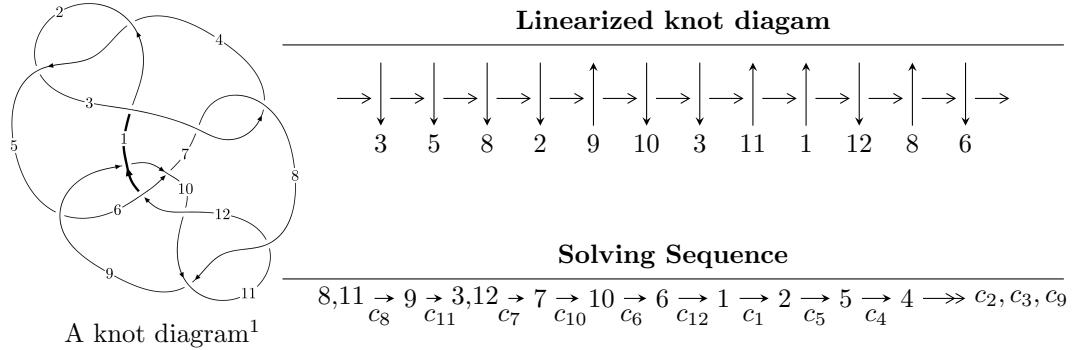


## $12n_{0099}$ ( $K12n_{0099}$ )



### Ideals for irreducible components<sup>2</sup> of $X_{\text{par}}$

$$\begin{aligned}
 I_1^u &= \langle -5.67717 \times 10^{122} u^{80} + 2.40640 \times 10^{123} u^{79} + \dots + 1.36344 \times 10^{123} b - 1.28567 \times 10^{122}, \\
 &\quad - 1.49380 \times 10^{122} u^{80} + 9.63422 \times 10^{122} u^{79} + \dots + 6.81720 \times 10^{122} a - 3.22718 \times 10^{124}, \\
 &\quad u^{81} - 4u^{80} + \dots + 83u + 1 \rangle \\
 I_2^u &= \langle b, -u^3 + a - 2, u^4 + u^2 + u + 1 \rangle \\
 I_3^u &= \langle b, -u^3 + u^2 + a - 2u + 1, u^6 - u^5 + 2u^4 - 2u^3 + 2u^2 - 2u + 1 \rangle \\
 I_4^u &= \langle -au + b + 2u, a^2 + au - 3a - 3u + 2, u^2 + u + 1 \rangle
 \end{aligned}$$

\* 4 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 95 representations.

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<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/math/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\text{I. } I_1^u = \langle -5.68 \times 10^{122}u^{80} + 2.41 \times 10^{123}u^{79} + \dots + 1.36 \times 10^{123}b - 1.29 \times 10^{122}, -1.49 \times 10^{122}u^{80} + 9.63 \times 10^{122}u^{79} + \dots + 6.82 \times 10^{122}a - 3.23 \times 10^{124}, u^{81} - 4u^{80} + \dots + 83u + 1 \rangle$$

(i) **Arc colorings**

$$a_8 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 0.219123u^{80} - 1.41322u^{79} + \dots + 157.415u + 47.3388 \\ 0.416386u^{80} - 1.76495u^{79} + \dots - 43.2149u + 0.0942957 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} u \\ u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -0.327866u^{80} + 1.87240u^{79} + \dots - 62.8797u - 27.5857 \\ -0.435511u^{80} + 1.87462u^{79} + \dots + 47.9628u + 0.199503 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} u^3 \\ u^3 + u \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -0.236666u^{80} + 1.65002u^{79} + \dots - 61.3415u - 27.5686 \\ -0.457531u^{80} + 2.08795u^{79} + \dots + 57.2670u + 0.314050 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 0.253925u^{80} - 0.469551u^{79} + \dots + 57.0053u + 9.60025 \\ -0.376132u^{80} + 1.67454u^{79} + \dots + 43.3245u + 0.630057 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 0.0290630u^{80} - 0.406433u^{79} + \dots + 115.361u + 29.5970 \\ 0.334532u^{80} - 1.24445u^{79} + \dots - 23.7001u + 0.0863807 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -0.567784u^{80} + 2.57406u^{79} + \dots - 60.4666u - 27.1793 \\ -0.334532u^{80} + 1.24445u^{79} + \dots + 23.7001u - 0.0863807 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 0.197263u^{80} - 0.351727u^{79} + \dots - 200.629u - 47.2445 \\ -0.416386u^{80} + 1.76495u^{79} + \dots + 43.2149u - 0.0942957 \end{pmatrix}$$

