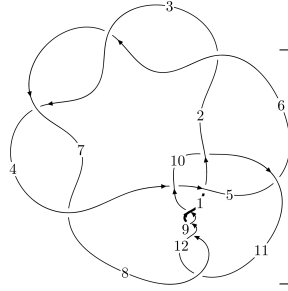
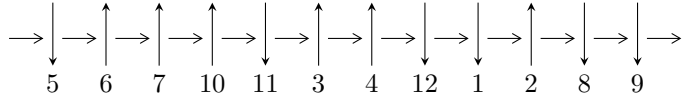


12a<sub>1218</sub> (K12a<sub>1218</sub>)



A knot diagram<sup>1</sup>

**Linearized knot diagram**



**Solving Sequence**

$$3,6 \xrightarrow{c_6} 7 \xrightarrow{c_3} 4 \xrightarrow{c_7} 8,11 \xrightarrow{c_{11}} 12 \xrightarrow{c_2} 2 \xrightarrow{c_5} 5 \xrightarrow{c_1} 1 \xrightarrow{c_{10}} 10 \xrightarrow{c_9} 9 \twoheadrightarrow c_4, c_8, c_{12}$$

**Ideals for irreducible components<sup>2</sup> of  $X_{\text{par}}$**

$$I_1^u = \langle -2.88764 \times 10^{38} u^{57} + 1.08762 \times 10^{39} u^{56} + \dots + 1.25794 \times 10^{38} b + 4.48859 \times 10^{38}, \\ -2.38160 \times 10^{37} u^{57} - 3.45850 \times 10^{38} u^{56} + \dots + 1.25794 \times 10^{38} a - 1.21766 \times 10^{39}, \\ u^{58} - 4u^{57} + \dots + 10u + 1 \rangle$$

$$I_2^u = \langle b - u, a - 1, u^2 + u - 1 \rangle$$

$$I_3^u = \langle b + a, a^2 + a - 1, u - 1 \rangle$$

\* 3 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 62 representations.

<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\text{I. } I_1^u = \langle -2.89 \times 10^{38} u^{57} + 1.09 \times 10^{39} u^{56} + \dots + 1.26 \times 10^{38} b + 4.49 \times 10^{38}, -2.38 \times 10^{37} u^{57} - 3.46 \times 10^{38} u^{56} + \dots + 1.26 \times 10^{38} a - 1.22 \times 10^{39}, u^{58} - 4u^{57} + \dots + 10u + 1 \rangle$$

