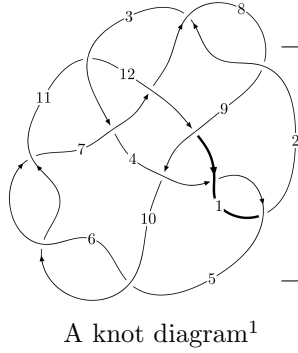
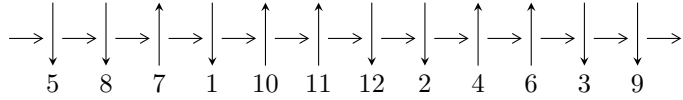


12a<sub>1272</sub> (K12a<sub>1272</sub>)



**Linearized knot diagram**



**Solving Sequence**

$$2,5 \xrightarrow{c_1} 1 \xrightarrow{c_4} 4,9 \xrightarrow{c_9} 10 \xrightarrow{c_5} 6 \xrightarrow{c_8} 8 \xrightarrow{c_2} 3 \xrightarrow{c_{12}} 12 \xrightarrow{c_7} 7 \xrightarrow{c_{11}} 11 \rightsquigarrow c_3, c_6, c_{10}$$

**Ideals for irreducible components<sup>2</sup> of  $X_{\text{par}}$**

$$I_1^u = \langle -5.27398 \times 10^{429} u^{131} - 9.58434 \times 10^{429} u^{130} + \dots + 9.61277 \times 10^{428} b - 5.45766 \times 10^{432}, \\ 1.80780 \times 10^{432} u^{131} + 3.29725 \times 10^{432} u^{130} + \dots + 2.02829 \times 10^{431} a + 1.86013 \times 10^{435}, \\ u^{132} + u^{131} + \dots - 1451u - 844 \rangle$$

$$I_2^u = \langle 2318651091u^{29} + 8025321455u^{28} + \dots + 9372903b + 4797253946, \\ -1257579720u^{29} - 4274580356u^{28} + \dots + 9372903a - 2710745983, u^{30} + 4u^{29} + \dots + 7u + 1 \rangle$$

$$I_3^u = \langle b + a - 1, a^2 - 3a + 3, u - 1 \rangle$$

\* 3 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 164 representations.

<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\text{I. } I_1^u = \langle -5.27 \times 10^{429} u^{131} - 9.58 \times 10^{429} u^{130} + \dots + 9.61 \times 10^{428} b - 5.46 \times 10^{432}, 1.81 \times 10^{432} u^{131} + 3.30 \times 10^{432} u^{130} + \dots + 2.03 \times 10^{431} a + 1.86 \times 10^{435}, u^{132} + u^{131} + \dots - 1451u - 844 \rangle$$

(i) Arc colorings

$$a_2 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} u \\ -u^3 + u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -8.91293u^{131} - 16.2563u^{130} + \dots - 26935.2u - 9170.89 \\ 5.48643u^{131} + 9.97042u^{130} + \dots + 16692.0u + 5677.51 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -3.34622u^{131} - 6.13050u^{130} + \dots - 9951.53u - 3393.85 \\ 7.33783u^{131} + 13.3479u^{130} + \dots + 22362.1u + 7606.69 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -4.96312u^{131} - 9.02635u^{130} + \dots - 15167.5u - 5149.06 \\ 12.2350u^{131} + 22.1179u^{130} + \dots + 37446.3u + 12681.3 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -3.42650u^{131} - 6.28584u^{130} + \dots - 10243.3u - 3493.38 \\ 5.48643u^{131} + 9.97042u^{130} + \dots + 16692.0u + 5677.51 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 11.5848u^{131} + 21.0113u^{130} + \dots + 35412.9u + 12022.8 \\ -19.5383u^{131} - 35.3500u^{130} + \dots - 60023.3u - 20340.8 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 0.967020u^{131} + 1.73517u^{130} + \dots + 3148.59u + 1041.78 \\ -0.912310u^{131} - 1.60702u^{130} + \dots - 2865.28u - 960.299 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -4.07589u^{131} - 7.57566u^{130} + \dots - 11810.1u - 4058.04 \\ 6.06028u^{131} + 10.9765u^{130} + \dots + 18294.1u + 6226.53 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 5.61423u^{131} + 10.2551u^{130} + \dots + 16930.8u + 5749.34 \\ -11.4857u^{131} - 20.7801u^{130} + \dots - 35554.7u - 12041.1 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes =  $769.616u^{131} + 1391.64u^{130} + \dots + 2.37325 \times 10^6 u + 803188$ .