(ii) **Obstruction class = -1**

(iii) **Cusp Shapes** =  $0.523679u^{80} - 1.64827u^{79} + \dots + 61.1096u - 9.44591$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1$	$u^{81} + 33u^{80} + \cdots + 130u + 1$
$c_2, c_4$	$u^{81} - 13u^{80} + \cdots - 12u + 1$
$c_3, c_7$	$u^{81} - 3u^{80} + \cdots + 1024u + 1024$
$c_5$	$u^{81} + u^{80} + \cdots + 8905262u + 2124511$
$c_6$	$u^{81} + 5u^{80} + \cdots - 47488u + 22208$
$c_8, c_{11}$	$u^{81} + 4u^{80} + \cdots + 83u - 1$
$c_9$	$u^{81} + 8u^{80} + \cdots + 256u + 16$
$c_{10}$	$u^{81} + 30u^{80} + \cdots + 6303u - 1$
$c_{12}$	$u^{81} - 4u^{80} + \cdots - 5u + 1$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1$	$y^{81} + 43y^{80} + \cdots + 5274y - 1$
$c_2, c_4$	$y^{81} - 33y^{80} + \cdots + 130y - 1$
$c_3, c_7$	$y^{81} + 57y^{80} + \cdots - 27787264y - 1048576$
$c_5$	$y^{81} + 47y^{80} + \cdots + 59668081079090y - 4513546989121$
$c_6$	$y^{81} + 103y^{80} + \cdots - 19451522048y - 493195264$
$c_8, c_{11}$	$y^{81} + 30y^{80} + \cdots + 6303y - 1$
$c_9$	$y^{81} - 20y^{80} + \cdots - 1152y - 256$
$c_{10}$	$y^{81} + 46y^{80} + \cdots + 39786411y - 1$
$c_{12}$	$y^{81} - 6y^{80} + \cdots + 11y - 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.505398 + 0.861438I$		
$a = -4.37384 - 2.52183I$	$-1.02453 - 2.05291I$	$-171.972 + 28.532I$
$b = 0.603292 - 0.010555I$		
$u = -0.505398 - 0.861438I$		
$a = -4.37384 + 2.52183I$	$-1.02453 + 2.05291I$	$-171.972 - 28.532I$
$b = 0.603292 + 0.010555I$		
$u = -0.009112 + 1.005390I$		
$a = -0.308654 + 0.203514I$	$-4.60609 - 1.52975I$	0
$b = -0.336499 - 0.810387I$		
$u = -0.009112 - 1.005390I$		
$a = -0.308654 - 0.203514I$	$-4.60609 + 1.52975I$	0
$b = -0.336499 + 0.810387I$		
$u = 0.742803 + 0.679982I$		
$a = -0.167793 + 0.282223I$	$6.21314 - 4.26930I$	0
$b = 0.67879 + 1.59644I$		
$u = 0.742803 - 0.679982I$		
$a = -0.167793 - 0.282223I$	$6.21314 + 4.26930I$	0
$b = 0.67879 - 1.59644I$		
$u = 0.724035 + 0.675293I$		
$a = 1.163810 + 0.739644I$	$0.58736 - 1.68614I$	0
$b = 0.239752 - 1.287670I$		
$u = 0.724035 - 0.675293I$		
$a = 1.163810 - 0.739644I$	$0.58736 + 1.68614I$	0
$b = 0.239752 + 1.287670I$		
$u = -0.264835 + 0.948397I$		
$a = -0.02548 - 2.76624I$	$1.73887 + 0.56914I$	0
$b = 0.086690 - 1.153850I$		
$u = -0.264835 - 0.948397I$		
$a = -0.02548 + 2.76624I$	$1.73887 - 0.56914I$	0
$b = 0.086690 + 1.153850I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.479721 + 0.852602I$		
$a = -1.22325 - 1.39529I$	$-8.92096 + 1.95711I$	$-29.9268 + 41.7453I$
$b = -1.59287 + 0.05128I$		
$u = 0.479721 - 0.852602I$		
$a = -1.22325 + 1.39529I$	$-8.92096 - 1.95711I$	$-29.9268 - 41.7453I$
$b = -1.59287 - 0.05128I$		
$u = -0.615664 + 0.829871I$		