(i) Arc colorings

$$a_3 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} u \\ -u^3 + u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -u^2 + 1 \\ u^4 - 2u^2 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0.189325u^{57} + 2.74933u^{56} + \dots + 51.6861u + 9.67976 \\ 2.29553u^{57} - 8.64604u^{56} + \dots - 52.0009u - 3.56820 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -3.31034u^{57} + 11.1720u^{56} + \dots + 74.9248u + 11.0418 \\ 5.11921u^{57} - 15.5570u^{56} + \dots - 75.3805u - 5.77324 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -u \\ u \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 1.35642u^{57} - 2.73919u^{56} + \dots - 31.4858u - 5.53784 \\ -3.83315u^{57} + 10.5013u^{56} + \dots + 40.7130u + 3.05633 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -1.73986u^{57} + 2.87590u^{56} + \dots - 2.41112u - 0.766687 \\ 1.73986u^{57} - 2.87590u^{56} + \dots + 2.41112u - 0.233313 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -5.92742u^{57} + 17.2187u^{56} + \dots + 94.5982u + 13.7225 \\ 8.41228u^{57} - 23.1154u^{56} + \dots - 94.9130u - 7.61093 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0.212480u^{57} + 0.0136304u^{56} + \dots + 18.3659u + 6.33053 \\ 1.59639u^{57} - 4.39858u^{56} + \dots - 18.8215u - 1.06192 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes =  $21.4511u^{57} - 79.0212u^{56} + \dots - 524.981u - 52.4582$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1$	$u^{58} + 3u^{57} + \dots + 4u + 4$
$c_2, c_3, c_6$ $c_7$	$u^{58} - 4u^{57} + \dots + 10u + 1$
$c_4$	$u^{58} - u^{57} + \dots + 519u + 83$
$c_5$	$u^{58} + u^{57} + \dots - 519u + 83$
$c_8, c_9, c_{11}$ $c_{12}$	$u^{58} + 4u^{57} + \dots - 10u + 1$
$c_{10}$	$u^{58} - 3u^{57} + \dots - 4u + 4$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_{10}$	$y^{58} - 17y^{57} + \dots - 120y + 16$
$c_2, c_3, c_6$ $c_7, c_8, c_9$ $c_{11}, c_{12}$	$y^{58} - 68y^{57} + \dots - 90y + 1$
$c_4, c_5$	$y^{58} + 51y^{57} + \dots - 36463y + 6889$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.803979 + 0.621852I$ $a = -0.271991 + 1.151380I$ $b = -1.08545 - 1.13142I$	$-8.28668 - 10.95660I$	0
$u = -0.803979 - 0.621852I$ $a = -0.271991 - 1.151380I$ $b = -1.08545 + 1.13142I$	$-8.28668 + 10.95660I$	0
$u = -0.793217 + 0.521649I$ $a = 0.498912 - 1.122630I$ $b = 0.946234 + 1.016640I$	$-8.39682I$	0
$u = -0.793217 - 0.521649I$ $a = 0.498912 + 1.122630I$ $b = 0.946234 - 1.016640I$	$8.39682I$	0
$u = 0.577533 + 0.730806I$ $a = -0.634988 - 0.459765I$ $b = -0.098643 + 1.074010I$	$-5.27688 + 2.48624I$	0
$u = 0.577533 - 0.730806I$ $a = -0.634988 + 0.459765I$ $b = -0.098643 - 1.074010I$	$-5.27688 - 2.48624I$	0
$u = 1.008620 + 0.380806I$ $a = -0.594450 - 0.045398I$ $b = 0.149754 + 0.464822I$	$1.242260 - 0.522127I$	0
$u = 1.008620 - 0.380806I$ $a = -0.594450 + 0.045398I$ $b = 0.149754 - 0.464822I$	$1.242260 + 0.522127I$	0
$u = -0.749389 + 0.385619I$ $a = -0.849917 + 1.075030I$ $b = -0.781148 - 0.827305I$	$2.11157 - 4.30929I$	$3.71388 + 6.70404I$
$u = -0.749389 - 0.385619I$ $a = -0.849917 - 1.075030I$ $b = -0.781148 + 0.827305I$	$2.11157 + 4.30929I$	$3.71388 - 6.70404I$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.154793 + 0.824875I$ $a = -0.217281 - 0.442528I$ $b = 0.869009 - 0.759634I$	$-10.25510 + 6.17839I$	$-4.76560 - 4.41616I$
$u = -0.154793 - 0.824875I$ $a = -0.217281 + 0.442528I$ $b = 0.869009 + 0.759634I$	$-10.25510 - 6.17839I$	$-4.76560 + 4.41616I$
$u = 0.668037 + 0.496903I$ $a = 0.637455 + 0.425308I$ $b = 0.087808 - 0.841653I$	$1.48873 + 1.56696I$	$6.38155 - 7.61387I$
$u = 0.668037 - 0.496903I$ $a = 0.637455 - 0.425308I$ $b = 0.087808 + 0.841653I$	$1.48873 - 1.56696I$	$6.38155 + 7.61387I$
$u = 0.805056$ $a = 0.0586228$ $b = -0.469605$	$1.37980$	$7.84380$
$u = -0.614408 + 0.433410I$ $a = -0.65974 - 1.92027I$ $b = 0.667344 + 0.163534I$	$-9.33906 - 4.00146I$	$-4.44972 + 5.66506I$
$u = -0.614408 - 0.433410I$ $a = -0.65974 + 1.92027I$ $b = 0.667344 - 0.163534I$	$-9.33906 + 4.00146I$	$-4.44972 - 5.66506I$
$u = 1.176150 + 0.494013I$ $a = 0.885445 - 0.099461I$ $b = -0.449248 - 0.435686I$	$-6.21754 - 1.60405I$	$0$
$u = 1.176150 - 0.494013I$ $a = 0.885445 + 0.099461I$ $b = -0.449248 + 0.435686I$	$-6.21754 + 1.60405I$	$0$
$u = -0.091748 + 0.703159I$ $a = -0.125386 + 0.534649I$ $b = -0.680727 + 0.714968I$	$-2.11157 + 4.30929I$	$-3.71388 - 6.70404I$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.091748 - 0.703159I$ $a = -0.125386 - 0.534649I$ $b = -0.680727 - 0.714968I$	$-2.11157 - 4.30929I$	$-3.71388 + 6.70404I$
$u = 0.635581 + 0.189573I$ $a = -0.89658 + 3.23104I$ $b = 0.93416 - 2.56648I$	$-7.67427 + 0.41875I$	$-15.8309 + 7.9264I$
$u = 0.635581 - 0.189573I$ $a = -0.89658 - 3.23104I$ $b = 0.93416 + 2.56648I$	$-7.67427 - 0.41875I$	$-15.8309 - 7.9264I$
$u = -0.550445 + 0.243751I$ $a = 1.52059 - 0.52439I$ $b = 0.749569 + 0.393249I$	$-1.242260 - 0.522127I$	$-4.85746 + 7.66329I$
$u = -0.550445 - 0.243751I$ $a = 1.52059 + 0.52439I$ $b = 0.749569 - 0.393249I$	$-1.242260 + 0.522127I$	$-4.85746 - 7.66329I$
$u = 0.584934 + 0.061813I$ $a = 0.15128 - 2.97701I$ $b = 0.05666 + 2.44383I$	$0.213446I$	$0. + 27.5576I$
$u = 0.584934 - 0.061813I$ $a = 0.15128 + 2.97701I$ $b = 0.05666 - 2.44383I$	$-0.213446I$	$0. - 27.5576I$
$u = -0.430814 + 0.285650I$ $a = 0.09371 + 2.24652I$ $b = -0.371702 + 0.056513I$	$-1.48873 - 1.56696I$	$-6.38155 + 7.61387I$
$u = -0.430814 - 0.285650I$ $a = 0.09371 - 2.24652I$ $b = -0.371702 - 0.056513I$	$-1.48873 + 1.56696I$	$-6.38155 - 7.61387I$
$u = -0.250271 + 0.449093I$ $a = -0.567142 - 0.727486I$ $b = -1.268190 - 0.096887I$	$-10.37260 + 0.86444I$	$-7.08102 + 2.87846I$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.250271 - 0.449093I$ $a = -0.567142 + 0.727486I$ $b = -1.268190 + 0.096887I$	$-10.37260 - 0.86444I$	$-7.08102 - 2.87846I$
$u = 1.50011$ $a = -0.813827$ $b = 1.76423$	$-4.86772$	$0$
$u = 1.54778 + 0.03907I$ $a = -0.22281 + 1.48990I$ $b = 0.058169 - 0.419643I$	$5.27688 + 2.48624I$	$0$
$u = 1.54778 - 0.03907I$ $a = -0.22281 - 1.48990I$ $b = 0.058169 + 0.419643I$	$5.27688 - 2.48624I$	$0$
$u = 0.001775 + 0.445857I$ $a = 1.000040 - 0.710446I$ $b = 0.364686 - 0.633641I$	$1.41091I$	$0. - 3.50261I$
$u = 0.001775 - 0.445857I$ $a = 1.000040 + 0.710446I$ $b = 0.364686 + 0.633641I$	$- 1.41091I$	$0. + 3.50261I$
$u = 1.57398 + 0.11293I$ $a = 0.56491 - 1.41977I$ $b = -0.204122 + 0.485422I$	$-1.93678 + 5.95845I$	$0$
$u = 1.57398 - 0.11293I$ $a = 0.56491 + 1.41977I$ $b = -0.204122 - 0.485422I$	$-1.93678 - 5.95845I$	$0$
$u = 1.58805 + 0.06429I$ $a = 0.055690 - 1.002130I$ $b = -1.144500 + 0.638936I$	$6.21754 + 1.60405I$	$0$
$u = 1.58805 - 0.06429I$ $a = 0.055690 + 1.002130I$ $b = -1.144500 - 0.638936I$	$6.21754 - 1.60405I$	$0$



Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.59261 + 0.05649I$ $a = -0.10696 + 3.02763I$ $b = 0.34217 - 2.56487I$	$-1.36403I$	0
$u = -1.59261 - 0.05649I$ $a = -0.10696 - 3.02763I$ $b = 0.34217 + 2.56487I$	$1.36403I$	0
$u = -1.58253 + 0.21992I$ $a = 0.43189 - 1.53582I$ $b = 0.242359 + 1.309890I$	$1.93678 - 5.95845I$	0
$u = -1.58253 - 0.21992I$ $a = 0.43189 + 1.53582I$ $b = 0.242359 - 1.309890I$	$1.93678 + 5.95845I$	0
$u = -1.60277 + 0.00806I$ $a = 0.94531 - 2.97432I$ $b = -1.17552 + 2.67763I$	$7.67427 - 0.41875I$	0
$u = -1.60277 - 0.00806I$ $a = 0.94531 + 2.97432I$ $b = -1.17552 - 2.67763I$	$7.67427 + 0.41875I$	0
$u = -1.61745 + 0.14658I$ $a = -0.199604 + 1.369900I$ $b = -0.401208 - 1.169100I$	$9.33906 - 4.00146I$	0
$u = -1.61745 - 0.14658I$ $a = -0.199604 - 1.369900I$ $b = -0.401208 + 1.169100I$	$9.33906 + 4.00146I$	0
$u = 1.62381 + 0.10972I$ $a = -0.13698 + 1.52608I$ $b = 1.07956 - 1.05237I$	$10.25510 + 6.17839I$	0
$u = 1.62381 - 0.10972I$ $a = -0.13698 - 1.52608I$ $b = 1.07956 + 1.05237I$	$10.25510 - 6.17839I$	0

