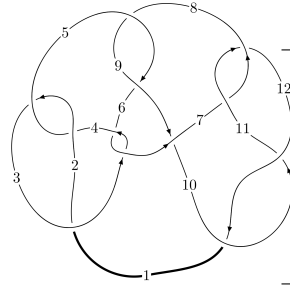
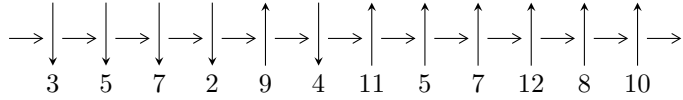


12n<sub>0082</sub> (K12n<sub>0082</sub>)



A knot diagram<sup>1</sup>

**Linearized knot diagram**



**Solving Sequence**

$$7,11 \xrightarrow{c_7} 8 \xrightarrow{c_{11}} 4,12 \xrightarrow{c_3} 3 \xrightarrow{c_6} 6 \xrightarrow{c_{10}} 10 \xrightarrow{c_{12}} 1 \xrightarrow{c_9} 9 \xrightarrow{c_5} 5 \xrightarrow{c_2} 2 \rightsquigarrow c_1, c_4, c_8$$

**Ideals for irreducible components<sup>2</sup> of  $X_{\text{par}}$**

$$I_1^u = \langle -1075292995u^{33} - 4308557086u^{32} + \dots + 1783382596b - 2108461367, \\ -16834407501u^{33} - 77191989494u^{32} + \dots + 1783382596a - 50354623549, \\ u^{34} + 5u^{33} + \dots + 17u + 1 \rangle$$

$$I_2^u = \langle b, 3u^7 + u^6 - 4u^5 - 4u^4 + 5u^3 + 3u^2 + a - u - 5, u^8 + u^7 - u^6 - 2u^5 + u^4 + 2u^3 - 2u - 1 \rangle$$

$$I_3^u = \langle -u^2a - 2u^2 + b + a + u + 2, a^2 + 2au + 4u^2 + a - 4u + 4, u^3 - u^2 + 1 \rangle$$

$$I_4^u = \langle u^2 + b, a - u, u^3 - u^2 + 1 \rangle$$

\* 4 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 51 representations.

<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

I.

$$I_1^u = \langle -1.08 \times 10^9 u^{33} - 4.31 \times 10^9 u^{32} + \dots + 1.78 \times 10^9 b - 2.11 \times 10^9, -1.68 \times 10^{10} u^{33} - 7.72 \times 10^{10} u^{32} + \dots + 1.78 \times 10^9 a - 5.04 \times 10^{10}, u^{34} + 5u^{33} + \dots + 17u + 1 \rangle$$

(i) Arc colorings

$$a_7 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 9.43959u^{33} + 43.2840u^{32} + \dots + 295.933u + 28.2355 \\ 0.602951u^{33} + 2.41595u^{32} + \dots + 10.5760u + 1.18228 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} u \\ -u^3 + u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 10.0425u^{33} + 45.7000u^{32} + \dots + 306.509u + 29.4177 \\ 0.602951u^{33} + 2.41595u^{32} + \dots + 10.5760u + 1.18228 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -8.32985u^{33} - 34.9914u^{32} + \dots - 174.842u - 14.4784 \\ 1.50407u^{33} + 6.20192u^{32} + \dots + 28.1402u + 1.51861 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -u^3 \\ u^5 - u^3 + u \end{pmatrix}$$

$$a_1 = \begin{pmatrix} u^5 + u \\ -u^7 + u^5 - 2u^3 + u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -u^5 - u \\ u^5 - u^3 + u \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -3.94864u^{33} - 16.6164u^{32} + \dots - 92.4717u - 9.25517 \\ -0.647049u^{33} - 2.83405u^{32} + \dots - 12.4240u - 1.06772 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 7.18982u^{33} + 33.9328u^{32} + \dots + 248.452u + 22.9281 \\ 0.647049u^{33} + 2.83405u^{32} + \dots + 12.4240u + 1.06772 \end{pmatrix}$$

