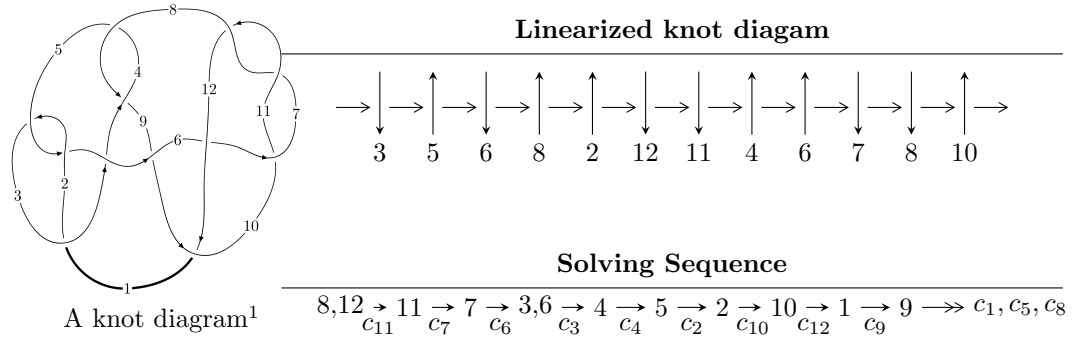


12n<sub>0044</sub> (K12n<sub>0044</sub>)



**Ideals for irreducible components<sup>2</sup> of  $X_{\text{par}}$**

$$I_1^u = \langle 2u^{34} + 4u^{33} + \dots + 2b - 3u, -6u^{34} - 12u^{33} + \dots + 2a - 5, u^{35} + 3u^{34} + \dots - u + 1 \rangle$$

$$I_2^u = \langle u^3a - au + b - a, -u^3a - u^4 + u^3 + a^2 + 2au + 2u^2 - 2u - 1, u^5 - u^4 - 2u^3 + u^2 + u + 1 \rangle$$

\* 2 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 45 representations.

<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\langle 2u^{34} + 4u^{33} + \dots + 2b - 3u, -6u^{34} - 12u^{33} + \dots + 2a - 5, u^{35} + 3u^{34} + \dots - u + 1 \rangle$$

I.  $I_1^u =$

(i) Arc colorings

$$a_8 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} u \\ -u^3 + u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 3u^{34} + 6u^{33} + \dots - \frac{3}{2}u + \frac{5}{2} \\ -u^{34} - 2u^{33} + \dots - \frac{7}{2}u^2 + \frac{3}{2}u \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -u^3 + 2u \\ -u^3 + u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} u^{34} + 2u^{33} + \dots - u + 1 \\ -2u^{34} - \frac{7}{2}u^{33} + \dots + u - \frac{1}{2} \end{pmatrix}$$

$$a_5 = \begin{pmatrix} u^{34} + 2u^{33} + \dots - u + 1 \\ -4u^{34} - \frac{13}{2}u^{33} + \dots + 3u - \frac{3}{2} \end{pmatrix}$$