$a = -1.37738 + 1.51974I$	$3.68961 + 0.58365I$	0
$b = 0.154661 - 1.382630I$		
$u = -0.615664 - 0.829871I$		
$a = -1.37738 - 1.51974I$	$3.68961 - 0.58365I$	0
$b = 0.154661 + 1.382630I$		
$u = 0.825094 + 0.624144I$		
$a = -0.916453 - 0.626602I$	$2.74432 - 4.49163I$	0
$b = -1.357180 + 0.050552I$		
$u = 0.825094 - 0.624144I$		
$a = -0.916453 + 0.626602I$	$2.74432 + 4.49163I$	0
$b = -1.357180 - 0.050552I$		
$u = -0.524882 + 0.802233I$		
$a = 4.37321 + 0.45617I$	$-1.11518 - 1.63608I$	$-22.5154 + 16.4209I$
$b = 0.458462 + 0.233945I$		
$u = -0.524882 - 0.802233I$		
$a = 4.37321 - 0.45617I$	$-1.11518 + 1.63608I$	$-22.5154 - 16.4209I$
$b = 0.458462 - 0.233945I$		
$u = 0.703049 + 0.783366I$		
$a = 0.83771 + 1.13988I$	$1.96531 + 1.49483I$	0
$b = 1.42270 + 0.44570I$		
$u = 0.703049 - 0.783366I$		
$a = 0.83771 - 1.13988I$	$1.96531 - 1.49483I$	0
$b = 1.42270 - 0.44570I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.026493 + 0.936757I$	$0.95414 - 4.42889I$	$-4.00000 + 4.19606I$
$a = 0.59780 + 2.29454I$		
$b = 0.439042 + 1.154740I$		
$u = -0.026493 - 0.936757I$		
$a = 0.59780 - 2.29454I$	$0.95414 + 4.42889I$	$-4.00000 - 4.19606I$
$b = 0.439042 - 1.154740I$		
$u = -0.671407 + 0.627762I$		
$a = -0.913409 - 0.028748I$	$1.15026 - 1.50439I$	$2.46877 + 2.61626I$
$b = -0.412488 + 0.213180I$		
$u = -0.671407 - 0.627762I$		
$a = -0.913409 + 0.028748I$	$1.15026 + 1.50439I$	$2.46877 - 2.61626I$
$b = -0.412488 - 0.213180I$		
$u = -0.599484 + 0.904512I$		
$a = 2.63171 - 1.35351I$	$3.45045 - 5.35632I$	0
$b = 0.277078 + 1.371800I$		
$u = -0.599484 - 0.904512I$		
$a = 2.63171 + 1.35351I$	$3.45045 + 5.35632I$	0
$b = 0.277078 - 1.371800I$		
$u = -0.561505 + 0.944951I$		
$a = 1.70785 + 3.15850I$	$-1.63060 - 2.73282I$	0
$b = 0.110600 - 0.423339I$		
$u = -0.561505 - 0.944951I$		
$a = 1.70785 - 3.15850I$	$-1.63060 + 2.73282I$	0
$b = 0.110600 + 0.423339I$		
$u = -0.455620 + 1.013820I$		
$a = -0.238189 + 0.544842I$	$-0.39491 - 2.82152I$	0
$b = 0.029747 + 0.351694I$		
$u = -0.455620 - 1.013820I$		
$a = -0.238189 - 0.544842I$	$-0.39491 + 2.82152I$	0
$b = 0.029747 - 0.351694I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.761415 + 0.820530I$	$8.06491 + 2.92024I$	0
$a = 0.531324 - 0.454947I$		
$b = -0.42765 - 1.74880I$		
$u = 0.761415 - 0.820530I$	$8.06491 - 2.92024I$	0
$a = 0.531324 + 0.454947I$		
$b = -0.42765 + 1.74880I$		
$u = -0.108997 + 1.122070I$	$-3.72961 - 3.73093I$	0
$a = -2.39634 - 0.23797I$		
$b = -0.890661 + 0.321140I$		
$u = -0.108997 - 1.122070I$	$-3.72961 + 3.73093I$	0
$a = -2.39634 + 0.23797I$		
$b = -0.890661 - 0.321140I$		
$u = 0.997287 + 0.541891I$	$7.29123 - 11.70270I$	0
$a = -0.369368 - 0.079618I$		
$b = -0.66734 - 1.50573I$		
