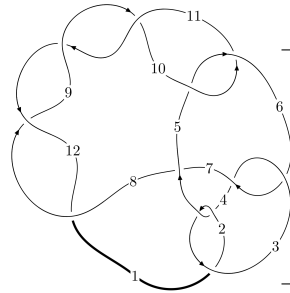
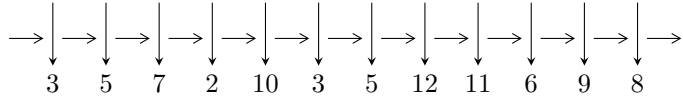


12n₀₀₇₇ (K12n₀₀₇₇)



A knot diagram¹

Linearized knot diagram



Solving Sequence

$$5,10 \xrightarrow{c_5} 3,6 \xrightarrow{c_6} 7 \xrightarrow{c_7} 8 \xrightarrow{c_{10}} 11 \xrightarrow{c_2} 2 \xrightarrow{c_1} 1 \xrightarrow{c_4} 4 \xrightarrow{c_9} 9 \xrightarrow{c_{12}} 12 \Rightarrow c_3, c_8, c_{11}$$

Ideals for irreducible components² of X_{par}

$$I_1^u = \langle u^{25} - u^{24} + \dots + b + 1, u^{22} - 3u^{20} + \dots + a + 4u, u^{26} - 2u^{25} + \dots - 2u - 1 \rangle$$

$$I_2^u = \langle b + 1, u^4 - u^2 + a + u + 2, u^5 - u^4 + u^2 + u - 1 \rangle$$

* 2 irreducible components of $\dim_{\mathbb{C}} = 0$, with total 31 representations.

¹The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

²All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$I_1^u = \langle u^{25} - u^{24} + \dots + b + 1, u^{22} - 3u^{20} + \dots + a + 4u, u^{26} - 2u^{25} + \dots - 2u - 1 \rangle \quad \text{I.}$$

(i) Arc colorings

$$a_5 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -u^{22} + 3u^{20} + \dots - 4u^2 - 4u \\ -u^{25} + u^{24} + \dots - u - 1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -u^9 - 3u^5 - u \\ -u^9 + u^7 - 3u^5 + 2u^3 - u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -u^7 - 2u^3 \\ -u^9 + u^7 - 3u^5 + 2u^3 - u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -u \\ -u^3 + u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -u^{25} + u^{24} + \dots - 5u - 1 \\ -u^{25} + u^{24} + \dots - u - 1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -u^9 - 3u^5 - u \\ -u^{11} + u^9 - 4u^7 + 3u^5 - 3u^3 + u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -2u^{25} + 2u^{24} + \dots - 7u - 1 \\ -u^{25} + u^{24} + \dots - 2u - 1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} u^3 \\ u^5 - u^3 + u \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -u^5 - u \\ -u^7 + u^5 - 2u^3 + u \end{pmatrix}$$

(ii) Obstruction class = -1

$$\begin{aligned} \text{(iii) Cusp Shapes} &= -2u^{25} + u^{24} + 8u^{23} - 10u^{22} - 26u^{21} + 30u^{20} + 57u^{19} - 86u^{18} - \\ &103u^{17} + 156u^{16} + 148u^{15} - 242u^{14} - 181u^{13} + 278u^{12} + 205u^{11} - 248u^{10} - 197u^9 + \\ &159u^8 + 194u^7 - 60u^6 - 148u^5 + 8u^4 + 77u^3 + 10u^2 - 19u - 20 \end{aligned}$$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1	$u^{26} + 34u^{25} + \dots + 68u + 1$
c_2, c_4	$u^{26} - 6u^{25} + \dots + 34u^2 - 1$
c_3, c_6	$u^{26} + u^{25} + \dots + 96u + 32$
c_5, c_{10}	$u^{26} - 2u^{25} + \dots - 2u - 1$
c_7	$u^{26} - 2u^{25} + \dots - 2u - 1$
c_8, c_9, c_{11} c_{12}	$u^{26} + 6u^{25} + \dots + 10u + 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1	$y^{26} - 78y^{25} + \dots - 1224y + 1$
c_2, c_4	$y^{26} - 34y^{25} + \dots - 68y + 1$
c_3, c_6	$y^{26} - 33y^{25} + \dots - 1536y + 1024$
c_5, c_{10}	$y^{26} - 6y^{25} + \dots - 10y + 1$
c_7	$y^{26} - 54y^{25} + \dots - 10y + 1$
c_8, c_9, c_{11} c_{12}	$y^{26} + 30y^{25} + \dots + 18y + 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.03768$ $a = 3.52363$ $b = 1.79564$	-14.3257	-18.8510
$u = -0.848363 + 0.365549I$ $a = -1.78442 - 1.39985I$ $b = -0.876527 + 0.552462I$	$-2.09559 + 3.16364I$	$-16.0021 - 6.5670I$
$u = -0.848363 - 0.365549I$ $a = -1.78442 + 1.39985I$ $b = -0.876527 - 0.552462I$	$-2.09559 - 3.16364I$	$-16.0021 + 6.5670I$
$u = 0.743105 + 0.536823I$ $a = 0.594036 - 0.232636I$ $b = 0.265907 - 0.097994I$	$1.42344 - 2.05884I$	$-4.65256 + 4.58362I$
$u = 0.743105 - 0.536823I$ $a = 0.594036 + 0.232636I$ $b = 0.265907 + 0.097994I$	$1.42344 + 2.05884I$	$-4.65256 - 4.58362I$
$u = -1.016900 + 0.465737I$ $a = 2.21366 + 1.97366I$ $b = 1.76028 - 0.15334I$	$-11.56550 + 6.15142I$	$-15.5995 - 5.2395I$
$u = -1.016900 - 0.465737I$ $a = 2.21366 - 1.97366I$ $b = 1.76028 + 0.15334I$	$-11.56550 - 6.15142I$	$-15.5995 + 5.2395I$
$u = -0.340992 + 0.772246I$ $a = 0.190362 - 0.001300I$ $b = 1.70063 + 0.08748I$	$-9.33177 - 1.67049I$	$-11.65109 + 0.28027I$
$u = -0.340992 - 0.772246I$ $a = 0.190362 + 0.001300I$ $b = 1.70063 - 0.08748I$	$-9.33177 + 1.67049I$	$-11.65109 - 0.28027I$
$u = 0.780793 + 0.228604I$ $a = -2.51035 + 0.76802I$ $b = -1.168300 + 0.232886I$	$-2.90735 - 0.78726I$	$-17.0746 + 5.9643I$

