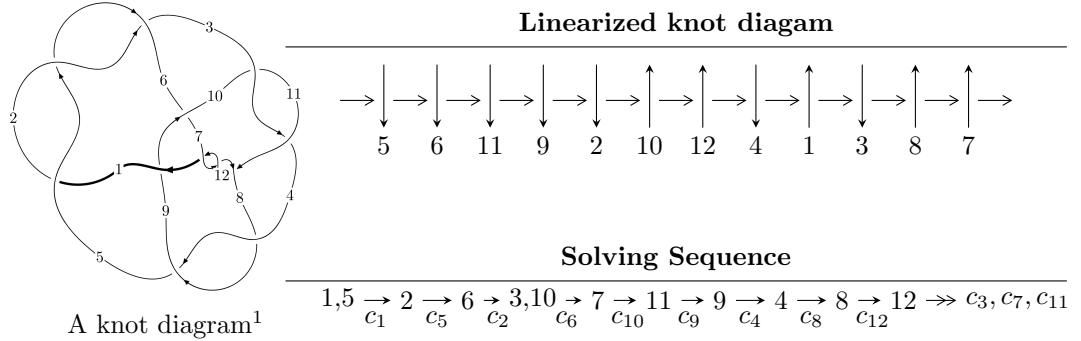


$12a_{1247}$  ( $K12a_{1247}$ )



### Ideals for irreducible components<sup>2</sup> of $X_{\text{par}}$

$$I_1^u = \langle -1931u^{31} + 20740u^{30} + \dots + 8b - 23592, -7773u^{31} + 82554u^{30} + \dots + 16a - 89232, u^{32} - 12u^{31} + \dots - 48u - 16 \rangle$$

$$I_2^u = \langle -1.02625 \times 10^{22}a^7u^5 + 8.99106 \times 10^{21}a^6u^5 + \dots - 4.39399 \times 10^{21}a + 3.98524 \times 10^{22}, -a^7u^5 + 8a^6u^5 + \dots - 489a + 821, u^6 + u^5 - 3u^4 - 2u^3 + 2u^2 - u - 1 \rangle$$

$$I_3^u = \langle u^{21} + 2u^{20} + \dots + b + u, 4u^{21} + 8u^{20} + \dots + a + 5, u^{22} + 3u^{21} + \dots + 3u + 1 \rangle$$

\* 3 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 102 representations.

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<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/math/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\text{I. } I_1^u = \langle -1931u^{31} + 20740u^{30} + \cdots + 8b - 23592, -7773u^{31} + 82554u^{30} + \cdots + 16a - 89232, u^{32} - 12u^{31} + \cdots - 48u - 16 \rangle$$