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_4$	$u^{132} - u^{131} + \dots + 1451u - 844$
$c_2, c_8$	$u^{132} + 44u^{130} + \dots - 21827u - 1189$
$c_3$	$u^{132} - 4u^{131} + \dots + 9472u - 2239$
$c_5, c_6, c_{10}$	$u^{132} + 2u^{131} + \dots + 130u + 19$
$c_7$	$u^{132} + u^{130} + \dots - 28u + 8$
$c_9$	$u^{132} - 4u^{130} + \dots - 37881u + 2437$
$c_{11}$	$u^{132} + 6u^{131} + \dots + 89459u + 56393$
$c_{12}$	$u^{132} - 5u^{131} + \dots + 4452u + 103$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_4$	$y^{132} - 63y^{131} + \dots - 11311753y + 712336$
$c_2, c_8$	$y^{132} + 88y^{131} + \dots - 71456419y + 1413721$
$c_3$	$y^{132} - 36y^{131} + \dots - 304367236y + 5013121$
$c_5, c_6, c_{10}$	$y^{132} - 144y^{131} + \dots - 14848y + 361$
$c_7$	$y^{132} + 2y^{131} + \dots - 4464y + 64$
$c_9$	$y^{132} - 8y^{131} + \dots - 75967363y + 5938969$
$c_{11}$	$y^{132} + 62y^{131} + \dots + 237776842153y + 3180170449$
$c_{12}$	$y^{132} - 27y^{131} + \dots - 6883504y + 10609$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.888433 + 0.459649I$	$10.08520 - 8.84662I$	0
$a = -0.192013 + 1.130340I$		
$b = 0.135369 + 1.366530I$		
$u = 0.888433 - 0.459649I$	$10.08520 + 8.84662I$	0
$a = -0.192013 - 1.130340I$		
$b = 0.135369 - 1.366530I$		
$u = -0.860001 + 0.505931I$	$10.41720 + 2.03214I$	0
$a = -0.524831 - 0.211304I$		
$b = 0.00912 - 1.53664I$		
$u = -0.860001 - 0.505931I$	$10.41720 - 2.03214I$	0
$a = -0.524831 + 0.211304I$		
$b = 0.00912 + 1.53664I$		
$u = -0.128893 + 0.987034I$	$6.25496 - 6.63131I$	0
$a = -0.107867 + 0.455133I$		
$b = -1.064690 - 0.044525I$		
$u = -0.128893 - 0.987034I$	$6.25496 + 6.63131I$	0
$a = -0.107867 - 0.455133I$		
$b = -1.064690 + 0.044525I$		
$u = -0.817665 + 0.595071I$	$10.91990 + 2.34128I$	0
$a = -1.375280 - 0.085348I$		
$b = -0.01154 - 1.61726I$		
$u = -0.817665 - 0.595071I$	$10.91990 - 2.34128I$	0
$a = -1.375280 + 0.085348I$		
$b = -0.01154 + 1.61726I$		
$u = -0.887029 + 0.426126I$	$9.85464 - 4.57208I$	0
$a = -0.238037 - 0.107971I$		
$b = 0.44793 + 1.51254I$		
$u = -0.887029 - 0.426126I$	$9.85464 + 4.57208I$	0
$a = -0.238037 + 0.107971I$		
$b = 0.44793 - 1.51254I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.299028 + 0.934814I$ $a = -0.339354 + 0.092362I$ $b = 0.388248 + 1.036060I$	$6.49844 - 4.55251I$	0
$u = -0.299028 - 0.934814I$ $a = -0.339354 - 0.092362I$ $b = 0.388248 - 1.036060I$	$6.49844 + 4.55251I$	0
$u = 0.259667 + 1.010660I$ $a = -0.136638 - 0.521034I$ $b = 0.403078 - 1.345030I$	$3.78458 + 8.55429I$	0
$u = 0.259667 - 1.010660I$ $a = -0.136638 + 0.521034I$ $b = 0.403078 + 1.345030I$	$3.78458 - 8.55429I$	0
$u = 0.881749 + 0.328399I$ $a = 2.48900 + 0.26366I$ $b = -0.17445 - 1.63310I$	$9.18224 - 1.20024I$	0
$u = 0.881749 - 0.328399I$ $a = 2.48900 - 0.26366I$ $b = -0.17445 + 1.63310I$	$9.18224 + 1.20024I$	0
$u = -0.971761 + 0.434578I$ $a = 1.40070 + 0.56574I$ $b = -0.282247 + 0.929840I$	$1.49064 + 1.85110I$	0
$u = -0.971761 - 0.434578I$ $a = 1.40070 - 0.56574I$ $b = -0.282247 - 0.929840I$	$1.49064 - 1.85110I$	0
$u = -0.917872 + 0.166230I$ $a = 1.326400 + 0.401788I$ $b = -0.149482 + 0.636067I$	$1.40547 + 1.62272I$	0
$u = -0.917872 - 0.166230I$ $a = 1.326400 - 0.401788I$ $b = -0.149482 - 0.636067I$	$1.40547 - 1.62272I$	0

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.902863 + 0.202398I$ $a = 1.93367 - 1.39062I$ $b = -0.181766 + 0.639474I$	$-0.956671 - 0.870714I$	0
$u = 0.902863 - 0.202398I$ $a = 1.93367 + 1.39062I$ $b = -0.181766 - 0.639474I$	$-0.956671 + 0.870714I$	0
$u = 0.924821$ $a = -3.20484$ $b = 2.41225$	$-0.379463$	0
$u = 0.919150 + 0.062875I$ $a = -1.22487 - 1.47381I$ $b = 0.43120 + 1.81191I$	$-0.312377 - 0.392334I$	0
$u = 0.919150 - 0.062875I$ $a = -1.22487 + 1.47381I$ $b = 0.43120 - 1.81191I$	$-0.312377 + 0.392334I$	0
$u = 0.854419 + 0.330939I$ $a = 1.40388 - 0.54442I$ $b = 0.05937 - 1.64090I$	$9.26391 - 1.67107I$	0
$u = 0.854419 - 0.330939I$ $a = 1.40388 + 0.54442I$ $b = 0.05937 + 1.64090I$	$9.26391 + 1.67107I$	0
$u = -0.747724 + 0.524870I$ $a = -2.12221 - 0.04445I$ $b = -0.080811 - 1.350620I$	$10.74310 + 2.15226I$	0
$u = -0.747724 - 0.524870I$ $a = -2.12221 + 0.04445I$ $b = -0.080811 + 1.350620I$	$10.74310 - 2.15226I$	0
$u = -0.989013 + 0.458677I$ $a = 2.20619 + 0.31109I$ $b = -0.232381 + 1.160650I$	$1.20534 + 2.58602I$	0

