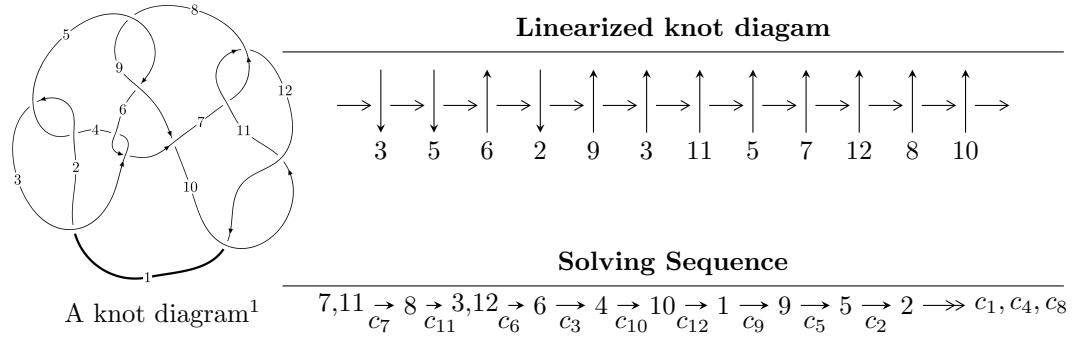


$12n_{0080}$  ( $K12n_{0080}$ )



### Ideals for irreducible components<sup>2</sup> of $X_{\text{par}}$

$$\begin{aligned}
 I_1^u &= \langle 11188446734u^{40} + 14624888210u^{39} + \dots + 38482965369b - 18882609362, \\
 &\quad - 471858393299u^{40} - 603105686012u^{39} + \dots + 38482965369a + 737953573358, \\
 &\quad u^{41} + 2u^{40} + \dots - u - 1 \rangle \\
 I_2^u &= \langle b, 3u^7 + u^6 - 4u^5 - 4u^4 + 5u^3 + 3u^2 + a - u - 5, u^8 + u^7 - u^6 - 2u^5 + u^4 + 2u^3 - 2u - 1 \rangle
 \end{aligned}$$

\* 2 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 49 representations.

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<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/math/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

**I.**

$$I_1^u = \langle 1.12 \times 10^{10} u^{40} + 1.46 \times 10^{10} u^{39} + \dots + 3.85 \times 10^{10} b - 1.89 \times 10^{10}, -4.72 \times 10^{11} u^{40} - 6.03 \times 10^{11} u^{39} + \dots + 3.85 \times 10^{10} a + 7.38 \times 10^{11}, u^{41} + 2u^{40} + \dots - u - 1 \rangle$$

(i) **Arc colorings**

$$a_7 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 12.2615u^{40} + 15.6720u^{39} + \dots + 6.84293u - 19.1761 \\ -0.290738u^{40} - 0.380035u^{39} + \dots + 1.44537u + 0.490674 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} u \\ -u^3 + u \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -3.45682u^{40} - 4.64440u^{39} + \dots - 4.50872u + 4.12223 \\ 0.869179u^{40} + 1.73038u^{39} + \dots - 0.134593u - 0.868998 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 9.93735u^{40} + 13.3319u^{39} + \dots + 8.96828u - 18.9057 \\ 2.61664u^{40} + 5.42032u^{39} + \dots - 0.00831753u - 2.41607 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -u^3 \\ u^5 - u^3 + u \end{pmatrix}$$

$$a_1 = \begin{pmatrix} u^5 + u \\ -u^7 + u^5 - 2u^3 + u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -u^5 - u \\ u^5 - u^3 + u \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -2.06817u^{40} - 2.86404u^{39} + \dots - 3.90693u + 2.53206 \\ -0.127787u^{40} + 0.140106u^{39} + \dots - 0.336106u + 0.527977 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 10.3978u^{40} + 13.4001u^{39} + \dots + 5.65679u - 18.2402 \\ 0.964836u^{40} + 2.33975u^{39} + \dots + 1.11758u - 0.565279 \end{pmatrix}$$