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.780793 - 0.228604I$ $a = -2.51035 - 0.76802I$ $b = -1.168300 - 0.232886I$	$-2.90735 + 0.78726I$	$-17.0746 - 5.9643I$
$u = -0.901624 + 0.824241I$ $a = -0.978749 - 0.966956I$ $b = -1.49560 - 0.03445I$	$3.16228 + 3.07757I$	$-10.53156 - 2.75315I$
$u = -0.901624 - 0.824241I$ $a = -0.978749 + 0.966956I$ $b = -1.49560 + 0.03445I$	$3.16228 - 3.07757I$	$-10.53156 + 2.75315I$
$u = 0.875285 + 0.858337I$ $a = 0.452866 - 0.465694I$ $b = -0.617869 + 0.854688I$	$5.39540 - 0.25204I$	$-9.68980 - 0.25577I$
$u = 0.875285 - 0.858337I$ $a = 0.452866 + 0.465694I$ $b = -0.617869 - 0.854688I$	$5.39540 + 0.25204I$	$-9.68980 + 0.25577I$
$u = 0.840955 + 0.925824I$ $a = 0.193479 + 0.004136I$ $b = 1.65874 - 0.26853I$	$-2.27912 + 3.95861I$	$-11.45131 - 0.83940I$
$u = 0.840955 - 0.925824I$ $a = 0.193479 - 0.004136I$ $b = 1.65874 + 0.26853I$	$-2.27912 - 3.95861I$	$-11.45131 + 0.83940I$
$u = 0.939409 + 0.834109I$ $a = -0.76938 + 1.23390I$ $b = -0.687301 - 0.869387I$	$5.19384 - 6.03805I$	$-10.26289 + 5.25215I$
$u = 0.939409 - 0.834109I$ $a = -0.76938 - 1.23390I$ $b = -0.687301 + 0.869387I$	$5.19384 + 6.03805I$	$-10.26289 - 5.25215I$
$u = -0.931297 + 0.895111I$ $a = 0.372833 + 0.308620I$ $b = 0.537292 + 0.017409I$	$10.10520 + 3.30342I$	$-2.39471 - 2.26919I$

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.931297 - 0.895111I$		
$a = 0.372833 - 0.308620I$	$10.10520 - 3.30342I$	$-2.39471 + 2.26919I$
$b = 0.537292 - 0.017409I$		
$u = 0.998011 + 0.849444I$		
$a = 0.83951 - 1.88704I$	$-2.78496 - 10.50130I$	$-12.09690 + 5.41863I$
$b = 1.68410 + 0.28961I$		
$u = 0.998011 - 0.849444I$		
$a = 0.83951 + 1.88704I$	$-2.78496 + 10.50130I$	$-12.09690 - 5.41863I$
$b = 1.68410 - 0.28961I$		
$u = -0.527536$		
$a = 0.849795$	-0.708379	-14.2100
$b = -0.171524$		
$u = -0.393456 + 0.342390I$		
$a = 0.999444 + 0.387392I$	$-0.780751 - 0.150062I$	$-11.06268 - 0.12594I$
$b = -0.573413 - 0.271251I$		
$u = -0.393456 - 0.342390I$		
$a = 0.999444 - 0.387392I$	$-0.780751 + 0.150062I$	$-11.06268 + 0.12594I$
$b = -0.573413 + 0.271251I$		

$$\text{II. } I_2^u = \langle b + 1, u^4 - u^2 + a + u + 2, u^5 - u^4 + u^2 + u - 1 \rangle$$

