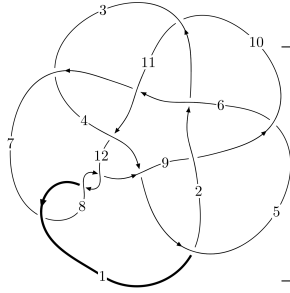
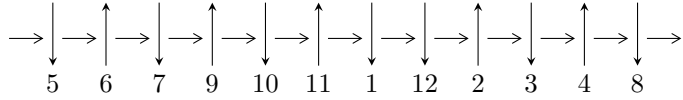


12a<sub>1213</sub> (K12a<sub>1213</sub>)



A knot diagram<sup>1</sup>

**Linearized knot diagram**



**Solving Sequence**

$$6, 11 \xrightarrow{c_6} 3, 7 \xrightarrow{c_3} 4 \xrightarrow{c_{11}} 12 \xrightarrow{c_2} 2 \xrightarrow{c_{10}} 10 \xrightarrow{c_5} 5 \xrightarrow{c_1} 1 \xrightarrow{c_9} 9 \xrightarrow{c_8} 8 \rightsquigarrow c_4, c_7, c_{12}$$

**Ideals for irreducible components<sup>2</sup> of  $X_{\text{par}}$**

$$\begin{aligned}
 I_1^u &= \langle -2.38072 \times 10^{36} u^{34} + 2.10788 \times 10^{36} u^{33} + \dots + 2.31436 \times 10^{37} b - 1.18052 \times 10^{37}, \\
 &\quad 1.34556 \times 10^{38} u^{34} + 1.19595 \times 10^{38} u^{33} + \dots + 2.31436 \times 10^{37} a + 9.18534 \times 10^{38}, u^{35} + u^{34} + \dots + 8u + 1 \rangle \\
 I_2^u &= \langle -1.95779 \times 10^{17} u^{24} + 2.57330 \times 10^{16} u^{23} + \dots + 3.09631 \times 10^{18} b + 3.53328 \times 10^{18}, \\
 &\quad -1.02595 \times 10^{18} u^{24} + 1.39827 \times 10^{18} u^{23} + \dots + 1.23853 \times 10^{19} a + 2.15965 \times 10^{19}, u^{25} - u^{24} + \dots - 8u - \\
 I_3^u &= \langle 6.80801 \times 10^{870} u^{115} - 1.02067 \times 10^{872} u^{114} + \dots + 2.89851 \times 10^{874} b + 3.50026 \times 10^{875}, \\
 &\quad -3.25101 \times 10^{874} u^{115} + 2.16113 \times 10^{875} u^{114} + \dots + 1.53436 \times 10^{879} a + 1.14628 \times 10^{881}, \\
 &\quad u^{116} - 15u^{115} + \dots - 417760u + 52936 \rangle
 \end{aligned}$$

\* 3 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 176 representations.

<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

I.

$$I_1^u = \langle -2.38 \times 10^{36} u^{34} + 2.11 \times 10^{36} u^{33} + \dots + 2.31 \times 10^{37} b - 1.18 \times 10^{37}, 1.35 \times 10^{38} u^{34} + 1.20 \times 10^{38} u^{33} + \dots + 2.31 \times 10^{37} a + 9.19 \times 10^{38}, u^{35} + u^{34} + \dots + 8u + 1 \rangle$$

(i) Arc colorings

$$\begin{aligned} a_6 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_{11} &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_3 &= \begin{pmatrix} -5.81398u^{34} - 5.16753u^{33} + \dots - 72.6444u - 39.6884 \\ 0.102867u^{34} - 0.0910783u^{33} + \dots - 3.09658u + 0.510083 \end{pmatrix} \\ a_7 &= \begin{pmatrix} 1 \\ -u^2 \end{pmatrix} \\ a_4 &= \begin{pmatrix} -5.70378u^{34} - 4.93508u^{33} + \dots - 70.1903u - 39.5521 \\ 0.182861u^{34} + 0.0177861u^{33} + \dots - 2.00831u + 0.632342 \end{pmatrix} \\ a_{12} &= \begin{pmatrix} -33.5755u^{34} - 29.3518u^{33} + \dots - 371.933u - 214.961 \\ 0.712298u^{34} + 0.384179u^{33} + \dots + 4.97991u + 5.59420 \end{pmatrix} \\ a_2 &= \begin{pmatrix} -5.91684u^{34} - 5.07645u^{33} + \dots - 69.5478u - 40.1985 \\ 0.102867u^{34} - 0.0910783u^{33} + \dots - 3.09658u + 0.510083 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} -33.5988u^{34} - 29.1991u^{33} + \dots - 363.943u - 212.176 \\ 0.646444u^{34} + 0.433382u^{33} + \dots + 6.82336u + 5.81398 \end{pmatrix} \\ a_5 &= \begin{pmatrix} 183.007u^{34} + 155.083u^{33} + \dots + 1861.33u + 1147.00 \\ -4.39975u^{34} - 3.75957u^{33} + \dots - 56.6144u - 33.5988 \end{pmatrix} \\ a_1 &= \begin{pmatrix} 24.6736u^{34} + 19.7265u^{33} + \dots + 217.291u + 153.213 \\ -1.01831u^{34} - 1.24880u^{33} + \dots - 18.6808u - 5.81082 \end{pmatrix} \\ a_9 &= \begin{pmatrix} -34.4392u^{34} - 29.7788u^{33} + \dots - 371.080u - 218.093 \\ 0.840389u^{34} + 0.579717u^{33} + \dots + 7.13622u + 5.91684 \end{pmatrix} \\ a_8 &= \begin{pmatrix} -17.5414u^{34} - 15.2732u^{33} + \dots - 157.692u - 91.1189 \\ -0.242519u^{34} - 0.107367u^{33} + \dots + 8.50491u + 3.47843 \end{pmatrix} \end{aligned}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes =  $-68.4106u^{34} - 55.3484u^{33} + \dots - 679.743u - 457.303$

(iv) u-Polynomials at the component

| Crossings          | u-Polynomials at each crossing              |
|--------------------|---|
| $c_1, c_3$         | $u^{35} - 3u^{34} + \dots + 13u - 1$        |
| $c_2$              | $u^{35} - 25u^{34} + \dots + 24576u - 2048$ |
| $c_4, c_{11}$      | $u^{35} + 7u^{34} + \dots - 3u + 1$         |
| $c_5, c_{10}$      | $u^{35} + 5u^{34} + \dots - 3u + 1$         |
| $c_6, c_9$         | $u^{35} - u^{34} + \dots + 8u - 1$          |
| $c_7, c_8, c_{12}$ | $u^{35} + 11u^{34} + \dots + 384u + 32$     |

(v) Riley Polynomials at the component

| Crossings          | Riley Polynomials at each crossing                |
|--------------------|---|
| $c_1, c_3$         | $y^{35} + 11y^{34} + \dots + 29y - 1$             |
| $c_2$              | $y^{35} + 15y^{34} + \dots - 90177536y - 4194304$ |
| $c_4, c_{11}$      | $y^{35} - 51y^{34} + \dots + 35y - 1$             |
| $c_5, c_{10}$      | $y^{35} - 39y^{34} + \dots + 27y - 1$             |
| $c_6, c_9$         | $y^{35} - y^{34} + \dots + 28y - 1$               |
| $c_7, c_8, c_{12}$ | $y^{35} + 31y^{34} + \dots - 7680y - 1024$        |