(ii) Obstruction class = -1

$$(iii) \text{ Cusp Shapes} = -\frac{749238525}{445845649}u^{33} - \frac{25224574109}{1783382596}u^{32} + \dots - \frac{515748589297}{1783382596}u - \frac{13447700611}{445845649}$$

(iv) u-Polynomials at the component

| Crossings        | u-Polynomials at each crossing             |
|------------------|--|
| $c_1$            | $u^{34} + 40u^{32} + \dots + 1011u + 1$    |
| $c_2, c_4$       | $u^{34} - 12u^{33} + \dots + 27u + 1$      |
| $c_3, c_6$       | $u^{34} - 4u^{33} + \dots + 896u - 256$    |
| $c_5, c_8$       | $u^{34} - 2u^{33} + \dots - 1536u - 512$   |
| $c_7, c_{11}$    | $u^{34} - 5u^{33} + \dots - 17u + 1$       |
| $c_9$            | $u^{34} + 5u^{33} + \dots - 34224u + 2116$ |
| $c_{10}, c_{12}$ | $u^{34} - 15u^{33} + \dots - 147u + 1$     |

(v) Riley Polynomials at the component

| Crossings        | Riley Polynomials at each crossing                 |
|------------------|--|
| $c_1$            | $y^{34} + 80y^{33} + \dots - 1049111y + 1$         |
| $c_2, c_4$       | $y^{34} + 40y^{32} + \dots - 1011y + 1$            |
| $c_3, c_6$       | $y^{34} + 60y^{33} + \dots - 2146304y + 65536$     |
| $c_5, c_8$       | $y^{34} - 56y^{33} + \dots - 1441792y + 262144$    |
| $c_7, c_{11}$    | $y^{34} - 15y^{33} + \dots - 147y + 1$             |
| $c_9$            | $y^{34} - 83y^{33} + \dots - 660094664y + 4477456$ |
| $c_{10}, c_{12}$ | $y^{34} + 13y^{33} + \dots - 18915y + 1$           |

(vi) Complex Volumes and Cusp Shapes

| Solutions to $I_1^u$   | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape           |
|--|---------------------------------------|----------------------|
| $u = -0.675479 + 0.712354I$<br>$a = -0.270719 + 0.161827I$<br>$b = 0.097932 - 0.857151I$ | $0.11560 + 2.14584I$                  | $4.84697 - 4.28283I$ |
| $u = -0.675479 - 0.712354I$<br>$a = -0.270719 - 0.161827I$<br>$b = 0.097932 + 0.857151I$ | $0.11560 - 2.14584I$                  | $4.84697 + 4.28283I$ |
| $u = 0.787838 + 0.675769I$<br>$a = -0.413189 + 0.782228I$<br>$b = 0.360422 - 0.507830I$  | $-2.05683 + 2.19416I$                 | $2.78133 - 4.16804I$ |
| $u = 0.787838 - 0.675769I$<br>$a = -0.413189 - 0.782228I$<br>$b = 0.360422 + 0.507830I$  | $-2.05683 - 2.19416I$                 | $2.78133 + 4.16804I$ |
| $u = -0.994788 + 0.364572I$<br>$a = -1.43728 - 0.32761I$<br>$b = 1.097360 - 0.422286I$   | $0.27995 - 2.43239I$                  | $4.42150 + 3.66524I$ |
| $u = -0.994788 - 0.364572I$<br>$a = -1.43728 + 0.32761I$<br>$b = 1.097360 + 0.422286I$   | $0.27995 + 2.43239I$                  | $4.42150 - 3.66524I$ |
| $u = 0.883198 + 0.167536I$<br>$a = -0.82822 - 2.77937I$<br>$b = 0.390635 + 1.309810I$    | $4.40661 - 2.39050I$                  | $8.72484 - 4.03068I$ |
| $u = 0.883198 - 0.167536I$<br>$a = -0.82822 + 2.77937I$<br>$b = 0.390635 - 1.309810I$    | $4.40661 + 2.39050I$                  | $8.72484 + 4.03068I$ |
| $u = -0.439134 + 1.012860I$<br>$a = -0.14054 + 2.08289I$<br>$b = -0.21712 - 2.33804I$    | $12.94380 - 1.52834I$                 | $2.89091 + 1.52951I$ |
| $u = -0.439134 - 1.012860I$<br>$a = -0.14054 - 2.08289I$<br>$b = -0.21712 + 2.33804I$    | $12.94380 + 1.52834I$                 | $2.89091 - 1.52951I$ |