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.989013 - 0.458677I$		
$a = 2.20619 - 0.31109I$	$1.20534 - 2.58602I$	0
$b = -0.232381 - 1.160650I$		
$u = 1.017390 + 0.399155I$		
$a = 2.00809 + 0.70527I$	$2.53408 + 1.30747I$	0
$b = -0.011529 - 1.090260I$		
$u = 1.017390 - 0.399155I$		
$a = 2.00809 - 0.70527I$	$2.53408 - 1.30747I$	0
$b = -0.011529 + 1.090260I$		
$u = 1.025520 + 0.398648I$		
$a = -1.23586 + 0.83864I$	$-3.47015 - 2.63906I$	0
$b = 0.657096 - 0.430489I$		
$u = 1.025520 - 0.398648I$		
$a = -1.23586 - 0.83864I$	$-3.47015 + 2.63906I$	0
$b = 0.657096 + 0.430489I$		
$u = 0.777156 + 0.445739I$		
$a = -2.98626 - 0.24164I$	$10.45930 + 5.07607I$	0
$b = -0.139684 + 1.116770I$		
$u = 0.777156 - 0.445739I$		
$a = -2.98626 + 0.24164I$	$10.45930 - 5.07607I$	0
$b = -0.139684 - 1.116770I$		
$u = 1.086330 + 0.215183I$		
$a = 1.114480 - 0.586549I$	$-1.66184 - 0.75099I$	0
$b = -1.144630 + 0.562319I$		
$u = 1.086330 - 0.215183I$		
$a = 1.114480 + 0.586549I$	$-1.66184 + 0.75099I$	0
$b = -1.144630 - 0.562319I$		
$u = -0.798505 + 0.397196I$		
$a = 2.86222 - 0.71894I$	$10.17010 + 8.06121I$	0
$b = -0.63968 + 1.32038I$		



Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.798505 - 0.397196I$ $a = 2.86222 + 0.71894I$ $b = -0.63968 - 1.32038I$	$10.17010 - 8.06121I$	0
$u = -1.065870 + 0.319329I$ $a = -0.671097 + 0.337438I$ $b = 0.065196 + 0.246846I$	$-1.06962 + 3.70198I$	0
$u = -1.065870 - 0.319329I$ $a = -0.671097 - 0.337438I$ $b = 0.065196 - 0.246846I$	$-1.06962 - 3.70198I$	0
$u = -1.045210 + 0.408453I$ $a = -1.81053 + 0.50219I$ $b = 0.63280 - 1.27162I$	$2.58381 + 7.13715I$	0
$u = -1.045210 - 0.408453I$ $a = -1.81053 - 0.50219I$ $b = 0.63280 + 1.27162I$	$2.58381 - 7.13715I$	0
$u = -0.159394 + 0.861713I$ $a = -0.568599 - 0.640734I$ $b = -0.457630 + 0.026165I$	$7.95380 - 2.88865I$	0
$u = -0.159394 - 0.861713I$ $a = -0.568599 + 0.640734I$ $b = -0.457630 - 0.026165I$	$7.95380 + 2.88865I$	0
$u = 0.218566 + 1.107950I$ $a = 0.175980 + 0.419203I$ $b = 0.113053 + 1.137110I$	$4.87895 - 0.96047I$	0
$u = 0.218566 - 1.107950I$ $a = 0.175980 - 0.419203I$ $b = 0.113053 - 1.137110I$	$4.87895 + 0.96047I$	0
$u = 1.089370 + 0.342018I$ $a = -0.336039 + 0.778881I$ $b = 0.288735 - 0.667558I$	$-2.55378 - 0.72472I$	0

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.089370 - 0.342018I$ $a = -0.336039 - 0.778881I$ $b = 0.288735 + 0.667558I$	$-2.55378 + 0.72472I$	0
$u = 0.954127 + 0.635674I$ $a = 0.038859 - 0.760829I$ $b = -0.138686 + 0.697586I$	$2.05134 - 2.56323I$	0
$u = 0.954127 - 0.635674I$ $a = 0.038859 + 0.760829I$ $b = -0.138686 - 0.697586I$	$2.05134 + 2.56323I$	0
$u = -1.114630 + 0.308899I$ $a = -1.60111 - 0.32041I$ $b = 0.781702 - 0.119471I$	$-4.68421 + 3.54811I$	0
$u = -1.114630 - 0.308899I$ $a = -1.60111 + 0.32041I$ $b = 0.781702 + 0.119471I$	$-4.68421 - 3.54811I$	0
$u = -0.962547 + 0.685515I$ $a = -1.13022 - 0.93033I$ $b = 0.155733 - 0.969552I$	$-2.01475 + 2.72647I$	0
$u = -0.962547 - 0.685515I$ $a = -1.13022 + 0.93033I$ $b = 0.155733 + 0.969552I$	$-2.01475 - 2.72647I$	0
$u = 1.072570 + 0.500941I$ $a = 1.029600 - 0.741523I$ $b = -0.903930 + 0.587094I$	$2.25264 - 4.65575I$	0
$u = 1.072570 - 0.500941I$ $a = 1.029600 + 0.741523I$ $b = -0.903930 - 0.587094I$	$2.25264 + 4.65575I$	0
$u = 0.813276$ $a = 5.52679$ $b = -3.46759$	7.70114	0

