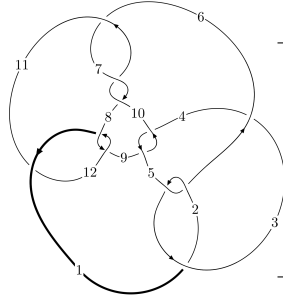
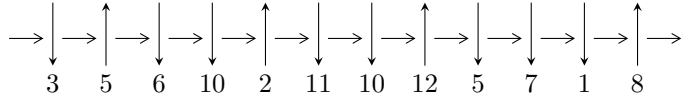


12n<sub>0050</sub> (K12n<sub>0050</sub>)



A knot diagram<sup>1</sup>

**Linearized knot diagram**



**Solving Sequence**

$$6, 11 \xrightarrow{c_6} 2, 7 \xrightarrow{c_5} 5 \xrightarrow{c_2} 3 \xrightarrow{c_1} 1 \xrightarrow{c_{10}} 10 \xrightarrow{c_7} 8 \xrightarrow{c_4} 4 \xrightarrow{c_{12}} 12 \xrightarrow{c_8} 9 \rightsquigarrow c_3, c_9, c_{11}$$

**Ideals for irreducible components<sup>2</sup> of  $X_{\text{par}}$**

$$I_1^u = \langle 1.86448 \times 10^{23} u^{41} - 4.54607 \times 10^{23} u^{40} + \dots + 2.14051 \times 10^{24} b - 1.33994 \times 10^{24}, \\ 1.55777 \times 10^{24} u^{41} - 3.49226 \times 10^{24} u^{40} + \dots + 4.28103 \times 10^{24} a - 8.66921 \times 10^{24}, u^{42} - 3u^{41} + \dots - 4u + 1 \rangle$$

$$I_2^u = \langle u^2 a - au + u^2 + b - u, 2u^3 a - 4u^2 a - 5u^3 + 4a^2 + 6au + 6u^2 - 2a - 13u + 15, u^4 - u^3 + 3u^2 - 2u + 1 \rangle$$

$$I_3^u = \langle -u^6 - 2u^4 - 2u^3 - u^2 + b - 2u, -u^6 - 3u^4 - 2u^3 - 2u^2 + a - 4u - 1, \\ u^{15} + 5u^{13} + 5u^{12} + 10u^{11} + 20u^{10} + 18u^9 + 30u^8 + 29u^7 + 23u^6 + 25u^5 + 11u^4 + 7u^3 + 3u^2 - u + 1 \rangle$$

\* 3 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 65 representations.

<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

I.

$$I_1^u = \langle 1.86 \times 10^{23} u^{41} - 4.55 \times 10^{23} u^{40} + \dots + 2.14 \times 10^{24} b - 1.34 \times 10^{24}, 1.56 \times 10^{24} u^{41} - 3.49 \times 10^{24} u^{40} + \dots + 4.28 \times 10^{24} a - 8.67 \times 10^{24}, u^{42} - 3u^{41} + \dots - 4u + 1 \rangle$$

(i) Arc colorings

$$a_6 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -0.363877u^{41} + 0.815753u^{40} + \dots - 0.334201u + 2.02503 \\ -0.0871043u^{41} + 0.212382u^{40} + \dots - 0.482611u + 0.625989 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -0.659564u^{41} + 1.39975u^{40} + \dots + 0.0845241u + 0.435332 \\ -0.0702325u^{41} + 0.143960u^{40} + \dots - 0.391861u - 0.363693 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -0.574443u^{41} + 1.03501u^{40} + \dots + 1.04901u - 0.509224 \\ 0.0313582u^{41} - 0.169378u^{40} + \dots + 0.191274u - 0.637085 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 0.545703u^{41} - 1.87495u^{40} + \dots + 6.14055u - 3.12407 \\ 0.0705453u^{41} - 0.437164u^{40} + \dots + 2.10999u - 0.698937 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} u \\ u^3 + u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} u^2 + 1 \\ u^4 + 2u^2 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -0.605801u^{41} + 1.20439u^{40} + \dots + 0.857736u + 0.127861 \\ 0.0313582u^{41} - 0.169378u^{40} + \dots + 0.191274u - 0.637085 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 0.112025u^{41} - 0.738600u^{40} + \dots + 1.78402u - 2.01029 \\ -0.179156u^{41} + 0.123997u^{40} + \dots + 1.38787u - 0.296413 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0.711251u^{41} - 1.94978u^{40} + \dots + 4.85792u - 0.210599 \\ -0.0109483u^{41} + 0.102515u^{40} + \dots + 0.549153u + 0.291182 \end{pmatrix}$$