$u = 0.997287 - 0.541891I$	$7.29123 + 11.70270I$	0
$a = -0.369368 + 0.079618I$		
$b = -0.66734 + 1.50573I$		
$u = 0.959008 + 0.624962I$	$9.10043 - 4.86820I$	0
$a = -0.148070 + 0.092204I$		
$b = 0.36850 + 1.64315I$		
$u = 0.959008 - 0.624962I$	$9.10043 + 4.86820I$	0
$a = -0.148070 - 0.092204I$		
$b = 0.36850 - 1.64315I$		
$u = 0.682699 + 0.926132I$	$1.52644 + 3.83350I$	0
$a = 1.43843 + 0.92415I$		
$b = 1.54169 - 0.19466I$		
$u = 0.682699 - 0.926132I$	$1.52644 - 3.83350I$	0
$a = 1.43843 - 0.92415I$		
$b = 1.54169 + 0.19466I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.745953 + 0.906662I$		
$a = -1.80870 - 0.05187I$	$7.80552 + 2.77364I$	0
$b = -0.63390 + 1.61836I$		
$u = 0.745953 - 0.906662I$		
$a = -1.80870 + 0.05187I$	$7.80552 - 2.77364I$	0
$b = -0.63390 - 1.61836I$		
$u = -0.714581 + 0.401247I$		
$a = -1.165920 - 0.348917I$	$1.29375 - 1.45245I$	$3.62930 + 4.86424I$
$b = -0.616988 - 0.161976I$		
$u = -0.714581 - 0.401247I$		
$a = -1.165920 + 0.348917I$	$1.29375 + 1.45245I$	$3.62930 - 4.86424I$
$b = -0.616988 + 0.161976I$		
$u = 0.062348 + 0.798476I$		
$a = 1.53880 + 1.10941I$	$-2.15630 + 0.07606I$	$-8.00350 + 0.07144I$
$b = 0.880183 - 0.328930I$		
$u = 0.062348 - 0.798476I$		
$a = 1.53880 - 1.10941I$	$-2.15630 - 0.07606I$	$-8.00350 - 0.07144I$
$b = 0.880183 + 0.328930I$		
$u = 0.675941 + 0.993873I$		
$a = -0.976588 - 0.077747I$	$-0.36837 + 7.06216I$	0
$b = 0.00539 + 1.42943I$		
$u = 0.675941 - 0.993873I$		
$a = -0.976588 + 0.077747I$	$-0.36837 - 7.06216I$	0
$b = 0.00539 - 1.42943I$		
$u = 0.680506 + 0.995566I$		
$a = 2.16987 + 0.15146I$	$5.25967 + 9.70670I$	0
$b = 0.83647 - 1.48482I$		
$u = 0.680506 - 0.995566I$		
$a = 2.16987 - 0.15146I$	$5.25967 - 9.70670I$	0
$b = 0.83647 + 1.48482I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.753433 + 0.220803I$	$-1.20619 - 3.00339I$	$2.21341 + 3.98452I$
$a = -0.235608 + 0.164102I$		
$b = 0.020461 + 0.617454I$		
$u = 0.753433 - 0.220803I$	$-1.20619 + 3.00339I$	$2.21341 - 3.98452I$
$a = -0.235608 - 0.164102I$		
$b = 0.020461 - 0.617454I$		
$u = 0.292757 + 1.184200I$	$-5.47007 + 0.37522I$	0
$a = -0.573258 + 0.779271I$		
$b = -0.077263 + 0.631820I$		
$u = 0.292757 - 1.184200I$	$-5.47007 - 0.37522I$	0
$a = -0.573258 - 0.779271I$		
$b = -0.077263 - 0.631820I$		
$u = -1.152240 + 0.412570I$	$7.13557 + 1.25582I$	0
$a = -0.130976 + 0.209918I$		
$b = -0.16545 + 1.48707I$		
$u = -1.152240 - 0.412570I$	$7.13557 - 1.25582I$	0
$a = -0.130976 - 0.209918I$		
$b = -0.16545 - 1.48707I$		
$u = -0.684988 + 1.023750I$	$-0.12016 - 3.83503I$	0
$a = -1.51416 + 0.44312I$		
$b = -0.757611 + 0.003546I$		
$u = -0.684988 - 1.023750I$	$-0.12016 + 3.83503I$	0
$a = -1.51416 - 0.44312I$		
