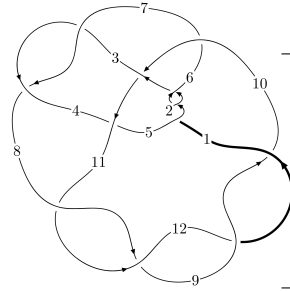
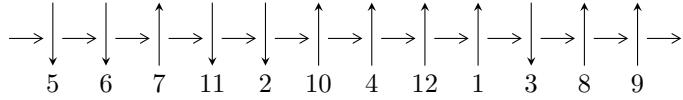


12a₁₂₁₉ (K12a₁₂₁₉)



A knot diagram¹

Linearized knot diagram



Solving Sequence

$$8,12 \xrightarrow{c_8} 9 \xrightarrow{c_{12}} 1 \xrightarrow{c_9} 4,10 \xrightarrow{c_7} 7 \xrightarrow{c_3} 3 \xrightarrow{c_6} 6 \xrightarrow{c_{11}} 11 \xrightarrow{c_4} 5 \xrightarrow{c_1} 2 \rightsquigarrow c_2, c_5, c_{10}$$

Ideals for irreducible components² of X_{par}

$$I_1^u = \langle 8.75661 \times 10^{64} u^{63} + 2.76997 \times 10^{65} u^{62} + \dots + 1.65696 \times 10^{65} b + 2.96457 \times 10^{65}, \\ 1.00296 \times 10^{66} u^{63} + 3.44551 \times 10^{66} u^{62} + \dots + 8.28478 \times 10^{64} a + 2.84103 \times 10^{65}, u^{64} + 4u^{63} + \dots - 10u + \dots \rangle$$

$$I_2^u = \langle b - 1, a + 2, u + 1 \rangle$$

$$I_3^u = \langle b + 1, a^2 - 4a + 2, u + 1 \rangle$$

* 3 irreducible components of $\dim_{\mathbb{C}} = 0$, with total 67 representations.

¹The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

²All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\mathbf{I. } I_1^u = \langle 8.76 \times 10^{64} u^{63} + 2.77 \times 10^{65} u^{62} + \dots + 1.66 \times 10^{65} b + 2.96 \times 10^{65}, 1.00 \times 10^{66} u^{63} + 3.45 \times 10^{66} u^{62} + \dots + 8.28 \times 10^{64} a + 2.84 \times 10^{65}, u^{64} + 4u^{63} + \dots - 10u + 1 \rangle$$

(i) Arc colorings

$$\begin{aligned} a_8 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_{12} &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_9 &= \begin{pmatrix} 1 \\ -u^2 \end{pmatrix} \\ a_1 &= \begin{pmatrix} u \\ -u^3 + u \end{pmatrix} \\ a_4 &= \begin{pmatrix} -12.1060u^{63} - 41.5885u^{62} + \dots + 205.872u - 3.42922 \\ -0.528476u^{63} - 1.67172u^{62} + \dots + 7.65402u - 1.78916 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} -u^2 + 1 \\ u^4 - 2u^2 \end{pmatrix} \\ a_7 &= \begin{pmatrix} 13.7729u^{63} + 46.8393u^{62} + \dots - 229.931u + 4.46101 \\ 0.181537u^{63} + 0.533529u^{62} + \dots - 1.36851u + 1.37956 \end{pmatrix} \\ a_3 &= \begin{pmatrix} 4.35303u^{63} + 10.6700u^{62} + \dots - 32.5922u - 0.381251 \\ -3.47471u^{63} - 8.31368u^{62} + \dots + 28.6251u - 2.38908 \end{pmatrix} \\ a_6 &= \begin{pmatrix} 8.57909u^{63} + 30.0107u^{62} + \dots - 140.536u - 4.30529 \\ 5.95601u^{63} + 19.1387u^{62} + \dots - 97.4281u + 9.72466 \end{pmatrix} \\ a_{11} &= \begin{pmatrix} -u \\ u \end{pmatrix} \\ a_5 &= \begin{pmatrix} -7.27418u^{63} - 25.7859u^{62} + \dots + 120.459u + 3.84863 \\ -5.36032u^{63} - 17.4743u^{62} + \dots + 93.0670u - 9.06702 \end{pmatrix} \\ a_2 &= \begin{pmatrix} -8.95289u^{63} - 28.0262u^{62} + \dots + 182.432u - 36.5824 \\ -5.59890u^{63} - 20.4560u^{62} + \dots + 122.657u - 8.92048 \end{pmatrix} \end{aligned}$$