(ii) Obstruction class = -1

$$\text{(iii) Cusp Shapes} = \frac{8819869146154630149250287}{8562054330498891123064064} u^{41} - \frac{6951105346810345728611581}{2140513582624722780766016} u^{40} + \dots - \frac{9809601898657334062772699}{8562054330498891123064064} u - \frac{77878813575983057100937417}{8562054330498891123064064}$$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1$	$u^{42} + 22u^{41} + \dots + 383u + 16$
$c_2, c_5$	$u^{42} + 2u^{41} + \dots - 3u + 4$
$c_3$	$u^{42} - 2u^{41} + \dots - 23400u + 3104$
$c_4, c_9$	$u^{42} + 2u^{41} + \dots + 3584u + 2048$
$c_6, c_7, c_{10}$	$u^{42} - 3u^{41} + \dots - 4u + 1$
$c_8, c_{12}$	$u^{42} - 3u^{41} + \dots - 2u + 1$
$c_{11}$	$u^{42} + 23u^{41} + \dots + 6u + 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1$	$y^{42} - 2y^{41} + \dots + 33759y + 256$
$c_2, c_5$	$y^{42} + 22y^{41} + \dots + 383y + 16$
$c_3$	$y^{42} - 26y^{41} + \dots + 359975104y + 9634816$
$c_4, c_9$	$y^{42} - 30y^{41} + \dots - 36438016y + 4194304$
$c_6, c_7, c_{10}$	$y^{42} + 35y^{41} + \dots + 6y + 1$
$c_8, c_{12}$	$y^{42} + 23y^{41} + \dots + 6y + 1$
$c_{11}$	$y^{42} - 5y^{41} + \dots - 54y + 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.027970 + 0.100105I$		
$a = 0.24960 + 1.85629I$	$-9.37503 - 10.09150I$	$-8.44713 + 6.42657I$
$b = -0.546190 + 1.233220I$		
$u = 1.027970 - 0.100105I$		
$a = 0.24960 - 1.85629I$	$-9.37503 + 10.09150I$	$-8.44713 - 6.42657I$
$b = -0.546190 - 1.233220I$		
$u = 0.929724 + 0.138462I$		
$a = 0.54776 + 2.00727I$	$-10.74190 + 0.44052I$	$-10.40215 + 0.18999I$
$b = -0.357906 + 1.293250I$		
$u = 0.929724 - 0.138462I$		
$a = 0.54776 - 2.00727I$	$-10.74190 - 0.44052I$	$-10.40215 - 0.18999I$
$b = -0.357906 - 1.293250I$		
$u = 0.914941 + 0.045259I$		
$a = -0.416878 - 0.222543I$	$-6.11647 - 4.80305I$	$-6.31453 + 3.22976I$
$b = -0.915244 - 0.158700I$		
$u = 0.914941 - 0.045259I$		
$a = -0.416878 + 0.222543I$	$-6.11647 + 4.80305I$	$-6.31453 - 3.22976I$
$b = -0.915244 + 0.158700I$		
$u = 0.176790 + 1.089910I$		
$a = -1.33651 - 1.33318I$	$1.83107 - 3.60410I$	$1.23384 + 2.84738I$
$b = 0.552991 - 1.072730I$		
$u = 0.176790 - 1.089910I$		
$a = -1.33651 + 1.33318I$	$1.83107 + 3.60410I$	$1.23384 - 2.84738I$
$b = 0.552991 + 1.072730I$		
$u = -0.638546 + 0.536386I$		
$a = 1.17338 - 1.37011I$	$-1.04750 + 2.07664I$	$-7.01132 - 2.89392I$
$b = -0.089750 - 0.808861I$		
$u = -0.638546 - 0.536386I$		
$a = 1.17338 + 1.37011I$	$-1.04750 - 2.07664I$	$-7.01132 + 2.89392I$
$b = -0.089750 + 0.808861I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.257246 + 1.141800I$ $a = -0.74697 + 1.25063I$ $b = 0.48378 + 1.32908I$	$-0.81918 + 6.49392I$	$-4.00000 - 8.90623I$
$u = -0.257246 - 1.141800I$ $a = -0.74697 - 1.25063I$ $b = 0.48378 - 1.32908I$	$-0.81918 - 6.49392I$	$-4.00000 + 8.90623I$
$u = -0.051623 + 1.181420I$ $a = -0.529834 - 0.226212I$ $b = 0.820994 + 0.618988I$	$3.71536 + 1.69010I$	$3.26218 - 1.55976I$
$u = -0.051623 - 1.181420I$ $a = -0.529834 + 0.226212I$ $b = 0.820994 - 0.618988I$	$3.71536 - 1.69010I$	$3.26218 + 1.55976I$
