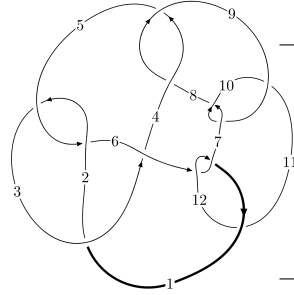
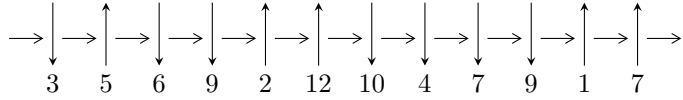


12n<sub>0061</sub> (K12n<sub>0061</sub>)



A knot diagram<sup>1</sup>

**Linearized knot diagram**



**Solving Sequence**

$$4,9 \xrightarrow{c_4} 5,7 \xrightarrow{c_9} 10,12 \xrightarrow{c_{12}} 1 \xrightarrow{c_6} 6 \xrightarrow{c_3} 3 \xrightarrow{c_2} 2 \xrightarrow{c_8} 8 \xrightarrow{c_{11}} 11 \longrightarrow c_1, c_5, c_7, c_{10}$$

**Ideals for irreducible components<sup>2</sup> of  $X_{\text{par}}$**

$$I_1^u = \langle -6.70930 \times 10^{96} u^{46} - 9.84287 \times 10^{96} u^{45} + \dots + 6.09681 \times 10^{98} d - 6.16018 \times 10^{99}, \\ -1.03963 \times 10^{97} u^{46} - 1.48428 \times 10^{97} u^{45} + \dots + 3.04841 \times 10^{98} c - 8.34618 \times 10^{99}, \\ -3.55708 \times 10^{84} u^{46} - 5.87581 \times 10^{84} u^{45} + \dots + 4.44856 \times 10^{87} b - 3.91588 \times 10^{87}, \\ 2.90225 \times 10^{85} u^{46} + 4.18154 \times 10^{85} u^{45} + \dots + 4.44856 \times 10^{87} a + 2.35085 \times 10^{88}, \\ u^{47} + 2u^{46} + \dots + 1024u + 512 \rangle$$

$$I_2^u = \langle a^2 u + d - a, a^2 u + c, a^2 u + b - a, -u^4 a + 2u^3 a - u^4 + a^3 + u^2 a + u^3 - 3au + 2u^2 - u - 1, \\ u^5 - u^4 - 2u^3 + u^2 + u + 1 \rangle$$

$$I_1^v = \langle c, d - v + 1, b, a - v, v^2 - v + 1 \rangle$$

$$I_2^v = \langle a, d + v + 1, c + a, b - v - 1, v^2 + v + 1 \rangle$$

$$I_3^v = \langle a, d - 1, c + a - 1, b + 1, v - 1 \rangle$$

$$I_4^v = \langle a, d^2 + 2db + b^2 + d + b + 1, dc - dv + 2cb + ba - av + c + a - v + 2, da - cb - 1, \\ a^2 v^2 - cav - a^2 v + v^2 a + c^2 + 2ca - 2cv + a^2 - 2av + v^2, bv + 1 \rangle$$

\* 5 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 67 representations.

\* 1 irreducible components of  $\dim_{\mathbb{C}} = 1$

<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\mathbf{I. } I_1^u = \langle -6.71 \times 10^{96} u^{46} - 9.84 \times 10^{96} u^{45} + \dots + 6.10 \times 10^{98} d - 6.16 \times 10^{99}, -1.04 \times 10^{97} u^{46} - 1.48 \times 10^{97} u^{45} + \dots + 3.05 \times 10^{98} c - 8.35 \times 10^{99}, -3.56 \times 10^{84} u^{46} - 5.88 \times 10^{84} u^{45} + \dots + 4.45 \times 10^{87} b - 3.92 \times 10^{87}, 2.90 \times 10^{85} u^{46} + 4.18 \times 10^{85} u^{45} + \dots + 4.45 \times 10^{87} a + 2.35 \times 10^{88}, u^{47} + 2u^{46} + \dots + 1024u + 512 \rangle$$