(i) Arc colorings

$$\begin{aligned} a_1 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_5 &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_2 &= \begin{pmatrix} 1 \\ u^2 \end{pmatrix} \\ a_6 &= \begin{pmatrix} -u \\ -u^3 + u \end{pmatrix} \\ a_3 &= \begin{pmatrix} -u^2 + 1 \\ -u^4 + 2u^2 \end{pmatrix} \\ a_{10} &= \left( \frac{7773}{1931}u^{31} - \frac{41277}{8}u^{30} + \cdots + \frac{41415}{2}u + 5577 \right. \\ &\quad \left. - \frac{5185}{2}u^{30} + \cdots + 11043u + 2949 \right) \\ a_7 &= \left( \frac{107}{143}u^{31} - 546u^{30} + \cdots + \frac{3227}{2}u + \frac{921}{2} \right. \\ &\quad \left. - 740u^{30} + \cdots + \frac{4873}{2}u + 680 \right) \\ a_{11} &= \left( \frac{247}{16}u^{31} - \frac{1881}{8}u^{30} + \cdots + \frac{5429}{2}u + 656 \right. \\ &\quad \left. - \frac{181}{2}u^{31} + \frac{345}{2}u^{30} + \cdots + 1311u + 261 \right) \\ a_9 &= \left( \frac{3911}{1931}u^{31} - \frac{20537}{8}u^{30} + \cdots + \frac{19329}{2}u + 2628 \right. \\ &\quad \left. - \frac{5185}{2}u^{30} + \cdots + 11043u + 2949 \right) \\ a_4 &= \left( \frac{43}{22}u^{31} - \frac{441}{240}u^{30} + \cdots + 660u + \frac{377}{2} \right. \\ &\quad \left. - 240u^{30} + \cdots + \frac{2169}{2}u + 288 \right) \\ a_8 &= \left( \frac{2271}{8}u^{31} - \frac{24371}{8795}u^{30} + \cdots + 13172u + \frac{7009}{2} \right. \\ &\quad \left. - \frac{1689}{8}u^{31} + \frac{8795}{2}u^{30} + \cdots - \frac{14811}{2}u - 2064 \right) \\ a_{12} &= \left( \frac{566}{355}u^{31} - \frac{23745}{14985}u^{30} + \cdots + \frac{86833}{4}u + 5945 \right. \\ &\quad \left. - \frac{14985}{4}u^{30} + \cdots + 14324u + 3892 \right) \end{aligned}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes =  $\frac{4311}{2}u^{31} - 22730u^{30} + \cdots + 87134u + 23654$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_2, c_5$	$u^{32} + 12u^{31} + \cdots + 48u - 16$
$c_3, c_4, c_8$ $c_{10}$	$u^{32} - u^{31} + \cdots + u^2 + 1$
$c_6, c_9$	$u^{32} + u^{31} + \cdots - 17u - 1$
$c_7, c_{11}, c_{12}$	$u^{32} - 14u^{31} + \cdots + 736u - 64$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_5$	$y^{32} - 32y^{31} + \cdots - 1408y + 256$
$c_3, c_4, c_8$ $c_{10}$	$y^{32} - 35y^{31} + \cdots + 2y + 1$
$c_6, c_9$	$y^{32} + 25y^{31} + \cdots - 121y + 1$
$c_7, c_{11}, c_{12}$	$y^{32} + 30y^{31} + \cdots - 46080y + 4096$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.680828 + 0.815159I$		
$a = 0.589852 - 0.500904I$	$-15.1501 + 11.2353I$	$-10.12137 - 6.63149I$
$b = -0.68125 - 1.37591I$		
$u = -0.680828 - 0.815159I$		
$a = 0.589852 + 0.500904I$	$-15.1501 - 11.2353I$	$-10.12137 + 6.63149I$
$b = -0.68125 + 1.37591I$		
$u = -0.494831 + 0.951026I$		
$a = -0.617680 - 0.176687I$	$-14.5005 - 5.4219I$	$-10.91537 + 2.28879I$
$b = -0.232561 + 1.197900I$		
$u = -0.494831 - 0.951026I$		
$a = -0.617680 + 0.176687I$	$-14.5005 + 5.4219I$	$-10.91537 - 2.28879I$
$b = -0.232561 - 1.197900I$		
$u = -1.14307$		
$a = -0.439539$	$-1.32792$	$-8.36980$
$b = -1.07672$		
$u = -0.713057 + 0.906916I$		
$a = -0.473999 + 0.283951I$	$-7.22904 + 6.56235I$	$0$
$b = 0.435641 + 1.156230I$		
$u = -0.713057 - 0.906916I$		
$a = -0.473999 - 0.283951I$	$-7.22904 - 6.56235I$	$0$
$b = 0.435641 - 1.156230I$		
$u = -0.615956 + 1.004530I$		
$a = 0.488535 - 0.045297I$	$-6.84872 - 0.16660I$	$0$
$b = -0.108266 - 1.094690I$		
$u = -0.615956 - 1.004530I$		
$a = 0.488535 + 0.045297I$	$-6.84872 + 0.16660I$	$0$
$b = -0.108266 + 1.094690I$		
$u = 1.157610 + 0.416068I$		
$a = 0.506893 - 0.188759I$	$-4.34328 - 2.34802I$	$0$
$b = 0.108022 + 0.275619I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.157610 - 0.416068I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = 0.506893 + 0.188759I$	$-4.34328 + 2.34802I$	0
$b = 0.108022 - 0.275619I$		
$u = -1.232110 + 0.231185I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = 0.300965 + 0.165464I$	$-4.97841 + 4.31582I$	0
$b = 0.944141 + 0.205181I$		
$u = -1.232110 - 0.231185I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = 0.300965 - 0.165464I$	$-4.97841 - 4.31582I$	0
$b = 0.944141 - 0.205181I$		
$u = 0.739575$		
$a = -0.445134$	$-0.987038$	-12.9270
$b = 0.0857344$		
$u = 0.057187 + 0.603926I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = -0.204724 + 0.701064I$	$-1.25850 - 1.44721I$	$-2.35502 + 5.22658I$
$b = 0.460672 - 0.183999I$		
$u = 0.057187 - 0.603926I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = -0.204724 - 0.701064I$	$-1.25850 + 1.44721I$	$-2.35502 - 5.22658I$
$b = 0.460672 + 0.183999I$		
$u = 1.45355 + 0.03396I$		
$a = -0.23567 + 1.66598I$	$-4.57485 - 1.68293I$	0
$b = -0.262994 + 1.081130I$		
$u = 1.45355 - 0.03396I$		
$a = -0.23567 - 1.66598I$	$-4.57485 + 1.68293I$	0
$b = -0.262994 - 1.081130I$		
$u = 1.50382 + 0.05578I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = 0.50318 - 1.98250I$	$-10.29120 - 4.14932I$	0
$b = 0.60170 - 1.43953I$		
$u = 1.50382 - 0.05578I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = 0.50318 + 1.98250I$	$-10.29120 + 4.14932I$	0
$b = 0.60170 + 1.43953I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.456157 + 0.188264I$		
$a = 0.30670 + 1.62184I$	$-3.74818 + 3.21761I$	$2.70792 - 3.34583I$
$b = 0.776747 + 0.909381I$		
$u = -0.456157 - 0.188264I$		
$a = 0.30670 - 1.62184I$	$-3.74818 - 3.21761I$	$2.70792 + 3.34583I$
$b = 0.776747 - 0.909381I$		
$u = -0.247450 + 0.286515I$		
$a = 0.10986 - 1.41840I$	$0.987106 + 0.748744I$	$5.19413 - 3.21537I$
$b = -0.582621 - 0.368449I$		
$u = -0.247450 - 0.286515I$		
$a = 0.10986 + 1.41840I$	$0.987106 - 0.748744I$	$5.19413 + 3.21537I$
$b = -0.582621 + 0.368449I$		
$u = 1.60347 + 0.26376I$		
$a = 0.08484 + 1.83824I$	$16.7864 - 15.2459I$	0
$b = -0.99385 + 1.70026I$		
$u = 1.60347 - 0.26376I$		
$a = 0.08484 - 1.83824I$	$16.7864 + 15.2459I$	0
$b = -0.99385 - 1.70026I$		
$u = 1.60023 + 0.36433I$		
$a = -0.567147 - 0.962796I$	$18.1780 + 0.4768I$	0
$b = 0.302404 - 1.251650I$		
$u = 1.60023 - 0.36433I$		
$a = -0.567147 + 0.962796I$	$18.1780 - 0.4768I$	0
$b = 0.302404 + 1.251650I$		
$u = 1.62632 + 0.27751I$		
$a = -0.07773 - 1.52430I$	$-14.9769 - 10.9327I$	0
$b = 0.87969 - 1.48385I$		
$u = 1.62632 - 0.27751I$		
$a = -0.07773 + 1.52430I$	$-14.9769 + 10.9327I$	0
$b = 0.87969 + 1.48385I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.63995 + 0.31827I$		
$a = 0.228456 + 1.197060I$	$-14.3366 - 4.7680I$	0
$b = -0.65199 + 1.30081I$		
$u = 1.63995 - 0.31827I$		
$a = 0.228456 - 1.197060I$	$-14.3366 + 4.7680I$	0
$b = -0.65199 - 1.30081I$		