$u = 0.118844 + 1.181270I$ $a = -0.851838 - 0.430624I$ $b = 0.891940 - 0.979743I$	$2.63448 - 4.63960I$	$0. + 8.16254I$
$u = 0.118844 - 1.181270I$ $a = -0.851838 + 0.430624I$ $b = 0.891940 + 0.979743I$	$2.63448 + 4.63960I$	$0. - 8.16254I$
$u = -0.023170 + 1.204780I$ $a = -0.160324 - 0.092419I$ $b = 0.914501 + 0.286896I$	$3.99481 + 1.55693I$	$4.40114 - 3.96530I$
$u = -0.023170 - 1.204780I$ $a = -0.160324 + 0.092419I$ $b = 0.914501 - 0.286896I$	$3.99481 - 1.55693I$	$4.40114 + 3.96530I$
$u = 0.487771 + 1.186180I$ $a = -0.360345 - 1.006100I$ $b = -0.229714 - 1.369840I$	$-7.52698 - 5.48459I$	$0$
$u = 0.487771 - 1.186180I$ $a = -0.360345 + 1.006100I$ $b = -0.229714 + 1.369840I$	$-7.52698 + 5.48459I$	$0$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.579810 + 1.160310I$ $a = -0.178403 + 0.945878I$ $b = -0.304232 + 1.178570I$	$-2.78929 + 1.17087I$	0
$u = -0.579810 - 1.160310I$ $a = -0.178403 - 0.945878I$ $b = -0.304232 - 1.178570I$	$-2.78929 - 1.17087I$	0
$u = -0.404098 + 1.316080I$ $a = 0.296578 - 0.436654I$ $b = -0.825719 + 0.274258I$	$1.73633 + 4.52361I$	0
$u = -0.404098 - 1.316080I$ $a = 0.296578 + 0.436654I$ $b = -0.825719 - 0.274258I$	$1.73633 - 4.52361I$	0
$u = 0.438573 + 1.326070I$ $a = 0.146351 + 0.500553I$ $b = -0.991101 - 0.284626I$	$-1.83637 - 9.65354I$	0
$u = 0.438573 - 1.326070I$ $a = 0.146351 - 0.500553I$ $b = -0.991101 + 0.284626I$	$-1.83637 + 9.65354I$	0
$u = 0.48276 + 1.38315I$ $a = 1.29723 + 1.22335I$ $b = -0.619520 + 1.226280I$	$-4.7316 - 15.4661I$	0
$u = 0.48276 - 1.38315I$ $a = 1.29723 - 1.22335I$ $b = -0.619520 - 1.226280I$	$-4.7316 + 15.4661I$	0
$u = -0.518309 + 0.081810I$ $a = 1.62251 - 2.04492I$ $b = 0.313840 - 1.152440I$	$-3.86435 - 3.51413I$	$-10.49218 + 3.82170I$
$u = -0.518309 - 0.081810I$ $a = 1.62251 + 2.04492I$ $b = 0.313840 + 1.152440I$	$-3.86435 + 3.51413I$	$-10.49218 - 3.82170I$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.46833 + 1.40959I$ $a = 1.28786 - 1.10744I$ $b = -0.562936 - 1.175720I$	$-0.96374 + 9.68671I$	0
$u = -0.46833 - 1.40959I$ $a = 1.28786 + 1.10744I$ $b = -0.562936 + 1.175720I$	$-0.96374 - 9.68671I$	0
$u = -0.256255 + 0.421847I$ $a = 1.193230 + 0.520583I$ $b = 0.123371 + 0.236807I$	$-0.427988 + 1.171450I$	$-4.97387 - 5.79413I$
$u = -0.256255 - 0.421847I$ $a = 1.193230 - 0.520583I$ $b = 0.123371 - 0.236807I$	$-0.427988 - 1.171450I$	$-4.97387 + 5.79413I$
$u = -0.05066 + 1.56885I$ $a = 0.821923 + 0.217869I$ $b = -0.377724 + 0.762011I$	$6.69834 + 1.66397I$	0
$u = -0.05066 - 1.56885I$ $a = 0.821923 - 0.217869I$ $b = -0.377724 - 0.762011I$	$6.69834 - 1.66397I$	0
$u = 0.040527 + 0.421390I$ $a = 2.04288 + 1.54331I$ $b = 0.455512 + 0.708227I$	$-0.32690 + 1.38361I$	$-5.63624 - 5.27111I$
$u = 0.040527 - 0.421390I$ $a = 2.04288 - 1.54331I$ $b = 0.455512 - 0.708227I$	$-0.32690 - 1.38361I$	$-5.63624 + 5.27111I$
$u = -0.14166 + 1.59539I$ $a = 1.013790 - 0.413700I$ $b = -0.360591 - 0.879206I$	$6.34972 + 4.89959I$	0
$u = -0.14166 - 1.59539I$ $a = 1.013790 + 0.413700I$ $b = -0.360591 + 0.879206I$	$6.34972 - 4.89959I$	0



Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.271803 + 0.171548I$	$-1.06689 - 3.17946I$	$-11.00684 + 2.84027I$
$a = 2.13801 - 1.84885I$		
$b = 0.623695 - 0.921062I$		
$u = 0.271803 - 0.171548I$	$-1.06689 + 3.17946I$	$-11.00684 - 2.84027I$
$a = 2.13801 + 1.84885I$		
$b = 0.623695 + 0.921062I$		

**II.**

$$I_2^u = \langle u^2a - au + u^2 + b - u, 2u^3a - 5u^3 + \dots - 2a + 15, u^4 - u^3 + 3u^2 - 2u + 1 \rangle$$

**(i) Arc colorings**

$$a_6 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} a \\ -u^2a + au - u^2 + u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} u^2a + \frac{1}{2}u^3 - au + a + \frac{1}{2}u - \frac{1}{2} \\ -u^2a + au - u^2 + u - 1 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} \frac{1}{2}u^3 - u^2 + a + \frac{3}{2}u - \frac{3}{2} \\ -u^2a + au - u^2 + u - 1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} u \\ u^3 + u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} u^2 + 1 \\ u^3 - u^2 + 2u - 1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} u^2a + \frac{1}{2}u^3 - au + a + \frac{1}{2}u - \frac{1}{2} \\ -u^2a + au - u^2 + u - 1 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -u \\ u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} u \\ u^3 + u \end{pmatrix}$$