(i) Arc colorings

$$a_4 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -0.00652403u^{46} - 0.00939975u^{45} + \dots - 0.175259u - 5.28451 \\ 0.000799603u^{46} + 0.00132083u^{45} + \dots + 1.47622u + 0.880259 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0.00732363u^{46} + 0.0107206u^{45} + \dots + 1.65147u + 6.16477 \\ 0.000799603u^{46} + 0.00132083u^{45} + \dots + 1.47622u + 0.880259 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 0.0341039u^{46} + 0.0486904u^{45} + \dots + 14.6818u + 27.3788 \\ 0.0110046u^{46} + 0.0161443u^{45} + \dots + 4.15721u + 10.1039 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 0.0252497u^{46} + 0.0366947u^{45} + \dots + 11.3108u + 20.0129 \\ 0.00558802u^{46} + 0.00914935u^{45} + \dots + 0.890394u + 6.27203 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -0.0265369u^{46} - 0.0375470u^{45} + \dots - 11.6287u - 20.8089 \\ -0.00128717u^{46} - 0.000852284u^{45} + \dots - 0.317834u - 0.796018 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 0.00513208u^{46} + 0.00817440u^{45} + \dots - 0.763266u + 5.03316 \\ 0.00862965u^{46} + 0.0123123u^{45} + \dots + 4.96716u + 7.59297 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -0.00521744u^{46} - 0.00448641u^{45} + \dots - 6.21813u - 1.48986 \\ 0.00291266u^{46} + 0.00502319u^{45} + \dots + 2.03496u + 3.47740 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} u \\ u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0.00732363u^{46} + 0.0107206u^{45} + \dots + 1.65147u + 6.16477 \\ 0.00275888u^{46} + 0.00400645u^{45} + \dots + 1.74743u + 2.89071 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes =  $0.0132573u^{46} + 0.0100723u^{45} + \dots + 23.2337u - 1.69873$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1$	$u^{47} + 24u^{46} + \dots + 216u - 16$
$c_2, c_5$	$u^{47} + 2u^{46} + \dots + 16u + 4$
$c_3$	$u^{47} - 2u^{46} + \dots - 21456u + 2592$
$c_4, c_8$	$u^{47} + 2u^{46} + \dots + 1024u + 512$
$c_6, c_{12}$	$u^{47} + 8u^{46} + \dots + 56u + 16$
$c_7, c_9$	$u^{47} - 8u^{46} + \dots + 56u + 16$
$c_{10}$	$u^{47} + 54u^{46} + \dots + 544u + 256$
$c_{11}$	$u^{47} - 14u^{46} + \dots + 6688u - 256$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1$	$y^{47} + 48y^{45} + \dots + 67872y - 256$
$c_2, c_5$	$y^{47} + 24y^{46} + \dots + 216y - 16$
$c_3$	$y^{47} - 24y^{46} + \dots + 353776896y - 6718464$
$c_4, c_8$	$y^{47} - 30y^{46} + \dots + 1572864y - 262144$
$c_6, c_{12}$	$y^{47} - 14y^{46} + \dots + 6688y - 256$
$c_7, c_9$	$y^{47} - 54y^{46} + \dots + 544y - 256$
$c_{10}$	$y^{47} - 114y^{46} + \dots - 1990144y - 65536$
$c_{11}$	$y^{47} + 46y^{46} + \dots + 11182592y - 65536$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.168857 + 0.977277I$ $a = -0.502467 + 0.614921I$ $b = -1.127600 + 0.633374I$ $c = -0.961290 + 0.734797I$ $d = -0.756569 + 0.908522I$	$-0.50019 - 4.79223I$	$-2.43501 + 7.48976I$
$u = -0.168857 - 0.977277I$ $a = -0.502467 - 0.614921I$ $b = -1.127600 - 0.633374I$ $c = -0.961290 - 0.734797I$ $d = -0.756569 - 0.908522I$	$-0.50019 + 4.79223I$	$-2.43501 - 7.48976I$
$u = 0.758370 + 0.572620I$ $a = 0.677402 - 0.992682I$ $b = 0.306606 + 0.328751I$ $c = -0.587766 + 0.872152I$ $d = -0.654201 + 0.089268I$	$-3.62778 + 1.19000I$	$-10.45074 - 1.01195I$
$u = 0.758370 - 0.572620I$ $a = 0.677402 + 0.992682I$ $b = 0.306606 - 0.328751I$ $c = -0.587766 - 0.872152I$ $d = -0.654201 - 0.089268I$	$-3.62778 - 1.19000I$	$-10.45074 + 1.01195I$
$u = 0.798854 + 0.256222I$ $a = 0.588853 + 0.419968I$ $b = 0.579476 - 0.018798I$ $c = -0.544662 - 1.097250I$ $d = -0.20396 - 1.54472I$	$1.43042 - 3.68269I$	$-0.57615 + 8.67104I$