$$\text{III. } I_2^u = \langle -1.03 \times 10^{22}a^7u^5 + 8.99 \times 10^{21}a^6u^5 + \dots - 4.39 \times 10^{21}a + 3.99 \times 10^{22}, -a^7u^5 + 8a^6u^5 + \dots - 489a + 821, u^6 + u^5 - 3u^4 - 2u^3 + 2u^2 - u - 1 \rangle$$

(i) Arc colorings

$$\begin{aligned} a_1 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_5 &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_2 &= \begin{pmatrix} 1 \\ u^2 \end{pmatrix} \\ a_6 &= \begin{pmatrix} -u \\ -u^3 + u \end{pmatrix} \\ a_3 &= \begin{pmatrix} -u^2 + 1 \\ -u^4 + 2u^2 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} a \\ 0.493774a^7u^5 - 0.432600a^6u^5 + \dots + 0.211415a - 1.91748 \end{pmatrix} \\ a_7 &= \begin{pmatrix} -0.0990366a^7u^5 + 0.0845549a^6u^5 + \dots + 0.244699a + 0.622156 \\ 0.550411a^7u^5 - 1.43426a^6u^5 + \dots - 0.965495a - 1.46874 \end{pmatrix} \\ a_{11} &= \begin{pmatrix} -1.24509a^7u^5 + 1.54783a^6u^5 + \dots + 0.631576a + 0.985297 \\ 0.939975a^7u^5 - 1.15258a^6u^5 + \dots - 0.412776a - 2.64976 \end{pmatrix} \\ a_9 &= \begin{pmatrix} -0.493774a^7u^5 + 0.432600a^6u^5 + \dots + 0.788585a + 1.91748 \\ 0.493774a^7u^5 - 0.432600a^6u^5 + \dots + 0.211415a - 1.91748 \end{pmatrix} \\ a_4 &= \begin{pmatrix} 1.15029a^7u^5 - 1.79608a^6u^5 + \dots - 1.16871a - 4.70289 \\ -1.05125a^7u^5 + 1.71153a^6u^5 + \dots + 0.924014a + 4.08073 \end{pmatrix} \\ a_8 &= \begin{pmatrix} 0.634934a^7u^5 - 1.65705a^6u^5 + \dots - 2.68099a - 1.05272 \\ -0.970106a^7u^5 + 1.96530a^6u^5 + \dots + 1.88294a + 3.88034 \end{pmatrix} \\ a_{12} &= \begin{pmatrix} -0.590593a^7u^5 + 1.21867a^6u^5 + \dots + 0.288049a + 1.83640 \\ 0.520280a^7u^5 - 0.621535a^6u^5 + \dots + 0.504665a - 1.23816 \end{pmatrix} \end{aligned}$$