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.356229 + 1.148630I$ $a = 0.168781 + 0.343370I$ $b = 0.433166 + 1.136880I$	$4.67103 - 1.62587I$	0
$u = -0.356229 - 1.148630I$ $a = 0.168781 - 0.343370I$ $b = 0.433166 - 1.136880I$	$4.67103 + 1.62587I$	0
$u = 0.022902 + 0.792156I$ $a = -0.047072 - 0.341718I$ $b = 0.798408 + 0.086019I$	$-0.69629 - 4.11755I$	0
$u = 0.022902 - 0.792156I$ $a = -0.047072 + 0.341718I$ $b = 0.798408 - 0.086019I$	$-0.69629 + 4.11755I$	0
$u = 0.437509 + 1.134300I$ $a = 0.033613 + 0.440353I$ $b = -0.51268 + 1.38631I$	$10.7695 + 12.2620I$	0
$u = 0.437509 - 1.134300I$ $a = 0.033613 - 0.440353I$ $b = -0.51268 - 1.38631I$	$10.7695 - 12.2620I$	0
$u = 0.783115$ $a = 0.911346$ $b = -0.608263$	$-1.26571$	0
$u = -0.598940 + 0.479604I$ $a = 0.448566 + 1.299910I$ $b = 0.052445 + 1.214290I$	$2.37714 + 1.31479I$	0
$u = -0.598940 - 0.479604I$ $a = 0.448566 - 1.299910I$ $b = 0.052445 - 1.214290I$	$2.37714 - 1.31479I$	0
$u = -1.120900 + 0.520454I$ $a = -1.92871 + 0.05999I$ $b = 0.404571 - 1.109500I$	$-1.30487 + 6.80594I$	0

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.120900 - 0.520454I$ $a = -1.92871 - 0.05999I$ $b = 0.404571 + 1.109500I$	$-1.30487 - 6.80594I$	0
$u = 1.164660 + 0.451459I$ $a = -1.95379 - 0.33001I$ $b = 0.35644 + 1.40839I$	$0.23382 - 7.72074I$	0
$u = 1.164660 - 0.451459I$ $a = -1.95379 + 0.33001I$ $b = 0.35644 - 1.40839I$	$0.23382 + 7.72074I$	0
$u = -0.736825$ $a = 3.08179$ $b = -0.0914915$	3.02836	0
$u = 1.203490 + 0.441169I$ $a = -0.969440 + 0.454908I$ $b = 1.325330 - 0.289045I$	$4.00324 - 1.47776I$	0
$u = 1.203490 - 0.441169I$ $a = -0.969440 - 0.454908I$ $b = 1.325330 + 0.289045I$	$4.00324 + 1.47776I$	0
$u = -0.261769 + 0.668003I$ $a = 0.590878 - 0.537091I$ $b = -0.209541 - 1.078610I$	$1.14713 - 2.21877I$	0
$u = -0.261769 - 0.668003I$ $a = 0.590878 + 0.537091I$ $b = -0.209541 + 1.078610I$	$1.14713 + 2.21877I$	0
$u = -1.205320 + 0.443525I$ $a = 1.37582 + 0.46499I$ $b = -1.145380 + 0.183326I$	$-4.29889 + 8.50488I$	0
$u = -1.205320 - 0.443525I$ $a = 1.37582 - 0.46499I$ $b = -1.145380 - 0.183326I$	$-4.29889 - 8.50488I$	0

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.171030 + 0.567634I$ $a = 0.574993 - 0.152351I$ $b = -0.110535 - 0.133405I$	$5.04933 + 8.10612I$	0
$u = -1.171030 - 0.567634I$ $a = 0.574993 + 0.152351I$ $b = -0.110535 + 0.133405I$	$5.04933 - 8.10612I$	0
$u = -0.982808 + 0.857356I$ $a = 0.894536 + 0.951800I$ $b = -0.061059 + 1.106970I$	$3.38915 + 3.27485I$	0
$u = -0.982808 - 0.857356I$ $a = 0.894536 - 0.951800I$ $b = -0.061059 - 1.106970I$	$3.38915 - 3.27485I$	0
$u = 1.228330 + 0.450570I$ $a = 1.077480 - 0.460181I$ $b = -0.888292 - 0.412295I$	$-4.23965 - 0.44921I$	0
$u = 1.228330 - 0.450570I$ $a = 1.077480 + 0.460181I$ $b = -0.888292 + 0.412295I$	$-4.23965 + 0.44921I$	0
$u = -1.230990 + 0.456388I$ $a = 0.181491 - 0.569155I$ $b = 0.262429 + 1.124450I$	$0.303412 + 0.871916I$	0
$u = -1.230990 - 0.456388I$ $a = 0.181491 + 0.569155I$ $b = 0.262429 - 1.124450I$	$0.303412 - 0.871916I$	0
$u = -0.088702 + 0.669160I$ $a = 0.589046 + 0.615861I$ $b = -0.232592 + 1.350320I$	$3.53727 + 3.67602I$	0
$u = -0.088702 - 0.669160I$ $a = 0.589046 - 0.615861I$ $b = -0.232592 - 1.350320I$	$3.53727 - 3.67602I$	0