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.63751 + 0.15124I$ $a = 0.28012 - 1.77911I$ $b = -1.14258 + 1.30370I$	$8.28668 + 10.95660I$	0
$u = 1.63751 - 0.15124I$ $a = 0.28012 + 1.77911I$ $b = -1.14258 - 1.30370I$	$8.28668 - 10.95660I$	0
$u = 1.64399 + 0.18789I$ $a = -0.39793 + 1.95590I$ $b = 1.21392 - 1.48592I$	$14.0571I$	0
$u = 1.64399 - 0.18789I$ $a = -0.39793 - 1.95590I$ $b = 1.21392 + 1.48592I$	$-14.0571I$	0
$u = -1.65526 + 0.07461I$ $a = -0.184098 - 0.969973I$ $b = 0.710486 + 0.840147I$	$10.37260 - 0.86444I$	0
$u = -1.65526 - 0.07461I$ $a = -0.184098 + 0.969973I$ $b = 0.710486 - 0.840147I$	$10.37260 + 0.86444I$	0
$u = -1.74741$ $a = -0.264052$ $b = -0.316899$	$4.86772$	0
$u = -0.113883$ $a = 5.02027$ $b = 0.684561$	$-1.37980$	$-7.84380$

$$\text{II. } I_2^u = \langle b - u, a - 1, u^2 + u - 1 \rangle$$

(i) Arc colorings

$$a_3 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1 \\ u - 1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} u \\ -u + 1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} u \\ -u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ u \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -u + 1 \\ 2u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -u \\ u \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -u + 1 \\ u - 1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -u \\ u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -u + 1 \\ 2u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ u \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = 5

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1$	$u^2$
$c_2, c_3$	$u^2 - u - 1$
$c_4, c_5, c_6$ $c_7$	$u^2 + u - 1$
$c_8, c_9, c_{10}$	$(u - 1)^2$
$c_{11}, c_{12}$	$(u + 1)^2$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1$	$y^2$
$c_2, c_3, c_4$ $c_5, c_6, c_7$	$y^2 - 3y + 1$
$c_8, c_9, c_{10}$ $c_{11}, c_{12}$	$(y - 1)^2$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.618034$ $a = 1.00000$ $b = 0.618034$	-0.657974	5.00000
$u = -1.61803$ $a = 1.00000$ $b = -1.61803$	7.23771	5.00000

$$\text{III. } I_3^u = \langle b + a, a^2 + a - 1, u - 1 \rangle$$

(i) Arc colorings

$$a_3 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} a \\ -a \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} a \\ 0 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -1 \\ 1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -a + 2 \\ a - 1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -a + 1 \\ a \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} a \\ -a \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -a + 1 \\ -1 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = -5

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_2, c_3$	$(u + 1)^2$
$c_4, c_5, c_{11}$ $c_{12}$	$u^2 - u - 1$
$c_6, c_7$	$(u - 1)^2$
$c_8, c_9$	$u^2 + u - 1$
$c_{10}$	$u^2$



(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_3$ $c_6, c_7$	$(y - 1)^2$
$c_4, c_5, c_8$ $c_9, c_{11}, c_{12}$	$y^2 - 3y + 1$
$c_{10}$	$y^2$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.00000$ $a = 0.618034$ $b = -0.618034$	0.657974	-5.00000
$u = 1.00000$ $a = -1.61803$ $b = 1.61803$	-7.23771	-5.00000

#### IV. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1$	$u^2(u+1)^2(u^{58} + 3u^{57} + \dots + 4u + 4)$
$c_2, c_3$	$((u+1)^2)(u^2 - u - 1)(u^{58} - 4u^{57} + \dots + 10u + 1)$
$c_4$	$(u^2 - u - 1)(u^2 + u - 1)(u^{58} - u^{57} + \dots + 519u + 83)$
$c_5$	$(u^2 - u - 1)(u^2 + u - 1)(u^{58} + u^{57} + \dots - 519u + 83)$
$c_6, c_7$	$((u-1)^2)(u^2 + u - 1)(u^{58} - 4u^{57} + \dots + 10u + 1)$
$c_8, c_9$	$((u-1)^2)(u^2 + u - 1)(u^{58} + 4u^{57} + \dots - 10u + 1)$
$c_{10}$	$u^2(u-1)^2(u^{58} - 3u^{57} + \dots - 4u + 4)$
$c_{11}, c_{12}$	$((u+1)^2)(u^2 - u - 1)(u^{58} + 4u^{57} + \dots - 10u + 1)$

### V. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1, c_{10}$	$y^2(y-1)^2(y^{58} - 17y^{57} + \dots - 120y + 16)$
$c_2, c_3, c_6$ $c_7, c_8, c_9$ $c_{11}, c_{12}$	$((y-1)^2)(y^2 - 3y + 1)(y^{58} - 68y^{57} + \dots - 90y + 1)$
$c_4, c_5$	$((y^2 - 3y + 1)^2)(y^{58} + 51y^{57} + \dots - 36463y + 6889)$