(ii) Obstruction class = -1

$$(iii) \text{ Cusp Shapes} = \frac{32386428834844106415168}{20783768619782088516773}a^7u^5 + \frac{23417790588849644990728}{20783768619782088516773}a^6u^5 + \dots + \frac{45950322676565104630412}{20783768619782088516773}a - \frac{306021993643431809155814}{20783768619782088516773}$$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_2, c_5$	$(u^6 - u^5 - 3u^4 + 2u^3 + 2u^2 + u - 1)^8$
$c_3, c_4, c_8$ $c_{10}$	$u^{48} + u^{47} + \dots - 1444u + 479$
$c_6, c_9$	$u^{48} - 7u^{47} + \dots - 40272u + 71579$
$c_7, c_{11}, c_{12}$	$(u^4 + u^3 + 3u^2 + 2u + 1)^{12}$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_5$	$(y^6 - 7y^5 + 17y^4 - 16y^3 + 6y^2 - 5y + 1)^8$
$c_3, c_4, c_8$ $c_{10}$	$y^{48} - 49y^{47} + \dots + 10146608y + 229441$
$c_6, c_9$	$y^{48} + 23y^{47} + \dots + 117241967100y + 5123553241$
$c_7, c_{11}, c_{12}$	$(y^4 + 5y^3 + 7y^2 + 2y + 1)^{12}$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.493180 + 0.575288I$		
$a = -0.900819 + 0.089225I$	$-1.76355 - 0.55731I$	$-4.74899 - 1.22396I$
$b = 0.127208 - 0.784719I$		
$u = 0.493180 + 0.575288I$		
$a = -0.488061 - 1.039120I$	$-1.76355 - 3.38752I$	$-4.74899 + 8.59352I$
$b = 0.459656 - 0.638436I$		
$u = 0.493180 + 0.575288I$		
$a = -0.630925 - 0.290654I$	$-8.76530 - 5.13637I$	$-8.40246 + 6.24958I$
$b = 0.70939 - 1.58712I$		
$u = 0.493180 + 0.575288I$		
$a = 0.601944 + 0.215661I$	$-1.76355 - 3.38752I$	$-4.74899 + 8.59352I$
$b = -0.532273 + 1.115900I$		
$u = 0.493180 + 0.575288I$		
$a = 1.55616 - 0.32740I$	$-8.76530 + 1.19155I$	$-8.40246 + 1.11998I$
$b = 0.215809 + 1.064350I$		
$u = 0.493180 + 0.575288I$		
$a = 0.181370 + 0.327241I$	$-1.76355 - 0.55731I$	$-4.74899 - 1.22396I$
$b = 0.293994 + 0.548435I$		
$u = 0.493180 + 0.575288I$		
$a = -0.295940 + 0.035805I$	$-8.76530 + 1.19155I$	$-8.40246 + 1.11998I$
$b = -0.950173 - 0.904845I$		
$u = 0.493180 + 0.575288I$		
$a = 0.83692 + 1.56767I$	$-8.76530 - 5.13637I$	$-8.40246 + 6.24958I$
$b = -0.819030 + 0.843679I$		
$u = 0.493180 - 0.575288I$		
$a = -0.900819 - 0.089225I$	$-1.76355 + 0.55731I$	$-4.74899 + 1.22396I$
$b = 0.127208 + 0.784719I$		
$u = 0.493180 - 0.575288I$		
$a = -0.488061 + 1.039120I$	$-1.76355 + 3.38752I$	$-4.74899 - 8.59352I$
$b = 0.459656 + 0.638436I$		

