5 + 2u^3 + u \end{pmatrix} \\ a_{11} &= \begin{pmatrix} -u^3 + 2u \\ -u^3 + u \end{pmatrix} \\ a_7 &= \begin{pmatrix} u^6 - 3u^4 + 2u^2 + 1 \\ u^6 - 2u^4 + u^2 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} -u^9 + 4u^7 - 5u^5 + 3u \\ -u^9 + 3u^7 - 3u^5 + u \end{pmatrix} \\ a_8 &= \begin{pmatrix} u^{12} - 5u^{10} + 9u^8 - 4u^6 - 6u^4 + 5u^2 + 1 \\ u^{12} - 4u^{10} + 6u^8 - 2u^6 - 3u^4 + 2u^2 \end{pmatrix} \\ a_3 &= \begin{pmatrix} -u^{28} + 11u^{26} + \dots + 3u^2 + 1 \\ -u^{28} + 10u^{26} + \dots + 9u^4 - 2u^2 \end{pmatrix} \\ a_9 &= \begin{pmatrix} u^{21} - 8u^{19} + \dots - 4u^3 + 3u \\ -u^{23} + 9u^{21} + \dots + 4u^3 + u \end{pmatrix} \end{aligned}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes

$$\begin{aligned} &= 4u^{30} - 44u^{28} + 4u^{27} + 216u^{26} - 40u^{25} - 592u^{24} + 176u^{23} + 892u^{22} - 420u^{21} - \\ &420u^{20} + 508u^{19} - 948u^{18} - 52u^{17} + 1812u^{16} - 716u^{15} - 808u^{14} + 840u^{13} - 896u^{12} - \\ &64u^{11} + 1080u^{10} - 520u^9 - 56u^8 + 264u^7 - 352u^6 + 96u^5 + 64u^4 - 64u^3 + 48u^2 - 16u - 2 \end{aligned}$$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_6, c_7$ $c_{10}, c_{11}$	$u^{33} - 3u^{32} + \dots + 9u - 3$
$c_2, c_3, c_8$ $c_9$	$u^{33} + u^{32} + \dots + u + 1$
$c_4, c_5, c_{12}$	$u^{33} + u^{32} + \dots + u + 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_6, c_7$ $c_{10}, c_{11}$	$y^{33} + 43y^{32} + \dots - 15y - 9$
$c_2, c_3, c_8$ $c_9$	$y^{33} + 35y^{32} + \dots - 7y - 1$
$c_4, c_5, c_{12}$	$y^{33} - 25y^{32} + \dots - 7y - 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.007187 + 0.927489I$	$13.69600 + 2.31895I$	$1.75304 - 2.85786I$
$u = -0.007187 - 0.927489I$	$13.69600 - 2.31895I$	$1.75304 + 2.85786I$
$u = 0.022659 + 0.925236I$	$7.06487 - 5.65946I$	$-1.58265 + 2.87323I$
$u = 0.022659 - 0.925236I$	$7.06487 + 5.65946I$	$-1.58265 - 2.87323I$
$u = 1.089610 + 0.294783I$	$-5.38539 + 0.42351I$	$-5.40857 + 0.36274I$
$u = 1.089610 - 0.294783I$	$-5.38539 - 0.42351I$	$-5.40857 - 0.36274I$
$u = -1.14314$	$-2.30256$	$-1.78270$
$u = -1.182680 + 0.290002I$	$0.43739 + 1.77292I$	$-1.59025 - 0.21543I$
$u = -1.182680 - 0.290002I$	$0.43739 - 1.77292I$	$-1.59025 + 0.21543I$
$u = 1.234350 + 0.088067I$	$-4.21894 - 1.97469I$	$-11.37360 + 5.72658I$
$u = 1.234350 - 0.088067I$	$-4.21894 + 1.97469I$	$-11.37360 - 5.72658I$
$u = 1.244790 + 0.290367I$	$-0.08256 - 5.33404I$	$-3.84371 + 7.86352I$
$u = 1.244790 - 0.290367I$	$-0.08256 + 5.33404I$	$-3.84371 - 7.86352I$
$u = 0.124967 + 0.695815I$	$-2.55035 - 4.09733I$	$-2.17456 + 4.30313I$
$u = 0.124967 - 0.695815I$	$-2.55035 + 4.09733I$	$-2.17456 - 4.30313I$
$u = -1.303370 + 0.091971I$	$-11.41980 + 2.77587I$	$-12.69893 - 3.54173I$
$u = -1.303370 - 0.091971I$	$-11.41980 - 2.77587I$	$-12.69893 + 3.54173I$
$u = -0.042773 + 0.691881I$	$3.85716 + 1.79630I$	$2.14795 - 4.42092I$
$u = -0.042773 - 0.691881I$	$3.85716 - 1.79630I$	$2.14795 + 4.42092I$
$u = -1.290570 + 0.282135I$	$-6.93611 + 7.59600I$	$-7.80083 - 6.53721I$
$u = -1.290570 - 0.282135I$	$-6.93611 - 7.59600I$	$-7.80083 + 6.53721I$
$u = 1.271570 + 0.457494I$	$3.19600 + 0.72997I$	$-4.74001 + 0.15304I$
$u = 1.271570 - 0.457494I$	$3.19600 - 0.72997I$	$-4.74001 - 0.15304I$
$u = -1.285040 + 0.453763I$	$9.72993 + 2.60735I$	$-1.44806 - 0.13745I$
$u = -1.285040 - 0.453763I$	$9.72993 - 2.60735I$	$-1.44806 + 0.13745I$
$u = 1.296000 + 0.449004I$	$9.64446 - 7.23064I$	$-1.69264 + 5.79671I$
$u = 1.296000 - 0.449004I$	$9.64446 + 7.23064I$	$-1.69264 - 5.79671I$
$u = -1.306320 + 0.442632I$	$2.92604 + 10.54330I$	$-5.09643 - 5.66423I$
$u = -1.306320 - 0.442632I$	$2.92604 - 10.54330I$	$-5.09643 + 5.66423I$
$u = 0.391381 + 0.352338I$	$-6.35493 - 1.38874I$	$-6.74266 + 4.47575I$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.391381 - 0.352338I$	$-6.35493 + 1.38874I$	$-6.74266 - 4.47575I$
$u = -0.185818 + 0.264071I$	$-0.115512 + 0.725231I$	$-3.81673 - 9.57308I$
$u = -0.185818 - 0.264071I$	$-0.115512 - 0.725231I$	$-3.81673 + 9.57308I$

## II. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1, c_6, c_7$ $c_{10}, c_{11}$	$u^{33} - 3u^{32} + \dots + 9u - 3$
$c_2, c_3, c_8$ $c_9$	$u^{33} + u^{32} + \dots + u + 1$
$c_4, c_5, c_{12}$	$u^{33} + u^{32} + \dots + u + 1$

### III. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1, c_6, c_7$ $c_{10}, c_{11}$	$y^{33} + 43y^{32} + \dots - 15y - 9$
$c_2, c_3, c_8$ $c_9$	$y^{33} + 35y^{32} + \dots - 7y - 1$
$c_4, c_5, c_{12}$	$y^{33} - 25y^{32} + \dots - 7y - 1$