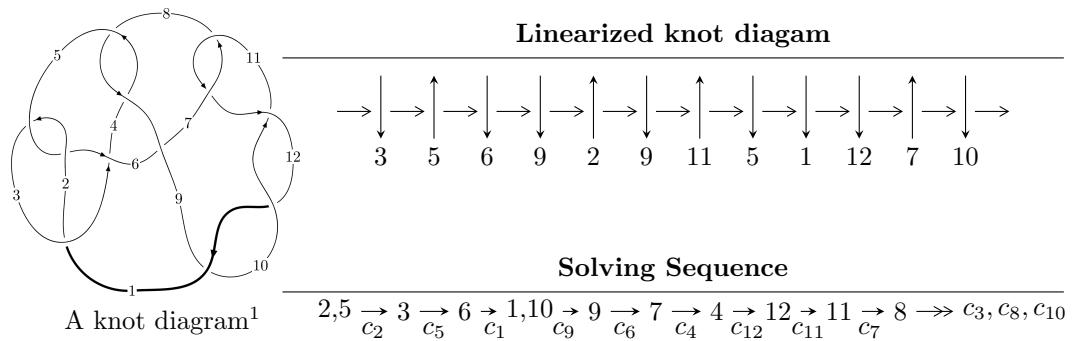


$12n_{0012}$  ( $K12n_{0012}$ )



### Ideals for irreducible components<sup>2</sup> of $X_{\text{par}}$

$$I_1^u = \langle -39u^{46} + 220u^{45} + \dots + 8b - 74, -3u^{46} + 13u^{45} + \dots + 8a - 17, u^{47} - 5u^{46} + \dots + 2u - 1 \rangle$$

$$I_2^u = \langle au + b - a, a^4 + a^3u - 3a^2u - 3a^2 + 2a + u, u^2 + u + 1 \rangle$$

\* 2 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 55 representations.

<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/math/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\text{I. } I_1^u = \langle -39u^{46} + 220u^{45} + \cdots + 8b - 74, -3u^{46} + 13u^{45} + \cdots + 8a - 17, u^{47} - 5u^{46} + \cdots + 2u - 1 \rangle$$