| Solutions to $I_1^u$  | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape            |
|---|---------------------------------------|-----------------------|
| $u = -0.554438 + 0.988490I$<br>$a = 0.37372 - 1.78363I$<br>$b = -0.69939 + 2.06047I$    | $12.1480 + 7.3055I$                   | $2.34511 - 2.34014I$  |
| $u = -0.554438 - 0.988490I$<br>$a = 0.37372 + 1.78363I$<br>$b = -0.69939 - 2.06047I$    | $12.1480 - 7.3055I$                   | $2.34511 + 2.34014I$  |
| $u = 0.877826 + 0.731952I$<br>$a = -2.89148 - 0.75774I$<br>$b = -0.433493 + 0.039285I$  | $-4.30564 + 2.78916I$                 | $-43.5792 - 1.9775I$  |
| $u = 0.877826 - 0.731952I$<br>$a = -2.89148 + 0.75774I$<br>$b = -0.433493 - 0.039285I$  | $-4.30564 - 2.78916I$                 | $-43.5792 + 1.9775I$  |
| $u = 0.960792 + 0.643718I$<br>$a = -1.56912 - 0.34499I$<br>$b = 0.705310 + 0.607713I$   | $-1.51157 + 2.93275I$                 | $3.49597 - 2.09060I$  |
| $u = 0.960792 - 0.643718I$<br>$a = -1.56912 + 0.34499I$<br>$b = 0.705310 - 0.607713I$   | $-1.51157 - 2.93275I$                 | $3.49597 + 2.09060I$  |
| $u = -0.988094 + 0.655947I$<br>$a = 0.798191 - 0.915301I$<br>$b = 0.242079 + 0.838628I$ | $1.06007 - 7.41163I$                  | $6.37706 + 10.12845I$ |
| $u = -0.988094 - 0.655947I$<br>$a = 0.798191 + 0.915301I$<br>$b = 0.242079 - 0.838628I$ | $1.06007 + 7.41163I$                  | $6.37706 - 10.12845I$ |
| $u = 1.134070 + 0.366301I$<br>$a = 1.64472 + 3.48212I$<br>$b = -0.39273 - 1.87590I$     | $6.17981 + 3.91713I$                  | $6.50133 - 4.05550I$  |
| $u = 1.134070 - 0.366301I$<br>$a = 1.64472 - 3.48212I$<br>$b = -0.39273 + 1.87590I$     | $6.17981 - 3.91713I$                  | $6.50133 + 4.05550I$  |

| Solutions to $I_1^u$   | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape            |
|--|---------------------------------------|-----------------------|
| $u = -0.759460 + 0.212841I$<br>$a = 2.07551 - 3.57649I$<br>$b = 0.167778 + 0.535642I$    | $-0.839427 - 0.307998I$               | $10.22671 + 6.42071I$ |
| $u = -0.759460 - 0.212841I$<br>$a = 2.07551 + 3.57649I$<br>$b = 0.167778 - 0.535642I$    | $-0.839427 + 0.307998I$               | $10.22671 - 6.42071I$ |
| $u = -0.199261 + 0.726308I$<br>$a = 0.009119 - 0.678462I$<br>$b = -0.695938 + 1.120220I$ | $2.39265 - 0.51912I$                  | $3.37017 + 1.09835I$  |
| $u = -0.199261 - 0.726308I$<br>$a = 0.009119 + 0.678462I$<br>$b = -0.695938 - 1.120220I$ | $2.39265 + 0.51912I$                  | $3.37017 - 1.09835I$  |
| $u = -1.155100 + 0.509124I$<br>$a = 0.68550 + 3.05854I$<br>$b = -1.31414 - 1.23344I$     | $5.17110 - 4.13601I$                  | $6.26603 + 3.46699I$  |
| $u = -1.155100 - 0.509124I$<br>$a = 0.68550 - 3.05854I$<br>$b = -1.31414 + 1.23344I$     | $5.17110 + 4.13601I$                  | $6.26603 - 3.46699I$  |
| $u = 1.331470 + 0.064618I$<br>$a = 0.73597 - 5.01515I$<br>$b = -0.62913 + 2.45336I$      | $19.5904 + 4.8180I$                   | $6.85242 - 2.12746I$  |
| $u = 1.331470 - 0.064618I$<br>$a = 0.73597 + 5.01515I$<br>$b = -0.62913 - 2.45336I$      | $19.5904 - 4.8180I$                   | $6.85242 + 2.12746I$  |
| $u = -0.647070$<br>$a = -0.602677$<br>$b = -0.176681$                                    | $0.883121$                            | $11.7300$             |
| $u = -1.141270 + 0.734626I$<br>$a = -1.07593 + 3.44611I$<br>$b = -0.83809 - 1.99730I$    | $13.9751 - 13.5871I$                  | $3.82321 + 6.38940I$  |

