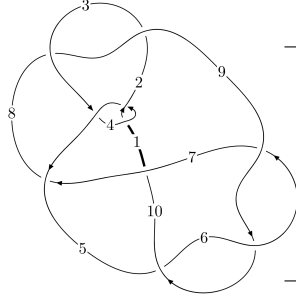
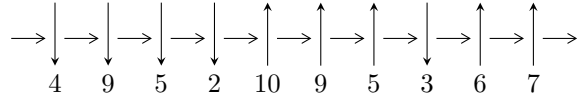


10₁₂₉ (K10n₁₈)



A knot diagram¹

Linearized knot diagram



Solving Sequence

$$5,10 \xrightarrow{c_5} 2,6 \xrightarrow{c_4} 4 \xrightarrow{c_1} 1 \xrightarrow{c_3} 3 \xrightarrow{c_9} 9 \xrightarrow{c_6} 7 \xrightarrow{c_7} 8 \longrightarrow c_2, c_8, c_{10}$$

Ideals for irreducible components² of X_{par}

$$I_1^u = \langle u^{12} + u^{11} + 5u^{10} + 4u^9 + 9u^8 + 6u^7 + 5u^6 + 4u^5 - 2u^4 + u^3 - 2u^2 + b + 1, \\ -u^{14} - 2u^{13} - 8u^{12} - 11u^{11} - 23u^{10} - 23u^9 - 28u^8 - 20u^7 - 9u^6 - 5u^5 + 7u^4 + u^3 + u^2 + a - u - 3, \\ u^{15} + 2u^{14} + 8u^{13} + 12u^{12} + 24u^{11} + 28u^{10} + 32u^9 + 29u^8 + 14u^7 + 9u^6 - 6u^5 - 5u^4 - 2u^3 - 2u^2 + 4u + 1 \rangle \\ I_2^u = \langle b + 1, -u^2 + a - u - 1, u^3 + u^2 + 2u + 1 \rangle$$

* 2 irreducible components of $\dim_{\mathbb{C}} = 0$, with total 18 representations.

¹The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

²All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$I_1^u = \langle u^{12} + u^{11} + \dots + b + 1, -u^{14} - 2u^{13} + \dots + a - 3, u^{15} + 2u^{14} + \dots + 4u + 1 \rangle \quad \text{I.}$$

(i) Arc colorings

$$a_5 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} u^{14} + 2u^{13} + \dots + u + 3 \\ -u^{12} - u^{11} - 5u^{10} - 4u^9 - 9u^8 - 6u^7 - 5u^6 - 4u^5 + 2u^4 - u^3 + 2u^2 - 1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} u^{14} + 2u^{13} + \dots - u + 3 \\ -u^{13} - u^{12} + \dots - u - 1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} u^5 + 2u^3 + u \\ -u^7 - 3u^5 - 2u^3 + u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} u^{14} + u^{13} + \dots - 2u + 2 \\ -u^{13} - u^{12} + \dots - u - 1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -u \\ u^3 + u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} u^2 + 1 \\ -u^4 - 2u^2 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -u^4 - u^2 + 1 \\ -u^4 - 2u^2 \end{pmatrix}$$

(ii) Obstruction class = -1

$$\text{(iii) Cusp Shapes} = -u^{14} - 2u^{13} - 11u^{12} - 16u^{11} - 42u^{10} - 47u^9 - 71u^8 - 62u^7 - 44u^6 - 31u^5 + 12u^4 + 4u^3 + 14u^2 + 5u - 9$$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1, c_4	$u^{15} - 4u^{14} + \dots - 3u + 1$
c_2, c_8	$u^{15} + u^{14} + \dots + 12u + 8$
c_3	$u^{15} + 2u^{14} + \dots - 3u + 1$
c_5, c_6, c_9	$u^{15} + 2u^{14} + \dots + 4u + 1$
c_7	$u^{15} + 8u^{14} + \dots + 280u - 49$
c_{10}	$u^{15} - 2u^{14} + \dots + 2u + 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1, c_4	$y^{15} - 2y^{14} + \dots - 3y - 1$
c_2, c_8	$y^{15} + 21y^{14} + \dots - 48y - 64$
c_3	$y^{15} + 26y^{14} + \dots - 3y - 1$
c_5, c_6, c_9	$y^{15} + 12y^{14} + \dots + 20y - 1$
c_7	$y^{15} - 32y^{14} + \dots + 220108y - 2401$
c_{10}	$y^{15} - 20y^{14} + \dots + 20y - 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.946822 + 0.058779I$ $a = -0.57292 - 1.67757I$ $b = 1.05231 + 1.07767I$	$10.46560 - 3.92970I$	$3.25200 + 2.37642I$
$u = -0.946822 - 0.058779I$ $a = -0.57292 + 1.67757I$ $b = 1.05231 - 1.07767I$	$10.46560 + 3.92970I$	$3.25200 - 2.37642I$
$u = -0.078813 + 1.147950I$ $a = -0.99527 + 1.21138I$ $b = -1.148380 - 0.278021I$	$-4.30318 - 1.14653I$	$-3.69630 - 0.14216I$
$u = -0.078813 - 1.147950I$ $a = -0.99527 - 1.21138I$ $b = -1.148380 + 0.278021I$	$-4.30318 + 1.14653I$	$-3.69630 + 0.14216I$
$u = 0.271249 + 1.119280I$ $a = 0.070766 - 0.823663I$ $b = -0.282237 + 0.716387I$	$-1.32042 + 2.58137I$	$0.00443 - 4.00241I$
$u = 0.271249 - 1.119280I$ $a = 0.070766 + 0.823663I$ $b = -0.282237 - 0.716387I$	$-1.32042 - 2.58137I$	$0.00443 + 4.00241I$
$u = -0.488190 + 1.251290I$ $a = -0.601814 + 0.190541I$ $b = 0.92821 - 1.13080I$	$6.78648 - 1.17157I$	$0.521469 + 0.840506I$
$u = -0.488190 - 1.251290I$ $a = -0.601814 - 0.190541I$ $b = 0.92821 + 1.13080I$	$6.78648 + 1.17157I$	$0.521469 - 0.840506I$
$u = 0.604547 + 0.198361I$ $a = 0.727011 + 0.890995I$ $b = 0.195944 - 0.500014I$	$1.37013 + 0.70150I$	$5.29100 - 2.23884I$
$u = 0.604547 - 0.198361I$ $a = 0.727011 - 0.890995I$ $b = 0.195944 + 0.500014I$	$1.37013 - 0.70150I$	$5.29100 + 2.23884I$