(vi) Complex Volumes and Cusp Shapes

| Solutions to $I_1^u$  | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape            |
|---|---------------------------------------|-----------------------|
| $u = -0.473191 + 0.955601I$<br>$a = 0.164857 - 0.773336I$<br>$b = 0.73632 - 1.23689I$   | $-0.87815 - 2.10009I$                 | $-6.29124 + 3.74115I$ |
| $u = -0.473191 - 0.955601I$<br>$a = 0.164857 + 0.773336I$<br>$b = 0.73632 + 1.23689I$   | $-0.87815 + 2.10009I$                 | $-6.29124 - 3.74115I$ |
| $u = -0.561860 + 0.934680I$<br>$a = 0.721974 + 0.705652I$<br>$b = 0.291621 + 0.692365I$ | $2.74039 + 5.52452I$                  | $-2.61115 - 4.68081I$ |
| $u = -0.561860 - 0.934680I$<br>$a = 0.721974 - 0.705652I$<br>$b = 0.291621 - 0.692365I$ | $2.74039 - 5.52452I$                  | $-2.61115 + 4.68081I$ |
| $u = 0.728850 + 0.833231I$<br>$a = 0.690527 - 0.506887I$<br>$b = 0.058923 - 0.690806I$  | $-2.68642 - 1.48594I$                 | $-5.76171 + 5.39125I$ |
| $u = 0.728850 - 0.833231I$<br>$a = 0.690527 + 0.506887I$<br>$b = 0.058923 + 0.690806I$  | $-2.68642 + 1.48594I$                 | $-5.76171 - 5.39125I$ |
| $u = 0.486606 + 1.044960I$<br>$a = 0.195291 - 0.498321I$<br>$b = 0.31826 - 1.73957I$    | $-0.68127 + 1.41250I$                 | $-3.06396 - 1.29126I$ |
| $u = 0.486606 - 1.044960I$<br>$a = 0.195291 + 0.498321I$<br>$b = 0.31826 + 1.73957I$    | $-0.68127 - 1.41250I$                 | $-3.06396 + 1.29126I$ |
| $u = -0.798627 + 0.123489I$<br>$a = -0.533379 - 0.839803I$<br>$b = 1.53890 - 0.84849I$  | $10.09970 - 2.57123I$                 | $7.26146 + 7.35567I$  |
| $u = -0.798627 - 0.123489I$<br>$a = -0.533379 + 0.839803I$<br>$b = 1.53890 + 0.84849I$  | $10.09970 + 2.57123I$                 | $7.26146 - 7.35567I$  |

| Solutions to $I_1^u$   | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape            |
|--|---------------------------------------|-----------------------|
| $u = -0.300719 + 0.744013I$<br>$a = 0.189534 + 0.400172I$<br>$b = 0.03329 + 2.04106I$    | $7.92447 + 1.85760I$                  | $-9.7550 - 10.3352I$  |
| $u = -0.300719 - 0.744013I$<br>$a = 0.189534 - 0.400172I$<br>$b = 0.03329 - 2.04106I$    | $7.92447 - 1.85760I$                  | $-9.7550 + 10.3352I$  |
| $u = -0.663483 + 1.024170I$<br>$a = 0.189870 + 0.547409I$<br>$b = 0.43442 + 1.63061I$    | $-1.65342 - 7.27417I$                 | $-5.53901 + 7.92193I$ |
| $u = -0.663483 - 1.024170I$<br>$a = 0.189870 - 0.547409I$<br>$b = 0.43442 - 1.63061I$    | $-1.65342 + 7.27417I$                 | $-5.53901 - 7.92193I$ |
| $u = -1.023220 + 0.684265I$<br>$a = 0.615312 + 0.295804I$<br>$b = -0.320104 + 0.634624I$ | $-0.17224 - 3.30186I$                 | $4.00752 - 4.42363I$  |
| $u = -1.023220 - 0.684265I$<br>$a = 0.615312 - 0.295804I$<br>$b = -0.320104 - 0.634624I$ | $-0.17224 + 3.30186I$                 | $4.00752 + 4.42363I$  |
| $u = 0.748659 + 0.978142I$<br>$a = 0.165026 - 0.583693I$<br>$b = 0.55147 - 1.58642I$     | $4.79967 + 11.80520I$                 | $-2.00000 - 8.67473I$ |
| $u = 0.748659 - 0.978142I$<br>$a = 0.165026 + 0.583693I$<br>$b = 0.55147 + 1.58642I$     | $4.79967 - 11.80520I$                 | $-2.00000 + 8.67473I$ |
| $u = 0.894095 + 0.973220I$<br>$a = -0.088879 + 0.809478I$<br>$b = 1.13402 + 1.22065I$    | $0.21423 + 7.00365I$                  | $0. - 4.77334I$       |
| $u = 0.894095 - 0.973220I$<br>$a = -0.088879 - 0.809478I$<br>$b = 1.13402 - 1.22065I$    | $0.21423 - 7.00365I$                  | $0. + 4.77334I$       |

| Solutions to $I_1^u$   | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape            |
|--|---------------------------------------|-----------------------|
| $u = 0.599988 + 0.271035I$<br>$a = -0.65464 + 1.47497I$<br>$b = 1.251390 + 0.566406I$    | $3.12898 + 2.04422I$                  | $4.59072 - 3.04484I$  |
| $u = 0.599988 - 0.271035I$<br>$a = -0.65464 - 1.47497I$<br>$b = 1.251390 - 0.566406I$    | $3.12898 - 2.04422I$                  | $4.59072 + 3.04484I$  |
| $u = -0.132382 + 0.519991I$<br>$a = 0.881561 - 0.313861I$<br>$b = -0.006740 - 0.358428I$ | $-0.184960 - 1.127700I$               | $-2.22637 + 6.73061I$ |
| $u = -0.132382 - 0.519991I$<br>$a = 0.881561 + 0.313861I$<br>$b = -0.006740 + 0.358428I$ | $-0.184960 + 1.127700I$               | $-2.22637 - 6.73061I$ |
| $u = -1.24107 + 0.80628I$<br>$a = -0.224566 - 0.903591I$<br>$b = 1.25904 - 1.04232I$     | $10.26990 - 7.64955I$                 | 0                     |
| $u = -1.24107 - 0.80628I$<br>$a = -0.224566 + 0.903591I$<br>$b = 1.25904 + 1.04232I$     | $10.26990 + 7.64955I$                 | 0                     |
| $u = 0.014885 + 0.497734I$<br>$a = 3.54266 - 2.08972I$<br>$b = 0.790590 - 0.123525I$     | $4.73898 + 2.59865I$                  | $-10.3277 - 11.9450I$ |
| $u = 0.014885 - 0.497734I$<br>$a = 3.54266 + 2.08972I$<br>$b = 0.790590 + 0.123525I$     | $4.73898 - 2.59865I$                  | $-10.3277 + 11.9450I$ |
| $u = 1.27290 + 0.91763I$<br>$a = -0.284094 + 0.896949I$<br>$b = 1.32093 + 1.01324I$      | $1.91254 + 10.46930I$                 | 0                     |
| $u = 1.27290 - 0.91763I$<br>$a = -0.284094 - 0.896949I$<br>$b = 1.32093 - 1.01324I$      | $1.91254 - 10.46930I$                 | 0                     |

| Solutions to $I_1^u$   | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|--|---------------------------------------|------------|
| $u = -1.30681 + 0.93603I$<br>$a = -0.298108 - 0.936803I$<br>$b = 1.30845 - 0.96931I$ | $0.8251 - 15.9095I$                   | 0          |
| $u = -1.30681 - 0.93603I$<br>$a = -0.298108 + 0.936803I$<br>$b = 1.30845 + 0.96931I$ | $0.8251 + 15.9095I$                   | 0          |
| $u = 1.33364 + 0.94709I$<br>$a = -0.286932 + 0.961649I$<br>$b = 1.28491 + 0.95487I$  | $7.0349 + 20.2665I$                   | 0          |
| $u = 1.33364 - 0.94709I$<br>$a = -0.286932 - 0.961649I$<br>$b = 1.28491 - 0.95487I$  | $7.0349 - 20.2665I$                   | 0          |
| $u = -0.156518$<br>$a = -34.9720$<br>$b = 1.02859$                                   | 0.541372                              | -424.140   |