(i) Arc colorings

$$\begin{aligned} a_2 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_5 &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_3 &= \begin{pmatrix} 1 \\ -u^2 \end{pmatrix} \\ a_6 &= \begin{pmatrix} u \\ u \end{pmatrix} \\ a_1 &= \begin{pmatrix} u^2 + 1 \\ -u^4 \end{pmatrix} \\ a_{10} &= \left( \frac{3}{8}u^{46} - \frac{13}{8}u^{45} + \cdots - \frac{25}{4}u + \frac{17}{8} \right) \\ a_9 &= \left( -\frac{9}{4}u^{46} + \frac{39}{4}u^{45} + \cdots - 5u + \frac{11}{4} \right) \\ a_7 &= \left( -\frac{1}{8}u^{46} + \frac{5}{8}u^{45} + \cdots + \frac{9}{4}u - \frac{1}{8} \right) \\ a_4 &= \begin{pmatrix} u^4 + u^2 + 1 \\ u^4 \end{pmatrix} \\ a_{12} &= \left( \frac{1}{8}u^{46} - \frac{1}{2}u^{45} + \cdots + \frac{7}{8}u + 2 \right) \\ a_{11} &= \left( -2u^{46} + \frac{145}{8}u^{45} + \cdots + \frac{121}{8}u - \frac{93}{8} \right) \\ a_8 &= \left( \frac{9}{4}u^{46} - \frac{39}{4}u^{45} + \cdots + 5u - \frac{11}{4} \right) \end{aligned}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes =  $\frac{3}{8}u^{46} + 6u^{45} + \cdots + \frac{335}{8}u - \frac{31}{2}$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1$	$u^{47} + 27u^{46} + \cdots - 40u - 1$
$c_2, c_5$	$u^{47} + 5u^{46} + \cdots + 2u + 1$
$c_3$	$u^{47} - 5u^{46} + \cdots - 12u + 1$
$c_4, c_8$	$u^{47} + u^{46} + \cdots + 640u + 256$
$c_6$	$u^{47} - 3u^{46} + \cdots - 4u + 1$
$c_7, c_{11}$	$u^{47} - 3u^{46} + \cdots - 2u + 1$
$c_9, c_{10}, c_{12}$	$u^{47} + 13u^{46} + \cdots - 16u - 1$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1$	$y^{47} - 9y^{46} + \cdots + 512y - 1$
$c_2, c_5$	$y^{47} + 27y^{46} + \cdots - 40y - 1$
$c_3$	$y^{47} - 45y^{46} + \cdots - 152y - 1$
$c_4, c_8$	$y^{47} - 45y^{46} + \cdots + 638976y - 65536$
$c_6$	$y^{47} - 55y^{46} + \cdots - 16y - 1$
$c_7, c_{11}$	$y^{47} + 13y^{46} + \cdots - 16y - 1$
$c_9, c_{10}, c_{12}$	$y^{47} + 45y^{46} + \cdots - 8y - 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.026441 + 0.959622I$ $a = -0.602286 + 0.667947I$ $b = -0.28964 + 2.11687I$	$-1.66847 + 2.07597I$	$-8.19599 - 3.58729I$
$u = 0.026441 - 0.959622I$ $a = -0.602286 - 0.667947I$ $b = -0.28964 - 2.11687I$	$-1.66847 - 2.07597I$	$-8.19599 + 3.58729I$
$u = 0.925280 + 0.194352I$ $a = -1.48851 + 2.82129I$ $b = 0.86927 - 1.38303I$	$0.19889 - 8.32605I$	$-2.17091 + 5.11912I$
$u = 0.925280 - 0.194352I$ $a = -1.48851 - 2.82129I$ $b = 0.86927 + 1.38303I$	$0.19889 + 8.32605I$	$-2.17091 - 5.11912I$
$u = 0.933825 + 0.065187I$ $a = 0.120868 + 1.140740I$ $b = -0.501416 - 0.737782I$	$-6.55195 - 3.23257I$	$-7.12321 + 3.54877I$
$u = 0.933825 - 0.065187I$ $a = 0.120868 - 1.140740I$ $b = -0.501416 + 0.737782I$	$-6.55195 + 3.23257I$	$-7.12321 - 3.54877I$
