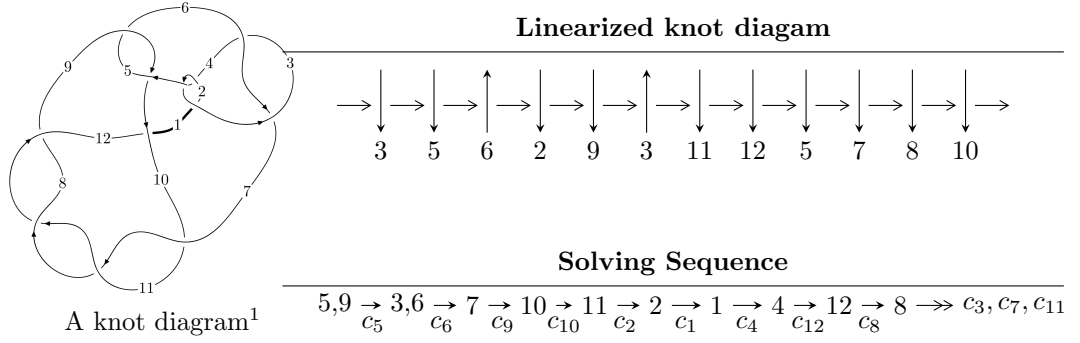


12n<sub>0103</sub> (K12n<sub>0103</sub>)



**Ideals for irreducible components<sup>2</sup> of  $X_{\text{par}}$**

$$I_1^u = \langle 2.50755 \times 10^{20} u^{28} - 4.57339 \times 10^{20} u^{27} + \dots + 6.70474 \times 10^{20} b + 2.31276 \times 10^{20}, \\ 4.30865 \times 10^{20} u^{28} - 1.13718 \times 10^{21} u^{27} + \dots + 6.70474 \times 10^{20} a + 6.48791 \times 10^{20}, u^{29} - 2u^{28} + \dots - u + 1 \rangle$$

$$I_2^u = \langle b + 1, u^5 + 2u^4 + 4u^3 + 5u^2 + a + 4u + 3, u^6 + u^5 + 3u^4 + 2u^3 + 2u^2 + u - 1 \rangle$$

\* 2 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 35 representations.

<sup>1</sup>The image of knot diagram is generated by the software "Draw programme" developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

I.

$$I_1^u = \langle 2.51 \times 10^{20} u^{28} - 4.57 \times 10^{20} u^{27} + \dots + 6.70 \times 10^{20} b + 2.31 \times 10^{20}, 4.31 \times 10^{20} u^{28} - 1.14 \times 10^{21} u^{27} + \dots + 6.70 \times 10^{20} a + 6.49 \times 10^{20}, u^{29} - 2u^{28} + \dots - u + 1 \rangle$$

(i) Arc colorings

$$a_5 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -0.642627u^{28} + 1.69608u^{27} + \dots + 4.76582u - 0.967660 \\ -0.373996u^{28} + 0.682112u^{27} + \dots + 1.36157u - 0.344944 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -0.525413u^{28} + 0.870263u^{27} + \dots + 1.86350u + 0.104816 \\ -0.165523u^{28} + 0.372194u^{27} + \dots + 0.644339u + 0.119793 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -u \\ u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0.00550978u^{28} - 0.113964u^{27} + \dots - 2.05097u - 0.744280 \\ -0.0294122u^{28} + 0.103634u^{27} + \dots + 0.884693u + 0.0789002 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -1.01662u^{28} + 2.37819u^{27} + \dots + 6.12739u - 1.31260 \\ -0.373996u^{28} + 0.682112u^{27} + \dots + 1.36157u - 0.344944 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -0.582562u^{28} + 1.02418u^{27} + \dots + 2.16299u + 0.0440466 \\ 0.0571491u^{28} - 0.153913u^{27} + \dots - 0.299489u + 0.0607697 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -0.715822u^{28} + 1.86209u^{27} + \dots + 5.07394u - 0.901780 \\ -0.390136u^{28} + 0.726358u^{27} + \dots + 1.45438u - 0.364566 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -0.690936u^{28} + 1.24246u^{27} + \dots + 2.50784u + 0.224610 \\ 0.165523u^{28} - 0.372194u^{27} + \dots - 0.644339u - 0.119793 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 0.0239024u^{28} + 0.0103299u^{27} + \dots + 1.16628u + 0.665380 \\ -0.0294122u^{28} + 0.103634u^{27} + \dots + 0.884693u + 0.0789002 \end{pmatrix}$$

