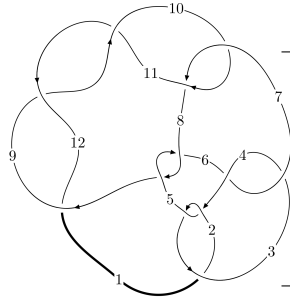
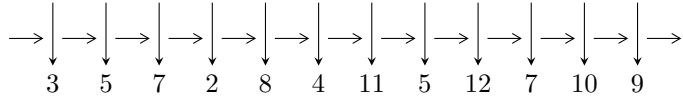


12n₀₀₉₆ (K12n₀₀₉₆)



A knot diagram¹

Linearized knot diagram



Solving Sequence

$$7, 11 \xrightarrow{c_7} 4, 8 \xrightarrow{c_3} 3 \xrightarrow{c_6} 6 \xrightarrow{c_5} 5 \xrightarrow{c_2} 2 \xrightarrow{c_1} 1 \xrightarrow{c_{10}} 10 \xrightarrow{c_{11}} 12 \xrightarrow{c_9} 9 \rightsquigarrow c_4, c_8, c_{12}$$

Ideals for irreducible components² of X_{par}

$$I_1^u = \langle -4915u^{16} + 20254u^{15} + \dots + 7156b + 9167, -123805u^{16} + 530300u^{15} + \dots + 7156a + 154261, u^{17} - 5u^{16} + \dots - 9u + 1 \rangle$$

$$I_2^u = \langle u^2 + b, a + u + 2, u^3 + u^2 - 1 \rangle$$

$$I_3^u = \langle b, 3u^4 - u^3 - u^2 + a + 3u + 4, u^5 - u^4 + u^2 + u - 1 \rangle$$

$$I_4^u = \langle -3u^2a - 2au - 4u^2 + 5b - a - u + 2, a^2 + 2u^2 + a + 2u, u^3 + u^2 - 1 \rangle$$

* 4 irreducible components of $\dim_{\mathbb{C}} = 0$, with total 31 representations.

¹The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

²All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\mathbf{I. } I_1^u = \langle -4915u^{16} + 20254u^{15} + \dots + 7156b + 9167, -1.24 \times 10^5 u^{16} + 5.30 \times 10^5 u^{15} + \dots + 7156a + 1.54 \times 10^5, u^{17} - 5u^{16} + \dots - 9u + 1 \rangle$$

(i) Arc colorings

$$a_7 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 17.3009u^{16} - 74.1056u^{15} + \dots + 179.512u - 21.5569 \\ 0.686836u^{16} - 2.83035u^{15} + \dots + 5.34754u - 1.28102 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 17.9877u^{16} - 76.9360u^{15} + \dots + 184.860u - 22.8379 \\ 0.686836u^{16} - 2.83035u^{15} + \dots + 5.34754u - 1.28102 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -4.26593u^{16} + 18.3215u^{15} + \dots - 48.9090u + 8.75545 \\ -0.297652u^{16} + 1.56051u^{15} + \dots - 5.66867u + 0.378144 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -2.46297u^{16} + 10.6539u^{15} + \dots - 31.7707u + 6.12549 \\ 0.563164u^{16} - 2.41965u^{15} + \dots + 4.65246u - 0.968977 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 18.8118u^{16} - 80.6283u^{15} + \dots + 197.318u - 25.5869 \\ 0.563164u^{16} - 2.41965u^{15} + \dots + 4.65246u - 0.968977 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} u^7 + 2u^3 \\ u^7 - u^5 + 2u^3 - u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} u \\ u \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -u^3 \\ -u^3 + u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} u^5 + u \\ u^5 - u^3 + u \end{pmatrix}$$

