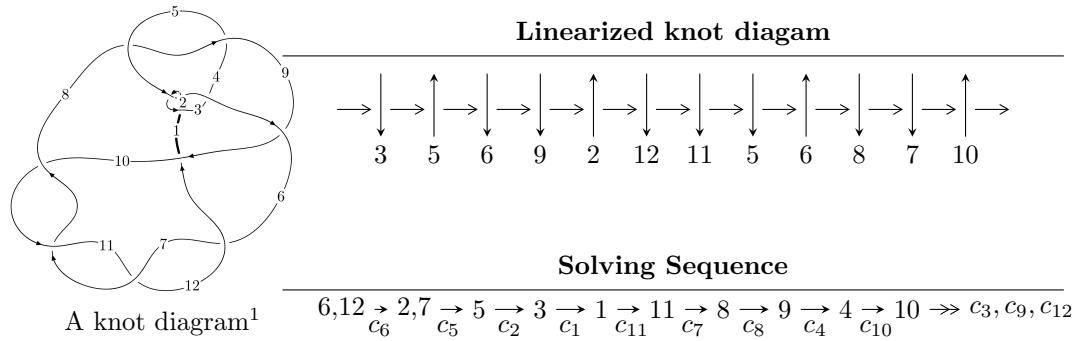


$12n_{0046}$ ($K12n_{0046}$)



Ideals for irreducible components² of X_{par}

$$I_1^u = \langle -u^{27} - 2u^{26} + \dots + 2b - 6u, u^{26} + 2u^{25} + \dots + 2a + 4, u^{28} + 3u^{27} + \dots + 6u + 1 \rangle$$

$$I_2^u = \langle -au + b - u, u^3a - u^2a - u^3 + a^2 + 3au - 2u, u^4 - u^3 + 3u^2 - 2u + 1 \rangle$$

* 2 irreducible components of $\dim_{\mathbb{C}} = 0$, with total 36 representations.

¹The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/math/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

²All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\text{I. } I_1^u = \langle -u^{27} - 2u^{26} + \dots + 2b - 6u, u^{26} + 2u^{25} + \dots + 2a + 4, u^{28} + 3u^{27} + \dots + 6u + 1 \rangle$$

(i) Arc colorings

$$a_6 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -\frac{1}{2}u^{26} - u^{25} + \dots - \frac{33}{2}u^2 - 2 \\ \frac{1}{2}u^{27} + u^{26} + \dots + u^2 + 3u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -\frac{1}{2}u^{27} - \frac{3}{2}u^{26} + \dots - 15u - 2 \\ -\frac{1}{2}u^{27} - u^{26} + \dots - 3u - 1 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} u^{27} + \frac{7}{2}u^{26} + \dots + 20u + 3 \\ -\frac{1}{2}u^{27} - 2u^{26} + \dots - 14u^2 - 2u \end{pmatrix}$$

$$a_1 = \begin{pmatrix} u^7 + 4u^5 + 4u^3 \\ u^9 + 5u^7 + 7u^5 + 2u^3 + u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} u \\ u^3 + u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} u^2 + 1 \\ u^4 + 2u^2 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -u^5 - 2u^3 + u \\ u^5 + 3u^3 + u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -\frac{3}{2}u^{27} - \frac{11}{2}u^{26} + \dots - 22u - 3 \\ \frac{1}{2}u^{27} + 2u^{26} + \dots + 14u^2 + 2u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} u^3 + 2u \\ u^5 + 3u^3 + u \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes = $\frac{5}{2}u^{27} + 5u^{26} + \dots + 21u + \frac{1}{2}$

(iv) u-Polynomials at the component

| Crossings | u-Polynomials at each crossing |
|--------------------------------|--|
| c_1 | $u^{28} + 5u^{27} + \cdots + 14u + 1$ |
| c_2, c_5 | $u^{28} + 5u^{27} + \cdots + 4u + 1$ |
| c_3 | $u^{28} - 5u^{27} + \cdots + 5562u + 1321$ |
| c_4, c_8 | $u^{28} + u^{27} + \cdots + 384u + 256$ |
| c_6, c_7, c_{10} c_{11} | $u^{28} - 3u^{27} + \cdots - 6u + 1$ |
| c_9 | $u^{28} - 3u^{27} + \cdots - 2u + 1$ |
| c_{12} | $u^{28} + 11u^{27} + \cdots + 184u + 209$ |