$u = 0.798854 - 0.256222I$ $a = 0.588853 - 0.419968I$ $b = 0.579476 + 0.018798I$ $c = -0.544662 + 1.097250I$ $d = -0.20396 + 1.54472I$	$1.43042 + 3.68269I$	$-0.57615 - 8.67104I$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.287114 + 0.709757I$ $a = 0.383641 + 0.556567I$ $b = 0.733419 + 0.549353I$ $c = 1.205770 + 0.404495I$ $d = 0.597302 + 0.839395I$	$1.71355 + 0.99880I$	$4.04476 - 2.43406I$
$u = 0.287114 - 0.709757I$ $a = 0.383641 - 0.556567I$ $b = 0.733419 - 0.549353I$ $c = 1.205770 - 0.404495I$ $d = 0.597302 - 0.839395I$	$1.71355 - 0.99880I$	$4.04476 + 2.43406I$
$u = -0.723521 + 0.092490I$ $a = -0.704709 + 0.351766I$ $b = -0.480781 - 0.041433I$ $c = -3.56166 + 1.78408I$ $d = -1.048200 + 0.427037I$	$0.84436 + 2.80891I$	$-4.36866 - 6.45196I$
$u = -0.723521 - 0.092490I$ $a = -0.704709 - 0.351766I$ $b = -0.480781 + 0.041433I$ $c = -3.56166 - 1.78408I$ $d = -1.048200 - 0.427037I$	$0.84436 - 2.80891I$	$-4.36866 + 6.45196I$
$u = 0.549584 + 0.433005I$ $a = 0.450542 + 0.396109I$ $b = 0.579765 + 0.179992I$ $c = 2.21899 + 0.55940I$ $d = 0.703512 + 0.579046I$	$2.18982 + 0.74670I$	$2.91211 + 1.96105I$
$u = 0.549584 - 0.433005I$ $a = 0.450542 - 0.396109I$ $b = 0.579765 - 0.179992I$ $c = 2.21899 - 0.55940I$ $d = 0.703512 - 0.579046I$	$2.18982 - 0.74670I$	$2.91211 - 1.96105I$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.659997 + 0.157577I$ $a = -0.620233 + 0.304010I$ $b = -0.486762 + 0.009061I$ $c = 0.225348 - 0.901957I$ $d = -0.488745 - 1.323290I$	$1.05099 - 1.22135I$	$-3.11104 - 2.86511I$
$u = -0.659997 - 0.157577I$ $a = -0.620233 - 0.304010I$ $b = -0.486762 - 0.009061I$ $c = 0.225348 + 0.901957I$ $d = -0.488745 + 1.323290I$	$1.05099 + 1.22135I$	$-3.11104 + 2.86511I$
$u = -0.226818 + 1.310000I$ $a = -0.108597 - 1.104710I$ $b = -0.068409 + 0.532975I$ $c = 0.830749 - 0.602517I$ $d = -1.046880 - 0.665279I$	$-4.12204 - 2.83071I$	$-3.10594 + 2.47522I$
$u = -0.226818 - 1.310000I$ $a = -0.108597 + 1.104710I$ $b = -0.068409 - 0.532975I$ $c = 0.830749 + 0.602517I$ $d = -1.046880 + 0.665279I$	$-4.12204 + 2.83071I$	$-3.10594 - 2.47522I$
$u = 0.024914 + 0.666306I$ $a = -0.311476 + 0.943178I$ $b = -0.68322 + 1.48591I$ $c = -0.472994 + 0.671049I$ $d = -0.54160 + 1.46349I$	$-0.68586 + 1.51893I$	$-2.03699 + 0.09471I$
$u = 0.024914 - 0.666306I$ $a = -0.311476 - 0.943178I$ $b = -0.68322 - 1.48591I$ $c = -0.472994 - 0.671049I$ $d = -0.54160 - 1.46349I$	$-0.68586 - 1.51893I$	$-2.03699 - 0.09471I$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.275400 + 0.425723I$ $a = 0.527825 + 0.529108I$ $b = 0.767343 - 0.182692I$ $c = -1.00554 - 1.01478I$ $d = -1.17436 - 1.26704I$	$-1.49383 - 5.48046I$	$-1.24533 + 5.03878I$
$u = 1.275400 - 0.425723I$ $a = 0.527825 - 0.529108I$ $b = 0.767343 + 0.182692I$ $c = -1.00554 + 1.01478I$ $d = -1.17436 + 1.26704I$	$-1.49383 + 5.48046I$	$-1.24533 - 5.03878I$
$u = 1.351470 + 0.126259I$ $a = -1.098230 + 0.058069I$ $b = -2.73978 + 0.07859I$ $c = 0.428611 + 0.687312I$ $d = 0.23689 + 2.41586I$	$-5.10242 + 0.08441I$	$-6.12902 + 0.I$
$u = 1.351470 - 0.126259I$ $a = -1.098230 - 0.058069I$ $b = -2.73978 - 0.07859I$ $c = 0.428611 - 0.687312I$ $d = 0.23689 - 2.41586I$	$-5.10242 - 0.08441I$	$-6.12902 + 0.I$
$u = -0.062543 + 0.611080I$ $a = -0.14897 - 1.86717I$ $b = -0.025679 + 0.284490I$ $c = 3.03261 + 4.80458I$ $d = -0.366383 - 1.198400I$	$-0.53961 - 2.33649I$	$-0.16377 + 3.97632I$
$u = -0.062543 - 0.611080I$ $a = -0.14897 + 1.86717I$ $b = -0.025679 - 0.284490I$ $c = 3.03261 - 4.80458I$ $d = -0.366383 + 1.198400I$	$-0.53961 + 2.33649I$	$-0.16377 - 3.97632I$



Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.354510 + 0.305217I$ $a = 1.072310 + 0.133945I$ $b = 2.69315 + 0.17757I$ $c = -0.777654 + 0.758804I$ $d = -0.87546 + 2.59578I$	$-4.74548 + 5.93381I$	$-5.07129 - 5.57342I$
$u = -1.354510 - 0.305217I$ $a = 1.072310 - 0.133945I$ $b = 2.69315 - 0.17757I$ $c = -0.777654 - 0.758804I$ $d = -0.87546 - 2.59578I$	$-4.74548 - 5.93381I$	$-5.07129 + 5.57342I$
$u = -1.42975 + 0.19774I$ $a = -0.527124 + 0.570614I$ $b = -0.714333 - 0.280041I$ $c = 0.985847 - 0.867635I$ $d = 1.15748 - 0.96588I$	$-5.91128 + 1.72117I$	$-6.79419 + 0.I$
$u = -1.42975 - 0.19774I$ $a = -0.527124 - 0.570614I$ $b = -0.714333 + 0.280041I$ $c = 0.985847 + 0.867635I$ $d = 1.15748 + 0.96588I$	$-5.91128 - 1.72117I$	$-6.79419 + 0.I$
$u = -0.01170 + 1.48787I$ $a = -0.004491 - 1.046020I$ $b = -0.003311 + 0.582025I$ $c = -0.374959 - 0.326873I$ $d = 1.076620 - 0.549413I$	$-8.14593 - 1.35024I$	0
$u = -0.01170 - 1.48787I$ $a = -0.004491 + 1.046020I$ $b = -0.003311 - 0.582025I$ $c = -0.374959 + 0.326873I$ $d = 1.076620 + 0.549413I$	$-8.14593 + 1.35024I$	0

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.509235$ $a = -1.62785$ $b = -0.278429$ $c = 1.42620$ $d = 0.0709079$	-1.19981	-8.75910
$u = -1.38697 + 0.55724I$ $a = -0.508516 + 0.527555I$ $b = -0.834857 - 0.205621I$ $c = 1.10528 - 1.01088I$ $d = 1.36984 - 1.26145I$	$-4.40802 + 10.56830I$	0
$u = -1.38697 - 0.55724I$ $a = -0.508516 - 0.527555I$ $b = -0.834857 + 0.205621I$ $c = 1.10528 + 1.01088I$ $d = 1.36984 + 1.26145I$	$-4.40802 - 10.56830I$	0
$u = 0.40359 + 1.45989I$ $a = 0.149185 - 1.016750I$ $b = 0.114536 + 0.582400I$ $c = -0.560529 - 0.949843I$ $d = 1.124480 - 0.685590I$	$-7.37650 + 7.69255I$	0
$u = 0.40359 - 1.45989I$ $a = 0.149185 + 1.016750I$ $b = 0.114536 - 0.582400I$ $c = -0.560529 + 0.949843I$ $d = 1.124480 + 0.685590I$	$-7.37650 - 7.69255I$	0
$u = -1.43182 + 0.71566I$ $a = 0.954104 + 0.236457I$ $b = 2.50037 + 0.27104I$ $c = -1.42231 + 0.42095I$ $d = -2.09633 + 2.01103I$	$-7.91018 + 10.04820I$	0