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.493180 - 0.575288I$		
$a = -0.630925 + 0.290654I$	$-8.76530 + 5.13637I$	$-8.40246 - 6.24958I$
$b = 0.70939 + 1.58712I$		
$u = 0.493180 - 0.575288I$		
$a = 0.601944 - 0.215661I$	$-1.76355 + 3.38752I$	$-4.74899 - 8.59352I$
$b = -0.532273 - 1.115900I$		
$u = 0.493180 - 0.575288I$		
$a = 1.55616 + 0.32740I$	$-8.76530 - 1.19155I$	$-8.40246 - 1.11998I$
$b = 0.215809 - 1.064350I$		
$u = 0.493180 - 0.575288I$		
$a = 0.181370 - 0.327241I$	$-1.76355 + 0.55731I$	$-4.74899 + 1.22396I$
$b = 0.293994 - 0.548435I$		
$u = 0.493180 - 0.575288I$		
$a = -0.295940 - 0.035805I$	$-8.76530 - 1.19155I$	$-8.40246 - 1.11998I$
$b = -0.950173 + 0.904845I$		
$u = 0.493180 - 0.575288I$		
$a = 0.83692 - 1.56767I$	$-8.76530 + 5.13637I$	$-8.40246 - 6.24958I$
$b = -0.819030 - 0.843679I$		
$u = -0.483672$		
$a = 1.243000 + 0.503165I$	$-12.46440 + 3.16396I$	$-17.2435 - 2.5648I$
$b = -1.55666 + 1.20761I$		
$u = -0.483672$		
$a = 1.243000 - 0.503165I$	$-12.46440 - 3.16396I$	$-17.2435 + 2.5648I$
$b = -1.55666 - 1.20761I$		
$u = -0.483672$		
$a = -1.68596 + 0.76343I$	$-5.46265 - 1.41510I$	$-13.5900 + 4.9087I$
$b = 0.935756 + 0.863246I$		
$u = -0.483672$		
$a = -1.68596 - 0.76343I$	$-5.46265 + 1.41510I$	$-13.5900 - 4.9087I$
$b = 0.935756 - 0.863246I$		

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.483672$		
$a = 2.75014 + 1.41553I$	$-5.46265 - 1.41510I$	$-13.5900 + 4.9087I$
$b = -0.172089 + 0.700395I$		
$u = -0.483672$		
$a = 2.75014 - 1.41553I$	$-5.46265 + 1.41510I$	$-13.5900 - 4.9087I$
$b = -0.172089 - 0.700395I$		
$u = -0.483672$		
$a = -3.81963 + 2.25339I$	$-12.46440 + 3.16396I$	$-17.2435 - 2.5648I$
$b = -0.292353 + 0.770523I$		
$u = -0.483672$		
$a = -3.81963 - 2.25339I$	$-12.46440 - 3.16396I$	$-17.2435 + 2.5648I$
$b = -0.292353 - 0.770523I$		
$u = -1.52087 + 0.16310I$		
$a = 0.782884 - 1.127760I$	$-15.4211 + 1.4282I$	$-12.40788 - 0.64002I$
$b = -0.343085 - 1.002600I$		
$u = -1.52087 + 0.16310I$		
$a = -0.200569 + 1.374100I$	$-8.41938 + 3.17702I$	$-8.75440 + 1.70392I$
$b = 0.675225 + 1.150860I$		
$u = -1.52087 + 0.16310I$		
$a = 0.439631 - 1.327350I$	$-8.41938 + 3.17702I$	$-8.75440 + 1.70392I$
$b = 0.265769 - 1.130460I$		
$u = -1.52087 + 0.16310I$		
$a = -1.15986 + 1.16720I$	$-15.4211 + 1.4282I$	$-12.40788 - 0.64002I$
$b = -1.06617 + 1.40127I$		
$u = -1.52087 + 0.16310I$		
$a = -0.04775 + 1.70162I$	$-8.41938 + 6.00723I$	$-8.75440 - 8.11356I$
$b = 0.327173 + 1.006110I$		
$u = -1.52087 + 0.16310I$		
$a = -0.06236 - 1.91890I$	$-8.41938 + 6.00723I$	$-8.75440 - 8.11356I$
$b = -0.88964 - 1.76077I$		