(ii) Obstruction class = -1

$$\text{(iii) Cusp Shapes} = -112.789u^{63} - 383.132u^{62} + \dots + 2107.64u - 184.302$$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1, c_2, c_5	$u^{64} + 5u^{63} + \dots - 6u - 2$
c_3, c_7	$u^{64} - 2u^{63} + \dots + 6u - 1$
c_4	$u^{64} + 16u^{63} + \dots - 397046u + 45841$
c_6	$u^{64} - 18u^{63} + \dots - 8u + 1$
c_8, c_9, c_{11} c_{12}	$u^{64} - 4u^{63} + \dots + 10u + 1$
c_{10}	$u^{64} - 2u^{63} + \dots - 2u - 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1, c_2, c_5	$y^{64} - 61y^{63} + \dots + 12y + 4$
c_3, c_7	$y^{64} - 52y^{63} + \dots + 6y + 1$
c_4	$y^{64} - 440y^{63} + \dots + 63549675954y + 2101397281$
c_6	$y^{64} - 504y^{63} + \dots - 638y + 1$
c_8, c_9, c_{11} c_{12}	$y^{64} - 76y^{63} + \dots - 106y + 1$
c_{10}	$y^{64} - 8y^{63} + \dots - 114y + 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.626252 + 0.772749I$	$1.37703 - 2.62298I$	0
$a = -0.442645 - 0.836072I$		
$b = 1.282870 - 0.069070I$		
$u = -0.626252 - 0.772749I$	$1.37703 + 2.62298I$	0
$a = -0.442645 + 0.836072I$		
$b = 1.282870 + 0.069070I$		
$u = 0.892186 + 0.475186I$	$5.33163 + 8.09564I$	0
$a = 1.45927 - 1.01010I$		
$b = -1.37477 - 0.41692I$		
$u = 0.892186 - 0.475186I$	$5.33163 - 8.09564I$	0
$a = 1.45927 + 1.01010I$		
$b = -1.37477 + 0.41692I$		
$u = -0.885933 + 0.573263I$	$4.82419 - 0.31393I$	0
$a = 0.924110 + 0.935341I$		
$b = -1.224840 - 0.045601I$		
$u = -0.885933 - 0.573263I$	$4.82419 + 0.31393I$	0
$a = 0.924110 - 0.935341I$		
$b = -1.224840 + 0.045601I$		
$u = 0.866924 + 0.614790I$	$-0.85685 + 11.92020I$	0
$a = -1.33885 + 1.11410I$		
$b = 1.36865 + 0.42563I$		
$u = 0.866924 - 0.614790I$	$-0.85685 - 11.92020I$	0
$a = -1.33885 - 1.11410I$		
$b = 1.36865 - 0.42563I$		
$u = -1.088320 + 0.183319I$	$-3.32236 + 0.09828I$	0
$a = -1.033310 + 0.040437I$		
$b = 0.007127 - 0.240948I$		
$u = -1.088320 - 0.183319I$	$-3.32236 - 0.09828I$	0
$a = -1.033310 - 0.040437I$		
$b = 0.007127 + 0.240948I$		

