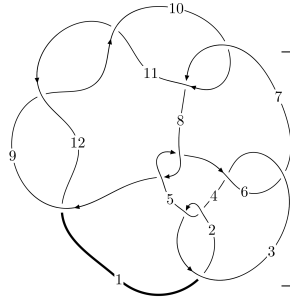
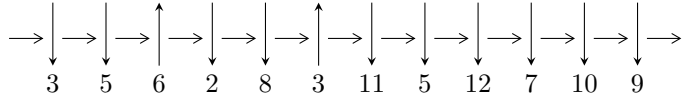


12n₀₀₉₄ (K12n₀₀₉₄)



A knot diagram¹

Linearized knot diagram



Solving Sequence

$$7,10 \xrightarrow{c_{10}} 11 \xrightarrow{c_7} 8 \xrightarrow{c_{11}} 3,12 \xrightarrow{c_6} 6 \xrightarrow{c_3} 4 \xrightarrow{c_5} 5 \xrightarrow{c_2} 2 \xrightarrow{c_9} 9 \xrightarrow{c_{12}} 1 \rightsquigarrow c_1, c_4, c_8$$

Ideals for irreducible components² of X_{par}

$$I_1^u = \langle 237180958840u^{40} + 426640636409u^{39} + \dots + 126602287463b - 603869550171, \\ 184156720841u^{40} + 260129939039u^{39} + \dots + 379806862389a - 927659389454, \\ u^{41} + 2u^{40} + \dots - 5u - 1 \rangle$$

$$I_2^u = \langle -2u^4 - u^3 + b + u - 3, a, u^5 + u^4 - u^2 + u + 1 \rangle$$

* 2 irreducible components of $\dim_{\mathbb{C}} = 0$, with total 46 representations.

¹The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

²All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

I.

$$I_1^u = \langle 2.37 \times 10^{11}u^{40} + 4.27 \times 10^{11}u^{39} + \dots + 1.27 \times 10^{11}b - 6.04 \times 10^{11}, 1.84 \times 10^{11}u^{40} + 2.60 \times 10^{11}u^{39} + \dots + 3.80 \times 10^{11}a - 9.28 \times 10^{11}, u^{41} + 2u^{40} + \dots - 5u - 1 \rangle$$

(i) Arc colorings

$$\begin{aligned} a_7 &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_{10} &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_{11} &= \begin{pmatrix} 1 \\ u^2 \end{pmatrix} \\ a_8 &= \begin{pmatrix} -u \\ -u^3 + u \end{pmatrix} \\ a_3 &= \begin{pmatrix} -0.484869u^{40} - 0.684901u^{39} + \dots + 1.43981u + 2.44245 \\ -1.87343u^{40} - 3.36993u^{39} + \dots + 10.8768u + 4.76982 \end{pmatrix} \\ a_{12} &= \begin{pmatrix} -u^2 + 1 \\ u^2 \end{pmatrix} \\ a_6 &= \begin{pmatrix} 0.839243u^{40} + 0.839308u^{39} + \dots - 4.68096u - 0.119652 \\ -3.44624u^{40} - 3.41234u^{39} + \dots + 13.1682u + 3.81213 \end{pmatrix} \\ a_4 &= \begin{pmatrix} 2.36382u^{40} + 2.16411u^{39} + \dots - 7.95826u + 1.01795 \\ -5.33759u^{40} - 3.95656u^{39} + \dots + 14.0481u + 5.35650 \end{pmatrix} \\ a_5 &= \begin{pmatrix} -0.545392u^{40} - 0.945298u^{39} + \dots + 1.68058u + 1.67265 \\ -2.45910u^{40} - 2.60458u^{39} + \dots + 10.3453u + 3.00449 \end{pmatrix} \\ a_2 &= \begin{pmatrix} 0.605914u^{40} + 0.205696u^{39} + \dots - 1.92135u + 3.09715 \\ -4.95524u^{40} - 5.16076u^{39} + \dots + 18.1862u + 6.76084 \end{pmatrix} \\ a_9 &= \begin{pmatrix} u^4 - u^2 + 1 \\ -u^4 \end{pmatrix} \\ a_1 &= \begin{pmatrix} -u^6 + u^4 - 2u^2 + 1 \\ u^6 + u^2 \end{pmatrix} \end{aligned}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes

$$= -\frac{159607686408}{126602287463}u^{40} - \frac{572526761426}{126602287463}u^{39} + \dots + \frac{127765468738}{126602287463}u + \frac{346980052385}{126602287463}$$