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.52087 + 0.16310I$		
$a = -0.07791 - 2.08226I$	$-15.4211 + 7.7561I$	$-12.40788 - 5.76962I$
$b = -0.593633 - 1.010750I$		
$u = -1.52087 + 0.16310I$		
$a = 0.14267 + 2.45572I$	$-15.4211 + 7.7561I$	$-12.40788 - 5.76962I$
$b = 1.08638 + 2.38993I$		
$u = -1.52087 - 0.16310I$		
$a = 0.782884 + 1.127760I$	$-15.4211 - 1.4282I$	$-12.40788 + 0.64002I$
$b = -0.343085 + 1.002600I$		
$u = -1.52087 - 0.16310I$		
$a = -0.200569 - 1.374100I$	$-8.41938 - 3.17702I$	$-8.75440 - 1.70392I$
$b = 0.675225 - 1.150860I$		
$u = -1.52087 - 0.16310I$		
$a = 0.439631 + 1.327350I$	$-8.41938 - 3.17702I$	$-8.75440 - 1.70392I$
$b = 0.265769 + 1.130460I$		
$u = -1.52087 - 0.16310I$		
$a = -1.15986 - 1.16720I$	$-15.4211 - 1.4282I$	$-12.40788 + 0.64002I$
$b = -1.06617 - 1.40127I$		
$u = -1.52087 - 0.16310I$		
$a = -0.04775 - 1.70162I$	$-8.41938 - 6.00723I$	$-8.75440 + 8.11356I$
$b = 0.327173 - 1.006110I$		
$u = -1.52087 - 0.16310I$		
$a = -0.06236 + 1.91890I$	$-8.41938 - 6.00723I$	$-8.75440 + 8.11356I$
$b = -0.88964 + 1.76077I$		
$u = -1.52087 - 0.16310I$		
$a = -0.07791 + 2.08226I$	$-15.4211 - 7.7561I$	$-12.40788 + 5.76962I$
$b = -0.593633 + 1.010750I$		
$u = -1.52087 - 0.16310I$		
$a = 0.14267 - 2.45572I$	$-15.4211 - 7.7561I$	$-12.40788 + 5.76962I$
$b = 1.08638 - 2.38993I$		

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.53904$		
$a = 0.244560 + 1.155160I$	$-12.38390 - 1.41510I$	$-12.44276 + 4.90874I$
$b = -0.847287 + 0.822406I$		
$u = 1.53904$		
$a = 0.244560 - 1.155160I$	$-12.38390 + 1.41510I$	$-12.44276 - 4.90874I$
$b = -0.847287 - 0.822406I$		
$u = 1.53904$		
$a = 0.92692 + 1.24349I$	$-12.38390 - 1.41510I$	$-12.44276 + 4.90874I$
$b = 1.81916 + 1.16754I$		
$u = 1.53904$		
$a = 0.92692 - 1.24349I$	$-12.38390 + 1.41510I$	$-12.44276 - 4.90874I$
$b = 1.81916 - 1.16754I$		
$u = 1.53904$		
$a = -1.03576 + 1.39658I$	$-19.3856 + 3.1640I$	$-16.0962 - 2.5648I$
$b = 0.317947 + 0.787184I$		
$u = 1.53904$		
$a = -1.03576 - 1.39658I$	$-19.3856 - 3.1640I$	$-16.0962 + 2.5648I$
$b = 0.317947 - 0.787184I$		
$u = 1.53904$		
$a = -1.80066 + 1.63792I$	$-19.3856 + 3.1640I$	$-16.0962 - 2.5648I$
$b = -2.67107 + 1.73026I$		
$u = 1.53904$		
$a = -1.80066 - 1.63792I$	$-19.3856 - 3.1640I$	$-16.0962 + 2.5648I$
$b = -2.67107 - 1.73026I$		

### III.

$$I_3^u = \langle u^{21} + 2u^{20} + \dots + b + u, 4u^{21} + 8u^{20} + \dots + a + 5, u^{22} + 3u^{21} + \dots + 3u + 1 \rangle$$

**(i) Arc colorings**

$$a_1 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -u \\ -u^3 + u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -u^2 + 1 \\ -u^4 + 2u^2 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -4u^{21} - 8u^{20} + \dots - 17u - 5 \\ -u^{21} - 2u^{20} + \dots - 10u^2 - u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -7u^{21} - 13u^{20} + \dots - 23u - 4 \\ -3u^{21} - 5u^{20} + \dots + u - 1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -u^{21} - 3u^{20} + \dots - 12u - 4 \\ -2u^{21} - 3u^{20} + \dots - 12u^2 - u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -3u^{21} - 6u^{20} + \dots - 16u - 5 \\ -u^{21} - 2u^{20} + \dots - 10u^2 - u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -3u^{20} - 4u^{19} + \dots - 20u - 3 \\ 4u^{21} + 7u^{20} + \dots + 10u + 4 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 4u^{21} + 9u^{20} + \dots + 26u + 1 \\ 3u^{21} + 4u^{20} + \dots + 19u^2 + 2 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 6u^{21} + 11u^{20} + \dots + 16u + 11 \\ 2u^{21} + 2u^{20} + \dots + 17u^2 + 6u \end{pmatrix}$$