| Solutions to $I_1^u$  | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape           |
|---|---------------------------------------|----------------------|
| $u = -1.141270 - 0.734626I$<br>$a = -1.07593 - 3.44611I$<br>$b = -0.83809 + 1.99730I$ | $13.9751 + 13.5871I$                  | $3.82321 - 6.38940I$ |
| $u = -1.202000 + 0.684331I$<br>$a = 1.86014 - 3.56344I$<br>$b = 0.00069 + 2.47834I$   | $15.3278 - 4.6468I$                   | $5.01393 + 2.36080I$ |
| $u = -1.202000 - 0.684331I$<br>$a = 1.86014 + 3.56344I$<br>$b = 0.00069 - 2.47834I$   | $15.3278 + 4.6468I$                   | $5.01393 - 2.36080I$ |
| $u = -0.0852780$<br>$a = 8.48988$<br>$b = 0.492352$                                   | $-1.21008$                            | $-9.44660$           |



$$\text{II. } I_2^u = \langle b, 3u^7 + u^6 - 4u^5 - 4u^4 + 5u^3 + 3u^2 + a - u - 5, u^8 + u^7 - u^6 - 2u^5 + u^4 + 2u^3 - 2u - 1 \rangle$$

(i) Arc colorings

$$a_7 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -3u^7 - u^6 + 4u^5 + 4u^4 - 5u^3 - 3u^2 + u + 5 \\ 0 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} u \\ -u^3 + u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -3u^7 - u^6 + 4u^5 + 4u^4 - 5u^3 - 3u^2 + u + 5 \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -u^3 \\ u^5 - u^3 + u \end{pmatrix}$$

$$a_1 = \begin{pmatrix} u^5 + u \\ -u^7 + u^5 - 2u^3 + u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -u^5 - u \\ u^5 - u^3 + u \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -u^5 - u \\ u^7 - u^5 + 2u^3 - u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -3u^7 - u^6 + 5u^5 + 4u^4 - 5u^3 - 3u^2 + 2u + 5 \\ -u^7 + u^5 - 2u^3 + u \end{pmatrix}$$

(ii) Obstruction class = 1

$$\text{(iii) Cusp Shapes} = -17u^7 - 6u^6 + 24u^5 + 22u^4 - 31u^3 - 17u^2 + 12u + 31$$

(iv) u-Polynomials at the component

| Crossings  | u-Polynomials at each crossing                              |
|------------|---|
| $c_1, c_2$ | $(u - 1)^8$   |
| $c_3, c_6$ | $u^8$   |
| $c_4$      | $(u + 1)^8$   |
| $c_5$      | $u^8 - u^7 - 3u^6 + 2u^5 + 3u^4 - 2u - 1$                   |
| $c_7$      | $u^8 + u^7 - u^6 - 2u^5 + u^4 + 2u^3 - 2u - 1$              |
| $c_8, c_9$ | $u^8 + u^7 - 3u^6 - 2u^5 + 3u^4 + 2u - 1$                   |
| $c_{10}$   | $u^8 + 3u^7 + 7u^6 + 10u^5 + 11u^4 + 10u^3 + 6u^2 + 4u + 1$ |
| $c_{11}$   | $u^8 - u^7 - u^6 + 2u^5 + u^4 - 2u^3 + 2u - 1$              |
| $c_{12}$   | $u^8 - 3u^7 + 7u^6 - 10u^5 + 11u^4 - 10u^3 + 6u^2 - 4u + 1$ |