(i) Arc colorings

$$a_5 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -u^4 + u^2 - u - 2 \\ -1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -u^2 + 1 \\ u^2 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -u \\ -u^3 + u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -u^4 + u^2 - u - 3 \\ -1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -u^4 + u^2 - u - 2 \\ -1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} u^3 \\ u^4 - u^3 - u^2 + 1 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -u^4 + u^2 - 1 \\ u^4 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = $-u^3 + 3u^2 - u - 14$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1, c_2	$(u - 1)^5$
c_3, c_6	u^5
c_4	$(u + 1)^5$
c_5	$u^5 - u^4 + u^2 + u - 1$
c_7, c_{11}, c_{12}	$u^5 + u^4 + 4u^3 + 3u^2 + 3u + 1$
c_8, c_9	$u^5 - u^4 + 4u^3 - 3u^2 + 3u - 1$
c_{10}	$u^5 + u^4 - u^2 + u + 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1, c_2, c_4	$(y - 1)^5$
c_3, c_6	y^5
c_5, c_{10}	$y^5 - y^4 + 4y^3 - 3y^2 + 3y - 1$
c_7, c_8, c_9 c_{11}, c_{12}	$y^5 + 7y^4 + 16y^3 + 13y^2 + 3y - 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to I_2^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.758138 + 0.584034I$ $a = -0.278580 - 1.055720I$ $b = -1.00000$	$0.17487 + 2.21397I$	$-12.88087 - 4.04855I$
$u = -0.758138 - 0.584034I$ $a = -0.278580 + 1.055720I$ $b = -1.00000$	$0.17487 - 2.21397I$	$-12.88087 + 4.04855I$
$u = 0.935538 + 0.903908I$ $a = -0.020316 + 0.590570I$ $b = -1.00000$	$9.31336 - 3.33174I$	$-13.28666 + 2.53508I$
$u = 0.935538 - 0.903908I$ $a = -0.020316 - 0.590570I$ $b = -1.00000$	$9.31336 + 3.33174I$	$-13.28666 - 2.53508I$
$u = 0.645200$ $a = -2.40221$ $b = -1.00000$	-2.52712	-13.6650

III. u-Polynomials

Crossings	u-Polynomials at each crossing
c_1	$((u-1)^5)(u^{26} + 34u^{25} + \dots + 68u + 1)$
c_2	$((u-1)^5)(u^{26} - 6u^{25} + \dots + 34u^2 - 1)$
c_3, c_6	$u^5(u^{26} + u^{25} + \dots + 96u + 32)$
c_4	$((u+1)^5)(u^{26} - 6u^{25} + \dots + 34u^2 - 1)$
c_5	$(u^5 - u^4 + u^2 + u - 1)(u^{26} - 2u^{25} + \dots - 2u - 1)$
c_7	$(u^5 + u^4 + 4u^3 + 3u^2 + 3u + 1)(u^{26} - 2u^{25} + \dots - 2u - 1)$
c_8, c_9	$(u^5 - u^4 + 4u^3 - 3u^2 + 3u - 1)(u^{26} + 6u^{25} + \dots + 10u + 1)$
c_{10}	$(u^5 + u^4 - u^2 + u + 1)(u^{26} - 2u^{25} + \dots - 2u - 1)$
c_{11}, c_{12}	$(u^5 + u^4 + 4u^3 + 3u^2 + 3u + 1)(u^{26} + 6u^{25} + \dots + 10u + 1)$

IV. Riley Polynomials

Crossings	Riley Polynomials at each crossing
c_1	$((y - 1)^5)(y^{26} - 78y^{25} + \dots - 1224y + 1)$
c_2, c_4	$((y - 1)^5)(y^{26} - 34y^{25} + \dots - 68y + 1)$
c_3, c_6	$y^5(y^{26} - 33y^{25} + \dots - 1536y + 1024)$
c_5, c_{10}	$(y^5 - y^4 + 4y^3 - 3y^2 + 3y - 1)(y^{26} - 6y^{25} + \dots - 10y + 1)$
c_7	$(y^5 + 7y^4 + 16y^3 + 13y^2 + 3y - 1)(y^{26} - 54y^{25} + \dots - 10y + 1)$
c_8, c_9, c_{11} c_{12}	$(y^5 + 7y^4 + 16y^3 + 13y^2 + 3y - 1)(y^{26} + 30y^{25} + \dots + 18y + 1)$