(iv) u-Polynomials at the component

| Crossings | u-Polynomials at each crossing |
|-----------------------|---|
| c_1 | $u^{41} + 44u^{40} + \dots + 2355u + 1$ |
| c_2, c_4 | $u^{41} - 6u^{40} + \dots + 47u - 1$ |
| c_3, c_6 | $u^{41} + 7u^{40} + \dots + 64u + 32$ |
| c_5, c_8 | $u^{41} - 2u^{40} + \dots + u - 1$ |
| c_7, c_{10} | $u^{41} + 2u^{40} + \dots - 5u - 1$ |
| c_9, c_{11}, c_{12} | $u^{41} + 12u^{40} + \dots + 9u + 1$ |

(v) Riley Polynomials at the component

| Crossings | Riley Polynomials at each crossing |
|-----------------------|---|
| c_1 | $y^{41} - 88y^{40} + \dots + 5466307y - 1$ |
| c_2, c_4 | $y^{41} - 44y^{40} + \dots + 2355y - 1$ |
| c_3, c_6 | $y^{41} + 33y^{40} + \dots + 49664y - 1024$ |
| c_5, c_8 | $y^{41} + 42y^{39} + \dots + 9y - 1$ |
| c_7, c_{10} | $y^{41} - 12y^{40} + \dots + 9y - 1$ |
| c_9, c_{11}, c_{12} | $y^{41} + 36y^{40} + \dots + 145y - 1$ |

(vi) Complex Volumes and Cusp Shapes

| Solutions to I_1^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|--|---------------------------------------|------------------------|
| $u = -0.809815 + 0.656518I$ $a = 0.18310 + 1.61197I$ $b = 2.10023 - 1.97578I$ | $-1.37603 + 0.57854I$ | $-11.62960 + 0.13351I$ |
| $u = -0.809815 - 0.656518I$ $a = 0.18310 - 1.61197I$ $b = 2.10023 + 1.97578I$ | $-1.37603 - 0.57854I$ | $-11.62960 - 0.13351I$ |
| $u = 0.934060 + 0.150205I$ $a = -0.18148 - 1.61697I$ $b = 0.203825 + 1.369510I$ | $-3.38084 - 3.41544I$ | $-14.4142 + 7.4507I$ |
| $u = 0.934060 - 0.150205I$ $a = -0.18148 + 1.61697I$ $b = 0.203825 - 1.369510I$ | $-3.38084 + 3.41544I$ | $-14.4142 - 7.4507I$ |
| $u = 0.940510$ $a = -1.80150$ $b = 0.154280$ | -5.56664 | -18.9570 |
| $u = -0.765786 + 0.781729I$ $a = -1.48698 + 0.38083I$ $b = 0.91217 + 1.53968I$ | $2.58614 - 2.24374I$ | $-5.47598 + 3.48781I$ |
| $u = -0.765786 - 0.781729I$ $a = -1.48698 - 0.38083I$ $b = 0.91217 - 1.53968I$ | $2.58614 + 2.24374I$ | $-5.47598 - 3.48781I$ |
| $u = 0.825264 + 0.768049I$ $a = -0.533792 - 0.264806I$ $b = -0.363252 - 0.579554I$ | $2.79960 - 1.79972I$ | $-4.96538 + 4.18830I$ |
| $u = 0.825264 - 0.768049I$ $a = -0.533792 + 0.264806I$ $b = -0.363252 + 0.579554I$ | $2.79960 + 1.79972I$ | $-4.96538 - 4.18830I$ |
| $u = 0.871525 + 0.715232I$ $a = 0.317178 - 0.359818I$ $b = 2.05567 + 2.91440I$ | $0.88954 - 2.73561I$ | $12.1135 + 7.6213I$ |