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.43182 - 0.71566I$ $a = 0.954104 - 0.236457I$ $b = 2.50037 - 0.27104I$ $c = -1.42231 - 0.42095I$ $d = -2.09633 - 2.01103I$	$-7.91018 - 10.04820I$	0
$u = 1.55076 + 0.46120I$ $a = -0.979860 + 0.150029I$ $b = -2.56948 + 0.17354I$ $c = 0.0100774 + 0.0710674I$ $d = -0.347517 - 0.964881I$	$-10.01530 - 3.44751I$	0
$u = 1.55076 - 0.46120I$ $a = -0.979860 - 0.150029I$ $b = -2.56948 - 0.17354I$ $c = 0.0100774 - 0.0710674I$ $d = -0.347517 + 0.964881I$	$-10.01530 + 3.44751I$	0
$u = 1.43192 + 0.83141I$ $a = -0.924993 + 0.257013I$ $b = -2.45089 + 0.28141I$ $c = 1.54648 + 0.31162I$ $d = 2.32957 + 1.80759I$	$-10.6565 - 15.7212I$	0
$u = 1.43192 - 0.83141I$ $a = -0.924993 - 0.257013I$ $b = -2.45089 - 0.28141I$ $c = 1.54648 - 0.31162I$ $d = 2.32957 - 1.80759I$	$-10.6565 + 15.7212I$	0
$u = -1.59024 + 0.63743I$ $a = 0.938344 + 0.185530I$ $b = 2.50574 + 0.19991I$ $c = 0.028561 + 0.229108I$ $d = 0.361646 - 0.685663I$	$-13.2358 + 8.9369I$	0

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.59024 - 0.63743I$ $a = 0.938344 - 0.185530I$ $b = 2.50574 - 0.19991I$ $c = 0.028561 - 0.229108I$ $d = 0.361646 + 0.685663I$	$-13.2358 - 8.9369I$	0
$u = 1.61640 + 0.61957I$ $a = -0.936055 + 0.176897I$ $b = -2.50694 + 0.18872I$ $c = 1.188010 + 0.269021I$ $d = 1.66723 + 1.72517I$	$-13.4084 - 6.2441I$	0
$u = 1.61640 - 0.61957I$ $a = -0.936055 - 0.176897I$ $b = -2.50694 - 0.18872I$ $c = 1.188010 - 0.269021I$ $d = 1.66723 - 1.72517I$	$-13.4084 + 6.2441I$	0
$u = -1.74703 + 0.30124I$ $a = 0.947443 + 0.082473I$ $b = 2.55085 + 0.08714I$ $c = -0.250062 + 0.065643I$ $d = -0.059801 - 1.037630I$	$-14.9547 - 0.9173I$	0
$u = -1.74703 - 0.30124I$ $a = 0.947443 - 0.082473I$ $b = 2.55085 - 0.08714I$ $c = -0.250062 - 0.065643I$ $d = -0.059801 + 1.037630I$	$-14.9547 + 0.9173I$	0

$$\text{II. } I_2^u = \langle a^2u + d - a, a^2u + c, a^2u + b - a, -u^4a - u^4 + \dots + a^3 - 1, u^5 - u^4 - 2u^3 + u^2 + u + 1 \rangle$$