II.

$$I_2^u = \langle -1.96 \times 10^{17} u^{24} + 2.57 \times 10^{16} u^{23} + \dots + 3.10 \times 10^{18} b + 3.53 \times 10^{18}, -1.03 \times 10^{18} u^{24} + 1.40 \times 10^{18} u^{23} + \dots + 1.24 \times 10^{19} a + 2.16 \times 10^{19}, u^{25} - u^{24} + \dots - 8u - 8 \rangle$$

(i) Arc colorings

$$\begin{aligned} a_6 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_{11} &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_3 &= \begin{pmatrix} 0.0828360u^{24} - 0.112898u^{23} + \dots - 1.89081u - 1.74372 \\ 0.0632297u^{24} - 0.00831085u^{23} + \dots - 1.12338u - 1.14113 \end{pmatrix} \\ a_7 &= \begin{pmatrix} 1 \\ -u^2 \end{pmatrix} \\ a_4 &= \begin{pmatrix} 0.0237886u^{24} - 0.0967624u^{23} + \dots - 1.18962u - 0.362102 \\ 0.0366311u^{24} - 0.0217545u^{23} + \dots - 0.307708u - 0.797832 \end{pmatrix} \\ a_{12} &= \begin{pmatrix} 0.0181137u^{24} - 0.00463381u^{23} + \dots - 1.87039u + 0.341855 \\ 0.0143600u^{24} - 0.0438065u^{23} + \dots + 1.45977u - 0.114605 \end{pmatrix} \\ a_2 &= \begin{pmatrix} 0.0196063u^{24} - 0.104587u^{23} + \dots - 0.767427u - 0.602598 \\ 0.0632297u^{24} - 0.00831085u^{23} + \dots - 1.12338u - 1.14113 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} 0.111772u^{24} - 0.130147u^{23} + \dots - 0.329660u - 0.474602 \\ 0.0300620u^{24} - 0.0258797u^{23} + \dots + 1.08104u - 0.662688 \end{pmatrix} \\ a_5 &= \begin{pmatrix} 0.0470114u^{24} - 0.123522u^{23} + \dots - 3.09053u + 0.235072 \\ 0.0183753u^{24} - 0.0403395u^{23} + \dots - 0.419572u - 0.894174 \end{pmatrix} \\ a_1 &= \begin{pmatrix} 0.0242955u^{24} + 0.00502972u^{23} + \dots + 2.56668u - 1.33845 \\ 0.0211853u^{24} + 0.0698665u^{23} + \dots - 0.0456261u + 0.124634 \end{pmatrix} \\ a_9 &= \begin{pmatrix} 0.0267908u^{24} - 0.0521712u^{23} + \dots - 0.775408u - 0.317751 \\ 0.0849809u^{24} - 0.0779759u^{23} + \dots + 0.445748u - 0.156850 \end{pmatrix} \\ a_8 &= \begin{pmatrix} 0.141789u^{24} - 0.189859u^{23} + \dots - 1.17851u - 1.06959 \\ -0.0355395u^{24} + 0.0698178u^{23} + \dots + 0.631153u - 0.896134 \end{pmatrix} \end{aligned}$$

(ii) Obstruction class = 1

$$\text{(iii) Cusp Shapes} = \frac{2452215208224550567}{12385251064844942024} u^{24} - \frac{846206872359813633}{12385251064844942024} u^{23} + \dots - \frac{8471824635934717355}{3096312766211235506} u - \frac{6668781122666694554}{1548156383105617753}$$

(iv) u-Polynomials at the component

| Crossings     | u-Polynomials at each crossing             |
|---------------|--|
| $c_1, c_3$    | $u^{25} - 3u^{24} + \dots - 40u + 56$      |
| $c_2$         | $u^{25} - 8u^{24} + \dots - 3u - 1$        |
| $c_4, c_{11}$ | $8(8u^{25} + 8u^{24} + \dots + 5u^2 + 1)$  |
| $c_5, c_{10}$ | $8(8u^{25} - 8u^{24} + \dots + 11u^2 - 1)$ |
| $c_6, c_9$    | $u^{25} - u^{24} + \dots - 8u - 8$         |
| $c_7, c_8$    | $u^{25} + 2u^{24} + \dots - 2u + 1$        |
| $c_{12}$      | $u^{25} - 2u^{24} + \dots - 2u - 1$        |

(v) Riley Polynomials at the component

| Crossings          | Riley Polynomials at each crossing           |
|--------------------|--|
| $c_1, c_3$         | $y^{25} - 3y^{24} + \dots + 19072y - 3136$   |
| $c_2$              | $y^{25} + 10y^{24} + \dots + 37y - 1$        |
| $c_4, c_{11}$      | $64(64y^{25} - 448y^{24} + \dots - 10y - 1)$ |
| $c_5, c_{10}$      | $64(64y^{25} - 704y^{24} + \dots + 22y - 1)$ |
| $c_6, c_9$         | $y^{25} - 7y^{24} + \dots + 192y - 64$       |
| $c_7, c_8, c_{12}$ | $y^{25} + 26y^{24} + \dots + 46y - 1$        |

(vi) Complex Volumes and Cusp Shapes

| Solutions to $I_2^u$   | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape            |
|--|---------------------------------------|-----------------------|
| $u = 0.317550 + 0.877564I$<br>$a = -0.229611 + 0.699890I$<br>$b = -0.576807 + 1.289960I$ | $-2.07306 + 0.81237I$                 | $-8.44018 - 1.80632I$ |
| $u = 0.317550 - 0.877564I$<br>$a = -0.229611 - 0.699890I$<br>$b = -0.576807 - 1.289960I$ | $-2.07306 - 0.81237I$                 | $-8.44018 + 1.80632I$ |
| $u = 0.374639 + 0.814667I$<br>$a = -0.133763 - 0.490884I$<br>$b = -0.48326 - 1.89633I$   | $8.08619 - 1.60054I$                  | $4.91227 - 11.32939I$ |
| $u = 0.374639 - 0.814667I$<br>$a = -0.133763 + 0.490884I$<br>$b = -0.48326 + 1.89633I$   | $8.08619 + 1.60054I$                  | $4.91227 + 11.32939I$ |
| $u = -1.10397$<br>$a = -0.450023$<br>$b = 1.22211$                                       | $4.61475$                             | $8.27900$             |
| $u = 1.081950 + 0.250410I$<br>$a = -0.465508 - 0.085599I$<br>$b = 1.077930 - 0.382096I$  | $9.67308 - 1.37757I$                  | $5.79906 + 0.19770I$  |
| $u = 1.081950 - 0.250410I$<br>$a = -0.465508 + 0.085599I$<br>$b = 1.077930 + 0.382096I$  | $9.67308 + 1.37757I$                  | $5.79906 - 0.19770I$  |
| $u = -1.010210 + 0.558270I$<br>$a = -0.685743 - 0.374548I$<br>$b = 0.123193 - 0.613480I$ | $-0.50342 - 3.65382I$                 | $-7.55217 + 7.75024I$ |
| $u = -1.010210 - 0.558270I$<br>$a = -0.685743 + 0.374548I$<br>$b = 0.123193 + 0.613480I$ | $-0.50342 + 3.65382I$                 | $-7.55217 - 7.75024I$ |
| $u = -0.888892 + 0.794377I$<br>$a = 0.20872 + 1.44121I$<br>$b = -1.098420 + 0.679608I$   | $1.26033 - 8.21911I$                  | $0.36152 + 8.38035I$  |