$u = -0.733010 + 0.802557I$ $a = -2.03414 - 2.16959I$ $b = -0.82061 - 2.32750I$	$4.57748 + 0.17561I$	$-4.00000 + 0.I$
$u = -0.733010 - 0.802557I$ $a = -2.03414 + 2.16959I$ $b = -0.82061 + 2.32750I$	$4.57748 - 0.17561I$	$-4.00000 + 0.I$
$u = -0.580519 + 0.922395I$ $a = 1.018240 - 0.170806I$ $b = 1.221000 - 0.367778I$	$-0.75821 - 2.95186I$	$-10.26739 + 0.I$
$u = -0.580519 - 0.922395I$ $a = 1.018240 + 0.170806I$ $b = 1.221000 + 0.367778I$	$-0.75821 + 2.95186I$	$-10.26739 + 0.I$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.886435 + 0.192716I$		
$a = 1.79497 - 2.22924I$	$0.91039 - 2.22540I$	$-1.015220 + 0.333993I$
$b = -0.835270 + 0.957471I$		
$u = 0.886435 - 0.192716I$		
$a = 1.79497 + 2.22924I$	$0.91039 + 2.22540I$	$-1.015220 - 0.333993I$
$b = -0.835270 - 0.957471I$		
$u = -0.232117 + 1.073970I$		
$a = -0.764740 + 0.107154I$	$-3.32956 - 2.69471I$	$-11.16965 + 4.64357I$
$b = -0.930392 - 0.122544I$		
$u = -0.232117 - 1.073970I$		
$a = -0.764740 - 0.107154I$	$-3.32956 + 2.69471I$	$-11.16965 - 4.64357I$
$b = -0.930392 + 0.122544I$		
$u = -0.732051 + 0.844151I$		
$a = 2.53321 + 1.61725I$	$4.45822 - 5.68770I$	$0. + 5.85551I$
$b = 1.64457 + 2.36743I$		
$u = -0.732051 - 0.844151I$		
$a = 2.53321 - 1.61725I$	$4.45822 + 5.68770I$	$0. - 5.85551I$
$b = 1.64457 - 2.36743I$		
$u = 0.278391 + 0.834871I$		
$a = 0.195597 - 0.017136I$	$6.29656 + 4.54704I$	$-5.32988 - 0.19475I$
$b = 2.04050 + 2.00587I$		
$u = 0.278391 - 0.834871I$		
$a = 0.195597 + 0.017136I$	$6.29656 - 4.54704I$	$-5.32988 + 0.19475I$
$b = 2.04050 - 2.00587I$		
$u = -0.468535 + 0.741736I$		
$a = 0.169080 - 0.871234I$	$-0.10080 - 1.41741I$	$-3.72542 + 5.86093I$
$b = -0.179453 - 0.614868I$		
$u = -0.468535 - 0.741736I$		
$a = 0.169080 + 0.871234I$	$-0.10080 + 1.41741I$	$-3.72542 - 5.86093I$
$b = -0.179453 + 0.614868I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.856224$		
$a = 0.798257$	-3.24343	-1.24520
$b = 0.0288409$		
$u = 0.277747 + 0.799964I$		
$a = -0.031950 + 0.201535I$	$6.39944 - 1.84713I$	$-4.44776 + 5.17555I$
$b = -1.99709 - 1.62792I$		
$u = 0.277747 - 0.799964I$		
$a = -0.031950 - 0.201535I$	$6.39944 + 1.84713I$	$-4.44776 - 5.17555I$
$b = -1.99709 + 1.62792I$		
$u = -0.215715 + 0.766929I$		
$a = 0.623937 - 0.580705I$	-0.273553 - 1.319440I	$-1.87412 + 4.02854I$
$b = -0.040575 - 0.820520I$		
$u = -0.215715 - 0.766929I$		
$a = 0.623937 + 0.580705I$	-0.273553 + 1.319440I	$-1.87412 - 4.02854I$
$b = -0.040575 + 0.820520I$		
$u = -0.443222 + 1.123720I$		
$a = -0.306235 - 0.216455I$	$2.20908 - 1.05804I$	0
$b = -1.89659 - 0.62970I$		
$u = -0.443222 - 1.123720I$		
$a = -0.306235 + 0.216455I$	$2.20908 + 1.05804I$	0
$b = -1.89659 + 0.62970I$		
$u = -0.403667 + 1.155110I$		
$a = 0.258478 - 0.232515I$	$1.85423 - 6.77428I$	0
$b = 2.08868 - 0.64022I$		