**(ii) Obstruction class = 1**

**(iii) Cusp Shapes**

$$\begin{aligned} &= -5u^{21} - 12u^{20} + 41u^{19} + 109u^{18} - 134u^{17} - 397u^{16} + 250u^{15} + 753u^{14} - 378u^{13} - 815u^{12} + \\ &539u^{11} + 500u^{10} - 577u^9 - 125u^8 + 397u^7 - 16u^6 - 155u^5 + 15u^4 + 39u^3 - 7u^2 - u - 7 \end{aligned}$$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_2$	$u^{22} + 3u^{21} + \cdots + 3u + 1$
$c_3, c_8$	$u^{22} + u^{21} + \cdots + u - 1$
$c_4, c_{10}$	$u^{22} - u^{21} + \cdots - u - 1$
$c_5$	$u^{22} - 3u^{21} + \cdots - 3u + 1$
$c_6, c_9$	$u^{22} + u^{21} + \cdots - 5u^2 - 1$
$c_7$	$u^{22} - u^{21} + \cdots + 2u - 1$
$c_{11}, c_{12}$	$u^{22} + u^{21} + \cdots - 2u - 1$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_5$	$y^{22} - 25y^{21} + \cdots + 3y + 1$
$c_3, c_4, c_8$ $c_{10}$	$y^{22} - 25y^{21} + \cdots - 39y + 1$
$c_6, c_9$	$y^{22} + 7y^{21} + \cdots + 10y + 1$
$c_7, c_{11}, c_{12}$	$y^{22} + 25y^{21} + \cdots + 8y + 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.830041 + 0.372143I$	$-4.33333 - 3.17748I$	$-11.15222 + 4.56629I$
$a = 0.018859 + 0.570003I$		
$b = -0.538229 + 0.805569I$		
$u = 0.830041 - 0.372143I$	$-4.33333 + 3.17748I$	$-11.15222 - 4.56629I$
$a = 0.018859 - 0.570003I$		
$b = -0.538229 - 0.805569I$		
$u = 0.856682 + 0.292394I$	$-4.33137 - 3.17736I$	$-10.79809 + 3.65508I$
$a = -0.110513 + 0.558228I$		
$b = -0.609214 + 0.752506I$		
$u = 0.856682 - 0.292394I$	$-4.33137 + 3.17736I$	$-10.79809 - 3.65508I$
$a = -0.110513 - 0.558228I$		
$b = -0.609214 - 0.752506I$		
$u = 0.903347$		
$a = 0.392353$	$-0.339311$	$2.40450$
$b = 0.674604$		
$u = 0.366487 + 0.738621I$		
$a = -0.651754 - 0.018325I$	$-2.73349 - 1.32865I$	$-11.07966 + 3.39512I$
$b = 0.052630 - 0.833432I$		
$u = 0.366487 - 0.738621I$		
$a = -0.651754 + 0.018325I$	$-2.73349 + 1.32865I$	$-11.07966 - 3.39512I$
$b = 0.052630 + 0.833432I$		
$u = -1.133040 + 0.450430I$		
$a = -0.837685 + 0.173018I$	$-6.73763 + 4.05980I$	$-12.29979 - 3.84797I$
$b = 0.142357 + 0.468689I$		
$u = -1.133040 - 0.450430I$		
$a = -0.837685 - 0.173018I$	$-6.73763 - 4.05980I$	$-12.29979 + 3.84797I$
$b = 0.142357 - 0.468689I$		
$u = -0.556044 + 0.401150I$		
$a = 1.062440 + 0.854118I$	$-4.73125 - 0.60844I$	$-6.34000 - 1.21463I$
$b = -0.394837 - 0.396064I$		

Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.556044 - 0.401150I$		
$a = 1.062440 - 0.854118I$	$-4.73125 + 0.60844I$	$-6.34000 + 1.21463I$
$b = -0.394837 + 0.396064I$		
$u = -1.404820 + 0.132257I$		
$a = 1.38773 - 1.60582I$	$-16.0996 + 4.5307I$	$-12.95570 - 3.19344I$
$b = 0.380589 - 1.217270I$		
$u = -1.404820 - 0.132257I$		
$a = 1.38773 + 1.60582I$	$-16.0996 - 4.5307I$	$-12.95570 + 3.19344I$
$b = 0.380589 + 1.217270I$		
$u = -1.50090 + 0.18006I$		
$a = -0.45664 + 1.58550I$	$-8.89437 + 4.43912I$	$-12.33495 - 4.11395I$
$b = 0.243005 + 1.305180I$		
$u = -1.50090 - 0.18006I$		
$a = -0.45664 - 1.58550I$	$-8.89437 - 4.43912I$	$-12.33495 + 4.11395I$
$b = 0.243005 - 1.305180I$		
$u = 1.51916 + 0.06554I$		
$a = 0.358638 - 0.126439I$	$-17.6475 + 1.8704I$	$-12.10898 - 0.36759I$
$b = 1.40443 - 0.38841I$		
$u = 1.51916 - 0.06554I$		
$a = 0.358638 + 0.126439I$	$-17.6475 - 1.8704I$	$-12.10898 + 0.36759I$
$b = 1.40443 + 0.38841I$		
$u = 1.55580$		
$a = -0.343399$	$-12.3748$	$-12.4960$
$b = -1.36546$		
$u = -1.56422 + 0.13165I$		
$a = -0.14890 - 1.88832I$	$-11.90160 + 5.17271I$	$-12.89162 - 3.86694I$
$b = -0.65795 - 1.59210I$		
$u = -1.56422 - 0.13165I$		
$a = -0.14890 + 1.88832I$	$-11.90160 - 5.17271I$	$-12.89162 + 3.86694I$
$b = -0.65795 + 1.59210I$		

Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.142925 + 0.254512I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$
$a = -0.14665 - 4.37491I$	$-11.63890 - 3.03242I$	$-5.49334 + 0.66440I$
$b = 0.822645 + 0.792653I$		
$u = -0.142925 - 0.254512I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$
$a = -0.14665 + 4.37491I$	$-11.63890 + 3.03242I$	$-5.49334 - 0.66440I$
$b = 0.822645 - 0.792653I$		

#### IV. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1, c_2$	$((u^6 - u^5 - 3u^4 + 2u^3 + 2u^2 + u - 1)^8)(u^{22} + 3u^{21} + \dots + 3u + 1)$ $\cdot (u^{32} + 12u^{31} + \dots + 48u - 16)$
$c_3, c_8$	$(u^{22} + u^{21} + \dots + u - 1)(u^{32} - u^{31} + \dots + u^2 + 1)$ $\cdot (u^{48} + u^{47} + \dots - 1444u + 479)$
$c_4, c_{10}$	$(u^{22} - u^{21} + \dots - u - 1)(u^{32} - u^{31} + \dots + u^2 + 1)$ $\cdot (u^{48} + u^{47} + \dots - 1444u + 479)$
$c_5$	$((u^6 - u^5 - 3u^4 + 2u^3 + 2u^2 + u - 1)^8)(u^{22} - 3u^{21} + \dots - 3u + 1)$ $\cdot (u^{32} + 12u^{31} + \dots + 48u - 16)$
$c_6, c_9$	$(u^{22} + u^{21} + \dots - 5u^2 - 1)(u^{32} + u^{31} + \dots - 17u - 1)$ $\cdot (u^{48} - 7u^{47} + \dots - 40272u + 71579)$
$c_7$	$((u^4 + u^3 + 3u^2 + 2u + 1)^{12})(u^{22} - u^{21} + \dots + 2u - 1)$ $\cdot (u^{32} - 14u^{31} + \dots + 736u - 64)$
$c_{11}, c_{12}$	$((u^4 + u^3 + 3u^2 + 2u + 1)^{12})(u^{22} + u^{21} + \dots - 2u - 1)$ $\cdot (u^{32} - 14u^{31} + \dots + 736u - 64)$

## V. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_5$	$((y^6 - 7y^5 + \dots - 5y + 1)^8)(y^{22} - 25y^{21} + \dots + 3y + 1)$ $\cdot (y^{32} - 32y^{31} + \dots - 1408y + 256)$
$c_3, c_4, c_8$ $c_{10}$	$(y^{22} - 25y^{21} + \dots - 39y + 1)(y^{32} - 35y^{31} + \dots + 2y + 1)$ $\cdot (y^{48} - 49y^{47} + \dots + 10146608y + 229441)$
$c_6, c_9$	$(y^{22} + 7y^{21} + \dots + 10y + 1)(y^{32} + 25y^{31} + \dots - 121y + 1)$ $\cdot (y^{48} + 23y^{47} + \dots + 117241967100y + 5123553241)$
$c_7, c_{11}, c_{12}$	$((y^4 + 5y^3 + 7y^2 + 2y + 1)^{12})(y^{22} + 25y^{21} + \dots + 8y + 1)$ $\cdot (y^{32} + 30y^{31} + \dots - 46080y + 4096)$