(ii) Obstruction class = -1

$$\text{(iii) Cusp Shapes} = -\frac{440209}{1789}u^{16} + \frac{7557829}{7156}u^{15} + \dots - \frac{18828293}{7156}u + \frac{602132}{1789}$$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1	$u^{17} + 25u^{16} + \dots + 349u + 1$
c_2, c_4	$u^{17} - 9u^{16} + \dots - 23u - 1$
c_3, c_6	$u^{17} - 4u^{16} + \dots - 808u^2 + 32$
c_5, c_8	$u^{17} - 9u^{16} + \dots + 1536u + 512$
c_7, c_{10}	$u^{17} + 5u^{16} + \dots - 9u - 1$
c_9, c_{11}, c_{12}	$u^{17} + 9u^{16} + \dots + 19u + 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1	$y^{17} - 57y^{16} + \dots + 110253y - 1$
c_2, c_4	$y^{17} - 25y^{16} + \dots + 349y - 1$
c_3, c_6	$y^{17} - 48y^{16} + \dots + 51712y - 1024$
c_5, c_8	$y^{17} - 49y^{16} + \dots + 4063232y - 262144$
c_7, c_{10}	$y^{17} - 9y^{16} + \dots + 19y - 1$
c_9, c_{11}, c_{12}	$y^{17} + 3y^{16} + \dots - 149y - 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.838900 + 0.274006I$ $a = -0.541331 + 1.242290I$ $b = 0.022802 + 1.171600I$	$1.70067 + 3.40197I$	$-9.83492 - 9.12548I$
$u = -0.838900 - 0.274006I$ $a = -0.541331 - 1.242290I$ $b = 0.022802 - 1.171600I$	$1.70067 - 3.40197I$	$-9.83492 + 9.12548I$
$u = -0.888050 + 0.699587I$ $a = 0.963662 + 0.607402I$ $b = 0.599165 + 0.085043I$	$2.22871 + 2.69541I$	$-2.36795 - 0.48316I$
$u = -0.888050 - 0.699587I$ $a = 0.963662 - 0.607402I$ $b = 0.599165 - 0.085043I$	$2.22871 - 2.69541I$	$-2.36795 + 0.48316I$
$u = 0.702958$ $a = 8.08327$ $b = 0.212168$	-2.60036	-117.690
$u = 0.638788 + 1.195210I$ $a = -0.615352 + 0.257656I$ $b = 2.18853 - 1.40547I$	$-10.83360 + 4.83632I$	$-9.98493 - 0.99160I$
$u = 0.638788 - 1.195210I$ $a = -0.615352 - 0.257656I$ $b = 2.18853 + 1.40547I$	$-10.83360 - 4.83632I$	$-9.98493 + 0.99160I$
$u = 0.932524 + 0.992733I$ $a = 0.024900 + 0.723358I$ $b = -1.316500 - 0.396988I$	$8.46454 - 3.58781I$	$-11.43442 + 3.20089I$
$u = 0.932524 - 0.992733I$ $a = 0.024900 - 0.723358I$ $b = -1.316500 + 0.396988I$	$8.46454 + 3.58781I$	$-11.43442 - 3.20089I$
$u = 0.596043$ $a = 0.723994$ $b = -0.233910$	-0.842519	-11.7040

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.18905 + 0.84637I$	$-12.6169 - 12.0697I$	$-10.79554 + 4.97668I$
$a = 1.44006 - 1.34507I$		
$b = 1.69244 + 1.67258I$		
$u = 1.18905 - 0.84637I$	$-12.6169 + 12.0697I$	$-10.79554 - 4.97668I$
$a = 1.44006 + 1.34507I$		
$b = 1.69244 - 1.67258I$		
$u = 1.45050 + 0.33561I$	$-4.97113 - 2.77667I$	$-12.19520 + 1.72835I$
$a = -1.67908 + 1.23512I$		
$b = -2.95952 + 0.58336I$		
$u = 1.45050 - 0.33561I$	$-4.97113 + 2.77667I$	$-12.19520 - 1.72835I$
$a = -1.67908 - 1.23512I$		
$b = -2.95952 - 0.58336I$		
$u = 0.248594 + 0.150644I$	$-0.943827 + 0.013133I$	$-9.47910 + 0.58994I$
$a = 1.39946 - 0.69681I$		
$b = -0.634067 + 0.017100I$		
$u = 0.248594 - 0.150644I$	$-0.943827 - 0.013133I$	$-9.47910 - 0.58994I$
$a = 1.39946 + 0.69681I$		
$b = -0.634067 - 0.017100I$		
$u = -1.76401$	19.2915	-12.4240
$a = 2.20808$		
$b = 4.83602$		

$$\text{II. } I_2^u = \langle u^2 + b, a + u + 2, u^3 + u^2 - 1 \rangle$$

(i) Arc colorings

$$a_7 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -u - 2 \\ -u^2 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -u^2 - u - 2 \\ -u^2 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -u^2 \\ -u^2 - u + 1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -u^2 \\ -u^2 - u + 1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -2u^2 - u - 1 \\ -u^2 - u + 1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} u \\ u \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} u^2 - 1 \\ u^2 + u - 1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = $2u^2 - 5u - 14$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1, c_3, c_9	$u^3 - u^2 + 2u - 1$
c_2, c_7	$u^3 + u^2 - 1$
c_4, c_{10}	$u^3 - u^2 + 1$
c_5, c_8	u^3
c_6, c_{11}, c_{12}	$u^3 + u^2 + 2u + 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1, c_3, c_6 c_9, c_{11}, c_{12}	$y^3 + 3y^2 + 2y - 1$
c_2, c_4, c_7 c_{10}	$y^3 - y^2 + 2y - 1$
c_5, c_8	y^3