(v) Riley Polynomials at the component

| Crossings        | Riley Polynomials at each crossing                           |
|------------------|--|
| $c_1, c_2, c_4$  | $(y - 1)^8$  |
| $c_3, c_6$       | $y^8$  |
| $c_5, c_8, c_9$  | $y^8 - 7y^7 + 19y^6 - 22y^5 + 3y^4 + 14y^3 - 6y^2 - 4y + 1$  |
| $c_7, c_{11}$    | $y^8 - 3y^7 + 7y^6 - 10y^5 + 11y^4 - 10y^3 + 6y^2 - 4y + 1$  |
| $c_{10}, c_{12}$ | $y^8 + 5y^7 + 11y^6 + 6y^5 - 17y^4 - 34y^3 - 22y^2 - 4y + 1$ |

(vi) Complex Volumes and Cusp Shapes

| Solutions to $I_2^u$   | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape             |
|--|---------------------------------------|------------------------|
| $u = -0.570868 + 0.730671I$<br>$a = 0.615431 - 0.295452I$<br>$b = 0$ | $-0.604279 + 1.131230I$               | $1.048604 + 0.799861I$ |
| $u = -0.570868 - 0.730671I$<br>$a = 0.615431 + 0.295452I$<br>$b = 0$ | $-0.604279 - 1.131230I$               | $1.048604 - 0.799861I$ |
| $u = 0.855237 + 0.665892I$<br>$a = -1.68119 - 0.49658I$<br>$b = 0$   | $-3.80435 + 2.57849I$                 | $-0.86993 - 2.07507I$  |
| $u = 0.855237 - 0.665892I$<br>$a = -1.68119 + 0.49658I$<br>$b = 0$   | $-3.80435 - 2.57849I$                 | $-0.86993 + 2.07507I$  |
| $u = 1.09818$<br>$a = 0.532015$<br>$b = 0$                           | 4.85780                               | 9.68010                |
| $u = -1.031810 + 0.655470I$<br>$a = 0.473764 + 0.240160I$<br>$b = 0$ | $0.73474 - 6.44354I$                  | $3.69048 + 2.66284I$   |
| $u = -1.031810 - 0.655470I$<br>$a = 0.473764 - 0.240160I$<br>$b = 0$ | $0.73474 + 6.44354I$                  | $3.69048 - 2.66284I$   |
| $u = -0.603304$<br>$a = 4.65198$<br>$b = 0$                          | -0.799899                             | 25.5820                |

**III.**

$$I_3^u = \langle -u^2a - 2u^2 + b + a + u + 2, a^2 + 2au + 4u^2 + a - 4u + 4, u^3 - u^2 + 1 \rangle$$

**(i) Arc colorings**

$$a_7 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} a \\ u^2a + 2u^2 - a - u - 2 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} u \\ -u^2 + u + 1 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} u^2a + 2u^2 - u - 2 \\ u^2a + 2u^2 - a - u - 2 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} u^2a - au - a - 3 \\ u^2a + au + 3u^2 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -u^2 + 1 \\ -u^2 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} u^2a - au - a - 3 \\ u^2a + au + 3u^2 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 2u^2a + 3u^2 - a - 5 \\ u^2a + au + 3u^2 \end{pmatrix}$$

**(ii) Obstruction class = 1**

**(iii) Cusp Shapes =  $u^2a - 7au - 12u^2 - 3a - 4u + 4$**

(iv) u-Polynomials at the component

| Crossings                   | u-Polynomials at each crossing |
|-----------------------------|--------------------------------|
| $c_1, c_3, c_9$<br>$c_{12}$ | $(u^3 - u^2 + 2u - 1)^2$       |
| $c_2, c_{11}$               | $(u^3 + u^2 - 1)^2$            |
| $c_4, c_7$                  | $(u^3 - u^2 + 1)^2$            |
| $c_5, c_8$                  | $u^6$                          |
| $c_6, c_{10}$               | $(u^3 + u^2 + 2u + 1)^2$       |