(ii) **Obstruction class = -1**

(iii) **Cusp Shapes**

$$= \frac{1507194298715}{12827655123} u^{40} + \frac{1944574441589}{12827655123} u^{39} + \dots + \frac{274922951097}{4275885041} u - \frac{2104450199471}{12827655123}$$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1$	$u^{41} + 53u^{40} + \cdots + 381u + 1$
$c_2, c_4$	$u^{41} - 9u^{40} + \cdots - 29u + 1$
$c_3, c_6$	$u^{41} + 7u^{40} + \cdots + 2176u - 256$
$c_5, c_8$	$u^{41} - 2u^{40} + \cdots + u - 1$
$c_7, c_{11}$	$u^{41} - 2u^{40} + \cdots - u + 1$
$c_9$	$u^{41} + 2u^{40} + \cdots + 12241u + 8353$
$c_{10}, c_{12}$	$u^{41} - 12u^{40} + \cdots + 5u - 1$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1$	$y^{41} - 121y^{40} + \cdots + 73433y - 1$
$c_2, c_4$	$y^{41} - 53y^{40} + \cdots + 381y - 1$
$c_3, c_6$	$y^{41} + 51y^{40} + \cdots + 2801664y - 65536$
$c_5, c_8$	$y^{41} + 42y^{39} + \cdots + 5y - 1$
$c_7, c_{11}$	$y^{41} - 12y^{40} + \cdots + 5y - 1$
$c_9$	$y^{41} + 36y^{40} + \cdots + 949291005y - 69772609$
$c_{10}, c_{12}$	$y^{41} + 36y^{40} + \cdots + 37y - 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.645157 + 0.706341I$		
$a = 0.129346 + 0.199509I$	$0.314025 + 0.700329I$	$9.78155 + 0.42575I$
$b = -0.707026 - 0.083217I$		
$u = -0.645157 - 0.706341I$		
$a = 0.129346 - 0.199509I$	$0.314025 - 0.700329I$	$9.78155 - 0.42575I$
$b = -0.707026 + 0.083217I$		
$u = 1.06514$		
$a = 1.21465$	5.55858	18.6510
$b = -0.619887$		
$u = 0.878483 + 0.257640I$		
$a = 1.36190 + 1.41715I$	$0.35281 + 3.72015I$	$8.01877 - 8.67695I$
$b = -0.395484 - 1.274730I$		
$u = 0.878483 - 0.257640I$		
$a = 1.36190 - 1.41715I$	$0.35281 - 3.72015I$	$8.01877 + 8.67695I$
$b = -0.395484 + 1.274730I$		
$u = 0.863822 + 0.692291I$		
$a = -0.710177 + 0.248903I$	$-2.33978 + 2.66185I$	$4.87613 - 3.55699I$
$b = 0.360833 - 0.064088I$		
$u = 0.863822 - 0.692291I$		
$a = -0.710177 - 0.248903I$	$-2.33978 - 2.66185I$	$4.87613 + 3.55699I$
$b = 0.360833 + 0.064088I$		
$u = 0.850650 + 0.773602I$		
$a = 0.65587 - 1.74300I$	$-4.76432 + 2.07222I$	$3.47881 - 9.56031I$
$b = -0.305447 - 0.669138I$		
$u = 0.850650 - 0.773602I$		
$a = 0.65587 + 1.74300I$	$-4.76432 - 2.07222I$	$3.47881 + 9.56031I$
$b = -0.305447 + 0.669138I$		
$u = 1.113340 + 0.298427I$		
$a = -2.09473 - 1.98305I$	$-6.81237 + 7.94638I$	$6.00000 - 5.66643I$
$b = 0.58426 + 1.64109I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.113340 - 0.298427I$		
$a = -2.09473 + 1.98305I$	$-6.81237 - 7.94638I$	$6.00000 + 5.66643I$
$b = 0.58426 - 1.64109I$		
$u = -1.123200 + 0.281615I$		
$a = 0.82820 - 2.54731I$	$-6.69343 + 0.45475I$	$6.00000 + 0.74518I$
$b = 0.17091 + 1.62625I$		
$u = -1.123200 - 0.281615I$		
$a = 0.82820 + 2.54731I$	$-6.69343 - 0.45475I$	$6.00000 - 0.74518I$
$b = 0.17091 - 1.62625I$		
$u = -0.821741 + 0.155454I$		
$a = -1.49310 + 0.28695I$	$0.614586 - 0.353193I$	$8.75569 + 0.62140I$
$b = 0.000254 - 0.581031I$		
$u = -0.821741 - 0.155454I$		
$a = -1.49310 - 0.28695I$	$0.614586 + 0.353193I$	$8.75569 - 0.62140I$
$u = -0.829859 + 0.817277I$		
$a = -1.080080 - 0.171992I$	$-6.22251 + 1.37166I$	$0. - 2.74151I$
$b = 0.03664 - 2.09736I$		