| Solutions to I_1^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|--|---------------------------------------|------------------------|
| $u = 0.871525 - 0.715232I$ $a = 0.317178 + 0.359818I$ $b = 2.05567 - 2.91440I$ | $0.88954 + 2.73561I$ | $12.1135 - 7.6213I$ |
| $u = 0.710841 + 0.488347I$ $a = 0.458035 - 0.499819I$ $b = -0.032082 + 0.328781I$ | $1.44935 - 1.91021I$ | $-0.76032 + 4.38625I$ |
| $u = 0.710841 - 0.488347I$ $a = 0.458035 + 0.499819I$ $b = -0.032082 - 0.328781I$ | $1.44935 + 1.91021I$ | $-0.76032 - 4.38625I$ |
| $u = -0.923416 + 0.674039I$ $a = 1.66369 + 0.14363I$ $b = -0.43727 - 2.53225I$ | $-1.74586 + 4.59945I$ | $-12.56472 - 5.90817I$ |
| $u = -0.923416 - 0.674039I$ $a = 1.66369 - 0.14363I$ $b = -0.43727 + 2.53225I$ | $-1.74586 - 4.59945I$ | $-12.56472 + 5.90817I$ |
| $u = 1.118030 + 0.271471I$ $a = -0.17044 + 1.50981I$ $b = -0.89384 - 1.26952I$ | $-11.21910 - 7.94660I$ | $-13.0997 + 5.5632I$ |
| $u = 1.118030 - 0.271471I$ $a = -0.17044 - 1.50981I$ $b = -0.89384 + 1.26952I$ | $-11.21910 + 7.94660I$ | $-13.0997 - 5.5632I$ |
| $u = -0.720515 + 0.902697I$ $a = 1.42868 - 0.16952I$ $b = -0.66709 - 1.95032I$ | $-3.31648 - 7.81279I$ | $-7.43198 + 3.38635I$ |
| $u = -0.720515 - 0.902697I$ $a = 1.42868 + 0.16952I$ $b = -0.66709 + 1.95032I$ | $-3.31648 + 7.81279I$ | $-7.43198 - 3.38635I$ |
| $u = -1.121650 + 0.291198I$ $a = 0.498876 - 1.312020I$ $b = -1.197720 + 0.633604I$ | $-11.09620 - 0.45608I$ | $-13.41842 - 0.76918I$ |

| Solutions to I_1^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|--|---------------------------------------|------------------------|
| $u = -1.121650 - 0.291198I$ $a = 0.498876 + 1.312020I$ $b = -1.197720 - 0.633604I$ | $-11.09620 + 0.45608I$ | $-13.41842 + 0.76918I$ |
| $u = -0.019251 + 0.828572I$ $a = -1.74001 + 0.53051I$ $b = 1.287330 - 0.377518I$ | $-7.34491 + 4.27339I$ | $-8.31191 - 2.78880I$ |
| $u = -0.019251 - 0.828572I$ $a = -1.74001 - 0.53051I$ $b = 1.287330 + 0.377518I$ | $-7.34491 - 4.27339I$ | $-8.31191 + 2.78880I$ |
| $u = 0.731013 + 0.924450I$ $a = 0.923425 + 0.604573I$ $b = -1.26483 + 1.04082I$ | $-2.90816 - 0.63484I$ | $-9.12562 + 1.25059I$ |
| $u = 0.731013 - 0.924450I$ $a = 0.923425 - 0.604573I$ $b = -1.26483 - 1.04082I$ | $-2.90816 + 0.63484I$ | $-9.12562 - 1.25059I$ |
| $u = -0.804662 + 0.114668I$ $a = -0.147294 + 0.641401I$ $b = 0.80950 - 2.46652I$ | $-2.53010 + 0.33755I$ | $-19.6414 + 2.1587I$ |
| $u = -0.804662 - 0.114668I$ $a = -0.147294 - 0.641401I$ $b = 0.80950 + 2.46652I$ | $-2.53010 - 0.33755I$ | $-19.6414 - 2.1587I$ |
| $u = 0.926559 + 0.745351I$ $a = 0.274837 + 0.567927I$ $b = -1.08422 - 1.33352I$ | $2.48539 - 3.92858I$ | $-5.87670 + 1.12171I$ |
| $u = 0.926559 - 0.745351I$ $a = 0.274837 - 0.567927I$ $b = -1.08422 + 1.33352I$ | $2.48539 + 3.92858I$ | $-5.87670 - 1.12171I$ |
| $u = -0.965249 + 0.735330I$ $a = 0.31200 - 1.49463I$ $b = -2.37280 + 1.50589I$ | $1.97721 + 7.97688I$ | $-7.20424 - 8.75185I$ |