(v) Riley Polynomials at the component

| Crossings                                | Riley Polynomials at each crossing |
|--|------------------------------------|
| $c_1, c_3, c_6$<br>$c_9, c_{10}, c_{12}$ | $(y^3 + 3y^2 + 2y - 1)^2$          |
| $c_2, c_4, c_7$<br>$c_{11}$              | $(y^3 - y^2 + 2y - 1)^2$           |
| $c_5, c_8$                               | $y^6$                              |

(vi) Complex Volumes and Cusp Shapes

| Solutions to $I_3^u$   | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape            |
|--|---------------------------------------|-----------------------|
| $u = 0.877439 + 0.744862I$<br>$a = -1.06984 - 1.06527I$<br>$b = -0.215080 + 1.307140I$ | $5.65624I$                            | $3.29784 - 4.97572I$  |
| $u = 0.877439 + 0.744862I$<br>$a = -1.68504 - 0.42445I$<br>$b = -0.569840$             | $-4.13758 + 2.82812I$                 | $11.29331 - 8.29280I$ |
| $u = 0.877439 - 0.744862I$<br>$a = -1.06984 + 1.06527I$<br>$b = -0.215080 - 1.307140I$ | $-5.65624I$                           | $3.29784 + 4.97572I$  |
| $u = 0.877439 - 0.744862I$<br>$a = -1.68504 + 0.42445I$<br>$b = -0.569840$             | $-4.13758 - 2.82812I$                 | $11.29331 + 8.29280I$ |
| $u = -0.754878$<br>$a = 0.25488 + 3.03873I$<br>$b = -0.215080 - 1.307140I$             | $4.13758 - 2.82812I$                  | $0.90884 + 8.67250I$  |
| $u = -0.754878$<br>$a = 0.25488 - 3.03873I$<br>$b = -0.215080 + 1.307140I$             | $4.13758 + 2.82812I$                  | $0.90884 - 8.67250I$  |



$$\text{IV. } \Gamma_4^u = \langle u^2 + b, a - u, u^3 - u^2 + 1 \rangle$$

(i) Arc colorings

$$a_7 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} u \\ -u^2 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} u \\ -u^2 + u + 1 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -u^2 + u \\ -u^2 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} u^2 \\ -u^2 + u + 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -u^2 + 1 \\ -u^2 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} u^2 \\ -u^2 + u + 1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} u - 1 \\ -u^2 + u + 1 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes =  $-2u^2 + 3u + 2$

(iv) u-Polynomials at the component

| Crossings                   | u-Polynomials at each crossing |
|-----------------------------|--------------------------------|
| $c_1, c_3, c_9$<br>$c_{12}$ | $u^3 - u^2 + 2u - 1$           |
| $c_2, c_{11}$               | $u^3 + u^2 - 1$                |
| $c_4, c_7$                  | $u^3 - u^2 + 1$                |
| $c_5, c_8$                  | $u^3$                          |
| $c_6, c_{10}$               | $u^3 + u^2 + 2u + 1$           |

(v) Riley Polynomials at the component

| Crossings                                | Riley Polynomials at each crossing |
|--|------------------------------------|
| $c_1, c_3, c_6$<br>$c_9, c_{10}, c_{12}$ | $y^3 + 3y^2 + 2y - 1$              |
| $c_2, c_4, c_7$<br>$c_{11}$              | $y^3 - y^2 + 2y - 1$               |
| $c_5, c_8$                               | $y^3$                              |

(vi) Complex Volumes and Cusp Shapes

| Solutions to $I_4^u$  | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape           |
|---|---------------------------------------|----------------------|
| $u = 0.877439 + 0.744862I$<br>$a = 0.877439 + 0.744862I$<br>$b = -0.215080 - 1.307140I$ | 0                                     | $4.20216 - 0.37970I$ |
| $u = 0.877439 - 0.744862I$<br>$a = 0.877439 - 0.744862I$<br>$b = -0.215080 + 1.307140I$ | 0                                     | $4.20216 + 0.37970I$ |
| $u = -0.754878$<br>$a = -0.754878$<br>$b = -0.569840$                                   | 0                                     | $-1.40430$           |