$u = -0.829859 - 0.817277I$		
$a = -1.080080 + 0.171992I$	$-6.22251 - 1.37166I$	$0. + 2.74151I$
$b = 0.03664 + 2.09736I$		
$u = 0.739042 + 0.910928I$		
$a = -0.097736 - 0.296625I$	$-14.7874 + 0.6933I$	$0. - 1.66266I$
$b = -0.10739 + 1.92349I$		
$u = 0.739042 - 0.910928I$		
$a = -0.097736 + 0.296625I$	$-14.7874 - 0.6933I$	$0. + 1.66266I$
$b = -0.10739 - 1.92349I$		
$u = -0.746747 + 0.906172I$		
$a = -0.099105 - 0.285226I$	$-14.9445 + 7.5314I$	$0. - 2.54363I$
$b = 0.82858 + 1.91790I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.746747 - 0.906172I$		
$a = -0.099105 + 0.285226I$	$-14.9445 - 7.5314I$	$0. + 2.54363I$
$b = 0.82858 - 1.91790I$		
$u = 0.010347 + 0.818382I$		
$a = -0.096572 + 0.286828I$	$-10.51980 - 4.16733I$	$0.66529 + 2.27689I$
$b = 0.37826 - 1.80255I$		
$u = 0.010347 - 0.818382I$		
$a = -0.096572 - 0.286828I$	$-10.51980 + 4.16733I$	$0.66529 - 2.27689I$
$b = 0.37826 + 1.80255I$		
$u = 0.913540 + 0.760932I$		
$a = -0.676289 + 1.093800I$	$-4.56999 + 3.72466I$	$3.33454 + 2.09517I$
$b = -0.209840 + 0.757944I$		
$u = 0.913540 - 0.760932I$		
$a = -0.676289 - 1.093800I$	$-4.56999 - 3.72466I$	$3.33454 - 2.09517I$
$b = -0.209840 - 0.757944I$		
$u = -0.893232 + 0.810220I$		
$a = -0.95737 - 1.53330I$	$-8.47280 - 3.03045I$	$0. + 2.81396I$
$b = 2.34407 + 0.13131I$		
$u = -0.893232 - 0.810220I$		
$a = -0.95737 + 1.53330I$	$-8.47280 + 3.03045I$	$0. - 2.81396I$
$b = 2.34407 - 0.13131I$		
$u = -1.010010 + 0.669120I$		
$a = 0.541263 + 0.790129I$	$1.39688 - 6.02924I$	$12.17156 + 3.37002I$
$b = -0.710082 - 0.023150I$		
$u = -1.010010 - 0.669120I$		
$a = 0.541263 - 0.790129I$	$1.39688 + 6.02924I$	$12.17156 - 3.37002I$
$b = -0.710082 + 0.023150I$		
$u = -0.944017 + 0.784096I$		
$a = 1.80124 - 0.03860I$	$-5.86990 - 7.37157I$	$6.00000 + 8.00321I$
$b = -0.19373 + 2.11976I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.944017 - 0.784096I$		
$a = 1.80124 + 0.03860I$	$-5.86990 + 7.37157I$	$6.00000 - 8.00321I$
$b = -0.19373 - 2.11976I$		
$u = -1.028850 + 0.790391I$		
$a = -2.50865 - 0.19833I$	$-14.0605 - 13.8029I$	0
$b = 0.91594 - 1.85439I$		
$u = -1.028850 - 0.790391I$		
$a = -2.50865 + 0.19833I$	$-14.0605 + 13.8029I$	0
$b = 0.91594 + 1.85439I$		
$u = 1.035690 + 0.788962I$		
$a = 2.07595 + 0.63512I$	$-13.8581 + 5.5876I$	0
$b = -0.21521 - 1.85036I$		
$u = 1.035690 - 0.788962I$		
$a = 2.07595 - 0.63512I$	$-13.8581 - 5.5876I$	0
$b = -0.21521 + 1.85036I$		
$u = -0.691121$		
$a = 7.56339$	$-0.704951$	91.2610
$b = -0.229386$		
$u = 0.593654 + 0.309854I$		
$a = -2.47422 + 0.91083I$	$-2.54134 + 1.31981I$	$0.58683 - 4.31452I$
$b = 1.073020 - 0.556578I$		
$u = 0.593654 - 0.309854I$		
$a = -2.47422 - 0.91083I$	$-2.54134 - 1.31981I$	$0.58683 + 4.31452I$
$b = 1.073020 + 0.556578I$		
$u = -0.530048$		
$a = -0.522918$	$0.790977$	12.7730
$b = -0.246323$		
$u = 0.122257 + 0.387519I$		
$a = -1.73330 + 0.73700I$	$-1.72184 - 1.26203I$	$-0.75083 + 2.53377I$
$b = 0.199239 + 0.977182I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.122257 - 0.387519I$		
$a = -1.73330 - 0.73700I$	$-1.72184 + 1.26203I$	$-0.75083 - 2.53377I$
$b = 0.199239 - 0.977182I$		