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.727414 + 0.497209I$ $a = 0.517608 - 0.186664I$ $b = -0.136718 - 0.955922I$	$-5.57662 + 7.00157I$	0
$u = 0.727414 - 0.497209I$ $a = 0.517608 + 0.186664I$ $b = -0.136718 + 0.955922I$	$-5.57662 - 7.00157I$	0
$u = 0.086190 + 0.869107I$ $a = -0.161462 - 0.186514I$ $b = 1.276990 - 0.329837I$	$-3.24005 - 7.03352I$	0
$u = 0.086190 - 0.869107I$ $a = -0.161462 + 0.186514I$ $b = 1.276990 + 0.329837I$	$-3.24005 + 7.03352I$	0
$u = 0.826064 + 0.274343I$ $a = -1.68330 + 0.81928I$ $b = 1.39853 + 0.42614I$	$4.75434 + 3.17966I$	0
$u = 0.826064 - 0.274343I$ $a = -1.68330 - 0.81928I$ $b = 1.39853 - 0.42614I$	$4.75434 - 3.17966I$	0
$u = -1.20392$ $a = 1.35869$ $b = -0.745445$	2.67121	0
$u = -0.735824$ $a = -4.70570$ $b = 1.05067$	2.92949	-31.0790
$u = -0.061375 + 0.731517I$ $a = -0.056369 + 0.272785I$ $b = -1.230620 + 0.271880I$	$2.42658 - 4.10040I$	$5.18854 + 6.65155I$
$u = -0.061375 - 0.731517I$ $a = -0.056369 - 0.272785I$ $b = -1.230620 - 0.271880I$	$2.42658 + 4.10040I$	$5.18854 - 6.65155I$

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.156350 + 0.575363I$ $a = -1.056810 - 0.610432I$ $b = 1.251050 + 0.169381I$	$0.45977 + 2.04940I$	0
$u = -1.156350 - 0.575363I$ $a = -1.056810 + 0.610432I$ $b = 1.251050 - 0.169381I$	$0.45977 - 2.04940I$	0
$u = 0.645610 + 0.280609I$ $a = -0.622762 - 0.084173I$ $b = 0.227169 + 0.986896I$	$0.39947 + 3.16035I$	$2.81338 - 10.76378I$
$u = 0.645610 - 0.280609I$ $a = -0.622762 + 0.084173I$ $b = 0.227169 - 0.986896I$	$0.39947 - 3.16035I$	$2.81338 + 10.76378I$
$u = -0.537409 + 0.416579I$ $a = -0.908169 + 1.049400I$ $b = -0.301281 + 0.283446I$	$-3.30500 - 1.49850I$	$-1.71841 + 4.52498I$
$u = -0.537409 - 0.416579I$ $a = -0.908169 - 1.049400I$ $b = -0.301281 - 0.283446I$	$-3.30500 + 1.49850I$	$-1.71841 - 4.52498I$
$u = 0.171438 + 0.641396I$ $a = -0.810739 + 0.661600I$ $b = -0.011504 + 0.735189I$	$-7.24617 - 3.15234I$	$-4.81813 + 1.66839I$
$u = 0.171438 - 0.641396I$ $a = -0.810739 - 0.661600I$ $b = -0.011504 - 0.735189I$	$-7.24617 + 3.15234I$	$-4.81813 - 1.66839I$
$u = -0.622251 + 0.147718I$ $a = 0.623442 - 0.530311I$ $b = 0.140050 - 0.093500I$	$1.153010 - 0.371044I$	$8.52101 + 0.53269I$
$u = -0.622251 - 0.147718I$ $a = 0.623442 + 0.530311I$ $b = 0.140050 + 0.093500I$	$1.153010 + 0.371044I$	$8.52101 - 0.53269I$

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.625236$ $a = -32.6722$ $b = -0.982597$	-2.29108	-335.850
$u = 0.571354 + 0.216286I$ $a = 1.058770 - 0.384713I$ $b = -1.136650 + 0.669884I$	$-2.52737 + 1.49035I$	$-1.46490 - 10.14674I$
$u = 0.571354 - 0.216286I$ $a = 1.058770 + 0.384713I$ $b = -1.136650 - 0.669884I$	$-2.52737 - 1.49035I$	$-1.46490 + 10.14674I$
$u = -1.58313$ $a = 2.77393$ $b = -1.86821$	3.83757	0
$u = 1.58050 + 0.10884I$ $a = 0.006317 - 0.340356I$ $b = -0.242493 - 0.631350I$	$3.96868 + 3.34904I$	0
$u = 1.58050 - 0.10884I$ $a = 0.006317 + 0.340356I$ $b = -0.242493 + 0.631350I$	$3.96868 - 3.34904I$	0
$u = -1.58979 + 0.03598I$ $a = 1.41098 + 0.68557I$ $b = -1.17421 - 1.06495I$	$4.95069 - 2.27479I$	0
$u = -1.58979 - 0.03598I$ $a = 1.41098 - 0.68557I$ $b = -1.17421 + 1.06495I$	$4.95069 + 2.27479I$	0
$u = -1.60546 + 0.05832I$ $a = -0.671440 + 0.764979I$ $b = 0.437967 - 1.302070I$	$8.17400 - 4.30296I$	0
$u = -1.60546 - 0.05832I$ $a = -0.671440 - 0.764979I$ $b = 0.437967 + 1.302070I$	$8.17400 + 4.30296I$	0