(v) Riley Polynomials at the component

| Crossings | Riley Polynomials at each crossing |
|--------------------------------|---|
| c_1 | $y^{28} + 41y^{27} + \cdots + 14y + 1$ |
| c_2, c_5 | $y^{28} + 5y^{27} + \cdots + 14y + 1$ |
| c_3 | $y^{28} + 77y^{27} + \cdots + 102223598y + 1745041$ |
| c_4, c_8 | $y^{28} + 45y^{27} + \cdots + 344064y + 65536$ |
| c_6, c_7, c_{10} c_{11} | $y^{28} + 35y^{27} + \cdots + 6y + 1$ |
| c_9 | $y^{28} - 49y^{27} + \cdots + 6y + 1$ |
| c_{12} | $y^{28} - 29y^{27} + \cdots + 2808126y + 43681$ |

(vi) Complex Volumes and Cusp Shapes

| Solutions to I_1^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|-----------------------------|---------------------------------------|-----------------------|
| $u = -0.546864 + 0.864620I$ | | |
| $a = -1.78266 + 0.81365I$ | $12.0428 + 7.8502I$ | $0.54802 - 5.73315I$ |
| $b = 0.938673 + 1.030660I$ | | |
| $u = -0.546864 - 0.864620I$ | | |
| $a = -1.78266 - 0.81365I$ | $12.0428 - 7.8502I$ | $0.54802 + 5.73315I$ |
| $b = 0.938673 - 1.030660I$ | | |
| $u = -0.512075 + 0.914815I$ | | |
| $a = -0.310810 + 0.834490I$ | $12.40950 + 0.72573I$ | $1.20101 - 1.26627I$ |
| $b = 1.006070 - 0.921537I$ | | |
| $u = -0.512075 - 0.914815I$ | | |
| $a = -0.310810 - 0.834490I$ | $12.40950 - 0.72573I$ | $1.20101 + 1.26627I$ |
| $b = 1.006070 + 0.921537I$ | | |
| $u = 0.041750 + 0.816332I$ | | |
| $a = 0.984967 - 0.816170I$ | $2.67787 - 1.51352I$ | $3.15826 + 2.96332I$ |
| $b = -0.730216 + 0.546904I$ | | |
| $u = 0.041750 - 0.816332I$ | | |
| $a = 0.984967 + 0.816170I$ | $2.67787 + 1.51352I$ | $3.15826 - 2.96332I$ |
| $b = -0.730216 - 0.546904I$ | | |
| $u = -0.755205 + 0.031373I$ | | |
| $a = -0.154324 - 0.783184I$ | $9.53090 - 3.51075I$ | $-2.36490 + 2.10810I$ |
| $b = 0.955403 - 0.970517I$ | | |
| $u = -0.755205 - 0.031373I$ | | |
| $a = -0.154324 + 0.783184I$ | $9.53090 + 3.51075I$ | $-2.36490 - 2.10810I$ |
| $b = 0.955403 + 0.970517I$ | | |
| $u = 0.429610 + 0.590805I$ | | |
| $a = -1.30185 - 0.60397I$ | $-0.15101 - 2.02920I$ | $-3.29658 + 3.20774I$ |
| $b = 0.291696 - 0.394438I$ | | |
| $u = 0.429610 - 0.590805I$ | | |
| $a = -1.30185 + 0.60397I$ | $-0.15101 + 2.02920I$ | $-3.29658 - 3.20774I$ |
| $b = 0.291696 + 0.394438I$ | | |

| Solutions to I_1^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|-----------------------------|---------------------------------------|-----------------------|
| $u = -0.179883 + 0.692364I$ | | |
| $a = 2.11541 - 0.80616I$ | $1.04465 + 3.25872I$ | $1.94579 - 3.88394I$ |
| $b = -0.514946 - 1.029420I$ | | |
| $u = -0.179883 - 0.692364I$ | | |
| $a = 2.11541 + 0.80616I$ | $1.04465 - 3.25872I$ | $1.94579 + 3.88394I$ |
| $b = -0.514946 + 1.029420I$ | | |
| $u = 0.398241 + 0.347741I$ | | |
| $a = -0.595350 + 0.678601I$ | $-0.844911 - 0.963937I$ | $-7.23227 + 5.09608I$ |
| $b = -0.007486 + 0.515758I$ | | |
| $u = 0.398241 - 0.347741I$ | | |
| $a = -0.595350 - 0.678601I$ | $-0.844911 + 0.963937I$ | $-7.23227 - 5.09608I$ |
| $b = -0.007486 - 0.515758I$ | | |
| $u = 0.05307 + 1.53702I$ | | |
| $a = -0.565559 + 0.333640I$ | $5.52882 - 2.13387I$ | $-4.00000 + 3.29212I$ |
| $b = 0.007766 + 0.841204I$ | | |
| $u = 0.05307 - 1.53702I$ | | |
| $a = -0.565559 - 0.333640I$ | $5.52882 + 2.13387I$ | $-4.00000 - 3.29212I$ |
| $b = 0.007766 - 0.841204I$ | | |
| $u = 0.12702 + 1.57248I$ | | |
| $a = -1.339830 - 0.272553I$ | $7.19200 - 4.05999I$ | 0 |
| $b = 0.478138 - 0.445759I$ | | |
| $u = 0.12702 - 1.57248I$ | | |
| $a = -1.339830 + 0.272553I$ | $7.19200 + 4.05999I$ | 0 |
| $b = 0.478138 + 0.445759I$ | | |
| $u = -0.04195 + 1.63425I$ | | |
| $a = 1.62168 + 0.08443I$ | $9.22292 + 4.03870I$ | $0. - 2.65080I$ |
| $b = -0.578450 - 1.150140I$ | | |
| $u = -0.04195 - 1.63425I$ | | |
| $a = 1.62168 - 0.08443I$ | $9.22292 - 4.03870I$ | $0. + 2.65080I$ |
| $b = -0.578450 + 1.150140I$ | | |