$$\text{II. } I_2^u = \langle b, 3u^7 + u^6 - 4u^5 - 4u^4 + 5u^3 + 3u^2 + a - u - 5, u^8 + u^7 - u^6 - 2u^5 + u^4 + 2u^3 - 2u - 1 \rangle$$

(i) **Arc colorings**

$$a_7 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -3u^7 - u^6 + 4u^5 + 4u^4 - 5u^3 - 3u^2 + u + 5 \\ 0 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} u \\ -u^3 + u \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -3u^7 - u^6 + 4u^5 + 4u^4 - 5u^3 - 3u^2 + u + 5 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -u^3 \\ u^5 - u^3 + u \end{pmatrix}$$

$$a_1 = \begin{pmatrix} u^5 + u \\ -u^7 + u^5 - 2u^3 + u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -u^5 - u \\ u^5 - u^3 + u \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -u^5 - u \\ u^7 - u^5 + 2u^3 - u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -3u^7 - u^6 + 5u^5 + 4u^4 - 5u^3 - 3u^2 + 2u + 5 \\ -u^7 + u^5 - 2u^3 + u \end{pmatrix}$$

(ii) **Obstruction class = 1**

(iii) **Cusp Shapes** =  $9u^7 + 6u^6 - 8u^5 - 14u^4 + 15u^3 + 9u^2 - 4u - 15$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_2$	$(u - 1)^8$
$c_3, c_6$	$u^8$
$c_4$	$(u + 1)^8$
$c_5$	$u^8 - u^7 - 3u^6 + 2u^5 + 3u^4 - 2u - 1$
$c_7$	$u^8 + u^7 - u^6 - 2u^5 + u^4 + 2u^3 - 2u - 1$
$c_8, c_9$	$u^8 + u^7 - 3u^6 - 2u^5 + 3u^4 + 2u - 1$
$c_{10}$	$u^8 + 3u^7 + 7u^6 + 10u^5 + 11u^4 + 10u^3 + 6u^2 + 4u + 1$
$c_{11}$	$u^8 - u^7 - u^6 + 2u^5 + u^4 - 2u^3 + 2u - 1$
$c_{12}$	$u^8 - 3u^7 + 7u^6 - 10u^5 + 11u^4 - 10u^3 + 6u^2 - 4u + 1$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_4$	$(y - 1)^8$
$c_3, c_6$	$y^8$
$c_5, c_8, c_9$	$y^8 - 7y^7 + 19y^6 - 22y^5 + 3y^4 + 14y^3 - 6y^2 - 4y + 1$
$c_7, c_{11}$	$y^8 - 3y^7 + 7y^6 - 10y^5 + 11y^4 - 10y^3 + 6y^2 - 4y + 1$
$c_{10}, c_{12}$	$y^8 + 5y^7 + 11y^6 + 6y^5 - 17y^4 - 34y^3 - 22y^2 - 4y + 1$