$u = -0.403667 - 1.155110I$		
$a = 0.258478 + 0.232515I$	$1.85423 + 6.77428I$	0
$b = 2.08868 + 0.64022I$		
$u = 0.348879 + 1.251500I$		
$a = 0.68603 + 1.45153I$	-3.64593 + 1.84085I	0
$b = 2.92026 + 3.49905I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.348879 - 1.251500I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = 0.68603 - 1.45153I$	$-3.64593 - 1.84085I$	0
$b = 2.92026 - 3.49905I$		
$u = 0.467749 + 1.244070I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = -0.178953 + 0.487783I$	$-6.97041 + 4.72417I$	0
$b = -0.489450 + 0.885522I$		
$u = 0.467749 - 1.244070I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = -0.178953 - 0.487783I$	$-6.97041 - 4.72417I$	0
$b = -0.489450 - 0.885522I$		
$u = 0.339549 + 1.291160I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = -1.09098 - 1.58824I$	$-4.58314 - 4.07496I$	0
$b = -4.42832 - 3.64735I$		
$u = 0.339549 - 1.291160I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = -1.09098 + 1.58824I$	$-4.58314 + 4.07496I$	0
$b = -4.42832 + 3.64735I$		
$u = 0.552325 + 1.220220I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = -1.88083 + 0.66995I$	$-2.19262 + 7.48494I$	0
$b = -4.90066 + 2.68102I$		
$u = 0.552325 - 1.220220I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = -1.88083 - 0.66995I$	$-2.19262 - 7.48494I$	0
$b = -4.90066 - 2.68102I$		
$u = -0.643389 + 0.042276I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = 0.307917 + 0.399006I$	$5.17223 - 2.96380I$	$1.27670 + 2.94526I$
$b = -0.124452 - 1.032220I$		
$u = -0.643389 - 0.042276I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = 0.307917 - 0.399006I$	$5.17223 + 2.96380I$	$1.27670 - 2.94526I$
$b = -0.124452 + 1.032220I$		
$u = 0.564900 + 1.232880I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = 2.21676 - 0.36369I$	$-2.95715 + 13.73810I$	0
$b = 6.02517 - 2.25245I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.564900 - 1.232880I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = 2.21676 + 0.36369I$	$-2.95715 - 13.73810I$	0
$b = 6.02517 + 2.25245I$		
$u = 0.435963 + 1.291860I$		
$a = -0.743213 - 0.242847I$	$-10.77840 + 1.57100I$	0
$b = -2.18896 + 0.57747I$		
$u = 0.435963 - 1.291860I$		
$a = -0.743213 + 0.242847I$	$-10.77840 - 1.57100I$	0
$b = -2.18896 - 0.57747I$		
$u = 0.509079 + 1.270360I$		
$a = 0.692225 + 0.316516I$	$-10.24110 + 8.40839I$	0
$b = 2.63689 + 1.02049I$		
$u = 0.509079 - 1.270360I$		
$a = 0.692225 - 0.316516I$	$-10.24110 - 8.40839I$	0
$b = 2.63689 - 1.02049I$		
$u = -0.022449 + 0.247534I$		
$a = 1.60540 - 1.10956I$	$-0.255033 - 1.107400I$	$-3.72059 + 6.13127I$
$b = -0.337887 - 0.386120I$		
$u = -0.022449 - 0.247534I$		
$a = 1.60540 + 1.10956I$	$-0.255033 + 1.107400I$	$-3.72059 - 6.13127I$
$b = -0.337887 + 0.386120I$		