| Solutions to I_1^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|-----------------------------|---------------------------------------|-----------------------|
| $u = 0.01177 + 1.65893I$ | | |
| $a = 1.41681 - 0.67494I$ | $11.38100 - 1.72426I$ | $3.45594 + 0.I$ |
| $b = -0.955702 + 0.548085I$ | | |
| $u = 0.01177 - 1.65893I$ | | |
| $a = 1.41681 + 0.67494I$ | $11.38100 + 1.72426I$ | $3.45594 + 0.I$ |
| $b = -0.955702 - 0.548085I$ | | |
| $u = -0.16140 + 1.66866I$ | | |
| $a = -1.98113 + 0.05979I$ | $-18.7492 + 10.6138I$ | $0. - 4.77955I$ |
| $b = 0.93469 + 1.08649I$ | | |
| $u = -0.16140 - 1.66866I$ | | |
| $a = -1.98113 - 0.05979I$ | $-18.7492 - 10.6138I$ | $0. + 4.77955I$ |
| $b = 0.93469 - 1.08649I$ | | |
| $u = -0.14287 + 1.68669I$ | | |
| $a = -1.04698 + 1.01839I$ | $-18.0712 + 3.2992I$ | 0 |
| $b = 1.072160 - 0.890015I$ | | |
| $u = -0.14287 - 1.68669I$ | | |
| $a = -1.04698 - 1.01839I$ | $-18.0712 - 3.2992I$ | 0 |
| $b = 1.072160 + 0.890015I$ | | |
| $u = -0.221218 + 0.191391I$ | | |
| $a = -2.06037 + 1.41739I$ | $-0.31537 - 1.65529I$ | $-2.65586 + 5.38450I$ |
| $b = -0.397798 + 0.843645I$ | | |
| $u = -0.221218 - 0.191391I$ | | |
| $a = -2.06037 - 1.41739I$ | $-0.31537 + 1.65529I$ | $-2.65586 - 5.38450I$ |
| $b = -0.397798 - 0.843645I$ | | |

$$I_2^u = \langle -au + b - u, \ u^3a - u^2a - u^3 + a^2 + 3au - 2u, \ u^4 - u^3 + 3u^2 - 2u + 1 \rangle$$

(i) **Arc colorings**

$$a_6 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} a \\ au + u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} u^3 - au - u^2 + a + 2u \\ au + u - 1 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} u^3 - u^2 + a + 3u - 1 \\ au + u - 1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} u \\ u^3 + u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} u^2 + 1 \\ u^3 - u^2 + 2u - 1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} u^2 + 1 \\ u^3 - u^2 + 2u - 1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} u^3 - au - u^2 + a + 2u \\ au + u - 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} u^3 + 2u \\ u^3 - u^2 + 2u - 1 \end{pmatrix}$$

(ii) **Obstruction class = 1**

(iii) **Cusp Shapes** = $-u^2a + 4u^3 - 4au - 5u^2 + a + 9u - 5$

(iv) u-Polynomials at the component

| Crossings | u-Polynomials at each crossing |
|------------------|---------------------------------|
| c_1, c_3, c_5 | $(u^2 - u + 1)^4$ |
| c_2 | $(u^2 + u + 1)^4$ |
| c_4, c_8 | u^8 |
| c_6, c_7 | $(u^4 - u^3 + 3u^2 - 2u + 1)^2$ |
| c_9, c_{12} | $(u^4 + u^3 + u^2 + 1)^2$ |
| c_{10}, c_{11} | $(u^4 + u^3 + 3u^2 + 2u + 1)^2$ |

(v) Riley Polynomials at the component

| Crossings | Riley Polynomials at each crossing |
|--------------------------------|------------------------------------|
| c_1, c_2, c_3 c_5 | $(y^2 + y + 1)^4$ |
| c_4, c_8 | y^8 |
| c_6, c_7, c_{10} c_{11} | $(y^4 + 5y^3 + 7y^2 + 2y + 1)^2$ |
| c_9, c_{12} | $(y^4 + y^3 + 3y^2 + 2y + 1)^2$ |