(vi) Complex Volumes and Cusp Shapes

Solutions to I_2^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.877439 + 0.744862I$ $a = -1.122560 - 0.744862I$ $b = -0.215080 + 1.307140I$	$6.04826 + 5.65624I$	$-9.18265 - 6.33859I$
$u = -0.877439 - 0.744862I$ $a = -1.122560 + 0.744862I$ $b = -0.215080 - 1.307140I$	$6.04826 - 5.65624I$	$-9.18265 + 6.33859I$
$u = 0.754878$ $a = -2.75488$ $b = -0.569840$	-2.22691	-16.6350

$$\text{III. } I_3^u = \langle b, 3u^4 - u^3 - u^2 + a + 3u + 4, u^5 - u^4 + u^2 + u - 1 \rangle$$

(i) Arc colorings

$$a_7 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -3u^4 + u^3 + u^2 - 3u - 4 \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -3u^4 + u^3 + u^2 - 3u - 4 \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -u^2 + 1 \\ -u^4 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -3u^4 + u^3 + 2u^2 - 3u - 5 \\ u^4 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} u^2 - 1 \\ u^4 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} u \\ u \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -u^3 \\ -u^3 + u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} u^4 - u^2 + 1 \\ u^4 - u^3 - u^2 + 1 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = $10u^4 - 7u^3 + u^2 + 10u + 7$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1, c_2	$(u - 1)^5$
c_3, c_6	u^5
c_4	$(u + 1)^5$
c_5, c_9	$u^5 - u^4 + 4u^3 - 3u^2 + 3u - 1$
c_7	$u^5 - u^4 + u^2 + u - 1$
c_8, c_{11}, c_{12}	$u^5 + u^4 + 4u^3 + 3u^2 + 3u + 1$
c_{10}	$u^5 + u^4 - u^2 + u + 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1, c_2, c_4	$(y - 1)^5$
c_3, c_6	y^5
c_5, c_8, c_9 c_{11}, c_{12}	$y^5 + 7y^4 + 16y^3 + 13y^2 + 3y - 1$
c_7, c_{10}	$y^5 - y^4 + 4y^3 - 3y^2 + 3y - 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to I_3^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.758138 + 0.584034I$ $a = 1.036940 - 0.588205I$ $b = 0$	$0.17487 + 2.21397I$	$-10.02401 - 4.83884I$
$u = -0.758138 - 0.584034I$ $a = 1.036940 + 0.588205I$ $b = 0$	$0.17487 - 2.21397I$	$-10.02401 + 4.83884I$
$u = 0.935538 + 0.903908I$ $a = 0.348360 + 0.023996I$ $b = 0$	$9.31336 - 3.33174I$	$-1.83654 + 1.25445I$
$u = 0.935538 - 0.903908I$ $a = 0.348360 - 0.023996I$ $b = 0$	$9.31336 + 3.33174I$	$-1.83654 - 1.25445I$
$u = 0.645200$ $a = -5.77061$ $b = 0$	-2.52712	13.7210

$$\text{IV. } I_4^u = \langle -3u^2a - 2au - 4u^2 + 5b - a - u + 2, a^2 + 2u^2 + a + 2u, u^3 + u^2 - 1 \rangle$$

(i) Arc colorings

$$a_7 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} a \\ \frac{3}{5}u^2a + \frac{4}{5}u^2 + \cdots + \frac{1}{5}a - \frac{2}{5} \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} \frac{3}{5}u^2a + \frac{4}{5}u^2 + \cdots + \frac{6}{5}a - \frac{2}{5} \\ \frac{3}{5}u^2a + \frac{4}{5}u^2 + \cdots + \frac{1}{5}a - \frac{3}{5} \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -\frac{1}{5}u^2a + \frac{2}{5}u^2 + \cdots + \frac{3}{5}a + \frac{9}{5} \\ \frac{1}{5}u^2a + \frac{3}{5}u^2 + \cdots + \frac{2}{5}a + \frac{6}{5} \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -\frac{1}{5}u^2a + \frac{2}{5}u^2 + \cdots + \frac{3}{5}a + \frac{9}{5} \\ \frac{1}{5}u^2a + \frac{3}{5}u^2 + \cdots + \frac{2}{5}a + \frac{6}{5} \end{pmatrix}$$

$$a_2 = \begin{pmatrix} u^2 + a + 2u + 1 \\ \frac{1}{5}u^2a + \frac{3}{5}u^2 + \cdots + \frac{2}{5}a + \frac{6}{5} \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} u \\ u \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} u^2 - 1 \\ u^2 + u - 1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