| Solutions to $I_2^u$  | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape             |
|---|---------------------------------------|------------------------|
| $u = -0.888892 - 0.794377I$<br>$a = 0.20872 - 1.44121I$<br>$b = -1.098420 - 0.679608I$    | $1.26033 + 8.21911I$                  | $0.36152 - 8.38035I$   |
| $u = -0.550547 + 1.107680I$<br>$a = -0.133124 + 0.611398I$<br>$b = -0.65999 + 1.56156I$   | $0.01650 - 2.22543I$                  | $4.06322 + 5.84619I$   |
| $u = -0.550547 - 1.107680I$<br>$a = -0.133124 - 0.611398I$<br>$b = -0.65999 - 1.56156I$   | $0.01650 + 2.22543I$                  | $4.06322 - 5.84619I$   |
| $u = -0.768453 + 0.973451I$<br>$a = -0.374681 + 0.879750I$<br>$b = -0.590219 + 0.962163I$ | $6.96474 - 11.65060I$                 | $2.09612 + 9.34091I$   |
| $u = -0.768453 - 0.973451I$<br>$a = -0.374681 - 0.879750I$<br>$b = -0.590219 - 0.962163I$ | $6.96474 + 11.65060I$                 | $2.09612 - 9.34091I$   |
| $u = 0.770593 + 1.061120I$<br>$a = -0.135159 - 0.791525I$<br>$b = -0.79038 - 1.22759I$    | $0.04224 + 8.07532I$                  | $-0.32524 - 11.69521I$ |
| $u = 0.770593 - 1.061120I$<br>$a = -0.135159 + 0.791525I$<br>$b = -0.79038 + 1.22759I$    | $0.04224 - 8.07532I$                  | $-0.32524 + 11.69521I$ |
| $u = 0.671501$<br>$a = -1.58450$<br>$b = -0.368886$                                       | $-3.74850$                            | $-10.8400$             |
| $u = 0.942808 + 0.936636I$<br>$a = 0.128385 - 1.073180I$<br>$b = -1.10990 - 0.91866I$     | $-0.63864 + 8.33929I$                 | $-1.35664 - 7.88306I$  |
| $u = 0.942808 - 0.936636I$<br>$a = 0.128385 + 1.073180I$<br>$b = -1.10990 + 0.91866I$     | $-0.63864 - 8.33929I$                 | $-1.35664 + 7.88306I$  |

| Solutions to $I_2^u$  | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape              |
|---|---------------------------------------|-------------------------|
| $u = -0.370104 + 0.321579I$<br>$a = -1.00930 - 1.83683I$<br>$b = -0.770228 - 0.418162I$ | $-0.07970 - 3.22269I$                 | $-5.25315 + 3.28753I$   |
| $u = -0.370104 - 0.321579I$<br>$a = -1.00930 + 1.83683I$<br>$b = -0.770228 + 0.418162I$ | $-0.07970 + 3.22269I$                 | $-5.25315 - 3.28753I$   |
| $u = -1.52760$<br>$a = -0.771960$<br>$b = 0.295403$                                     | $0.0461358$                           | $-0.00449090$           |
| $u = 1.58070 + 0.12470I$<br>$a = -0.766976 - 0.004982I$<br>$b = 0.303767 - 0.008468I$   | $4.75943 - 0.77091I$                  | $-0.021983 + 0.140884I$ |
| $u = 1.58070 - 0.12470I$<br>$a = -0.766976 + 0.004982I$<br>$b = 0.303767 + 0.008468I$   | $4.75943 + 0.77091I$                  | $-0.021983 - 0.140884I$ |

$$\text{III. } I_3^u = \langle 6.81 \times 10^{870} u^{115} - 1.02 \times 10^{872} u^{114} + \dots + 2.90 \times 10^{874} b + 3.50 \times 10^{875}, -3.25 \times 10^{874} u^{115} + 2.16 \times 10^{875} u^{114} + \dots + 1.53 \times 10^{879} a + 1.15 \times 10^{881}, u^{116} - 15u^{115} + \dots - 417760u + 52936 \rangle$$

(i) Arc colorings

$$a_6 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 0.0000211881u^{115} - 0.000140850u^{114} + \dots + 332.880u - 74.7079 \\ -0.000234880u^{115} + 0.00352137u^{114} + \dots + 149.396u - 12.0761 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 0.000235461u^{115} - 0.00342005u^{114} + \dots + 110.674u - 53.2636 \\ -0.000258566u^{115} + 0.00389995u^{114} + \dots + 187.940u - 15.5229 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 3.09589 \times 10^{-6} u^{115} - 0.000142993u^{114} + \dots - 40.8529u - 28.0315 \\ 0.000275424u^{115} - 0.00411469u^{114} + \dots - 170.695u + 9.50168 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 0.000256068u^{115} - 0.00366222u^{114} + \dots + 183.484u - 62.6318 \\ -0.000234880u^{115} + 0.00352137u^{114} + \dots + 149.396u - 12.0761 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0.0000533118u^{115} - 0.00108371u^{114} + \dots - 344.514u - 5.40386 \\ -0.0000839813u^{115} + 0.00125485u^{114} + \dots + 31.0149u - 7.02085 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 0.000186726u^{115} - 0.00263160u^{114} + \dots + 357.144u - 102.550 \\ 0.000175190u^{115} - 0.00262080u^{114} + \dots - 52.7290u + 4.48737 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 0.0000329485u^{115} - 0.000439958u^{114} + \dots + 99.4761u - 74.2454 \\ -0.000110444u^{115} + 0.00159254u^{114} + \dots + 30.4766u - 5.18938 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 8.31143 \times 10^{-6} u^{115} + 0.0000178873u^{114} + \dots + 299.956u - 42.3593 \\ 0.0000764582u^{115} - 0.00146462u^{114} + \dots - 559.459u + 59.6749 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -0.000299255u^{115} + 0.00442911u^{114} + \dots - 138.230u + 81.9995 \\ 5.30386 \times 10^{-6} u^{115} - 0.000162142u^{114} + \dots - 178.360u + 16.8795 \end{pmatrix}$$

(ii) Obstruction class = -1

$$\text{(iii) Cusp Shapes} = -0.00136918u^{115} + 0.0205831u^{114} + \dots + 475.643u - 0.629277$$

(iv) u-Polynomials at the component

| Crossings          | u-Polynomials at each crossing   |
|--------------------|--|
| $c_1, c_3$         | $u^{116} + 5u^{115} + \dots - 293824u - 18872$                                   |
| $c_2$              | $(u^{58} + 14u^{57} + \dots + 2u + 1)^2$   |
| $c_4, c_{11}$      | $8(8u^{116} + 104u^{115} + \dots - 1.07834 \times 10^8 u + 3.68679 \times 10^7)$ |
| $c_5, c_{10}$      | $8(8u^{116} + 104u^{115} + \dots + 65126u - 4735)$                               |
| $c_6, c_9$         | $u^{116} + 15u^{115} + \dots + 417760u + 52936$                                  |
| $c_7, c_8, c_{12}$ | $(u^{58} - 6u^{57} + \dots - 24u + 1)^2$   |