(i) Arc colorings

$$a_4 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} a \\ -a^2u + a \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -a^2u \\ -a^2u + a \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -a^2u \\ -a^2u + a \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_6 = \begin{pmatrix} u \\ u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -u^2 + 1 \\ -u^2 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -u^4 + u^2 + 1 \\ -u^4 - u^3 + u^2 + 2u + 1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} u \\ u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -a^2u \\ -u^3a^2 - a^2u + a \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes =  $4u^3 - 8u - 6$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1$	$(u^5 + 3u^4 + 4u^3 + u^2 - u - 1)^3$
$c_2, c_5$	$(u^5 + u^4 + 2u^3 + u^2 + u + 1)^3$
$c_3, c_4, c_8$	$(u^5 - u^4 - 2u^3 + u^2 + u + 1)^3$
$c_6, c_7, c_9$ $c_{12}$	$u^{15} - 5u^{13} + \dots + u - 1$
$c_{10}$	$u^{15} + 10u^{14} + \dots - 5u + 1$
$c_{11}$	$u^{15} - 10u^{14} + \dots - 5u - 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1$	$(y^5 - y^4 + 8y^3 - 3y^2 + 3y - 1)^3$
$c_2, c_5$	$(y^5 + 3y^4 + 4y^3 + y^2 - y - 1)^3$
$c_3, c_4, c_8$	$(y^5 - 5y^4 + 8y^3 - 3y^2 - y - 1)^3$
$c_6, c_7, c_9$ $c_{12}$	$y^{15} - 10y^{14} + \dots - 5y - 1$
$c_{10}, c_{11}$	$y^{15} - 10y^{14} + \dots - 25y - 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.21774$ $a = -0.586248 + 0.597241I$ $b = -0.602091 - 0.255494I$ $c = -0.015843 - 0.852735I$ $d = -0.602091 - 0.255494I$	-2.40108	-3.48110
$u = -1.21774$ $a = -0.586248 - 0.597241I$ $b = -0.602091 + 0.255494I$ $c = -0.015843 + 0.852735I$ $d = -0.602091 + 0.255494I$	-2.40108	-3.48110
$u = -1.21774$ $a = 1.17250$ $b = 2.84657$ $c = 1.67408$ $d = 2.84657$	-2.40108	-3.48110
$u = -0.309916 + 0.549911I$ $a = -0.331889 + 0.475420I$ $b = -0.541336 + 0.441339I$ $c = -0.209448 - 0.034081I$ $d = -0.541336 + 0.441339I$	$-0.32910 + 1.53058I$	$-2.51511 - 4.43065I$
$u = -0.309916 + 0.549911I$ $a = 1.02081 + 1.15644I$ $b = 2.22763 + 2.05055I$ $c = 1.20682 + 0.89411I$ $d = 2.22763 + 2.05055I$	$-0.32910 + 1.53058I$	$-2.51511 - 4.43065I$
$u = -0.309916 + 0.549911I$ $a = -0.68892 - 1.63186I$ $b = -0.130685 + 0.268368I$ $c = 0.55823 + 1.90023I$ $d = -0.130685 + 0.268368I$	$-0.32910 + 1.53058I$	$-2.51511 - 4.43065I$



Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.309916 - 0.549911I$ $a = -0.331889 - 0.475420I$ $b = -0.541336 - 0.441339I$ $c = -0.209448 + 0.034081I$ $d = -0.541336 - 0.441339I$	$-0.32910 - 1.53058I$	$-2.51511 + 4.43065I$
$u = -0.309916 - 0.549911I$ $a = 1.02081 - 1.15644I$ $b = 2.22763 - 2.05055I$ $c = 1.20682 - 0.89411I$ $d = 2.22763 - 2.05055I$	$-0.32910 - 1.53058I$	$-2.51511 + 4.43065I$
$u = -0.309916 - 0.549911I$ $a = -0.68892 + 1.63186I$ $b = -0.130685 - 0.268368I$ $c = 0.55823 - 1.90023I$ $d = -0.130685 - 0.268368I$	$-0.32910 - 1.53058I$	$-2.51511 + 4.43065I$
$u = 1.41878 + 0.21917I$ $a = -1.060130 + 0.090162I$ $b = -2.68504 + 0.11685I$ $c = -1.62491 + 0.02669I$ $d = -2.68504 + 0.11685I$	$-5.87256 - 4.40083I$	$-6.74431 + 3.49859I$
$u = 1.41878 + 0.21917I$ $a = 0.532546 - 0.656825I$ $b = 0.588938 + 0.368121I$ $c = 0.056392 + 1.024950I$ $d = 0.588938 + 0.368121I$	$-5.87256 - 4.40083I$	$-6.74431 + 3.49859I$
$u = 1.41878 + 0.21917I$ $a = 0.527587 + 0.566662I$ $b = 0.719297 - 0.272295I$ $c = 0.191710 - 0.838957I$ $d = 0.719297 - 0.272295I$	$-5.87256 - 4.40083I$	$-6.74431 + 3.49859I$

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.41878 - 0.21917I$ $a = -1.060130 - 0.090162I$ $b = -2.68504 - 0.11685I$ $c = -1.62491 - 0.02669I$ $d = -2.68504 - 0.11685I$	$-5.87256 + 4.40083I$	$-6.74431 - 3.49859I$
$u = 1.41878 - 0.21917I$ $a = 0.532546 + 0.656825I$ $b = 0.588938 - 0.368121I$ $c = 0.056392 - 1.024950I$ $d = 0.588938 - 0.368121I$	$-5.87256 + 4.40083I$	$-6.74431 - 3.49859I$
$u = 1.41878 - 0.21917I$ $a = 0.527587 - 0.566662I$ $b = 0.719297 + 0.272295I$ $c = 0.191710 + 0.838957I$ $d = 0.719297 + 0.272295I$	$-5.87256 + 4.40083I$	$-6.74431 - 3.49859I$