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.60877 + 0.03569I$ $a = 0.077213 + 0.292537I$ $b = 0.219375 + 0.411958I$	$8.93615 + 1.02069I$	0
$u = 1.60877 - 0.03569I$ $a = 0.077213 - 0.292537I$ $b = 0.219375 - 0.411958I$	$8.93615 - 1.02069I$	0
$u = 0.385731$ $a = 4.06256$ $b = -1.41196$	-3.33490	-8.92110
$u = 0.129453 + 0.356601I$ $a = 1.25594 - 0.67953I$ $b = -0.129998 - 0.580705I$	$-1.019940 - 0.841014I$	$-4.44164 + 2.44385I$
$u = 0.129453 - 0.356601I$ $a = 1.25594 + 0.67953I$ $b = -0.129998 + 0.580705I$	$-1.019940 + 0.841014I$	$-4.44164 - 2.44385I$
$u = -0.151171 + 0.347893I$ $a = 1.51053 - 0.33569I$ $b = 1.087870 - 0.202838I$	$1.93096 - 1.01785I$	$2.25227 - 1.57609I$
$u = -0.151171 - 0.347893I$ $a = 1.51053 + 0.33569I$ $b = 1.087870 + 0.202838I$	$1.93096 + 1.01785I$	$2.25227 + 1.57609I$
$u = -1.61625 + 0.13512I$ $a = 0.579253 - 0.473421I$ $b = -0.254582 + 1.128060I$	$2.39807 - 9.34049I$	0
$u = -1.61625 - 0.13512I$ $a = 0.579253 + 0.473421I$ $b = -0.254582 - 1.128060I$	$2.39807 + 9.34049I$	0
$u = 1.63116 + 0.01107I$ $a = -1.17537 + 1.13475I$ $b = -0.795270 + 0.143585I$	$5.71807 + 0.01867I$	0

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.63116 - 0.01107I$ $a = -1.17537 - 1.13475I$ $b = -0.795270 - 0.143585I$	$5.71807 - 0.01867I$	0
$u = 1.62771 + 0.23629I$ $a = -1.53783 + 0.68857I$ $b = 1.350810 + 0.224077I$	$8.99118 + 6.39006I$	0
$u = 1.62771 - 0.23629I$ $a = -1.53783 - 0.68857I$ $b = 1.350810 - 0.224077I$	$8.99118 - 6.39006I$	0
$u = -1.65093 + 0.07673I$ $a = -2.22460 - 0.22306I$ $b = 1.61684 - 0.49505I$	$13.36180 - 4.53477I$	0
$u = -1.65093 - 0.07673I$ $a = -2.22460 + 0.22306I$ $b = 1.61684 + 0.49505I$	$13.36180 + 4.53477I$	0
$u = -1.67065 + 0.13316I$ $a = 2.09031 + 0.47257I$ $b = -1.51390 + 0.48815I$	$14.1665 - 10.4624I$	0
$u = -1.67065 - 0.13316I$ $a = 2.09031 - 0.47257I$ $b = -1.51390 - 0.48815I$	$14.1665 + 10.4624I$	0
$u = -1.66778 + 0.18149I$ $a = -2.03991 - 0.65692I$ $b = 1.46024 - 0.47787I$	$7.7777 - 15.0108I$	0
$u = -1.66778 - 0.18149I$ $a = -2.03991 + 0.65692I$ $b = 1.46024 + 0.47787I$	$7.7777 + 15.0108I$	0
$u = 1.68055$ $a = -2.49868$ $b = 1.25013$	11.5859	0