(v) Riley Polynomials at the component

| Crossings          | Riley Polynomials at each crossing   |
|--------------------|--|
| $c_1, c_3$         | $y^{116} - 93y^{115} + \dots - 74449976896y + 356152384$                                 |
| $c_2$              | $(y^{58} - 14y^{57} + \dots - 132y + 1)^2$   |
| $c_4, c_{11}$      | $64(64y^{116} - 6720y^{115} + \dots - 1.67721 \times 10^{17}y + 1.35924 \times 10^{15})$ |
| $c_5, c_{10}$      | $64(64y^{116} - 5184y^{115} + \dots - 3.55007 \times 10^9y + 2.24202 \times 10^7)$       |
| $c_6, c_9$         | $y^{116} - 105y^{115} + \dots - 367121525120y + 2802220096$                              |
| $c_7, c_8, c_{12}$ | $(y^{58} + 58y^{57} + \dots - 272y + 1)^2$   |

(vi) Complex Volumes and Cusp Shapes

| Solutions to $I_3^u$  | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|---|---------------------------------------|------------|
| $u = -1.01158$<br>$a = -8.79748$<br>$b = 0.0996704$                                       | 0.00210462                            | 0          |
| $u = 0.979940 + 0.270868I$<br>$a = 1.27783 + 0.75838I$<br>$b = -0.673521 - 0.205430I$     | $10.39060 + 0.33751I$                 | 0          |
| $u = 0.979940 - 0.270868I$<br>$a = 1.27783 - 0.75838I$<br>$b = -0.673521 + 0.205430I$     | $10.39060 - 0.33751I$                 | 0          |
| $u = 0.260251 + 0.936468I$<br>$a = 0.995159 + 0.468241I$<br>$b = 0.540330 - 0.147934I$    | $0.160870 - 0.671910I$                | 0          |
| $u = 0.260251 - 0.936468I$<br>$a = 0.995159 - 0.468241I$<br>$b = 0.540330 + 0.147934I$    | $0.160870 + 0.671910I$                | 0          |
| $u = 0.899381 + 0.324843I$<br>$a = 0.02723 + 1.66548I$<br>$b = 0.327313 + 0.897043I$      | $6.88898 - 0.12974I$                  | 0          |
| $u = 0.899381 - 0.324843I$<br>$a = 0.02723 - 1.66548I$<br>$b = 0.327313 - 0.897043I$      | $6.88898 + 0.12974I$                  | 0          |
| $u = 0.500073 + 0.812320I$<br>$a = 1.002650 + 0.655796I$<br>$b = 0.677148 + 0.214687I$    | $4.86393 + 2.30422I$                  | 0          |
| $u = 0.500073 - 0.812320I$<br>$a = 1.002650 - 0.655796I$<br>$b = 0.677148 - 0.214687I$    | $4.86393 - 2.30422I$                  | 0          |
| $u = -0.692472 + 0.649475I$<br>$a = -0.818612 + 0.006859I$<br>$b = -0.767777 - 0.502166I$ | $1.15556 + 5.12365I$                  | 0          |

| Solutions to $I_3^u$  | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|---|---------------------------------------|------------|
| $u = -0.692472 - 0.649475I$<br>$a = -0.818612 - 0.006859I$<br>$b = -0.767777 + 0.502166I$ | $1.15556 - 5.12365I$                  | 0          |
| $u = -0.941152 + 0.094794I$<br>$a = -0.138651 - 0.826278I$<br>$b = 1.013770 - 0.116777I$  | $3.73399 - 1.62934I$                  | 0          |
| $u = -0.941152 - 0.094794I$<br>$a = -0.138651 + 0.826278I$<br>$b = 1.013770 + 0.116777I$  | $3.73399 + 1.62934I$                  | 0          |
| $u = 0.234879 + 0.906360I$<br>$a = 0.130221 + 1.095070I$<br>$b = -0.751053 + 0.970955I$   | $1.50707 + 3.95116I$                  | 0          |
| $u = 0.234879 - 0.906360I$<br>$a = 0.130221 - 1.095070I$<br>$b = -0.751053 - 0.970955I$   | $1.50707 - 3.95116I$                  | 0          |
| $u = -0.817032 + 0.432974I$<br>$a = -0.409960 - 0.596017I$<br>$b = -0.751053 - 0.970955I$ | $1.50707 - 3.95116I$                  | 0          |
| $u = -0.817032 - 0.432974I$<br>$a = -0.409960 + 0.596017I$<br>$b = -0.751053 + 0.970955I$ | $1.50707 + 3.95116I$                  | 0          |
| $u = -0.905748 + 0.165780I$<br>$a = 0.90226 - 1.09537I$<br>$b = -0.704558 + 0.226547I$    | $3.59558 - 3.21071I$                  | 0          |
| $u = -0.905748 - 0.165780I$<br>$a = 0.90226 + 1.09537I$<br>$b = -0.704558 - 0.226547I$    | $3.59558 + 3.21071I$                  | 0          |
| $u = -0.873393 + 0.286666I$<br>$a = 0.212283 + 0.253939I$<br>$b = 1.53643 + 0.52266I$     | $7.01799 - 4.89766I$                  | 0          |

| Solutions to $I_3^u$   | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|--|---------------------------------------|------------|
| $u = -0.873393 - 0.286666I$<br>$a = 0.212283 - 0.253939I$<br>$b = 1.53643 - 0.52266I$    | $7.01799 + 4.89766I$                  | 0          |
| $u = 0.713535 + 0.577768I$<br>$a = 0.63911 - 1.49896I$<br>$b = -0.664418 - 0.629619I$    | $-3.06039 + 2.03547I$                 | 0          |
| $u = 0.713535 - 0.577768I$<br>$a = 0.63911 + 1.49896I$<br>$b = -0.664418 + 0.629619I$    | $-3.06039 - 2.03547I$                 | 0          |
| $u = -0.763410 + 0.771723I$<br>$a = 0.028077 - 1.034150I$<br>$b = 0.559985 - 1.250220I$  | $-0.90262 - 2.33430I$                 | 0          |
| $u = -0.763410 - 0.771723I$<br>$a = 0.028077 + 1.034150I$<br>$b = 0.559985 + 1.250220I$  | $-0.90262 + 2.33430I$                 | 0          |
| $u = 1.078240 + 0.136226I$<br>$a = 2.71578 - 1.12355I$<br>$b = -0.366627 - 0.170388I$    | $5.01112 - 0.52164I$                  | 0          |
| $u = 1.078240 - 0.136226I$<br>$a = 2.71578 + 1.12355I$<br>$b = -0.366627 + 0.170388I$    | $5.01112 + 0.52164I$                  | 0          |
| $u = 0.493381 + 0.764958I$<br>$a = -0.15233 - 1.51824I$<br>$b = -1.115670 - 0.750715I$   | $1.01755 + 6.41344I$                  | 0          |
| $u = 0.493381 - 0.764958I$<br>$a = -0.15233 + 1.51824I$<br>$b = -1.115670 + 0.750715I$   | $1.01755 - 6.41344I$                  | 0          |
| $u = 0.637789 + 0.647820I$<br>$a = -0.356755 + 0.693103I$<br>$b = -0.713517 + 0.945516I$ | $-3.36011 + 2.04094I$                 | 0          |