$b = -0.757611 - 0.003546I$		
$u = 0.703453 + 1.042720I$	$1.48186 + 10.21890I$	0
$a = -1.25123 - 1.15161I$		
$b = -1.45915 - 0.22710I$		
$u = 0.703453 - 1.042720I$	$1.48186 - 10.21890I$	0
$a = -1.25123 + 1.15161I$		
$b = -1.45915 + 0.22710I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.532163 + 1.140700I$		
$a = 0.456393 - 0.597727I$	$-3.86039 + 7.78753I$	0
$b = 0.060321 - 0.542689I$		
$u = 0.532163 - 1.140700I$		
$a = 0.456393 + 0.597727I$	$-3.86039 - 7.78753I$	0
$b = 0.060321 + 0.542689I$		
$u = -1.138710 + 0.566751I$		
$a = -0.479445 - 0.126460I$	$6.96738 - 5.09561I$	0
$b = -0.25605 - 1.48232I$		
$u = -1.138710 - 0.566751I$		
$a = -0.479445 + 0.126460I$	$6.96738 + 5.09561I$	0
$b = -0.25605 + 1.48232I$		
$u = 0.752599 + 1.093140I$		
$a = 1.79634 - 0.18613I$	$7.63873 + 11.12540I$	0
$b = 0.51625 - 1.63587I$		
$u = 0.752599 - 1.093140I$		
$a = 1.79634 + 0.18613I$	$7.63873 - 11.12540I$	0
$b = 0.51625 + 1.63587I$		
$u = -0.240383 + 1.329020I$		
$a = 0.39785 + 1.40917I$	$0.90648 - 3.26112I$	0
$b = 0.123794 + 1.279290I$		
$u = -0.240383 - 1.329020I$		
$a = 0.39785 - 1.40917I$	$0.90648 + 3.26112I$	0
$b = 0.123794 - 1.279290I$		
$u = 0.729533 + 1.141910I$		
$a = -2.16101 + 0.00371I$	$5.4200 + 17.9748I$	0
$b = -0.75699 + 1.47497I$		
$u = 0.729533 - 1.141910I$		
$a = -2.16101 - 0.00371I$	$5.4200 - 17.9748I$	0
$b = -0.75699 - 1.47497I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.100629 + 1.380790I$		
$a = -1.09077 - 1.42258I$	$-0.35544 - 9.04141I$	0
$b = -0.50450 - 1.33076I$		
$u = -0.100629 - 1.380790I$		
$a = -1.09077 + 1.42258I$	$-0.35544 + 9.04141I$	0
$b = -0.50450 + 1.33076I$		
$u = -0.87285 + 1.14057I$		
$a = 0.715969 + 0.518957I$	$5.23560 - 2.02485I$	0
$b = -0.05609 + 1.43328I$		
$u = -0.87285 - 1.14057I$		
$a = 0.715969 - 0.518957I$	$5.23560 + 2.02485I$	0
$b = -0.05609 - 1.43328I$		
$u = -0.80039 + 1.23078I$		
$a = -1.41250 - 0.47345I$	$4.66300 - 8.19652I$	0
$b = -0.35709 - 1.43000I$		
$u = -0.80039 - 1.23078I$		
$a = -1.41250 + 0.47345I$	$4.66300 + 8.19652I$	0
$b = -0.35709 + 1.43000I$		
$u = -0.455946 + 0.115914I$		
$a = -0.197228 + 1.245260I$	$4.09035 - 3.09672I$	$-6.42475 + 2.99947I$
$b = 0.21037 + 1.44375I$		
$u = -0.455946 - 0.115914I$		
$a = -0.197228 - 1.245260I$	$4.09035 + 3.09672I$	$-6.42475 - 2.99947I$
$b = 0.21037 - 1.44375I$		
$u = -0.293387 + 0.220524I$		
$a = 4.39202 + 0.48966I$	$-1.004280 - 0.810007I$	$-4.84130 - 2.46574I$
$b = 0.455347 - 0.441128I$		
$u = -0.293387 - 0.220524I$		
$a = 4.39202 - 0.48966I$	$-1.004280 + 0.810007I$	$-4.84130 + 2.46574I$
$b = 0.455347 + 0.441128I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.0125912$		
$a = 45.4131$	-1.00318	-10.1710
$b = 0.612334$		