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.320950 + 0.133082I$ $a = 0.478618 - 0.725833I$ $b = -0.277492 + 0.675710I$	$0.737823 + 0.896249I$	0
$u = 1.320950 - 0.133082I$ $a = 0.478618 + 0.725833I$ $b = -0.277492 - 0.675710I$	$0.737823 - 0.896249I$	0
$u = -1.185620 + 0.603238I$ $a = 1.68091 - 0.06456I$ $b = -0.567314 + 1.056540I$	$3.80200 + 10.11980I$	0
$u = -1.185620 - 0.603238I$ $a = 1.68091 + 0.06456I$ $b = -0.567314 - 1.056540I$	$3.80200 - 10.11980I$	0
$u = -1.328520 + 0.130575I$ $a = 0.398662 + 0.634277I$ $b = -0.472934 - 1.050020I$	$-2.16348 - 4.52737I$	0
$u = -1.328520 - 0.130575I$ $a = 0.398662 - 0.634277I$ $b = -0.472934 + 1.050020I$	$-2.16348 + 4.52737I$	0
$u = 1.081850 + 0.785669I$ $a = -0.640885 + 0.556637I$ $b = 0.254533 + 0.510690I$	$-2.02817 - 3.19514I$	0
$u = 1.081850 - 0.785669I$ $a = -0.640885 - 0.556637I$ $b = 0.254533 - 0.510690I$	$-2.02817 + 3.19514I$	0
$u = 1.231000 + 0.562678I$ $a = -1.340210 - 0.312386I$ $b = 0.111927 + 1.159600I$	$1.61202 - 4.74931I$	0
$u = 1.231000 - 0.562678I$ $a = -1.340210 + 0.312386I$ $b = 0.111927 - 1.159600I$	$1.61202 + 4.74931I$	0

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.237580 + 0.550508I$ $a = -1.254670 - 0.578778I$ $b = 1.40334 - 0.22807I$	$2.86994 + 12.04640I$	0
$u = -1.237580 - 0.550508I$ $a = -1.254670 + 0.578778I$ $b = 1.40334 + 0.22807I$	$2.86994 - 12.04640I$	0
$u = 0.598628 + 0.240960I$ $a = -0.41746 - 1.52277I$ $b = -0.128247 - 1.357570I$	$4.03807 - 4.46460I$	0
$u = 0.598628 - 0.240960I$ $a = -0.41746 + 1.52277I$ $b = -0.128247 + 1.357570I$	$4.03807 + 4.46460I$	0
$u = 0.364776 + 0.524785I$ $a = -1.53447 + 0.83795I$ $b = 0.754945 + 0.279104I$	$4.27359 + 0.41818I$	0
$u = 0.364776 - 0.524785I$ $a = -1.53447 - 0.83795I$ $b = 0.754945 - 0.279104I$	$4.27359 - 0.41818I$	0
$u = 1.225200 + 0.596736I$ $a = 1.70251 + 0.01514I$ $b = -0.50100 - 1.43795I$	$0.7781 - 14.2874I$	0
$u = 1.225200 - 0.596736I$ $a = 1.70251 - 0.01514I$ $b = -0.50100 + 1.43795I$	$0.7781 + 14.2874I$	0
$u = -0.209142 + 1.347150I$ $a = -0.218609 - 0.341615I$ $b = -0.294285 - 0.745193I$	$8.42783 - 2.79167I$	0
$u = -0.209142 - 1.347150I$ $a = -0.218609 + 0.341615I$ $b = -0.294285 + 0.745193I$	$8.42783 + 2.79167I$	0

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.219590 + 0.614211I$ $a = 1.46312 + 0.04774I$ $b = -0.61836 + 1.36761I$	$1.77093 + 7.69029I$	0
$u = -1.219590 - 0.614211I$ $a = 1.46312 - 0.04774I$ $b = -0.61836 - 1.36761I$	$1.77093 - 7.69029I$	0
$u = 0.607449 + 1.225470I$ $a = -0.008727 - 0.481828I$ $b = 0.061565 - 1.176820I$	$10.82320 + 2.58085I$	0
$u = 0.607449 - 1.225470I$ $a = -0.008727 + 0.481828I$ $b = 0.061565 + 1.176820I$	$10.82320 - 2.58085I$	0
$u = -0.559620 + 1.277610I$ $a = -0.167666 - 0.342309I$ $b = -0.603837 - 1.262080I$	$10.67920 - 1.72002I$	0
$u = -0.559620 - 1.277610I$ $a = -0.167666 + 0.342309I$ $b = -0.603837 + 1.262080I$	$10.67920 + 1.72002I$	0
$u = -0.492501 + 0.320631I$ $a = 0.129165 + 0.362271I$ $b = -0.32006 - 1.40564I$	$4.32601 - 3.70375I$	0
$u = -0.492501 - 0.320631I$ $a = 0.129165 - 0.362271I$ $b = -0.32006 + 1.40564I$	$4.32601 + 3.70375I$	0
$u = 1.23135 + 0.70339I$ $a = -1.61586 + 0.17680I$ $b = 0.57319 + 1.49506I$	$8.2076 - 18.7958I$	0
$u = 1.23135 - 0.70339I$ $a = -1.61586 - 0.17680I$ $b = 0.57319 - 1.49506I$	$8.2076 + 18.7958I$	0



Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.42213 + 0.13324I$ $a = -0.831170 + 0.429200I$ $b = 0.685492 - 1.091570I$	$2.81720 + 8.47909I$	0
$u = -1.42213 - 0.13324I$ $a = -0.831170 - 0.429200I$ $b = 0.685492 + 1.091570I$	$2.81720 - 8.47909I$	0
$u = 1.41683 + 0.26438I$ $a = -1.109950 + 0.168625I$ $b = 1.212520 + 0.615511I$	$0.99534 + 1.82942I$	0
$u = 1.41683 - 0.26438I$ $a = -1.109950 - 0.168625I$ $b = 1.212520 - 0.615511I$	$0.99534 - 1.82942I$	0
$u = 1.22825 + 0.75949I$ $a = 1.235980 - 0.105262I$ $b = -0.174476 - 1.243520I$	$8.61807 - 9.62658I$	0
$u = 1.22825 - 0.75949I$ $a = 1.235980 + 0.105262I$ $b = -0.174476 + 1.243520I$	$8.61807 + 9.62658I$	0
$u = -1.26281 + 0.76234I$ $a = -1.335770 - 0.250024I$ $b = 0.62952 - 1.50563I$	$8.22324 + 8.90731I$	0
$u = -1.26281 - 0.76234I$ $a = -1.335770 + 0.250024I$ $b = 0.62952 + 1.50563I$	$8.22324 - 8.90731I$	0
$u = 0.147938 + 0.455430I$ $a = 0.803767 - 0.078291I$ $b = -0.587379 - 0.193361I$	$-1.35324 - 0.77267I$	$-5.30506 + 0.81512I$
$u = 0.147938 - 0.455430I$ $a = 0.803767 + 0.078291I$ $b = -0.587379 + 0.193361I$	$-1.35324 + 0.77267I$	$-5.30506 - 0.81512I$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.151254 + 0.297937I$	$1.15096 - 0.92104I$	$4.55484 + 2.14940I$
$a = 1.78806 + 0.81849I$		
$b = 0.307687 - 0.326506I$		
$u = -0.151254 - 0.297937I$	$1.15096 + 0.92104I$	$4.55484 - 2.14940I$
$a = 1.78806 - 0.81849I$		
$b = 0.307687 + 0.326506I$		

**II.**

$$I_2^u = \langle 2.32 \times 10^9 u^{29} + 8.03 \times 10^9 u^{28} + \dots + 9.37 \times 10^6 b + 4.80 \times 10^9, -1.26 \times 10^9 u^{29} - 4.27 \times 10^9 u^{28} + \dots + 9.37 \times 10^6 a - 2.71 \times 10^9, u^{30} + 4u^{29} + \dots + 7u + 1 \rangle$$

**(i) Arc colorings**

$$\begin{aligned} a_2 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_5 &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_1 &= \begin{pmatrix} 1 \\ -u^2 \end{pmatrix} \\ a_4 &= \begin{pmatrix} u \\ -u^3 + u \end{pmatrix} \\ a_9 &= \begin{pmatrix} 134.172u^{29} + 456.057u^{28} + \dots + 1557.17u + 289.211 \\ -247.378u^{29} - 856.226u^{28} + \dots - 2556.65u - 511.822 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} 45.0125u^{29} + 152.845u^{28} + \dots + 560.461u + 96.1842 \\ -315.172u^{29} - 1089.94u^{28} + \dots - 3268.54u - 651.423 \end{pmatrix} \\ a_6 &= \begin{pmatrix} 141.162u^{29} + 473.575u^{28} + \dots + 1137.50u + 179.919 \\ -267.159u^{29} - 964.190u^{28} + \dots - 2740.63u - 585.096 \end{pmatrix} \\ a_8 &= \begin{pmatrix} -113.206u^{29} - 400.169u^{28} + \dots - 999.486u - 222.611 \\ -247.378u^{29} - 856.226u^{28} + \dots - 2556.65u - 511.822 \end{pmatrix} \\ a_3 &= \begin{pmatrix} 455.829u^{29} + 1623.13u^{28} + \dots + 5161.07u + 1090.23 \\ -74.5440u^{29} - 255.803u^{28} + \dots - 1160.53u - 242.557 \end{pmatrix} \\ a_{12} &= \begin{pmatrix} -366.303u^{29} - 1332.00u^{28} + \dots - 4413.63u - 979.914 \\ -u^{29} - 3u^{28} + \dots - 7u^2 - 7u \end{pmatrix} \\ a_7 &= \begin{pmatrix} 427.626u^{29} + 1511.62u^{28} + \dots + 4483.79u + 933.241 \\ 174.722u^{29} + 617.886u^{28} + \dots + 1617.71u + 318.379 \end{pmatrix} \\ a_{11} &= \begin{pmatrix} 72.2048u^{29} + 292.216u^{28} + \dots + 913.748u + 248.119 \\ 120.311u^{29} + 434.477u^{28} + \dots + 1633.83u + 355.868 \end{pmatrix} \end{aligned}$$