| Solutions to $I_3^u$   | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|--|---------------------------------------|------------|
| $u = 0.637789 - 0.647820I$<br>$a = -0.356755 - 0.693103I$<br>$b = -0.713517 - 0.945516I$ | $-3.36011 - 2.04094I$                 | 0          |
| $u = -0.898737 + 0.638239I$<br>$a = 0.62169 + 1.30815I$<br>$b = -0.767777 + 0.502166I$   | $1.15556 - 5.12365I$                  | 0          |
| $u = -0.898737 - 0.638239I$<br>$a = 0.62169 - 1.30815I$<br>$b = -0.767777 - 0.502166I$   | $1.15556 + 5.12365I$                  | 0          |
| $u = 1.135380 + 0.122044I$<br>$a = 0.086119 + 0.641099I$<br>$b = 1.026360 + 0.255290I$   | $9.75231 + 4.08244I$                  | 0          |
| $u = 1.135380 - 0.122044I$<br>$a = 0.086119 - 0.641099I$<br>$b = 1.026360 - 0.255290I$   | $9.75231 - 4.08244I$                  | 0          |
| $u = -0.746972 + 0.416669I$<br>$a = -1.49126 + 0.35281I$<br>$b = 1.026360 - 0.255290I$   | $9.75231 - 4.08244I$                  | 0          |
| $u = -0.746972 - 0.416669I$<br>$a = -1.49126 - 0.35281I$<br>$b = 1.026360 + 0.255290I$   | $9.75231 + 4.08244I$                  | 0          |
| $u = -0.843208 + 0.085931I$<br>$a = 0.57492 + 1.43425I$<br>$b = -1.15971 + 0.96631I$     | $9.5516 - 10.5652I$                   | 0          |
| $u = -0.843208 - 0.085931I$<br>$a = 0.57492 - 1.43425I$<br>$b = -1.15971 - 0.96631I$     | $9.5516 + 10.5652I$                   | 0          |
| $u = 0.823622 + 0.011430I$<br>$a = -0.53246 - 2.65982I$<br>$b = 0.432044 - 0.349969I$    | $4.00496 + 0.11590I$                  | 0          |

| Solutions to $I_3^u$  | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape            |
|---|---------------------------------------|-----------------------|
| $u = 0.823622 - 0.011430I$<br>$a = -0.53246 + 2.65982I$<br>$b = 0.432044 + 0.349969I$     | $4.00496 - 0.11590I$                  | 0                     |
| $u = 0.788196 + 0.199185I$<br>$a = 1.06705 + 1.58260I$<br>$b = -0.733347 - 0.206691I$     | $3.00880 + 7.71935I$                  | 0                     |
| $u = 0.788196 - 0.199185I$<br>$a = 1.06705 - 1.58260I$<br>$b = -0.733347 + 0.206691I$     | $3.00880 - 7.71935I$                  | 0                     |
| $u = -0.709071 + 0.962261I$<br>$a = -0.310202 - 0.555623I$<br>$b = -0.690086 - 0.845429I$ | $-0.358848 - 0.399308I$               | 0                     |
| $u = -0.709071 - 0.962261I$<br>$a = -0.310202 + 0.555623I$<br>$b = -0.690086 + 0.845429I$ | $-0.358848 + 0.399308I$               | 0                     |
| $u = -0.751367 + 0.270441I$<br>$a = 1.42199 - 1.70934I$<br>$b = -0.736192 + 0.183930I$    | $9.1239 - 11.3929I$                   | 0                     |
| $u = -0.751367 - 0.270441I$<br>$a = 1.42199 + 1.70934I$<br>$b = -0.736192 - 0.183930I$    | $9.1239 + 11.3929I$                   | 0                     |
| $u = 0.759086 + 0.167333I$<br>$a = -1.038420 - 0.884858I$<br>$b = 1.013770 + 0.116777I$   | $3.73399 + 1.62934I$                  | $0. - 5.11449I$       |
| $u = 0.759086 - 0.167333I$<br>$a = -1.038420 + 0.884858I$<br>$b = 1.013770 - 0.116777I$   | $3.73399 - 1.62934I$                  | $0. + 5.11449I$       |
| $u = -0.153958 + 0.761524I$<br>$a = -0.055312 - 1.198320I$<br>$b = -0.713517 - 0.945516I$ | $-3.36011 - 2.04094I$                 | $-8.79412 + 5.85740I$ |

| Solutions to $I_3^u$  | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape            |
|---|---------------------------------------|-----------------------|
| $u = -0.153958 - 0.761524I$<br>$a = -0.055312 + 1.198320I$<br>$b = -0.713517 + 0.945516I$ | $-3.36011 + 2.04094I$                 | $-8.79412 - 5.85740I$ |
| $u = 0.786939 + 0.941766I$<br>$a = -0.448228 + 0.268724I$<br>$b = -0.664418 + 0.629619I$  | $-3.06039 - 2.03547I$                 | 0                     |
| $u = 0.786939 - 0.941766I$<br>$a = -0.448228 - 0.268724I$<br>$b = -0.664418 - 0.629619I$  | $-3.06039 + 2.03547I$                 | 0                     |
| $u = 0.754748$<br>$a = 0.222173$<br>$b = 1.85662$   | 2.24749                               | 9.28120               |
| $u = -0.757678 + 0.996838I$<br>$a = -0.016211 + 1.208650I$<br>$b = -1.088980 + 0.799671I$ | $-2.18513 - 8.49069I$                 | 0                     |
| $u = -0.757678 - 0.996838I$<br>$a = -0.016211 - 1.208650I$<br>$b = -1.088980 - 0.799671I$ | $-2.18513 + 8.49069I$                 | 0                     |
| $u = -0.256825 + 0.697678I$<br>$a = 0.20777 + 1.57054I$<br>$b = -0.690086 + 0.845429I$    | $-0.358848 + 0.399308I$               | $-2.00000 + 0.I$      |
| $u = -0.256825 - 0.697678I$<br>$a = 0.20777 - 1.57054I$<br>$b = -0.690086 - 0.845429I$    | $-0.358848 - 0.399308I$               | $-2.00000 + 0.I$      |
| $u = 1.022720 + 0.775036I$<br>$a = -0.242532 + 1.097970I$<br>$b = 0.677280 + 1.077370I$   | $-1.81586 + 7.53048I$                 | 0                     |
| $u = 1.022720 - 0.775036I$<br>$a = -0.242532 - 1.097970I$<br>$b = 0.677280 - 1.077370I$   | $-1.81586 - 7.53048I$                 | 0                     |

| Solutions to $I_3^u$   | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape             |
|--|---------------------------------------|------------------------|
| $u = -1.098930 + 0.694343I$<br>$a = 0.325265 + 1.289590I$<br>$b = -1.076520 + 0.823273I$ | $2.54061 - 10.54650I$                 | 0                      |
| $u = -1.098930 - 0.694343I$<br>$a = 0.325265 - 1.289590I$<br>$b = -1.076520 - 0.823273I$ | $2.54061 + 10.54650I$                 | 0                      |
| $u = 1.054200 + 0.808278I$<br>$a = 0.283751 - 1.221210I$<br>$b = -1.088980 - 0.799671I$  | $-2.18513 + 8.49069I$                 | 0                      |
| $u = 1.054200 - 0.808278I$<br>$a = 0.283751 + 1.221210I$<br>$b = -1.088980 + 0.799671I$  | $-2.18513 - 8.49069I$                 | 0                      |
| $u = -1.115170 + 0.723638I$<br>$a = -0.339399 - 1.173380I$<br>$b = 0.681559 - 0.993043I$ | $4.42249 - 11.60810I$                 | 0                      |
| $u = -1.115170 - 0.723638I$<br>$a = -0.339399 + 1.173380I$<br>$b = 0.681559 + 0.993043I$ | $4.42249 + 11.60810I$                 | 0                      |
| $u = -0.578647 + 0.272996I$<br>$a = 0.57081 - 2.37898I$<br>$b = 0.540330 - 0.147934I$    | $0.160870 - 0.671910I$                | $-2.15622 + 10.18820I$ |
| $u = -0.578647 - 0.272996I$<br>$a = 0.57081 + 2.37898I$<br>$b = 0.540330 + 0.147934I$    | $0.160870 + 0.671910I$                | $-2.15622 - 10.18820I$ |
| $u = 0.625939 + 0.130720I$<br>$a = 0.69693 - 1.62006I$<br>$b = -1.27363 - 0.94541I$      | $2.36016 + 7.44357I$                  | $2.72331 - 8.71572I$   |
| $u = 0.625939 - 0.130720I$<br>$a = 0.69693 + 1.62006I$<br>$b = -1.27363 + 0.94541I$      | $2.36016 - 7.44357I$                  | $2.72331 + 8.71572I$   |



