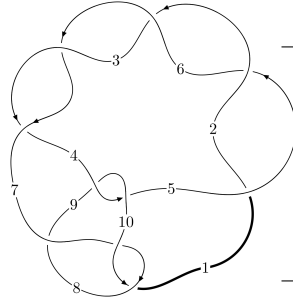
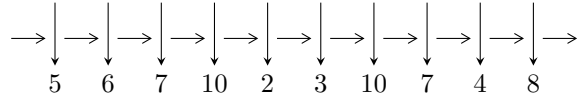


10<sub>124</sub> (K10n<sub>21</sub>)

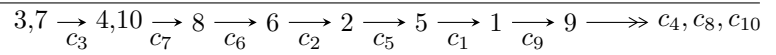


A knot diagram<sup>1</sup>

**Linearized knot diagram**



**Solving Sequence**



**Ideals for irreducible components<sup>2</sup> of  $X_{\text{par}}$**

$$I_1^u = \langle b + u, a + u + 1, u^2 + u - 1 \rangle$$

$$I_2^u = \langle b - u, a - u + 1, u^2 - 3u + 1 \rangle$$

\* 2 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 4 representations.

<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\text{I. } I_1^u = \langle b + u, a + u + 1, u^2 + u - 1 \rangle$$

(i) Arc colorings

$$a_3 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ -u + 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -u - 1 \\ -u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -u - 1 \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} u \\ u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} u \\ u - 1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 1 \\ -u + 1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 0 \\ -u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -u - 1 \\ -u \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = -15

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_2, c_3$	$u^2 + u - 1$
$c_4, c_9$	$u^2$
$c_5, c_6$	$u^2 - u - 1$
$c_7$	$(u - 1)^2$
$c_8, c_{10}$	$(u + 1)^2$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_3$ $c_5, c_6$	$y^2 - 3y + 1$
$c_4, c_9$	$y^2$
$c_7, c_8, c_{10}$	$(y - 1)^2$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.618034$ $a = -1.61803$ $b = -0.618034$	-2.63189	-15.0000
$u = -1.61803$ $a = 0.618034$ $b = 1.61803$	-10.5276	-15.0000

$$\text{II. } I_2^u = \langle b - u, a - u + 1, u^2 - 3u + 1 \rangle$$

(i) Arc colorings

$$a_3 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ 3u - 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} u - 1 \\ u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -3u + 1 \\ -4u + 2 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} u \\ u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -3u + 2 \\ -3u + 1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -6u + 3 \\ -7u + 3 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 12u - 4 \\ 15u - 6 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -3u + 1 \\ -25u + 10 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes = -15

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_2, c_3$ $c_5, c_6$	$u^2 + 3u + 1$
$c_4, c_9$	$u^2 - 8u - 4$
$c_7, c_{10}$	$u^2 - 4u - 1$
$c_8$	$u^2 + 18u + 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_3$ $c_5, c_6$	$y^2 - 7y + 1$
$c_4, c_9$	$y^2 - 72y + 16$
$c_7, c_{10}$	$y^2 - 18y + 1$
$c_8$	$y^2 - 322y + 1$



(vi) Complex Volumes and Cusp Shapes

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.381966$ $a = -0.618034$ $b = 0.381966$	-0.657974	-15.0000
$u = 2.61803$ $a = 1.61803$ $b = 2.61803$	7.23771	-15.0000

### III. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1, c_2, c_3$	$(u^2 + u - 1)(u^2 + 3u + 1)$
$c_4, c_9$	$u^2(u^2 - 8u - 4)$
$c_5, c_6$	$(u^2 - u - 1)(u^2 + 3u + 1)$
$c_7$	$(u - 1)^2(u^2 - 4u - 1)$
$c_8$	$(u + 1)^2(u^2 + 18u + 1)$
$c_{10}$	$(u + 1)^2(u^2 - 4u - 1)$

#### IV. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_3$ $c_5, c_6$	$(y^2 - 7y + 1)(y^2 - 3y + 1)$
$c_4, c_9$	$y^2(y^2 - 72y + 16)$
$c_7, c_{10}$	$(y - 1)^2(y^2 - 18y + 1)$
$c_8$	$(y - 1)^2(y^2 - 322y + 1)$