| Solutions to I_1^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|---|---------------------------------------|-----------------------|
| $u = -0.965249 - 0.735330I$ $a = 0.31200 + 1.49463I$ $b = -2.37280 - 1.50589I$ | $1.97721 - 7.97688I$ | $-7.20424 + 8.75185I$ |
| $u = -0.930134 + 0.890297I$ $a = -0.321692 - 0.288040I$ $b = -0.267302 + 0.867780I$ | $9.70942 + 3.28933I$ | $6.13928 - 1.45507I$ |
| $u = -0.930134 - 0.890297I$ $a = -0.321692 + 0.288040I$ $b = -0.267302 - 0.867780I$ | $9.70942 - 3.28933I$ | $6.13928 + 1.45507I$ |
| $u = -1.037090 + 0.774259I$ $a = -0.100822 + 1.364460I$ $b = 2.50179 - 1.88429I$ | $-4.3067 + 14.0138I$ | $-8.63515 - 7.83947I$ |
| $u = -1.037090 - 0.774259I$ $a = -0.100822 - 1.364460I$ $b = 2.50179 + 1.88429I$ | $-4.3067 - 14.0138I$ | $-8.63515 + 7.83947I$ |
| $u = 1.045430 + 0.785315I$ $a = -0.491121 - 0.952641I$ $b = 2.29006 + 0.47538I$ | $-3.90534 - 5.67266I$ | $-9.98188 + 3.51111I$ |
| $u = 1.045430 - 0.785315I$ $a = -0.491121 + 0.952641I$ $b = 2.29006 - 0.47538I$ | $-3.90534 + 5.67266I$ | $-9.98188 - 3.51111I$ |
| $u = -0.666990$ $a = 0.215563$ $b = 0.523845$ | -0.906933 | -11.3940 |
| $u = -0.035730 + 0.419728I$ $a = 2.06556 - 0.62654I$ $b = -0.346501 - 0.304456I$ | $-0.57624 + 1.50346I$ | $-4.65093 - 4.60849I$ |
| $u = -0.035730 - 0.419728I$ $a = 2.06556 + 0.62654I$ $b = -0.346501 + 0.304456I$ | $-0.57624 - 1.50346I$ | $-4.65093 + 4.60849I$ |

| Solutions to I_1^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|----------------------|---------------------------------------|------------|
| $u = -0.332380$ | | |
| $a = 1.68244$ | -2.28489 | 0.221560 |
| $b = 1.85453$ | | |

$$\text{II. } I_2^u = \langle -2u^4 - u^3 + b + u - 3, a, u^5 + u^4 - u^2 + u + 1 \rangle$$

(i) Arc colorings

$$a_7 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -u \\ -u^3 + u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 0 \\ 2u^4 + u^3 - u + 3 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -u^2 + 1 \\ u^2 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 0 \\ 2u^4 + u^3 - u + 3 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} u^3 \\ -u^4 - u^3 + u^2 - 1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -u^3 \\ 3u^4 + 2u^3 - u^2 - u + 4 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} u^4 - u^2 + 1 \\ -u^4 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -u^3 \\ u^4 + u^3 - u^2 + 1 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = $-18u^4 - 7u^3 + 7u^2 + 18u - 39$

(iv) u-Polynomials at the component

| Crossings | u-Polynomials at each crossing |
|-----------------------|------------------------------------|
| c_1, c_2 | $(u - 1)^5$ |
| c_3, c_6 | u^5 |
| c_4 | $(u + 1)^5$ |
| c_5, c_9 | $u^5 - u^4 + 4u^3 - 3u^2 + 3u - 1$ |
| c_7 | $u^5 - u^4 + u^2 + u - 1$ |
| c_8, c_{11}, c_{12} | $u^5 + u^4 + 4u^3 + 3u^2 + 3u + 1$ |
| c_{10} | $u^5 + u^4 - u^2 + u + 1$ |