| Solutions to $I_3^u$  | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape            |
|---|---------------------------------------|-----------------------|
| $u = -0.533442 + 1.266060I$<br>$a = -0.080396 - 0.396039I$<br>$b = -0.441070 - 0.879956I$ | $-0.767799 - 0.707140I$               | 0                     |
| $u = -0.533442 - 1.266060I$<br>$a = -0.080396 + 0.396039I$<br>$b = -0.441070 + 0.879956I$ | $-0.767799 + 0.707140I$               | 0                     |
| $u = 0.503153 + 0.320623I$<br>$a = 0.813514 + 1.061800I$<br>$b = -1.04228 + 1.32124I$     | $8.59840 + 2.41577I$                  | $10.35447 - 1.07003I$ |
| $u = 0.503153 - 0.320623I$<br>$a = 0.813514 - 1.061800I$<br>$b = -1.04228 - 1.32124I$     | $8.59840 - 2.41577I$                  | $10.35447 + 1.07003I$ |
| $u = -1.12741 + 0.87171I$<br>$a = 0.366742 + 1.095350I$<br>$b = -1.115670 + 0.750715I$    | $1.01755 - 6.41344I$                  | 0                     |
| $u = -1.12741 - 0.87171I$<br>$a = 0.366742 - 1.095350I$<br>$b = -1.115670 - 0.750715I$    | $1.01755 + 6.41344I$                  | 0                     |
| $u = 0.85018 + 1.18672I$<br>$a = -0.035511 - 1.062400I$<br>$b = -1.076520 - 0.823273I$    | $2.54061 + 10.54650I$                 | 0                     |
| $u = 0.85018 - 1.18672I$<br>$a = -0.035511 + 1.062400I$<br>$b = -1.076520 + 0.823273I$    | $2.54061 - 10.54650I$                 | 0                     |
| $u = -1.31779 + 0.75264I$<br>$a = 0.154248 + 0.681986I$<br>$b = -0.704558 + 0.226547I$    | $3.59558 - 3.21071I$                  | 0                     |
| $u = -1.31779 - 0.75264I$<br>$a = 0.154248 - 0.681986I$<br>$b = -0.704558 - 0.226547I$    | $3.59558 + 3.21071I$                  | 0                     |

| Solutions to $I_3^u$        | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape            |
|-----------------------------|---------------------------------------|-----------------------|
| $u = 0.07393 + 1.52551I$    |                                       |                       |
| $a = 0.188483 - 0.440292I$  | $-0.90262 - 2.33430I$                 | 0                     |
| $b = 0.559985 - 1.250220I$  |                                       |                       |
| $u = 0.07393 - 1.52551I$    |                                       |                       |
| $a = 0.188483 + 0.440292I$  | $-0.90262 + 2.33430I$                 | 0                     |
| $b = 0.559985 + 1.250220I$  |                                       |                       |
| $u = 1.24493 + 0.88674I$    |                                       |                       |
| $a = 0.003312 - 0.789661I$  | $3.00880 + 7.71935I$                  | 0                     |
| $b = -0.733347 - 0.206691I$ |                                       |                       |
| $u = 1.24493 - 0.88674I$    |                                       |                       |
| $a = 0.003312 + 0.789661I$  | $3.00880 - 7.71935I$                  | 0                     |
| $b = -0.733347 + 0.206691I$ |                                       |                       |
| $u = -0.453705 + 0.067556I$ |                                       |                       |
| $a = 1.09810 - 1.34637I$    | $1.44591 + 2.04368I$                  | $6.19891 - 7.65821I$  |
| $b = -1.45141 - 1.20638I$   |                                       |                       |
| $u = -0.453705 - 0.067556I$ |                                       |                       |
| $a = 1.09810 + 1.34637I$    | $1.44591 - 2.04368I$                  | $6.19891 + 7.65821I$  |
| $b = -1.45141 + 1.20638I$   |                                       |                       |
| $u = -0.404516 + 0.160541I$ |                                       |                       |
| $a = 0.82003 + 2.15188I$    | $-0.767799 + 0.707140I$               | $-1.24485 - 4.27067I$ |
| $b = -0.441070 + 0.879956I$ |                                       |                       |
| $u = -0.404516 - 0.160541I$ |                                       |                       |
| $a = 0.82003 - 2.15188I$    | $-0.767799 - 0.707140I$               | $-1.24485 + 4.27067I$ |
| $b = -0.441070 - 0.879956I$ |                                       |                       |
| $u = -1.25351 + 0.99399I$   |                                       |                       |
| $a = -0.115660 + 0.761637I$ | $9.1239 - 11.3929I$                   | 0                     |
| $b = -0.736192 + 0.183930I$ |                                       |                       |
| $u = -1.25351 - 0.99399I$   |                                       |                       |
| $a = -0.115660 - 0.761637I$ | $9.1239 + 11.3929I$                   | 0                     |
| $b = -0.736192 - 0.183930I$ |                                       |                       |

| Solutions to $I_3^u$        | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|-----------------------------|---------------------------------------|------------|
| $u = -0.36377 + 1.56837I$   |                                       |            |
| $a = 0.237958 + 0.409554I$  | $-1.81586 + 7.53048I$                 | 0          |
| $b = 0.677280 + 1.077370I$  |                                       |            |
| $u = -0.36377 - 1.56837I$   |                                       |            |
| $a = 0.237958 - 0.409554I$  | $-1.81586 - 7.53048I$                 | 0          |
| $b = 0.677280 - 1.077370I$  |                                       |            |
| $u = 1.51405 + 0.60574I$    |                                       |            |
| $a = -0.697006 + 0.215750I$ | $7.01799 - 4.89766I$                  | 0          |
| $b = 1.53643 + 0.52266I$    |                                       |            |
| $u = 1.51405 - 0.60574I$    |                                       |            |
| $a = -0.697006 - 0.215750I$ | $7.01799 + 4.89766I$                  | 0          |
| $b = 1.53643 - 0.52266I$    |                                       |            |
| $u = -1.12746 + 1.17840I$   |                                       |            |
| $a = 0.077668 + 0.451088I$  | $8.59840 + 2.41577I$                  | 0          |
| $b = -1.04228 + 1.32124I$   |                                       |            |
| $u = -1.12746 - 1.17840I$   |                                       |            |
| $a = 0.077668 - 0.451088I$  | $8.59840 - 2.41577I$                  | 0          |
| $b = -1.04228 - 1.32124I$   |                                       |            |
| $u = 1.52190 + 0.73520I$    |                                       |            |
| $a = 0.091226 - 0.489453I$  | $10.39060 + 0.33751I$                 | 0          |
| $b = -0.673521 - 0.205430I$ |                                       |            |
| $u = 1.52190 - 0.73520I$    |                                       |            |
| $a = 0.091226 + 0.489453I$  | $10.39060 - 0.33751I$                 | 0          |
| $b = -0.673521 + 0.205430I$ |                                       |            |
| $u = -1.37300 + 1.05302I$   |                                       |            |
| $a = 0.247643 + 0.695092I$  | $2.36016 - 7.44357I$                  | 0          |
| $b = -1.27363 + 0.94541I$   |                                       |            |
| $u = -1.37300 - 1.05302I$   |                                       |            |
| $a = 0.247643 - 0.695092I$  | $2.36016 + 7.44357I$                  | 0          |
| $b = -1.27363 - 0.94541I$   |                                       |            |