$$a_2 = \begin{pmatrix} u^{34} + 2u^{33} + \dots - \frac{5}{2}u + \frac{1}{2} \\ \frac{1}{2}u^{32} + \frac{1}{2}u^{31} + \dots + \frac{7}{2}u^2 + \frac{3}{2}u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -u^2 + 1 \\ u^4 - 2u^2 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} u^6 - 3u^4 + 2u^2 + 1 \\ -u^8 + 4u^6 - 4u^4 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -u^{10} + 5u^8 - 8u^6 + 3u^4 + u^2 + 1 \\ -u^{10} + 4u^8 - 5u^6 + 2u^4 - u^2 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes =  $\frac{13}{2}u^{34} + \frac{21}{2}u^{33} + \dots - 15u + \frac{21}{2}$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1$	$u^{35} + 24u^{34} + \dots - 4u - 1$
$c_2, c_5$	$u^{35} + 6u^{34} + \dots - 8u - 1$
$c_3$	$u^{35} - 6u^{34} + \dots + u - 2$
$c_4, c_8$	$u^{35} - u^{34} + \dots + 2048u + 1024$
$c_6$	$u^{35} - 9u^{34} + \dots + 959u - 176$
$c_7, c_{10}, c_{11}$	$u^{35} + 3u^{34} + \dots - u + 1$
$c_9$	$u^{35} - 3u^{34} + \dots + 109535u + 149381$
$c_{12}$	$u^{35} + 3u^{34} + \dots + 3u + 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1$	$y^{35} - 20y^{34} + \dots - 256y - 1$
$c_2, c_5$	$y^{35} + 24y^{34} + \dots - 4y - 1$
$c_3$	$y^{35} - 64y^{34} + \dots - 115y - 4$
$c_4, c_8$	$y^{35} + 55y^{34} + \dots - 7340032y - 1048576$
$c_6$	$y^{35} - 23y^{34} + \dots + 86145y - 30976$
$c_7, c_{10}, c_{11}$	$y^{35} - 35y^{34} + \dots - 13y - 1$
$c_9$	$y^{35} + 109y^{34} + \dots - 963686176609y - 22314683161$
$c_{12}$	$y^{35} + 49y^{34} + \dots - 13y - 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.567543 + 0.702485I$ $a = -1.79734 - 1.55953I$ $b = -2.27694 - 0.16811I$	$-13.52750 + 3.29825I$	$-4.52460 - 0.12830I$
$u = 0.567543 - 0.702485I$ $a = -1.79734 + 1.55953I$ $b = -2.27694 + 0.16811I$	$-13.52750 - 3.29825I$	$-4.52460 + 0.12830I$
$u = 0.480329 + 0.751506I$ $a = -2.12175 - 1.61713I$ $b = -2.31879 - 0.06298I$	$-13.2384 - 8.1531I$	$-3.91050 + 5.47003I$
$u = 0.480329 - 0.751506I$ $a = -2.12175 + 1.61713I$ $b = -2.31879 + 0.06298I$	$-13.2384 + 8.1531I$	$-3.91050 - 5.47003I$
$u = 0.509854 + 0.709144I$ $a = 1.95618 + 1.69499I$ $b = 2.34001 + 0.13274I$	$-9.08492 - 2.36143I$	$-1.70250 + 2.73634I$
$u = 0.509854 - 0.709144I$ $a = 1.95618 - 1.69499I$ $b = 2.34001 - 0.13274I$	$-9.08492 + 2.36143I$	$-1.70250 - 2.73634I$
$u = -1.217400 + 0.104228I$ $a = 0.556325 - 0.615249I$ $b = -0.001571 + 0.321064I$	$-3.05619 + 0.58484I$	$-4.25548 + 0.I$
$u = -1.217400 - 0.104228I$ $a = 0.556325 + 0.615249I$ $b = -0.001571 - 0.321064I$	$-3.05619 - 0.58484I$	$-4.25548 + 0.I$
$u = -0.293244 + 0.696609I$ $a = -0.846989 - 0.642400I$ $b = -0.423424 - 0.190758I$	$-2.39789 + 3.01714I$	$-3.73777 - 3.74303I$
$u = -0.293244 - 0.696609I$ $a = -0.846989 + 0.642400I$ $b = -0.423424 + 0.190758I$	$-2.39789 - 3.01714I$	$-3.73777 + 3.74303I$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.588530 + 0.465780I$ $a = 0.008324 + 1.173240I$ $b = -0.042665 + 0.372046I$	$-3.52618 + 0.88882I$	$-5.91074 - 2.69844I$
$u = -0.588530 - 0.465780I$ $a = 0.008324 - 1.173240I$ $b = -0.042665 - 0.372046I$	$-3.52618 - 0.88882I$	$-5.91074 + 2.69844I$
$u = -1.31854$ $a = 0.766887$ $b = -0.555364$	$-3.00411$	$-1.27090$
$u = 1.351890 + 0.040890I$ $a = 0.157041 + 0.958259I$ $b = 0.25925 + 1.39116I$	$-3.48501 - 2.60863I$	$-5.97774 + 4.12008I$
$u = 1.351890 - 0.040890I$ $a = 0.157041 - 0.958259I$ $b = 0.25925 - 1.39116I$	$-3.48501 + 2.60863I$	$-5.97774 - 4.12008I$
$u = 1.389190 + 0.197736I$ $a = 0.262507 + 0.317399I$ $b = 0.407675 + 0.409042I$	$-5.20091 - 3.82410I$	$-4.45749 + 4.83241I$
$u = 1.389190 - 0.197736I$ $a = 0.262507 - 0.317399I$ $b = 0.407675 - 0.409042I$	$-5.20091 + 3.82410I$	$-4.45749 - 4.83241I$
$u = -1.41548 + 0.08723I$ $a = -1.030240 - 0.153922I$ $b = 1.236690 - 0.650078I$	$-5.56076 + 3.95289I$	$-6.09734 + 0.I$
$u = -1.41548 - 0.08723I$ $a = -1.030240 + 0.153922I$ $b = 1.236690 + 0.650078I$	$-5.56076 - 3.95289I$	$-6.09734 + 0.I$
$u = 1.40268 + 0.27759I$ $a = -0.526430 + 0.056708I$ $b = -0.706415 + 0.164348I$	$-7.78555 - 6.56645I$	$-7.86488 + 0.I$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.40268 - 0.27759I$ $a = -0.526430 - 0.056708I$ $b = -0.706415 - 0.164348I$	$-7.78555 + 6.56645I$	$-7.86488 + 0.I$
$u = -0.234492 + 0.501034I$ $a = 0.744299 - 0.409065I$ $b = 0.189998 - 0.226205I$	$-0.008011 + 1.203150I$	$-0.07375 - 5.95308I$
$u = -0.234492 - 0.501034I$ $a = 0.744299 + 0.409065I$ $b = 0.189998 + 0.226205I$	$-0.008011 - 1.203150I$	$-0.07375 + 5.95308I$
$u = 1.49851 + 0.14408I$ $a = 0.114237 - 0.651402I$ $b = 0.105973 - 0.888851I$	$-10.28270 - 3.07368I$	0
$u = 1.49851 - 0.14408I$ $a = 0.114237 + 0.651402I$ $b = 0.105973 + 0.888851I$	$-10.28270 + 3.07368I$	0
$u = -1.50813 + 0.27067I$ $a = -0.11491 + 1.74410I$ $b = -2.45281 + 0.21864I$	$-19.6916 + 11.8912I$	0
$u = -1.50813 - 0.27067I$ $a = -0.11491 - 1.74410I$ $b = -2.45281 - 0.21864I$	$-19.6916 - 11.8912I$	0
$u = -1.51243 + 0.24615I$ $a = -0.07457 - 1.66019I$ $b = 2.49768 - 0.33604I$	$-15.6688 + 5.8511I$	0
$u = -1.51243 - 0.24615I$ $a = -0.07457 + 1.66019I$ $b = 2.49768 + 0.33604I$	$-15.6688 - 5.8511I$	0
$u = -1.53563 + 0.22688I$ $a = 0.106999 + 1.408270I$ $b = -2.40458 + 0.41233I$	$19.0477 + 0.0884I$	0