$$\text{III. } I_1^v = \langle c, d - v + 1, b, a - v, v^2 - v + 1 \rangle$$

(i) Arc colorings

$$a_4 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} v \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} v \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} v \\ 0 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 0 \\ v - 1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -v \\ v - 1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} v \\ -v + 1 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 0 \\ v \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -v \\ v \end{pmatrix}$$

$$a_8 = \begin{pmatrix} v \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} v \\ 0 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes =  $-4v + 5$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_3, c_5$	$u^2 - u + 1$
$c_2$	$u^2 + u + 1$
$c_4, c_7, c_8$ $c_9, c_{10}$	$u^2$
$c_6, c_{11}$	$(u + 1)^2$
$c_{12}$	$(u - 1)^2$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_3$ $c_5$	$y^2 + y + 1$
$c_4, c_7, c_8$ $c_9, c_{10}$	$y^2$
$c_6, c_{11}, c_{12}$	$(y - 1)^2$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^v$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$v = 0.500000 + 0.866025I$ $a = 0.500000 + 0.866025I$ $b = 0$ $c = 0$ $d = -0.500000 + 0.866025I$	$1.64493 + 2.02988I$	$3.00000 - 3.46410I$
$v = 0.500000 - 0.866025I$ $a = 0.500000 - 0.866025I$ $b = 0$ $c = 0$ $d = -0.500000 - 0.866025I$	$1.64493 - 2.02988I$	$3.00000 + 3.46410I$

$$\text{IV. } I_2^v = \langle a, d + v + 1, c + a, b - v - 1, v^2 + v + 1 \rangle$$

(i) Arc colorings

$$a_4 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} v \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 0 \\ v + 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} v \\ -v - 1 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 0 \\ -v - 1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 0 \\ -v - 1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 0 \\ v + 1 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 1 \\ -v \end{pmatrix}$$

$$a_2 = \begin{pmatrix} v + 1 \\ -v \end{pmatrix}$$

$$a_8 = \begin{pmatrix} v \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0 \\ -v - 1 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes =  $4v - 7$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_3, c_5$	$u^2 - u + 1$
$c_2$	$u^2 + u + 1$
$c_4, c_6, c_8$ $c_{11}, c_{12}$	$u^2$
$c_7$	$(u - 1)^2$
$c_9, c_{10}$	$(u + 1)^2$



(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_3$ $c_5$	$y^2 + y + 1$
$c_4, c_6, c_8$ $c_{11}, c_{12}$	$y^2$
$c_7, c_9, c_{10}$	$(y - 1)^2$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_2^v$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$v = -0.500000 + 0.866025I$		
$a = 0$		
$b = 0.500000 + 0.866025I$	$-1.64493 - 2.02988I$	$-9.00000 + 3.46410I$
$c = 0$		
$d = -0.500000 - 0.866025I$		
$v = -0.500000 - 0.866025I$		
$a = 0$		
$b = 0.500000 - 0.866025I$	$-1.64493 + 2.02988I$	$-9.00000 - 3.46410I$
$c = 0$		
$d = -0.500000 + 0.866025I$		

$$\mathbf{V. } I_3^v = \langle a, d - 1, c + a - 1, b + 1, v - 1 \rangle$$

**(i) Arc colorings**

$$a_4 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

**(ii) Obstruction class = 1**

**(iii) Cusp Shapes = 0**

(iv) **u**-Polynomials at the component

Crossings	<b>u</b> -Polynomials at each crossing
$c_1, c_2, c_3$ $c_4, c_5, c_8$	$u$
$c_6, c_7$	$u - 1$
$c_9, c_{10}, c_{11}$ $c_{12}$	$u + 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_3$ $c_4, c_5, c_8$	$y$
$c_6, c_7, c_9$ $c_{10}, c_{11}, c_{12}$	$y - 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_3^v$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$v = 1.00000$		
$a = 0$		
$b = -1.00000$	0	0
$c = 1.00000$		
$d = 1.00000$		

$$\text{VI. } I_4^v = \langle a, d^2 + 2db + \cdots + b + 1, -dv - av + \cdots + a + 2, da - cb - 1, a^2v^2 + v^2a + \cdots + 2ca + a^2, bv + 1 \rangle$$

**(i) Arc colorings**

$$a_4 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} v \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 0 \\ b \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} v \\ -b \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} v \\ d \end{pmatrix}$$

$$a_1 = \begin{pmatrix} v \\ d + b \end{pmatrix}$$

$$a_6 = \begin{pmatrix} v \\ d + b \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -dv + 2 \\ d + b + 1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -dv - d - b + 1 \\ d + b + 1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} v \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0 \\ -b \end{pmatrix}$$