| Solutions to $I_3^u$  | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape           |
|---|---------------------------------------|----------------------|
| $u = 0.47056 + 1.67845I$<br>$a = 0.246842 - 0.393743I$<br>$b = 0.681559 - 0.993043I$  | $4.42249 - 11.60810I$                 | 0                    |
| $u = 0.47056 - 1.67845I$<br>$a = 0.246842 + 0.393743I$<br>$b = 0.681559 + 0.993043I$  | $4.42249 + 11.60810I$                 | 0                    |
| $u = 1.34694 + 1.13133I$<br>$a = 0.119382 - 0.726589I$<br>$b = -1.15971 - 0.96631I$   | $9.5516 + 10.5652I$                   | 0                    |
| $u = 1.34694 - 1.13133I$<br>$a = 0.119382 + 0.726589I$<br>$b = -1.15971 + 0.96631I$   | $9.5516 - 10.5652I$                   | 0                    |
| $u = -1.81161$<br>$a = -0.588467$<br>$b = 1.85662$                                    | 2.24749                               | 0                    |
| $u = 0.149531 + 0.022926I$<br>$a = 3.10840 + 10.08440I$<br>$b = 0.677148 + 0.214687I$ | $4.86393 + 2.30422I$                  | $5.13678 - 7.19189I$ |
| $u = 0.149531 - 0.022926I$<br>$a = 3.10840 - 10.08440I$<br>$b = 0.677148 - 0.214687I$ | $4.86393 - 2.30422I$                  | $5.13678 + 7.19189I$ |
| $u = -0.07748 + 1.89589I$<br>$a = 0.421157 + 0.046884I$<br>$b = 0.432044 + 0.349969I$ | $4.00496 - 0.11590I$                  | 0                    |
| $u = -0.07748 - 1.89589I$<br>$a = 0.421157 - 0.046884I$<br>$b = 0.432044 - 0.349969I$ | $4.00496 + 0.11590I$                  | 0                    |
| $u = 1.51690 + 1.21579I$<br>$a = 0.246784 - 0.484838I$<br>$b = -1.45141 - 1.20638I$   | $1.44591 + 2.04368I$                  | 0                    |

| Solutions to $I_3^u$   | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|--|---------------------------------------|------------|
| $u = 1.51690 - 1.21579I$<br>$a = 0.246784 + 0.484838I$<br>$b = -1.45141 + 1.20638I$      | $1.44591 - 2.04368I$                  | 0          |
| $u = 0.00499 + 1.94799I$<br>$a = 0.181253 + 0.319408I$<br>$b = 0.327313 + 0.897043I$     | $6.88898 - 0.12974I$                  | 0          |
| $u = 0.00499 - 1.94799I$<br>$a = 0.181253 - 0.319408I$<br>$b = 0.327313 - 0.897043I$     | $6.88898 + 0.12974I$                  | 0          |
| $u = 3.02357 + 0.90413I$<br>$a = -0.0518628 + 0.0420595I$<br>$b = -0.366627 + 0.170388I$ | $5.01112 + 0.52164I$                  | 0          |
| $u = 3.02357 - 0.90413I$<br>$a = -0.0518628 - 0.0420595I$<br>$b = -0.366627 - 0.170388I$ | $5.01112 - 0.52164I$                  | 0          |
| $u = 8.91180$<br>$a = -0.0139790$<br>$b = 0.0996704$                                     | 0.00210462                            | 0          |

#### IV. u-Polynomials

| Crossings     | u-Polynomials at each crossing  |
|---------------|---|
| $c_1, c_3$    | $(u^{25} - 3u^{24} + \dots - 40u + 56)(u^{35} - 3u^{34} + \dots + 13u - 1)$ $\cdot (u^{116} + 5u^{115} + \dots - 293824u - 18872)$            |
| $c_2$         | $(u^{25} - 8u^{24} + \dots - 3u - 1)(u^{35} - 25u^{34} + \dots + 24576u - 2048)$ $\cdot (u^{58} + 14u^{57} + \dots + 2u + 1)^2$               |
| $c_4, c_{11}$ | $64(8u^{25} + 8u^{24} + \dots + 5u^2 + 1)(u^{35} + 7u^{34} + \dots - 3u + 1)$ $\cdot (8u^{116} + 104u^{115} + \dots - 107834072u + 36867937)$ |
| $c_5, c_{10}$ | $64(8u^{25} - 8u^{24} + \dots + 11u^2 - 1)(u^{35} + 5u^{34} + \dots - 3u + 1)$ $\cdot (8u^{116} + 104u^{115} + \dots + 65126u - 4735)$        |
| $c_6, c_9$    | $(u^{25} - u^{24} + \dots - 8u - 8)(u^{35} - u^{34} + \dots + 8u - 1)$ $\cdot (u^{116} + 15u^{115} + \dots + 417760u + 52936)$                |
| $c_7, c_8$    | $(u^{25} + 2u^{24} + \dots - 2u + 1)(u^{35} + 11u^{34} + \dots + 384u + 32)$ $\cdot (u^{58} - 6u^{57} + \dots - 24u + 1)^2$                   |
| $c_{12}$      | $(u^{25} - 2u^{24} + \dots - 2u - 1)(u^{35} + 11u^{34} + \dots + 384u + 32)$ $\cdot (u^{58} - 6u^{57} + \dots - 24u + 1)^2$                   |

## V. Riley Polynomials

| Crossings          | Riley Polynomials at each crossing   |
|--------------------|--|
| $c_1, c_3$         | $(y^{25} - 3y^{24} + \dots + 19072y - 3136)(y^{35} + 11y^{34} + \dots + 29y - 1)$ $\cdot (y^{116} - 93y^{115} + \dots - 74449976896y + 356152384)$                         |
| $c_2$              | $(y^{25} + 10y^{24} + \dots + 37y - 1)$ $\cdot (y^{35} + 15y^{34} + \dots - 90177536y - 4194304)$ $\cdot (y^{58} - 14y^{57} + \dots - 132y + 1)^2$                         |
| $c_4, c_{11}$      | $4096(64y^{25} - 448y^{24} + \dots - 10y - 1)(y^{35} - 51y^{34} + \dots + 35y - 1)$ $\cdot (64y^{116} - 6720y^{115} + \dots - 1.68 \times 10^{17}y + 1.36 \times 10^{15})$ |
| $c_5, c_{10}$      | $4096(64y^{25} - 704y^{24} + \dots + 22y - 1)(y^{35} - 39y^{34} + \dots + 27y - 1)$ $\cdot (64y^{116} - 5184y^{115} + \dots - 3550066936y + 22420225)$                     |
| $c_6, c_9$         | $(y^{25} - 7y^{24} + \dots + 192y - 64)(y^{35} - y^{34} + \dots + 28y - 1)$ $\cdot (y^{116} - 105y^{115} + \dots - 367121525120y + 2802220096)$                            |
| $c_7, c_8, c_{12}$ | $(y^{25} + 26y^{24} + \dots + 46y - 1)(y^{35} + 31y^{34} + \dots - 7680y - 1024)$ $\cdot (y^{58} + 58y^{57} + \dots - 272y + 1)^2$   |