**(ii) Obstruction class = 1**

**(iii) Cusp Shapes =**  $-\frac{3}{2}u^3a + 11u^2a + \frac{7}{2}u^3 - \frac{15}{2}au + 5u^2 + \frac{5}{2}a + \frac{11}{2}u - \frac{7}{2}$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_3, c_5$	$(u^2 - u + 1)^4$
$c_2$	$(u^2 + u + 1)^4$
$c_4, c_9$	$u^8$
$c_6, c_7, c_{11}$	$(u^4 - u^3 + 3u^2 - 2u + 1)^2$
$c_8$	$(u^4 - u^3 + u^2 + 1)^2$
$c_{10}$	$(u^4 + u^3 + 3u^2 + 2u + 1)^2$
$c_{12}$	$(u^4 + u^3 + u^2 + 1)^2$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_3$ $c_5$	$(y^2 + y + 1)^4$
$c_4, c_9$	$y^8$
$c_6, c_7, c_{10}$ $c_{11}$	$(y^4 + 5y^3 + 7y^2 + 2y + 1)^2$
$c_8, c_{12}$	$(y^4 + y^3 + 3y^2 + 2y + 1)^2$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.395123 + 0.506844I$		
$a = 0.32193 + 1.46300I$	$-0.211005 + 0.614778I$	$-3.71851 + 3.54153I$
$b = 0.500000 + 0.866025I$		
$u = 0.395123 + 0.506844I$		
$a = -0.39397 - 1.87632I$	$-0.21101 - 3.44499I$	$-1.37216 + 7.25656I$
$b = 0.500000 - 0.866025I$		
$u = 0.395123 - 0.506844I$		
$a = 0.32193 - 1.46300I$	$-0.211005 - 0.614778I$	$-3.71851 - 3.54153I$
$b = 0.500000 - 0.866025I$		
$u = 0.395123 - 0.506844I$		
$a = -0.39397 + 1.87632I$	$-0.21101 + 3.44499I$	$-1.37216 - 7.25656I$
$b = 0.500000 + 0.866025I$		
$u = 0.10488 + 1.55249I$		
$a = -0.975620 - 0.357786I$	$6.79074 - 5.19385I$	$4.49529 + 8.13693I$
$b = 0.500000 - 0.866025I$		
$u = 0.10488 + 1.55249I$		
$a = -0.702338 + 0.200007I$	$6.79074 - 1.13408I$	$-0.52961 - 5.68505I$
$b = 0.500000 + 0.866025I$		
$u = 0.10488 - 1.55249I$		
$a = -0.975620 + 0.357786I$	$6.79074 + 5.19385I$	$4.49529 - 8.13693I$
$b = 0.500000 + 0.866025I$		
$u = 0.10488 - 1.55249I$		
$a = -0.702338 - 0.200007I$	$6.79074 + 1.13408I$	$-0.52961 + 5.68505I$
$b = 0.500000 - 0.866025I$		

$$\text{III. } I_3^u = \langle -u^6 - 2u^4 - 2u^3 - u^2 + b - 2u, -u^6 - 3u^4 - 2u^3 - 2u^2 + a - 4u - 1, u^{15} + 5u^{13} + \dots - u + 1 \rangle$$

(i) Arc colorings

$$a_6 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} u^6 + 3u^4 + 2u^3 + 2u^2 + 4u + 1 \\ u^6 + 2u^4 + 2u^3 + u^2 + 2u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} u^{12} + 5u^{10} + \dots + 2u + 1 \\ u^{12} + 4u^{10} + 4u^9 + 6u^8 + 12u^7 + 8u^6 + 12u^5 + 9u^4 + 4u^3 + 4u^2 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} u^{13} + 4u^{11} + \dots + 6u^2 + 5u \\ -u^{12} - 4u^{10} - 3u^9 - 6u^8 - 9u^7 - 5u^6 - 9u^5 - 3u^4 - u^3 - u^2 + 2u - 1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} u \\ u^3 + u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} u \\ u^3 + u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} u^2 + 1 \\ u^4 + 2u^2 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} u^{13} + u^{12} + \dots + 3u + 1 \\ -u^{12} - 4u^{10} - 3u^9 - 6u^8 - 9u^7 - 5u^6 - 9u^5 - 3u^4 - u^3 - u^2 + 2u - 1 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -u^3 \\ -u^5 - u^3 + u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} u^4 + u^2 + 1 \\ u^6 + 2u^4 + u^2 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes =  $-4u^9 - 12u^7 - 12u^6 - 12u^5 - 24u^4 - 12u^3 - 12u^2 - 8u - 2$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1$	$(u^5 + 3u^4 + 4u^3 + u^2 - u - 1)^3$
$c_2, c_5$	$(u^5 + u^4 + 2u^3 + u^2 + u + 1)^3$
$c_3, c_4, c_9$	$(u^5 - u^4 - 2u^3 + u^2 + u + 1)^3$
$c_6, c_7, c_8$ $c_{10}, c_{12}$	$u^{15} + 5u^{13} + \dots - u + 1$
$c_{11}$	$u^{15} + 10u^{14} + \dots - 5u - 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1$	$(y^5 - y^4 + 8y^3 - 3y^2 + 3y - 1)^3$
$c_2, c_5$	$(y^5 + 3y^4 + 4y^3 + y^2 - y - 1)^3$
$c_3, c_4, c_9$	$(y^5 - 5y^4 + 8y^3 - 3y^2 - y - 1)^3$
$c_6, c_7, c_8$ $c_{10}, c_{12}$	$y^{15} + 10y^{14} + \dots - 5y - 1$
$c_{11}$	$y^{15} - 10y^{14} + \dots - 65y - 1$