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.53563 - 0.22688I$ $a = 0.106999 - 1.408270I$ $b = -2.40458 - 0.41233I$	$19.0477 - 0.0884I$	0
$u = 0.022155 + 0.410874I$ $a = 1.75998 - 0.97960I$ $b = 0.132570 - 0.734165I$	$0.57528 + 1.38421I$	$4.86232 - 4.69401I$
$u = 0.022155 - 0.410874I$ $a = 1.75998 + 0.97960I$ $b = 0.132570 + 0.734165I$	$0.57528 - 1.38421I$	$4.86232 + 4.69401I$
$u = 0.242449 + 0.281603I$ $a = -1.53711 + 1.37950I$ $b = 0.735025 + 0.827616I$	$-0.19025 - 2.59587I$	$1.54589 + 1.28231I$
$u = 0.242449 - 0.281603I$ $a = -1.53711 - 1.37950I$ $b = 0.735025 - 0.827616I$	$-0.19025 + 2.59587I$	$1.54589 - 1.28231I$



$$\text{II. } I_2^u = \langle u^3 a - au + b - a, -u^3 a - u^4 + u^3 + a^2 + 2au + 2u^2 - 2u - 1, u^5 - u^4 - 2u^3 + u^2 + u + 1 \rangle$$

(i) Arc colorings

$$a_8 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} u \\ -u^3 + u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} a \\ -u^3 a + au + a \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -u^3 + 2u \\ -u^3 + u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 0 \\ u^4 a - u^3 a - u^2 a \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 0 \\ u^4 a - u^3 a - u^2 a \end{pmatrix}$$