**(ii) Obstruction class = 1**

$$\text{(iii) Cusp Shapes} = -\frac{2124368078}{9372903}u^{29} - \frac{1389203474}{9372903}u^{28} + \dots - \frac{42689783696}{3124301}u - \frac{22166136335}{9372903}$$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1$	$u^{30} + 4u^{29} + \dots + 7u + 1$
$c_2$	$u^{30} - 2u^{29} + \dots - 4u - 1$
$c_3$	$u^{30} - 4u^{29} + \dots - 5u + 1$
$c_4$	$u^{30} - 4u^{29} + \dots - 7u + 1$
$c_5, c_6$	$u^{30} - u^{29} + \dots - 16u^2 - 1$
$c_7$	$u^{30} - u^{29} + \dots - 12u - 3$
$c_8$	$u^{30} + 2u^{29} + \dots + 4u - 1$
$c_9$	$u^{30} + 2u^{29} + \dots + 20u + 1$
$c_{10}$	$u^{30} + u^{29} + \dots - 16u^2 - 1$
$c_{11}$	$u^{30} + 12u^{28} + \dots + 8u - 1$
$c_{12}$	$u^{30} - 6u^{29} + \dots - 2u - 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_4$	$y^{30} - 10y^{29} + \dots - 23y + 1$
$c_2, c_8$	$y^{30} + 14y^{29} + \dots - 10y + 1$
$c_3$	$y^{30} - 18y^{29} + \dots + y + 1$
$c_5, c_6, c_{10}$	$y^{30} - 39y^{29} + \dots + 32y + 1$
$c_7$	$y^{30} - 7y^{29} + \dots - 1020y + 9$
$c_9$	$y^{30} - 14y^{29} + \dots - 214y + 1$
$c_{11}$	$y^{30} + 24y^{29} + \dots - 14y + 1$
$c_{12}$	$y^{30} - 14y^{29} + \dots - 40y + 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.914247 + 0.478404I$ $a = 1.93608 + 1.23966I$ $b = -0.161051 + 0.967060I$	$-0.08292 + 1.96806I$	$-3.02444 - 3.31718I$
$u = -0.914247 - 0.478404I$ $a = 1.93608 - 1.23966I$ $b = -0.161051 - 0.967060I$	$-0.08292 - 1.96806I$	$-3.02444 + 3.31718I$
$u = 0.966933 + 0.421943I$ $a = -1.066120 + 0.925837I$ $b = 0.344795 - 0.186269I$	$-3.48026 - 1.82580I$	$-8.91337 - 0.41811I$
$u = 0.966933 - 0.421943I$ $a = -1.066120 - 0.925837I$ $b = 0.344795 + 0.186269I$	$-3.48026 + 1.82580I$	$-8.91337 + 0.41811I$
$u = -0.843224 + 0.323111I$ $a = 2.18551 + 0.44187I$ $b = -0.02670 + 1.63927I$	$9.58575 + 1.48104I$	$15.8659 - 1.4053I$
$u = -0.843224 - 0.323111I$ $a = 2.18551 - 0.44187I$ $b = -0.02670 - 1.63927I$	$9.58575 - 1.48104I$	$15.8659 + 1.4053I$
$u = 0.892802$ $a = 2.51005$ $b = -1.68772$	$-0.327469$	$31.3600$
$u = 1.092830 + 0.410784I$ $a = -0.040120 + 0.596864I$ $b = 0.344289 - 0.968431I$	$-0.49604 - 1.69025I$	$-3.00353 + 2.31093I$
$u = 1.092830 - 0.410784I$ $a = -0.040120 - 0.596864I$ $b = 0.344289 + 0.968431I$	$-0.49604 + 1.69025I$	$-3.00353 - 2.31093I$
$u = 0.982431 + 0.678623I$ $a = 0.481945 - 0.966192I$ $b = -0.301537 + 0.216828I$	$1.13399 - 2.76492I$	$-4.71775 + 2.69778I$

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.982431 - 0.678623I$ $a = 0.481945 + 0.966192I$ $b = -0.301537 - 0.216828I$	$1.13399 + 2.76492I$	$-4.71775 - 2.69778I$
$u = -0.001235 + 0.805919I$ $a = 0.013308 + 1.372580I$ $b = 0.266019 + 1.380800I$	$10.77260 + 0.39997I$	$4.81859 + 0.26297I$
$u = -0.001235 - 0.805919I$ $a = 0.013308 - 1.372580I$ $b = 0.266019 - 1.380800I$	$10.77260 - 0.39997I$	$4.81859 - 0.26297I$
$u = 0.803639$ $a = -5.39360$ $b = 3.31619$	$7.71010$	$406.100$
$u = -0.188499 + 1.199910I$ $a = -0.100781 - 0.411198I$ $b = -0.334755 - 1.093000I$	$4.36107 - 1.46727I$	$-9.10722 + 0.91856I$
$u = -0.188499 - 1.199910I$ $a = -0.100781 + 0.411198I$ $b = -0.334755 + 1.093000I$	$4.36107 + 1.46727I$	$-9.10722 - 0.91856I$
$u = 0.769194$ $a = 3.09657$ $b = -0.392673$	$2.83265$	$-18.2700$
$u = 1.24130$ $a = 0.934361$ $b = -0.451498$	$0.517848$	$-1.73050$
$u = -1.188050 + 0.465930I$ $a = -1.63669 + 0.35983I$ $b = 0.437433 - 1.269120I$	$0.55049 + 6.62323I$	$-2.00000 - 4.98434I$
$u = -1.188050 - 0.465930I$ $a = -1.63669 - 0.35983I$ $b = 0.437433 + 1.269120I$	$0.55049 - 6.62323I$	$-2.00000 + 4.98434I$

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.058040 + 0.817556I$		
$a = -0.844520 - 0.579922I$	$-0.89236 + 3.28717I$	$0. - 4.27413I$
$b = 0.124690 - 0.940651I$		
$u = -1.058040 - 0.817556I$		
$a = -0.844520 + 0.579922I$	$-0.89236 - 3.28717I$	$0. + 4.27413I$
$b = 0.124690 + 0.940651I$		
$u = -0.590403 + 0.063266I$		
$a = 0.881544 - 0.820988I$	$3.71119 - 3.90958I$	$-5.50347 + 2.08979I$
$b = -0.226195 - 1.378450I$		
$u = -0.590403 - 0.063266I$		
$a = 0.881544 + 0.820988I$	$3.71119 + 3.90958I$	$-5.50347 - 2.08979I$
$b = -0.226195 + 1.378450I$		
$u = -1.277630 + 0.597190I$		
$a = 1.231240 - 0.157559I$	$5.09603 + 9.97190I$	$0. - 8.63860I$
$b = -0.603405 + 0.987716I$		
$u = -1.277630 - 0.597190I$		
$a = 1.231240 + 0.157559I$	$5.09603 - 9.97190I$	$0. + 8.63860I$
$b = -0.603405 - 0.987716I$		
$u = -0.38968 + 1.35980I$		
$a = 0.032493 + 0.174740I$	$8.57240 - 3.34121I$	$0. + 9.69583I$
$b = 0.361338 + 0.858086I$		
$u = -0.38968 - 1.35980I$		
$a = 0.032493 - 0.174740I$	$8.57240 + 3.34121I$	$0. - 9.69583I$
$b = 0.361338 - 0.858086I$		
$u = -0.444659 + 0.029162I$		
$a = -4.14758 - 0.30591I$	$10.08430 + 6.63124I$	$1.74300 - 4.80854I$
$b = 0.382925 - 1.299300I$		
$u = -0.444659 - 0.029162I$		
$a = -4.14758 + 0.30591I$	$10.08430 - 6.63124I$	$1.74300 + 4.80854I$
$b = 0.382925 + 1.299300I$		