$$\text{II. } I_2^u = \langle b, -u^3 + a - 2, u^4 + u^2 + u + 1 \rangle$$

(i) Arc colorings

$$a_8 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} u^3 + 2 \\ 0 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} u \\ u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} u^3 \\ u^3 + u \end{pmatrix}$$

$$a_6 = \begin{pmatrix} u^3 + u^2 + 1 \\ u^3 + u^2 + u + 1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -u^3 - u^2 - u - 1 \\ -u^2 - u - 1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -u^2 - u + 1 \\ -u^2 - u - 1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} u^3 + u^2 + u + 1 \\ u^2 + u + 1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} u^3 + 2 \\ 0 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes =  $9u^3 - 2u^2 + 2u - 1$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_2$	$(u - 1)^4$
$c_3, c_7$	$u^4$
$c_4$	$(u + 1)^4$
$c_5, c_8, c_9$	$u^4 + u^2 + u + 1$
$c_6$	$u^4 + 3u^3 + 4u^2 + 3u + 2$
$c_{10}$	$u^4 - 2u^3 + 3u^2 - u + 1$
$c_{11}$	$u^4 + u^2 - u + 1$
$c_{12}$	$u^4 + 2u^3 + 3u^2 + u + 1$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_4$	$(y - 1)^4$
$c_3, c_7$	$y^4$
$c_5, c_8, c_9$ $c_{11}$	$y^4 + 2y^3 + 3y^2 + y + 1$
$c_6$	$y^4 - y^3 + 2y^2 + 7y + 4$
$c_{10}, c_{12}$	$y^4 + 2y^3 + 7y^2 + 5y + 1$

**(vi) Complex Volumes and Cusp Shapes**

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.547424 + 0.585652I$		
$a = 2.39923 + 0.32564I$	$-0.66484 - 1.39709I$	$1.58487 + 5.38446I$
$b = 0$		
$u = -0.547424 - 0.585652I$		
$a = 2.39923 - 0.32564I$	$-0.66484 + 1.39709I$	$1.58487 - 5.38446I$
$b = 0$		
$u = 0.547424 + 1.120870I$		
$a = 0.100768 - 0.400532I$	$-4.26996 + 7.64338I$	$-15.0849 - 3.8174I$
$b = 0$		
$u = 0.547424 - 1.120870I$		
$a = 0.100768 + 0.400532I$	$-4.26996 - 7.64338I$	$-15.0849 + 3.8174I$
$b = 0$		

$$\text{III. } I_3^u = \langle b, -u^3 + u^2 + a - 2u + 1, u^6 - u^5 + 2u^4 - 2u^3 + 2u^2 - 2u + 1 \rangle$$

(i) Arc colorings

$$a_8 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} u^3 - u^2 + 2u - 1 \\ 0 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} u \\ u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} u^3 \\ u^3 + u \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -u^5 + u^4 - 2u^3 + 2u^2 - 2u + 2 \\ -u^5 - 2u^3 + u^2 - 2u + 1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -u^4 - u^2 + u - 1 \\ 2u^5 - u^4 + 3u^3 - 2u^2 + 3u - 2 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -u^4 + u^3 - 2u^2 + 3u - 2 \\ 2u^5 - u^4 + 3u^3 - 2u^2 + 3u - 2 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} u^4 + u^2 - u + 1 \\ -2u^5 + u^4 - 3u^3 + 2u^2 - 3u + 2 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} u^3 - u^2 + 2u - 1 \\ 0 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes =  $-u^5 + u^4 + 2u^2 + 3u - 12$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_2$	$(u - 1)^6$
$c_3, c_7$	$u^6$
$c_4$	$(u + 1)^6$
$c_5, c_8, c_9$	$u^6 - u^5 + 2u^4 - 2u^3 + 2u^2 - 2u + 1$
$c_6$	$(u^3 - u^2 + 1)^2$
$c_{10}$	$u^6 - 3u^5 + 4u^4 - 2u^3 + 1$
$c_{11}$	$u^6 + u^5 + 2u^4 + 2u^3 + 2u^2 + 2u + 1$
$c_{12}$	$u^6 + 3u^5 + 4u^4 + 2u^3 + 1$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_4$	$(y - 1)^6$
$c_3, c_7$	$y^6$
$c_5, c_8, c_9$ $c_{11}$	$y^6 + 3y^5 + 4y^4 + 2y^3 + 1$
$c_6$	$(y^3 - y^2 + 2y - 1)^2$
$c_{10}, c_{12}$	$y^6 - y^5 + 4y^4 - 2y^3 + 8y^2 + 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.498832 + 1.001300I$		
$a = 0.13238 + 2.74513I$	$-1.91067 - 2.82812I$	$-14.1402 + 3.6935I$
$b = 0$		
$u = -0.498832 - 1.001300I$		
$a = 0.13238 - 2.74513I$	$-1.91067 + 2.82812I$	$-14.1402 - 3.6935I$
$b = 0$		
$u = 0.284920 + 1.115140I$		
$a = -0.307599 + 0.479689I$	$-6.04826$	$-14.4399 + 2.5036I$
$b = 0$		
$u = 0.284920 - 1.115140I$		
$a = -0.307599 - 0.479689I$	$-6.04826$	$-14.4399 - 2.5036I$
$b = 0$		
$u = 0.713912 + 0.305839I$		
$a = 0.175218 + 0.614017I$	$-1.91067 - 2.82812I$	$-8.91986 + 1.90022I$
$b = 0$		
$u = 0.713912 - 0.305839I$		
$a = 0.175218 - 0.614017I$	$-1.91067 + 2.82812I$	$-8.91986 - 1.90022I$
$b = 0$		