**(ii) Obstruction class = -1**

**(iii) Cusp Shapes =  $b^2 + v^2 - 4d - 4b - 4$**

**(iv) u-Polynomials at the component :** It cannot be defined for a positive dimension component.

**(v) Riley Polynomials at the component :** It cannot be defined for a positive dimension component.

(iv) Complex Volumes and Cusp Shapes

Solution to $I_4^v$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$v = \dots$		
$a = \dots$		
$b = \dots$	$-2.02988I$	$-1.30108 + 3.68445I$
$c = \dots$		
$d = \dots$		



## VII. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1$	$u(u^2 - u + 1)^2(u^5 + 3u^4 + 4u^3 + u^2 - u - 1)^3 \cdot (u^{47} + 24u^{46} + \dots + 216u - 16)$
$c_2$	$u(u^2 + u + 1)^2(u^5 + u^4 + 2u^3 + u^2 + u + 1)^3 \cdot (u^{47} + 2u^{46} + \dots + 16u + 4)$
$c_3$	$u(u^2 - u + 1)^2(u^5 - u^4 - 2u^3 + u^2 + u + 1)^3 \cdot (u^{47} - 2u^{46} + \dots - 21456u + 2592)$
$c_4, c_8$	$u^5(u^5 - u^4 + \dots + u + 1)^3(u^{47} + 2u^{46} + \dots + 1024u + 512)$
$c_5$	$u(u^2 - u + 1)^2(u^5 + u^4 + 2u^3 + u^2 + u + 1)^3 \cdot (u^{47} + 2u^{46} + \dots + 16u + 4)$
$c_6$	$u^2(u - 1)(u + 1)^2(u^{15} - 5u^{13} + \dots + u - 1)(u^{47} + 8u^{46} + \dots + 56u + 16)$
$c_7$	$u^2(u - 1)^3(u^{15} - 5u^{13} + \dots + u - 1)(u^{47} - 8u^{46} + \dots + 56u + 16)$
$c_9$	$u^2(u + 1)^3(u^{15} - 5u^{13} + \dots + u - 1)(u^{47} - 8u^{46} + \dots + 56u + 16)$
$c_{10}$	$u^2(u + 1)^3(u^{15} + 10u^{14} + \dots - 5u + 1) \cdot (u^{47} + 54u^{46} + \dots + 544u + 256)$
$c_{11}$	$u^2(u + 1)^3(u^{15} - 10u^{14} + \dots - 5u - 1) \cdot (u^{47} - 14u^{46} + \dots + 6688u - 256)$
$c_{12}$	$u^2(u - 1)^2(u + 1)(u^{15} - 5u^{13} + \dots + u - 1)(u^{47} + 8u^{46} + \dots + 56u + 16)$

### VIII. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1$	$y(y^2 + y + 1)^2(y^5 - y^4 + 8y^3 - 3y^2 + 3y - 1)^3$ $\cdot (y^{47} + 48y^{45} + \dots + 67872y - 256)$
$c_2, c_5$	$y(y^2 + y + 1)^2(y^5 + 3y^4 + 4y^3 + y^2 - y - 1)^3$ $\cdot (y^{47} + 24y^{46} + \dots + 216y - 16)$
$c_3$	$y(y^2 + y + 1)^2(y^5 - 5y^4 + 8y^3 - 3y^2 - y - 1)^3$ $\cdot (y^{47} - 24y^{46} + \dots + 353776896y - 6718464)$
$c_4, c_8$	$y^5(y^5 - 5y^4 + 8y^3 - 3y^2 - y - 1)^3$ $\cdot (y^{47} - 30y^{46} + \dots + 1572864y - 262144)$
$c_6, c_{12}$	$y^2(y - 1)^3(y^{15} - 10y^{14} + \dots - 5y - 1)$ $\cdot (y^{47} - 14y^{46} + \dots + 6688y - 256)$
$c_7, c_9$	$y^2(y - 1)^3(y^{15} - 10y^{14} + \dots - 5y - 1)$ $\cdot (y^{47} - 54y^{46} + \dots + 544y - 256)$
$c_{10}$	$y^2(y - 1)^3(y^{15} - 10y^{14} + \dots - 25y - 1)$ $\cdot (y^{47} - 114y^{46} + \dots - 1990144y - 65536)$
$c_{11}$	$y^2(y - 1)^3(y^{15} - 10y^{14} + \dots - 25y - 1)$ $\cdot (y^{47} + 46y^{46} + \dots + 11182592y - 65536)$