### V. u-Polynomials

| Crossings | u-Polynomials at each crossing  |
|-----------|---|
| $c_1$     | $((u-1)^8)(u^3-u^2+2u-1)^3(u^{34}+40u^{32}+\dots+1011u+1)$  |
| $c_2$     | $((u-1)^8)(u^3+u^2-1)^3(u^{34}-12u^{33}+\dots+27u+1)$   |
| $c_3$     | $u^8(u^3-u^2+2u-1)^3(u^{34}-4u^{33}+\dots+896u-256)$  |
| $c_4$     | $((u+1)^8)(u^3-u^2+1)^3(u^{34}-12u^{33}+\dots+27u+1)$   |
| $c_5$     | $u^9(u^8-u^7+\dots-2u-1)(u^{34}-2u^{33}+\dots-1536u-512)$   |
| $c_6$     | $u^8(u^3+u^2+2u+1)^3(u^{34}-4u^{33}+\dots+896u-256)$  |
| $c_7$     | $(u^3-u^2+1)^3(u^8+u^7-u^6-2u^5+u^4+2u^3-2u-1)$<br>$\cdot (u^{34}-5u^{33}+\dots-17u+1)$                             |
| $c_8$     | $u^9(u^8+u^7+\dots+2u-1)(u^{34}-2u^{33}+\dots-1536u-512)$   |
| $c_9$     | $(u^3-u^2+2u-1)^3(u^8+u^7-3u^6-2u^5+3u^4+2u-1)$<br>$\cdot (u^{34}+5u^{33}+\dots-34224u+2116)$                       |
| $c_{10}$  | $(u^3+u^2+2u+1)^3$<br>$\cdot (u^8+3u^7+7u^6+10u^5+11u^4+10u^3+6u^2+4u+1)$<br>$\cdot (u^{34}-15u^{33}+\dots-147u+1)$ |
| $c_{11}$  | $(u^3+u^2-1)^3(u^8-u^7-u^6+2u^5+u^4-2u^3+2u-1)$<br>$\cdot (u^{34}-5u^{33}+\dots-17u+1)$                             |
| $c_{12}$  | $(u^3-u^2+2u-1)^3$<br>$\cdot (u^8-3u^7+7u^6-10u^5+11u^4-10u^3+6u^2-4u+1)$<br>$\cdot (u^{34}-15u^{33}+\dots-147u+1)$ |

## VI. Riley Polynomials

| Crossings        | Riley Polynomials at each crossing   |
|------------------|--|
| $c_1$            | $((y-1)^8)(y^3+3y^2+2y-1)^3(y^{34}+80y^{33}+\dots-1049111y+1)$   |
| $c_2, c_4$       | $((y-1)^8)(y^3-y^2+2y-1)^3(y^{34}+40y^{32}+\dots-1011y+1)$   |
| $c_3, c_6$       | $y^8(y^3+3y^2+2y-1)^3(y^{34}+60y^{33}+\dots-2146304y+65536)$   |
| $c_5, c_8$       | $y^9(y^8-7y^7+19y^6-22y^5+3y^4+14y^3-6y^2-4y+1)$<br>$\cdot (y^{34}-56y^{33}+\dots-1441792y+262144)$                              |
| $c_7, c_{11}$    | $(y^3-y^2+2y-1)^3$<br>$\cdot (y^8-3y^7+7y^6-10y^5+11y^4-10y^3+6y^2-4y+1)$<br>$\cdot (y^{34}-15y^{33}+\dots-147y+1)$              |
| $c_9$            | $(y^3+3y^2+2y-1)^3$<br>$\cdot (y^8-7y^7+19y^6-22y^5+3y^4+14y^3-6y^2-4y+1)$<br>$\cdot (y^{34}-83y^{33}+\dots-660094664y+4477456)$ |
| $c_{10}, c_{12}$ | $(y^3+3y^2+2y-1)^3$<br>$\cdot (y^8+5y^7+11y^6+6y^5-17y^4-34y^3-22y^2-4y+1)$<br>$\cdot (y^{34}+13y^{33}+\dots-18915y+1)$          |