$$\text{IV. } I_4^u = \langle -au + b + 2u, a^2 + au - 3a - 3u + 2, u^2 + u + 1 \rangle$$

(i) Arc colorings

$$a_8 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ u+1 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} a \\ au - 2u \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} u \\ u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -2au - a + 5u + 4 \\ -au + 2u - 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ u+1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -2au - 2a + 3u + 4 \\ -2au - a + 2u + 1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -3au - 3a + 8u + 6 \\ -3au + 6u - 2 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -au - a + 3u + 3 \\ -au + 2u - 1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -2au - a + 5u + 4 \\ -au + 2u - 1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -au + a + 2u \\ au - 2u \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes =  $-21au - 42a + 25u + 91$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_{12}$	$(u^2 - 3u + 1)^2$
$c_2, c_3$	$(u^2 + u - 1)^2$
$c_4, c_7$	$(u^2 - u - 1)^2$
$c_5, c_6$	$u^4 - 3u^3 + 8u^2 - 3u + 1$
$c_8$	$(u^2 + u + 1)^2$
$c_9$	$u^4$
$c_{10}, c_{11}$	$(u^2 - u + 1)^2$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_{12}$	$(y^2 - 7y + 1)^2$
$c_2, c_3, c_4$ $c_7$	$(y^2 - 3y + 1)^2$
$c_5, c_6$	$y^4 + 7y^3 + 48y^2 + 7y + 1$
$c_8, c_{10}, c_{11}$	$(y^2 + y + 1)^2$
$c_9$	$y^4$

**(vi) Complex Volumes and Cusp Shapes**

Solutions to $I_4^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.500000 + 0.866025I$		
$a = 1.19098 - 1.40126I$	$-8.88264 - 2.02988I$	$15.5000 + 44.1304I$
$b = 1.61803$		
$u = -0.500000 + 0.866025I$		
$a = 2.30902 + 0.53523I$	$-0.98696 - 2.02988I$	$15.5000 - 37.2022I$
$b = -0.618034$		
$u = -0.500000 - 0.866025I$		
$a = 1.19098 + 1.40126I$	$-8.88264 + 2.02988I$	$15.5000 - 44.1304I$
$b = 1.61803$		
$u = -0.500000 - 0.866025I$		
$a = 2.30902 - 0.53523I$	$-0.98696 + 2.02988I$	$15.5000 + 37.2022I$
$b = -0.618034$		