(vi) Complex Volumes and Cusp Shapes

Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.009180 + 0.154259I$ $a = 0.41296 - 1.82234I$ $b = -0.455697 - 1.200150I$	$-5.87256 + 4.40083I$	$-6.74431 - 3.49859I$
$u = -1.009180 - 0.154259I$ $a = 0.41296 + 1.82234I$ $b = -0.455697 + 1.200150I$	$-5.87256 - 4.40083I$	$-6.74431 + 3.49859I$
$u = -0.191814 + 0.839165I$ $a = 0.62987 + 2.60849I$ $b = 0.339110 + 0.822375I$	$-0.32910 + 1.53058I$	$-2.51511 - 4.43065I$
$u = -0.191814 - 0.839165I$ $a = 0.62987 - 2.60849I$ $b = 0.339110 - 0.822375I$	$-0.32910 - 1.53058I$	$-2.51511 + 4.43065I$
$u = -0.855893$ $a = -0.209424$ $b = -0.766826$	$-2.40108$	$-3.48110$
$u = -0.070375 + 1.145600I$ $a = 1.57432 + 1.72920I$ $b = 0.339110 - 0.822375I$	$-0.32910 - 1.53058I$	$-2.51511 + 4.43065I$
$u = -0.070375 - 1.145600I$ $a = 1.57432 - 1.72920I$ $b = 0.339110 + 0.822375I$	$-0.32910 + 1.53058I$	$-2.51511 - 4.43065I$
$u = 0.427947 + 1.244760I$ $a = 0.454474 + 0.643686I$ $b = -0.766826$	$-2.40108$	$-3.48114 + 0.I$
$u = 0.427947 - 1.244760I$ $a = 0.454474 - 0.643686I$ $b = -0.766826$	$-2.40108$	$-3.48114 + 0.I$
$u = 0.592752 + 1.247160I$ $a = -0.210506 - 0.787763I$ $b = -0.455697 - 1.200150I$	$-5.87256 + 4.40083I$	$-6.74431 - 3.49859I$

Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.592752 - 1.247160I$	$-5.87256 - 4.40083I$	$-6.74431 + 3.49859I$
$a = -0.210506 + 0.787763I$		
$b = -0.455697 + 1.200150I$		
$u = 0.41642 + 1.40142I$	$-5.87256 - 4.40083I$	$-6.74431 + 3.49859I$
$a = 1.43045 + 0.99035I$		
$b = -0.455697 + 1.200150I$		
$u = 0.41642 - 1.40142I$	$-5.87256 + 4.40083I$	$-6.74431 - 3.49859I$
$a = 1.43045 - 0.99035I$		
$b = -0.455697 - 1.200150I$		
$u = 0.262189 + 0.306431I$	$-0.32910 + 1.53058I$	$-2.51511 - 4.43065I$
$a = 1.81314 + 1.58784I$		
$b = 0.339110 + 0.822375I$		
$u = 0.262189 - 0.306431I$	$-0.32910 - 1.53058I$	$-2.51511 + 4.43065I$
$a = 1.81314 - 1.58784I$		
$b = 0.339110 - 0.822375I$		