$$\text{II. } I_2^u = \langle au + b - a, \ a^4 + a^3u - 3a^2u - 3a^2 + 2a + u, \ u^2 + u + 1 \rangle$$

(i) Arc colorings

$$a_2 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 1 \\ u + 1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} u \\ u \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -u \\ -u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} a \\ -au + a \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0 \\ -au \end{pmatrix}$$

$$a_7 = \begin{pmatrix} u \\ a^2 + u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} a^2u + a^2 - u \\ a^2u + 2a^2 - u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} a^3u + 2a \\ 2a^3u + a^3 - au + 2a \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 0 \\ -au \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes =  $2a^3u - 4a^3 - 5a^2u + 12au + 17a + 5u - 6$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_3, c_5$	$(u^2 - u + 1)^4$
$c_2$	$(u^2 + u + 1)^4$
$c_4, c_8$	$u^8$
$c_6, c_9, c_{10}$	$(u^4 - u^3 + 3u^2 - 2u + 1)^2$
$c_7$	$(u^4 - u^3 + u^2 + 1)^2$
$c_{11}$	$(u^4 + u^3 + u^2 + 1)^2$
$c_{12}$	$(u^4 + u^3 + 3u^2 + 2u + 1)^2$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_3$ $c_5$	$(y^2 + y + 1)^4$
$c_4, c_8$	$y^8$
$c_6, c_9, c_{10}$ $c_{12}$	$(y^4 + 5y^3 + 7y^2 + 2y + 1)^2$
$c_7, c_{11}$	$(y^4 + y^3 + 3y^2 + 2y + 1)^2$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.500000 + 0.866025I$		
$a = -0.241378 - 0.595609I$	$-0.211005 - 0.614778I$	$-5.86133 - 2.84273I$
$b = -0.877879 - 0.684374I$		
$u = -0.500000 + 0.866025I$		
$a = 0.636501 - 0.088765I$	$-0.21101 - 3.44499I$	$-1.10064 + 8.92228I$
$b = 0.877879 - 0.684374I$		
$u = -0.500000 + 0.866025I$		
$a = -1.29206 - 0.86707I$	$6.79074 + 1.13408I$	$0.90087 + 2.75771I$
$b = -2.68899 - 0.18165I$		
$u = -0.500000 + 0.866025I$		
$a = 1.39694 + 0.68542I$	$6.79074 - 5.19385I$	$1.56110 + 7.61722I$
$b = 2.68899 - 0.18165I$		
$u = -0.500000 - 0.866025I$		
$a = -0.241378 + 0.595609I$	$-0.211005 + 0.614778I$	$-5.86133 + 2.84273I$
$b = -0.877879 + 0.684374I$		
$u = -0.500000 - 0.866025I$		
$a = 0.636501 + 0.088765I$	$-0.21101 + 3.44499I$	$-1.10064 - 8.92228I$
$b = 0.877879 + 0.684374I$		
$u = -0.500000 - 0.866025I$		
$a = -1.29206 + 0.86707I$	$6.79074 - 1.13408I$	$0.90087 - 2.75771I$
$b = -2.68899 + 0.18165I$		
$u = -0.500000 - 0.866025I$		
$a = 1.39694 - 0.68542I$	$6.79074 + 5.19385I$	$1.56110 - 7.61722I$
$b = 2.68899 + 0.18165I$		

### III. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1$	$((u^2 - u + 1)^4)(u^{47} + 27u^{46} + \dots - 40u - 1)$
$c_2$	$((u^2 + u + 1)^4)(u^{47} + 5u^{46} + \dots + 2u + 1)$
$c_3$	$((u^2 - u + 1)^4)(u^{47} - 5u^{46} + \dots - 12u + 1)$
$c_4, c_8$	$u^8(u^{47} + u^{46} + \dots + 640u + 256)$
$c_5$	$((u^2 - u + 1)^4)(u^{47} + 5u^{46} + \dots + 2u + 1)$
$c_6$	$((u^4 - u^3 + 3u^2 - 2u + 1)^2)(u^{47} - 3u^{46} + \dots - 4u + 1)$
$c_7$	$((u^4 - u^3 + u^2 + 1)^2)(u^{47} - 3u^{46} + \dots - 2u + 1)$
$c_9, c_{10}$	$((u^4 - u^3 + 3u^2 - 2u + 1)^2)(u^{47} + 13u^{46} + \dots - 16u - 1)$
$c_{11}$	$((u^4 + u^3 + u^2 + 1)^2)(u^{47} - 3u^{46} + \dots - 2u + 1)$
$c_{12}$	$((u^4 + u^3 + 3u^2 + 2u + 1)^2)(u^{47} + 13u^{46} + \dots - 16u - 1)$

#### IV. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1$	$((y^2 + y + 1)^4)(y^{47} - 9y^{46} + \dots + 512y - 1)$
$c_2, c_5$	$((y^2 + y + 1)^4)(y^{47} + 27y^{46} + \dots - 40y - 1)$
$c_3$	$((y^2 + y + 1)^4)(y^{47} - 45y^{46} + \dots - 152y - 1)$
$c_4, c_8$	$y^8(y^{47} - 45y^{46} + \dots + 638976y - 65536)$
$c_6$	$((y^4 + 5y^3 + 7y^2 + 2y + 1)^2)(y^{47} - 55y^{46} + \dots - 16y - 1)$
$c_7, c_{11}$	$((y^4 + y^3 + 3y^2 + 2y + 1)^2)(y^{47} + 13y^{46} + \dots - 16y - 1)$
$c_9, c_{10}, c_{12}$	$((y^4 + 5y^3 + 7y^2 + 2y + 1)^2)(y^{47} + 45y^{46} + \dots - 8y - 1)$