(vi) Complex Volumes and Cusp Shapes

| Solutions to I_2^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|-----------------------------|---------------------------------------|-----------------------|
| $u = 0.395123 + 0.506844I$ | | |
| $a = 0.541116 + 0.214920I$ | $-0.211005 + 0.614778I$ | $-1.64912 + 1.57080I$ |
| $b = 0.500000 + 0.866025I$ | | |
| $u = 0.395123 + 0.506844I$ | | |
| $a = -1.58443 - 1.44211I$ | $-0.21101 - 3.44499I$ | $-4.65255 + 7.52635I$ |
| $b = 0.500000 - 0.866025I$ | | |
| $u = 0.395123 - 0.506844I$ | | |
| $a = 0.541116 - 0.214920I$ | $-0.211005 - 0.614778I$ | $-1.64912 - 1.57080I$ |
| $b = 0.500000 - 0.866025I$ | | |
| $u = 0.395123 - 0.506844I$ | | |
| $a = -1.58443 + 1.44211I$ | $-0.21101 + 3.44499I$ | $-4.65255 - 7.52635I$ |
| $b = 0.500000 + 0.866025I$ | | |
| $u = 0.10488 + 1.55249I$ | | |
| $a = -0.423047 - 0.283088I$ | $6.79074 - 1.13408I$ | $1.80063 - 0.49697I$ |
| $b = 0.500000 + 0.866025I$ | | |
| $u = 0.10488 + 1.55249I$ | | |
| $a = -1.53364 - 0.35811I$ | $6.79074 - 5.19385I$ | $-1.99896 + 6.53786I$ |
| $b = 0.500000 - 0.866025I$ | | |
| $u = 0.10488 - 1.55249I$ | | |
| $a = -0.423047 + 0.283088I$ | $6.79074 + 1.13408I$ | $1.80063 + 0.49697I$ |
| $b = 0.500000 - 0.866025I$ | | |
| $u = 0.10488 - 1.55249I$ | | |
| $a = -1.53364 + 0.35811I$ | $6.79074 + 5.19385I$ | $-1.99896 - 6.53786I$ |
| $b = 0.500000 + 0.866025I$ | | |

III. u-Polynomials

| Crossings | u-Polynomials at each crossing |
|------------------|--|
| c_1 | $((u^2 - u + 1)^4)(u^{28} + 5u^{27} + \dots + 14u + 1)$ |
| c_2 | $((u^2 + u + 1)^4)(u^{28} + 5u^{27} + \dots + 4u + 1)$ |
| c_3 | $((u^2 - u + 1)^4)(u^{28} - 5u^{27} + \dots + 5562u + 1321)$ |
| c_4, c_8 | $u^8(u^{28} + u^{27} + \dots + 384u + 256)$ |
| c_5 | $((u^2 - u + 1)^4)(u^{28} + 5u^{27} + \dots + 4u + 1)$ |
| c_6, c_7 | $((u^4 - u^3 + 3u^2 - 2u + 1)^2)(u^{28} - 3u^{27} + \dots - 6u + 1)$ |
| c_9 | $((u^4 + u^3 + u^2 + 1)^2)(u^{28} - 3u^{27} + \dots - 2u + 1)$ |
| c_{10}, c_{11} | $((u^4 + u^3 + 3u^2 + 2u + 1)^2)(u^{28} - 3u^{27} + \dots - 6u + 1)$ |
| c_{12} | $((u^4 + u^3 + u^2 + 1)^2)(u^{28} + 11u^{27} + \dots + 184u + 209)$ |

IV. Riley Polynomials

| Crossings | Riley Polynomials at each crossing |
|--------------------------------|--|
| c_1 | $((y^2 + y + 1)^4)(y^{28} + 41y^{27} + \dots + 14y + 1)$ |
| c_2, c_5 | $((y^2 + y + 1)^4)(y^{28} + 5y^{27} + \dots + 14y + 1)$ |
| c_3 | $((y^2 + y + 1)^4)(y^{28} + 77y^{27} + \dots + 1.02224 \times 10^8 y + 1745041)$ |
| c_4, c_8 | $y^8(y^{28} + 45y^{27} + \dots + 344064y + 65536)$ |
| c_6, c_7, c_{10} c_{11} | $((y^4 + 5y^3 + 7y^2 + 2y + 1)^2)(y^{28} + 35y^{27} + \dots + 6y + 1)$ |
| c_9 | $((y^4 + y^3 + 3y^2 + 2y + 1)^2)(y^{28} - 49y^{27} + \dots + 6y + 1)$ |
| c_{12} | $((y^4 + y^3 + 3y^2 + 2y + 1)^2)(y^{28} - 29y^{27} + \dots + 2808126y + 43681)$ |