#### IV. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1$	$(u^2 - u + 1)^4(u^5 + 3u^4 + 4u^3 + u^2 - u - 1)^3$ $\cdot (u^{42} + 22u^{41} + \dots + 383u + 16)$
$c_2$	$((u^2 + u + 1)^4)(u^5 + u^4 + \dots + u + 1)^3(u^{42} + 2u^{41} + \dots - 3u + 4)$
$c_3$	$(u^2 - u + 1)^4(u^5 - u^4 - 2u^3 + u^2 + u + 1)^3$ $\cdot (u^{42} - 2u^{41} + \dots - 23400u + 3104)$
$c_4, c_9$	$u^8(u^5 - u^4 + \dots + u + 1)^3(u^{42} + 2u^{41} + \dots + 3584u + 2048)$
$c_5$	$((u^2 - u + 1)^4)(u^5 + u^4 + \dots + u + 1)^3(u^{42} + 2u^{41} + \dots - 3u + 4)$
$c_6, c_7$	$((u^4 - u^3 + 3u^2 - 2u + 1)^2)(u^{15} + 5u^{13} + \dots - u + 1)$ $\cdot (u^{42} - 3u^{41} + \dots - 4u + 1)$
$c_8$	$((u^4 - u^3 + u^2 + 1)^2)(u^{15} + 5u^{13} + \dots - u + 1)(u^{42} - 3u^{41} + \dots - 2u + 1)$
$c_{10}$	$((u^4 + u^3 + 3u^2 + 2u + 1)^2)(u^{15} + 5u^{13} + \dots - u + 1)$ $\cdot (u^{42} - 3u^{41} + \dots - 4u + 1)$
$c_{11}$	$((u^4 - u^3 + 3u^2 - 2u + 1)^2)(u^{15} + 10u^{14} + \dots - 5u - 1)$ $\cdot (u^{42} + 23u^{41} + \dots + 6u + 1)$
$c_{12}$	$((u^4 + u^3 + u^2 + 1)^2)(u^{15} + 5u^{13} + \dots - u + 1)(u^{42} - 3u^{41} + \dots - 2u + 1)$

## V. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1$	$(y^2 + y + 1)^4(y^5 - y^4 + 8y^3 - 3y^2 + 3y - 1)^3$ $\cdot (y^{42} - 2y^{41} + \dots + 33759y + 256)$
$c_2, c_5$	$(y^2 + y + 1)^4(y^5 + 3y^4 + 4y^3 + y^2 - y - 1)^3$ $\cdot (y^{42} + 22y^{41} + \dots + 383y + 16)$
$c_3$	$(y^2 + y + 1)^4(y^5 - 5y^4 + 8y^3 - 3y^2 - y - 1)^3$ $\cdot (y^{42} - 26y^{41} + \dots + 359975104y + 9634816)$
$c_4, c_9$	$y^8(y^5 - 5y^4 + 8y^3 - 3y^2 - y - 1)^3$ $\cdot (y^{42} - 30y^{41} + \dots - 36438016y + 4194304)$
$c_6, c_7, c_{10}$	$((y^4 + 5y^3 + 7y^2 + 2y + 1)^2)(y^{15} + 10y^{14} + \dots - 5y - 1)$ $\cdot (y^{42} + 35y^{41} + \dots + 6y + 1)$
$c_8, c_{12}$	$((y^4 + y^3 + 3y^2 + 2y + 1)^2)(y^{15} + 10y^{14} + \dots - 5y - 1)$ $\cdot (y^{42} + 23y^{41} + \dots + 6y + 1)$
$c_{11}$	$((y^4 + 5y^3 + 7y^2 + 2y + 1)^2)(y^{15} - 10y^{14} + \dots - 65y - 1)$ $\cdot (y^{42} - 5y^{41} + \dots - 54y + 1)$