$$a_2 = \begin{pmatrix} a \\ -u^3 a + u^3 + au + a - u - 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -u^2 + 1 \\ u^4 - 2u^2 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} u^3 - 2u \\ u^3 - u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes =  $u^4 a - 4u^3 a - 2u^2 a + 4u^3 + 4au + u^2 + 3a - 9u - 7$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_3, c_5$	$(u^2 - u + 1)^5$
$c_2$	$(u^2 + u + 1)^5$
$c_4, c_8$	$u^{10}$
$c_6$	$(u^5 - 3u^4 + 4u^3 - u^2 - u + 1)^2$
$c_7$	$(u^5 + u^4 - 2u^3 - u^2 + u - 1)^2$
$c_9, c_{12}$	$(u^5 + u^4 + 2u^3 + u^2 + u + 1)^2$
$c_{10}, c_{11}$	$(u^5 - u^4 - 2u^3 + u^2 + u + 1)^2$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_3$ $c_5$	$(y^2 + y + 1)^5$
$c_4, c_8$	$y^{10}$
$c_6$	$(y^5 - y^4 + 8y^3 - 3y^2 + 3y - 1)^2$
$c_7, c_{10}, c_{11}$	$(y^5 - 5y^4 + 8y^3 - 3y^2 - y - 1)^2$
$c_9, c_{12}$	$(y^5 + 3y^4 + 4y^3 + y^2 - y - 1)^2$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.21774$		
$a = 0.314857 + 0.545349I$	$-2.40108 - 2.02988I$	$-0.33682 + 2.50057I$
$b = 0.500000 + 0.866025I$		
$u = -1.21774$		
$a = 0.314857 - 0.545349I$	$-2.40108 + 2.02988I$	$-0.33682 - 2.50057I$
$b = 0.500000 - 0.866025I$		
$u = -0.309916 + 0.549911I$		
$a = 1.394870 + 0.200669I$	$-0.32910 + 3.56046I$	$0.01046 - 8.35149I$
$b = 0.500000 + 0.866025I$		
$u = -0.309916 + 0.549911I$		
$a = -0.523653 - 1.308330I$	$-0.329100 - 0.499304I$	$-2.49844 - 0.84282I$
$b = 0.500000 - 0.866025I$		
$u = -0.309916 - 0.549911I$		
$a = 1.394870 - 0.200669I$	$-0.32910 - 3.56046I$	$0.01046 + 8.35149I$
$b = 0.500000 - 0.866025I$		
$u = -0.309916 - 0.549911I$		
$a = -0.523653 + 1.308330I$	$-0.329100 + 0.499304I$	$-2.49844 + 0.84282I$
$b = 0.500000 + 0.866025I$		
$u = 1.41878 + 0.21917I$		
$a = -0.850505 + 0.276175I$	$-5.87256 - 2.37095I$	$-6.88365 + 0.36343I$
$b = 0.500000 + 0.866025I$		
$u = 1.41878 + 0.21917I$		
$a = 0.664427 + 0.598472I$	$-5.87256 - 6.43072I$	$-4.29156 + 5.94266I$
$b = 0.500000 - 0.866025I$		
$u = 1.41878 - 0.21917I$		
$a = -0.850505 - 0.276175I$	$-5.87256 + 2.37095I$	$-6.88365 - 0.36343I$
$b = 0.500000 - 0.866025I$		
$u = 1.41878 - 0.21917I$		
$a = 0.664427 - 0.598472I$	$-5.87256 + 6.43072I$	$-4.29156 - 5.94266I$
$b = 0.500000 + 0.866025I$		

### III. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1$	$((u^2 - u + 1)^5)(u^{35} + 24u^{34} + \dots - 4u - 1)$
$c_2$	$((u^2 + u + 1)^5)(u^{35} + 6u^{34} + \dots - 8u - 1)$
$c_3$	$((u^2 - u + 1)^5)(u^{35} - 6u^{34} + \dots + u - 2)$
$c_4, c_8$	$u^{10}(u^{35} - u^{34} + \dots + 2048u + 1024)$
$c_5$	$((u^2 - u + 1)^5)(u^{35} + 6u^{34} + \dots - 8u - 1)$
$c_6$	$((u^5 - 3u^4 + 4u^3 - u^2 - u + 1)^2)(u^{35} - 9u^{34} + \dots + 959u - 176)$
$c_7$	$((u^5 + u^4 - 2u^3 - u^2 + u - 1)^2)(u^{35} + 3u^{34} + \dots - u + 1)$
$c_9$	$((u^5 + u^4 + 2u^3 + u^2 + u + 1)^2)(u^{35} - 3u^{34} + \dots + 109535u + 149381)$
$c_{10}, c_{11}$	$((u^5 - u^4 - 2u^3 + u^2 + u + 1)^2)(u^{35} + 3u^{34} + \dots - u + 1)$
$c_{12}$	$((u^5 + u^4 + 2u^3 + u^2 + u + 1)^2)(u^{35} + 3u^{34} + \dots + 3u + 1)$

#### IV. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1$	$((y^2 + y + 1)^5)(y^{35} - 20y^{34} + \dots - 256y - 1)$
$c_2, c_5$	$((y^2 + y + 1)^5)(y^{35} + 24y^{34} + \dots - 4y - 1)$
$c_3$	$((y^2 + y + 1)^5)(y^{35} - 64y^{34} + \dots - 115y - 4)$
$c_4, c_8$	$y^{10}(y^{35} + 55y^{34} + \dots - 7340032y - 1048576)$
$c_6$	$((y^5 - y^4 + 8y^3 - 3y^2 + 3y - 1)^2)(y^{35} - 23y^{34} + \dots + 86145y - 30976)$
$c_7, c_{10}, c_{11}$	$((y^5 - 5y^4 + 8y^3 - 3y^2 - y - 1)^2)(y^{35} - 35y^{34} + \dots - 13y - 1)$
$c_9$	$(y^5 + 3y^4 + 4y^3 + y^2 - y - 1)^2$ $\cdot (y^{35} + 109y^{34} + \dots - 963686176609y - 22314683161)$
$c_{12}$	$((y^5 + 3y^4 + 4y^3 + y^2 - y - 1)^2)(y^{35} + 49y^{34} + \dots - 13y - 1)$