(ii) Obstruction class = 1

$$\text{(iii) Cusp Shapes} = -\frac{13}{5}u^2a - \frac{17}{5}au + \frac{26}{5}u^2 + \frac{29}{5}a + \frac{24}{5}u - \frac{58}{5}$$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1, c_3, c_9	$(u^3 - u^2 + 2u - 1)^2$
c_2, c_7	$(u^3 + u^2 - 1)^2$
c_4, c_{10}	$(u^3 - u^2 + 1)^2$
c_5, c_8	u^6
c_6, c_{11}, c_{12}	$(u^3 + u^2 + 2u + 1)^2$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1, c_3, c_6 c_9, c_{11}, c_{12}	$(y^3 + 3y^2 + 2y - 1)^2$
c_2, c_4, c_7 c_{10}	$(y^3 - y^2 + 2y - 1)^2$
c_5, c_8	y^6

(vi) Complex Volumes and Cusp Shapes

Solutions to I_4^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.877439 + 0.744862I$ $a = 0.824718 + 0.424452I$ $b = -0.215080 - 1.307140I$	6.04826	$-8.27833 + 0.98317I$
$u = -0.877439 + 0.744862I$ $a = -1.82472 - 0.42445I$ $b = -0.569840$	$1.91067 + 2.82812I$	$-29.3323 - 8.2928I$
$u = -0.877439 - 0.744862I$ $a = 0.824718 - 0.424452I$ $b = -0.215080 + 1.307140I$	6.04826	$-8.27833 - 0.98317I$
$u = -0.877439 - 0.744862I$ $a = -1.82472 + 0.42445I$ $b = -0.569840$	$1.91067 - 2.82812I$	$-29.3323 + 8.2928I$
$u = 0.754878$ $a = -0.50000 + 1.54901I$ $b = -0.215080 + 1.307140I$	$1.91067 + 2.82812I$	$-5.88933 + 2.71361I$
$u = 0.754878$ $a = -0.50000 - 1.54901I$ $b = -0.215080 - 1.307140I$	$1.91067 - 2.82812I$	$-5.88933 - 2.71361I$

V. u-Polynomials

Crossings	u-Polynomials at each crossing
c_1	$((u-1)^5)(u^3-u^2+2u-1)^3(u^{17}+25u^{16}+\dots+349u+1)$
c_2	$((u-1)^5)(u^3+u^2-1)^3(u^{17}-9u^{16}+\dots-23u-1)$
c_3	$u^5(u^3-u^2+2u-1)^3(u^{17}-4u^{16}+\dots-808u^2+32)$
c_4	$((u+1)^5)(u^3-u^2+1)^3(u^{17}-9u^{16}+\dots-23u-1)$
c_5	$u^9(u^5-u^4+\dots+3u-1)(u^{17}-9u^{16}+\dots+1536u+512)$
c_6	$u^5(u^3+u^2+2u+1)^3(u^{17}-4u^{16}+\dots-808u^2+32)$
c_7	$((u^3+u^2-1)^3)(u^5-u^4+u^2+u-1)(u^{17}+5u^{16}+\dots-9u-1)$
c_8	$u^9(u^5+u^4+\dots+3u+1)(u^{17}-9u^{16}+\dots+1536u+512)$
c_9	$(u^3-u^2+2u-1)^3(u^5-u^4+4u^3-3u^2+3u-1)$ $\cdot (u^{17}+9u^{16}+\dots+19u+1)$
c_{10}	$((u^3-u^2+1)^3)(u^5+u^4-u^2+u+1)(u^{17}+5u^{16}+\dots-9u-1)$
c_{11}, c_{12}	$(u^3+u^2+2u+1)^3(u^5+u^4+4u^3+3u^2+3u+1)$ $\cdot (u^{17}+9u^{16}+\dots+19u+1)$

VI. Riley Polynomials

Crossings	Riley Polynomials at each crossing
c_1	$((y - 1)^5)(y^3 + 3y^2 + 2y - 1)^3(y^{17} - 57y^{16} + \dots + 110253y - 1)$
c_2, c_4	$((y - 1)^5)(y^3 - y^2 + 2y - 1)^3(y^{17} - 25y^{16} + \dots + 349y - 1)$
c_3, c_6	$y^5(y^3 + 3y^2 + 2y - 1)^3(y^{17} - 48y^{16} + \dots + 51712y - 1024)$
c_5, c_8	$y^9(y^5 + 7y^4 + 16y^3 + 13y^2 + 3y - 1)$ $\cdot (y^{17} - 49y^{16} + \dots + 4063232y - 262144)$
c_7, c_{10}	$(y^3 - y^2 + 2y - 1)^3(y^5 - y^4 + 4y^3 - 3y^2 + 3y - 1)$ $\cdot (y^{17} - 9y^{16} + \dots + 19y - 1)$
c_9, c_{11}, c_{12}	$(y^3 + 3y^2 + 2y - 1)^3(y^5 + 7y^4 + 16y^3 + 13y^2 + 3y - 1)$ $\cdot (y^{17} + 3y^{16} + \dots - 149y - 1)$