(v) Riley Polynomials at the component

| Crossings | Riley Polynomials at each crossing |
|-------------------------------------|---------------------------------------|
| c_1, c_2, c_4 | $(y - 1)^5$ |
| c_3, c_6 | y^5 |
| c_5, c_8, c_9 c_{11}, c_{12} | $y^5 + 7y^4 + 16y^3 + 13y^2 + 3y - 1$ |
| c_7, c_{10} | $y^5 - y^4 + 4y^3 - 3y^2 + 3y - 1$ |

(vi) Complex Volumes and Cusp Shapes

| Solutions to I_2^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|-----------------------------|---------------------------------------|-----------------------|
| $u = 0.758138 + 0.584034I$ | $0.17487 - 2.21397I$ | $-8.20462 + 3.60694I$ |
| $a = 0$ | | |
| $b = 0.442614 + 1.051550I$ | | |
| $u = 0.758138 - 0.584034I$ | $0.17487 + 2.21397I$ | $-8.20462 - 3.60694I$ |
| $a = 0$ | | |
| $b = 0.442614 - 1.051550I$ | | |
| $u = -0.935538 + 0.903908I$ | $9.31336 + 3.33174I$ | $-14.3260 - 3.4701I$ |
| $a = 0$ | | |
| $b = -0.304213 + 0.337334I$ | | |
| $u = -0.935538 - 0.903908I$ | $9.31336 - 3.33174I$ | $-14.3260 + 3.4701I$ |
| $a = 0$ | | |
| $b = -0.304213 - 0.337334I$ | | |
| $u = -0.645200$ | -2.52712 | -48.9390 |
| $a = 0$ | | |
| $b = 3.72320$ | | |

III. u-Polynomials

| Crossings | u-Polynomials at each crossing |
|------------------|--|
| c_1 | $((u-1)^5)(u^{41} + 44u^{40} + \dots + 2355u + 1)$ |
| c_2 | $((u-1)^5)(u^{41} - 6u^{40} + \dots + 47u - 1)$ |
| c_3, c_6 | $u^5(u^{41} + 7u^{40} + \dots + 64u + 32)$ |
| c_4 | $((u+1)^5)(u^{41} - 6u^{40} + \dots + 47u - 1)$ |
| c_5 | $(u^5 - u^4 + 4u^3 - 3u^2 + 3u - 1)(u^{41} - 2u^{40} + \dots + u - 1)$ |
| c_7 | $(u^5 - u^4 + u^2 + u - 1)(u^{41} + 2u^{40} + \dots - 5u - 1)$ |
| c_8 | $(u^5 + u^4 + 4u^3 + 3u^2 + 3u + 1)(u^{41} - 2u^{40} + \dots + u - 1)$ |
| c_9 | $(u^5 - u^4 + 4u^3 - 3u^2 + 3u - 1)(u^{41} + 12u^{40} + \dots + 9u + 1)$ |
| c_{10} | $(u^5 + u^4 - u^2 + u + 1)(u^{41} + 2u^{40} + \dots - 5u - 1)$ |
| c_{11}, c_{12} | $(u^5 + u^4 + 4u^3 + 3u^2 + 3u + 1)(u^{41} + 12u^{40} + \dots + 9u + 1)$ |

IV. Riley Polynomials

| Crossings | Riley Polynomials at each crossing |
|-----------------------|---|
| c_1 | $((y - 1)^5)(y^{41} - 88y^{40} + \dots + 5466307y - 1)$ |
| c_2, c_4 | $((y - 1)^5)(y^{41} - 44y^{40} + \dots + 2355y - 1)$ |
| c_3, c_6 | $y^5(y^{41} + 33y^{40} + \dots + 49664y - 1024)$ |
| c_5, c_8 | $(y^5 + 7y^4 + 16y^3 + 13y^2 + 3y - 1)(y^{41} + 42y^{39} + \dots + 9y - 1)$ |
| c_7, c_{10} | $(y^5 - y^4 + 4y^3 - 3y^2 + 3y - 1)(y^{41} - 12y^{40} + \dots + 9y - 1)$ |
| c_9, c_{11}, c_{12} | $(y^5 + 7y^4 + 16y^3 + 13y^2 + 3y - 1)(y^{41} + 36y^{40} + \dots + 145y - 1)$ |