$$\text{III. } I_3^u = \langle b + a - 1, a^2 - 3a + 3, u - 1 \rangle$$

(i) Arc colorings

$$a_2 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} a \\ -a + 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ -a + 1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 1 \\ -a + 2 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ -a + 1 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -a + 2 \\ a - 2 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -a + 1 \\ a - 2 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1 \\ -a + 1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = -3

(iv) **u**-Polynomials at the component

Crossings	<b>u</b> -Polynomials at each crossing
$c_1, c_{10}, c_{12}$	$(u - 1)^2$
$c_2, c_3$	$u^2 + u + 1$
$c_4, c_5, c_6$	$(u + 1)^2$
$c_7$	$u^2$
$c_8, c_9, c_{11}$	$u^2 - u + 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_4, c_5$ $c_6, c_{10}, c_{12}$	$(y - 1)^2$
$c_2, c_3, c_8$ $c_9, c_{11}$	$y^2 + y + 1$
$c_7$	$y^2$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.00000$	0	-3.00000
$a = 1.50000 + 0.86603I$		
$b = -0.500000 - 0.866025I$		
$u = 1.00000$	0	-3.00000
$a = 1.50000 - 0.86603I$		
$b = -0.500000 + 0.866025I$		

#### IV. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1$	$((u-1)^2)(u^{30} + 4u^{29} + \dots + 7u + 1)(u^{132} - u^{131} + \dots + 1451u - 844)$
$c_2$	$(u^2 + u + 1)(u^{30} - 2u^{29} + \dots - 4u - 1)$ $\cdot (u^{132} + 44u^{130} + \dots - 21827u - 1189)$
$c_3$	$(u^2 + u + 1)(u^{30} - 4u^{29} + \dots - 5u + 1)$ $\cdot (u^{132} - 4u^{131} + \dots + 9472u - 2239)$
$c_4$	$((u+1)^2)(u^{30} - 4u^{29} + \dots - 7u + 1)(u^{132} - u^{131} + \dots + 1451u - 844)$
$c_5, c_6$	$((u+1)^2)(u^{30} - u^{29} + \dots - 16u^2 - 1)(u^{132} + 2u^{131} + \dots + 130u + 19)$
$c_7$	$u^2(u^{30} - u^{29} + \dots - 12u - 3)(u^{132} + u^{130} + \dots - 28u + 8)$
$c_8$	$(u^2 - u + 1)(u^{30} + 2u^{29} + \dots + 4u - 1)$ $\cdot (u^{132} + 44u^{130} + \dots - 21827u - 1189)$
$c_9$	$(u^2 - u + 1)(u^{30} + 2u^{29} + \dots + 20u + 1)$ $\cdot (u^{132} - 4u^{130} + \dots - 37881u + 2437)$
$c_{10}$	$((u-1)^2)(u^{30} + u^{29} + \dots - 16u^2 - 1)(u^{132} + 2u^{131} + \dots + 130u + 19)$
$c_{11}$	$(u^2 - u + 1)(u^{30} + 12u^{28} + \dots + 8u - 1)$ $\cdot (u^{132} + 6u^{131} + \dots + 89459u + 56393)$
$c_{12}$	$((u-1)^2)(u^{30} - 6u^{29} + \dots - 2u - 1)(u^{132} - 5u^{131} + \dots + 4452u + 103)$

## V. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1, c_4$	$((y-1)^2)(y^{30} - 10y^{29} + \dots - 23y + 1)$ $\cdot (y^{132} - 63y^{131} + \dots - 11311753y + 712336)$
$c_2, c_8$	$(y^2 + y + 1)(y^{30} + 14y^{29} + \dots - 10y + 1)$ $\cdot (y^{132} + 88y^{131} + \dots - 71456419y + 1413721)$
$c_3$	$(y^2 + y + 1)(y^{30} - 18y^{29} + \dots + y + 1)$ $\cdot (y^{132} - 36y^{131} + \dots - 304367236y + 5013121)$
$c_5, c_6, c_{10}$	$((y-1)^2)(y^{30} - 39y^{29} + \dots + 32y + 1)$ $\cdot (y^{132} - 144y^{131} + \dots - 14848y + 361)$
$c_7$	$y^2(y^{30} - 7y^{29} + \dots - 1020y + 9)(y^{132} + 2y^{131} + \dots - 4464y + 64)$
$c_9$	$(y^2 + y + 1)(y^{30} - 14y^{29} + \dots - 214y + 1)$ $\cdot (y^{132} - 8y^{131} + \dots - 75967363y + 5938969)$
$c_{11}$	$(y^2 + y + 1)(y^{30} + 24y^{29} + \dots - 14y + 1)$ $\cdot (y^{132} + 62y^{131} + \dots + 237776842153y + 3180170449)$
$c_{12}$	$((y-1)^2)(y^{30} - 14y^{29} + \dots - 40y + 1)$ $\cdot (y^{132} - 27y^{131} + \dots - 6883504y + 10609)$