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.68516 + 0.14611I$ $a = 1.76330 - 0.59949I$ $b = -1.328680 - 0.151173I$	$13.75650 + 3.08420I$	0
$u = 1.68516 - 0.14611I$ $a = 1.76330 + 0.59949I$ $b = -1.328680 + 0.151173I$	$13.75650 - 3.08420I$	0
$u = 1.73966$ $a = -2.03600$ $b = 1.32403$	11.5124	0
$u = 0.102209$ $a = 13.6904$ $b = -1.15668$	-3.39768	-3.12270

$$\text{II. } I_2^u = \langle b - 1, a + 2, u + 1 \rangle$$

(i) Arc colorings

$$a_8 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -2 \\ 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -1 \\ 1 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = 12

(iv) **u**-Polynomials at the component

Crossings	u -Polynomials at each crossing
c_1, c_2, c_5	u
c_3, c_8, c_9 c_{10}	$u + 1$
c_4, c_6, c_7 c_{11}, c_{12}	$u - 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1, c_2, c_5	y
c_3, c_4, c_6 c_7, c_8, c_9 c_{10}, c_{11}, c_{12}	$y - 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to I_2^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.00000$	3.28987	12.0000
$a = -2.00000$		
$b = 1.00000$		

$$\text{III. } I_3^u = \langle b + 1, a^2 - 4a + 2, u + 1 \rangle$$

(i) Arc colorings

$$a_8 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} a \\ -1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -a + 1 \\ 1 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -a + 1 \\ -a + 2 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 1 \\ a - 2 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -a + 1 \\ -2 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = 4

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1, c_2, c_5	$u^2 - 2$
c_3, c_{10}, c_{11} c_{12}	$(u - 1)^2$
c_4	$u^2 + 2u - 1$
c_6	$u^2 - 2u - 1$
c_7, c_8, c_9	$(u + 1)^2$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1, c_2, c_5	$(y - 2)^2$
c_3, c_7, c_8 c_9, c_{10}, c_{11} c_{12}	$(y - 1)^2$
c_4, c_6	$y^2 - 6y + 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to I_3^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.00000$ $a = 0.585786$ $b = -1.00000$	-1.64493	4.00000
$u = -1.00000$ $a = 3.41421$ $b = -1.00000$	-1.64493	4.00000

IV. u-Polynomials

Crossings	u-Polynomials at each crossing
c_1, c_2, c_5	$u(u^2 - 2)(u^{64} + 5u^{63} + \dots - 6u - 2)$
c_3	$((u - 1)^2)(u + 1)(u^{64} - 2u^{63} + \dots + 6u - 1)$
c_4	$(u - 1)(u^2 + 2u - 1)(u^{64} + 16u^{63} + \dots - 397046u + 45841)$
c_6	$(u - 1)(u^2 - 2u - 1)(u^{64} - 18u^{63} + \dots - 8u + 1)$
c_7	$(u - 1)(u + 1)^2(u^{64} - 2u^{63} + \dots + 6u - 1)$
c_8, c_9	$((u + 1)^3)(u^{64} - 4u^{63} + \dots + 10u + 1)$
c_{10}	$((u - 1)^2)(u + 1)(u^{64} - 2u^{63} + \dots - 2u - 1)$
c_{11}, c_{12}	$((u - 1)^3)(u^{64} - 4u^{63} + \dots + 10u + 1)$

V. Riley Polynomials

Crossings	Riley Polynomials at each crossing
c_1, c_2, c_5	$y(y-2)^2(y^{64} - 61y^{63} + \dots + 12y + 4)$
c_3, c_7	$((y-1)^3)(y^{64} - 52y^{63} + \dots + 6y + 1)$
c_4	$(y-1)(y^2 - 6y + 1)$ $\cdot (y^{64} - 440y^{63} + \dots + 63549675954y + 2101397281)$
c_6	$(y-1)(y^2 - 6y + 1)(y^{64} - 504y^{63} + \dots - 638y + 1)$
c_8, c_9, c_{11} c_{12}	$((y-1)^3)(y^{64} - 76y^{63} + \dots - 106y + 1)$
c_{10}	$((y-1)^3)(y^{64} - 8y^{63} + \dots - 114y + 1)$