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.197329 + 1.368030I$		
$a = 1.103000 + 0.360621I$	$-3.65536 + 3.51330I$	$0.20706 - 4.67402I$
$b = 0.560305 - 0.345696I$		
$u = 0.197329 - 1.368030I$		
$a = 1.103000 - 0.360621I$	$-3.65536 - 3.51330I$	$0.20706 + 4.67402I$
$b = 0.560305 + 0.345696I$		
$u = -0.445416 + 1.338930I$		
$a = 0.91370 - 1.42147I$	$6.09422 - 8.90152I$	$-0.37309 + 5.02376I$
$b = 1.13244 + 0.99333I$		
$u = -0.445416 - 1.338930I$		
$a = 0.91370 + 1.42147I$	$6.09422 + 8.90152I$	$-0.37309 - 5.02376I$
$b = 1.13244 - 0.99333I$		
$u = -0.227769$		
$a = 2.71106$	-1.26612	-9.41310
$b = -0.877160$		

$$\text{II. } I_2^u = \langle b + 1, -u^2 + a - u - 1, u^3 + u^2 + 2u + 1 \rangle$$

(i) Arc colorings

$$a_5 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} u^2 + u + 1 \\ -1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} u^2 + u + 2 \\ -1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} u^2 + u + 1 \\ -1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -u \\ -u^2 - u - 1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} u^2 + 1 \\ -u^2 - u - 1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -u \\ -u^2 - u - 1 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = $5u^2 + 4u + 4$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1, c_3	$(u - 1)^3$
c_2, c_8	u^3
c_4	$(u + 1)^3$
c_5, c_6	$u^3 + u^2 + 2u + 1$
c_7, c_{10}	$u^3 + u^2 - 1$
c_9	$u^3 - u^2 + 2u - 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1, c_3, c_4	$(y - 1)^3$
c_2, c_8	y^3
c_5, c_6, c_9	$y^3 + 3y^2 + 2y - 1$
c_7, c_{10}	$y^3 - y^2 + 2y - 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to I_2^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.215080 + 1.307140I$ $a = -0.877439 + 0.744862I$ $b = -1.00000$	$-4.66906 - 2.82812I$	$-5.17211 + 2.41717I$
$u = -0.215080 - 1.307140I$ $a = -0.877439 - 0.744862I$ $b = -1.00000$	$-4.66906 + 2.82812I$	$-5.17211 - 2.41717I$
$u = -0.569840$ $a = 0.754878$ $b = -1.00000$	-0.531480	3.34420

III. u-Polynomials

Crossings	u-Polynomials at each crossing
c_1	$((u - 1)^3)(u^{15} - 4u^{14} + \dots - 3u + 1)$
c_2, c_8	$u^3(u^{15} + u^{14} + \dots + 12u + 8)$
c_3	$((u - 1)^3)(u^{15} + 2u^{14} + \dots - 3u + 1)$
c_4	$((u + 1)^3)(u^{15} - 4u^{14} + \dots - 3u + 1)$
c_5, c_6	$(u^3 + u^2 + 2u + 1)(u^{15} + 2u^{14} + \dots + 4u + 1)$
c_7	$(u^3 + u^2 - 1)(u^{15} + 8u^{14} + \dots + 280u - 49)$
c_9	$(u^3 - u^2 + 2u - 1)(u^{15} + 2u^{14} + \dots + 4u + 1)$
c_{10}	$(u^3 + u^2 - 1)(u^{15} - 2u^{14} + \dots + 2u + 1)$

IV. Riley Polynomials

Crossings	Riley Polynomials at each crossing
c_1, c_4	$((y - 1)^3)(y^{15} - 2y^{14} + \dots - 3y - 1)$
c_2, c_8	$y^3(y^{15} + 21y^{14} + \dots - 48y - 64)$
c_3	$((y - 1)^3)(y^{15} + 26y^{14} + \dots - 3y - 1)$
c_5, c_6, c_9	$(y^3 + 3y^2 + 2y - 1)(y^{15} + 12y^{14} + \dots + 20y - 1)$
c_7	$(y^3 - y^2 + 2y - 1)(y^{15} - 32y^{14} + \dots + 220108y - 2401)$
c_{10}	$(y^3 - y^2 + 2y - 1)(y^{15} - 20y^{14} + \dots + 20y - 1)$