## V. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1$	$((u - 1)^{10})(u^2 - 3u + 1)^2(u^{81} + 33u^{80} + \dots + 130u + 1)$
$c_2$	$((u - 1)^{10})(u^2 + u - 1)^2(u^{81} - 13u^{80} + \dots - 12u + 1)$
$c_3$	$u^{10}(u^2 + u - 1)^2(u^{81} - 3u^{80} + \dots + 1024u + 1024)$
$c_4$	$((u + 1)^{10})(u^2 - u - 1)^2(u^{81} - 13u^{80} + \dots - 12u + 1)$
$c_5$	$(u^4 + u^2 + u + 1)(u^4 - 3u^3 + 8u^2 - 3u + 1)$ $\cdot (u^6 - u^5 + 2u^4 - 2u^3 + 2u^2 - 2u + 1)$ $\cdot (u^{81} + u^{80} + \dots + 8905262u + 2124511)$
$c_6$	$(u^3 - u^2 + 1)^2(u^4 - 3u^3 + 8u^2 - 3u + 1)(u^4 + 3u^3 + 4u^2 + 3u + 2)$ $\cdot (u^{81} + 5u^{80} + \dots - 47488u + 22208)$
$c_7$	$u^{10}(u^2 - u - 1)^2(u^{81} - 3u^{80} + \dots + 1024u + 1024)$
$c_8$	$(u^2 + u + 1)^2(u^4 + u^2 + u + 1)(u^6 - u^5 + 2u^4 - 2u^3 + 2u^2 - 2u + 1)$ $\cdot (u^{81} + 4u^{80} + \dots + 83u - 1)$
$c_9$	$u^4(u^4 + u^2 + u + 1)(u^6 - u^5 + 2u^4 - 2u^3 + 2u^2 - 2u + 1)$ $\cdot (u^{81} + 8u^{80} + \dots + 256u + 16)$
$c_{10}$	$(u^2 - u + 1)^2(u^4 - 2u^3 + 3u^2 - u + 1)(u^6 - 3u^5 + 4u^4 - 2u^3 + 1)$ $\cdot (u^{81} + 30u^{80} + \dots + 6303u - 1)$
$c_{11}$	$(u^2 - u + 1)^2(u^4 + u^2 - u + 1)(u^6 + u^5 + 2u^4 + 2u^3 + 2u^2 + 2u + 1)$ $\cdot (u^{81} + 4u^{80} + \dots + 83u - 1)$
$c_{12}$	$(u^2 - 3u + 1)^2(u^4 + 2u^3 + 3u^2 + u + 1)(u^6 + 3u^5 + 4u^4 + 2u^3 + 1)$ $\cdot (u^{81} - 4u^{80} + \dots - 5u^6 + 1)$

## VI. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1$	$((y - 1)^{10})(y^2 - 7y + 1)^2(y^{81} + 43y^{80} + \dots + 5274y - 1)$
$c_2, c_4$	$((y - 1)^{10})(y^2 - 3y + 1)^2(y^{81} - 33y^{80} + \dots + 130y - 1)$
$c_3, c_7$	$y^{10}(y^2 - 3y + 1)^2(y^{81} + 57y^{80} + \dots - 2.77873 \times 10^7y - 1048576)$
$c_5$	$(y^4 + 2y^3 + 3y^2 + y + 1)(y^4 + 7y^3 + 48y^2 + 7y + 1)$ $\cdot (y^6 + 3y^5 + 4y^4 + 2y^3 + 1)$ $\cdot (y^{81} + 47y^{80} + \dots + 59668081079090y - 4513546989121)$
$c_6$	$((y^3 - y^2 + 2y - 1)^2)(y^4 - y^3 + 2y^2 + 7y + 4)(y^4 + 7y^3 + \dots + 7y + 1)$ $\cdot (y^{81} + 103y^{80} + \dots - 19451522048y - 493195264)$
$c_8, c_{11}$	$(y^2 + y + 1)^2(y^4 + 2y^3 + 3y^2 + y + 1)(y^6 + 3y^5 + 4y^4 + 2y^3 + 1)$ $\cdot (y^{81} + 30y^{80} + \dots + 6303y - 1)$
$c_9$	$y^4(y^4 + 2y^3 + 3y^2 + y + 1)(y^6 + 3y^5 + 4y^4 + 2y^3 + 1)$ $\cdot (y^{81} - 20y^{80} + \dots - 1152y - 256)$
$c_{10}$	$((y^2 + y + 1)^2)(y^4 + 2y^3 + \dots + 5y + 1)(y^6 - y^5 + \dots + 8y^2 + 1)$ $\cdot (y^{81} + 46y^{80} + \dots + 39786411y - 1)$
$c_{12}$	$((y^2 - 7y + 1)^2)(y^4 + 2y^3 + \dots + 5y + 1)(y^6 - y^5 + \dots + 8y^2 + 1)$ $\cdot (y^{81} - 6y^{80} + \dots + 11y - 1)$