**(vi) Complex Volumes and Cusp Shapes**

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.570868 + 0.730671I$		
$a = 0.615431 - 0.295452I$	$-0.604279 + 1.131230I$	$1.78185 - 1.82144I$
$b = 0$		
$u = -0.570868 - 0.730671I$		
$a = 0.615431 + 0.295452I$	$-0.604279 - 1.131230I$	$1.78185 + 1.82144I$
$b = 0$		
$u = 0.855237 + 0.665892I$		
$a = -1.68119 - 0.49658I$	$-3.80435 + 2.57849I$	$-2.57592 - 5.06085I$
$b = 0$		
$u = 0.855237 - 0.665892I$		
$a = -1.68119 + 0.49658I$	$-3.80435 - 2.57849I$	$-2.57592 + 5.06085I$
$b = 0$		
$u = 1.09818$		
$a = 0.532015$	4.85780	6.04790
$b = 0$		
$u = -1.031810 + 0.655470I$		
$a = 0.473764 + 0.240160I$	$0.73474 - 6.44354I$	$3.16642 + 7.92550I$
$b = 0$		
$u = -1.031810 - 0.655470I$		
$a = 0.473764 - 0.240160I$	$0.73474 + 6.44354I$	$3.16642 - 7.92550I$
$b = 0$		
$u = -0.603304$		
$a = 4.65198$	$-0.799899$	-13.7930
$b = 0$		

### III. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1$	$((u - 1)^8)(u^{41} + 53u^{40} + \dots + 381u + 1)$
$c_2$	$((u - 1)^8)(u^{41} - 9u^{40} + \dots - 29u + 1)$
$c_3, c_6$	$u^8(u^{41} + 7u^{40} + \dots + 2176u - 256)$
$c_4$	$((u + 1)^8)(u^{41} - 9u^{40} + \dots - 29u + 1)$
$c_5$	$(u^8 - u^7 - 3u^6 + 2u^5 + 3u^4 - 2u - 1)(u^{41} - 2u^{40} + \dots + u - 1)$
$c_7$	$(u^8 + u^7 + \dots - 2u - 1)(u^{41} - 2u^{40} + \dots - u + 1)$
$c_8$	$(u^8 + u^7 - 3u^6 - 2u^5 + 3u^4 + 2u - 1)(u^{41} - 2u^{40} + \dots + u - 1)$
$c_9$	$(u^8 + u^7 - 3u^6 - 2u^5 + 3u^4 + 2u - 1)(u^{41} + 2u^{40} + \dots + 12241u + 8353)$
$c_{10}$	$(u^8 + 3u^7 + 7u^6 + 10u^5 + 11u^4 + 10u^3 + 6u^2 + 4u + 1) \cdot (u^{41} - 12u^{40} + \dots + 5u - 1)$
$c_{11}$	$(u^8 - u^7 + \dots + 2u - 1)(u^{41} - 2u^{40} + \dots - u + 1)$
$c_{12}$	$(u^8 - 3u^7 + 7u^6 - 10u^5 + 11u^4 - 10u^3 + 6u^2 - 4u + 1) \cdot (u^{41} - 12u^{40} + \dots + 5u - 1)$

#### IV. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1$	$((y - 1)^8)(y^{41} - 121y^{40} + \dots + 73433y - 1)$
$c_2, c_4$	$((y - 1)^8)(y^{41} - 53y^{40} + \dots + 381y - 1)$
$c_3, c_6$	$y^8(y^{41} + 51y^{40} + \dots + 2801664y - 65536)$
$c_5, c_8$	$(y^8 - 7y^7 + 19y^6 - 22y^5 + 3y^4 + 14y^3 - 6y^2 - 4y + 1) \cdot (y^{41} + 42y^{39} + \dots + 5y - 1)$
$c_7, c_{11}$	$(y^8 - 3y^7 + 7y^6 - 10y^5 + 11y^4 - 10y^3 + 6y^2 - 4y + 1) \cdot (y^{41} - 12y^{40} + \dots + 5y - 1)$
$c_9$	$(y^8 - 7y^7 + 19y^6 - 22y^5 + 3y^4 + 14y^3 - 6y^2 - 4y + 1) \cdot (y^{41} + 36y^{40} + \dots + 949291005y - 69772609)$
$c_{10}, c_{12}$	$(y^8 + 5y^7 + 11y^6 + 6y^5 - 17y^4 - 34y^3 - 22y^2 - 4y + 1) \cdot (y^{41} + 36y^{40} + \dots + 37y - 1)$