(ii) Obstruction class = -1

$$(iii) \text{ Cusp Shapes} = \frac{478078822365653903278}{134094852819026608583} u^{28} - \frac{5561400214755760811553}{670474264095133042915} u^{27} + \dots - \frac{2275460989738397018314}{134094852819026608583} u - \frac{5831311641101896181097}{670474264095133042915}$$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1$	$u^{29} + 39u^{28} + \dots + 2258u + 1$
$c_2, c_4$	$u^{29} - 7u^{28} + \dots - 54u + 1$
$c_3, c_6$	$u^{29} + 5u^{28} + \dots + 384u + 64$
$c_5, c_9$	$u^{29} + 2u^{28} + \dots - u - 1$
$c_7, c_8, c_{10}$ $c_{11}$	$u^{29} + 2u^{28} + \dots + 5u + 1$
$c_{12}$	$u^{29} - 12u^{28} + \dots + 3529u + 937$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1$	$y^{29} - 91y^{28} + \dots + 4903026y - 1$
$c_2, c_4$	$y^{29} - 39y^{28} + \dots + 2258y - 1$
$c_3, c_6$	$y^{29} + 39y^{28} + \dots + 212992y - 4096$
$c_5, c_9$	$y^{29} + 30y^{27} + \dots + 13y - 1$
$c_7, c_8, c_{10}$ $c_{11}$	$y^{29} - 36y^{28} + \dots + 13y - 1$
$c_{12}$	$y^{29} - 36y^{28} + \dots + 62137329y - 877969$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.867238 + 0.470147I$ $a = 0.237339 + 1.389930I$ $b = -0.92240 - 1.35617I$	$-12.12860 - 4.62991I$	$-15.7252 + 5.0837I$
$u = 0.867238 - 0.470147I$ $a = 0.237339 - 1.389930I$ $b = -0.92240 + 1.35617I$	$-12.12860 + 4.62991I$	$-15.7252 - 5.0837I$
$u = -0.915025$ $a = 0.602737$ $b = -2.04399$	$-14.6155$	$-18.8040$
$u = 0.160840 + 1.087590I$ $a = 0.0855322 + 0.1114450I$ $b = 0.493211 - 0.128104I$	$2.18324 - 1.77578I$	$-1.23792 + 3.54893I$
$u = 0.160840 - 1.087590I$ $a = 0.0855322 - 0.1114450I$ $b = 0.493211 + 0.128104I$	$2.18324 + 1.77578I$	$-1.23792 - 3.54893I$
$u = -0.766809 + 0.460777I$ $a = 0.217501 - 1.292190I$ $b = -0.793934 + 1.006770I$	$-3.36571 + 3.55459I$	$-14.7590 - 7.4317I$
$u = -0.766809 - 0.460777I$ $a = 0.217501 + 1.292190I$ $b = -0.793934 - 1.006770I$	$-3.36571 - 3.55459I$	$-14.7590 + 7.4317I$
$u = 0.807312$ $a = 0.103435$ $b = -1.67794$	$-5.54567$	$-19.0490$
$u = -0.452011 + 1.154640I$ $a = -0.089699 - 0.245433I$ $b = 0.631471 + 0.354822I$	$-4.66125 + 4.01059I$	$-6.69076 - 1.05481I$
$u = -0.452011 - 1.154640I$ $a = -0.089699 + 0.245433I$ $b = 0.631471 - 0.354822I$	$-4.66125 - 4.01059I$	$-6.69076 + 1.05481I$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.580536 + 0.452475I$		
$a = 0.450270 + 1.338160I$	$-0.77928 - 1.44092I$	$-6.71227 + 4.83159I$
$b = -0.597116 - 0.490346I$		
$u = 0.580536 - 0.452475I$		
$a = 0.450270 - 1.338160I$	$-0.77928 + 1.44092I$	$-6.71227 - 4.83159I$
$b = -0.597116 + 0.490346I$		
$u = -0.734655$		
$a = 1.16704$	$-7.96223$	$-11.3580$
$b = 0.195873$		
$u = 0.317549 + 0.579846I$		
$a = 3.74066 + 0.93387I$	$-10.62150 + 0.95783I$	$-12.17772 + 5.24325I$
$b = -0.910186 + 0.367717I$		
$u = 0.317549 - 0.579846I$		
$a = 3.74066 - 0.93387I$	$-10.62150 - 0.95783I$	$-12.17772 - 5.24325I$
$b = -0.910186 - 0.367717I$		
$u = -0.355366 + 0.430210I$		
$a = 2.58524 - 2.38862I$	$-2.40653 - 0.39885I$	$-18.5948 - 3.1258I$
$b = -0.804622 - 0.092789I$		
$u = -0.355366 - 0.430210I$		
$a = 2.58524 + 2.38862I$	$-2.40653 + 0.39885I$	$-18.5948 + 3.1258I$
$b = -0.804622 + 0.092789I$		
$u = -0.465770$		
$a = -2.93524$	$-2.20812$	$4.71460$
$b = -1.09023$		
$u = 1.12576 + 1.06472I$		
$a = -0.564004 - 1.170310I$	$18.7699 - 11.3822I$	$-14.5597 + 4.9176I$
$b = 1.78727 + 0.43721I$		
$u = 1.12576 - 1.06472I$		
$a = -0.564004 + 1.170310I$	$18.7699 + 11.3822I$	$-14.5597 - 4.9176I$
$b = 1.78727 - 0.43721I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.14151 + 1.07839I$ $a = -0.559145 + 1.007550I$ $b = 1.72676 - 0.31572I$	$-11.7546 + 8.6101I$	$-13.1323 - 5.7611I$
$u = -1.14151 - 1.07839I$ $a = -0.559145 - 1.007550I$ $b = 1.72676 + 0.31572I$	$-11.7546 - 8.6101I$	$-13.1323 + 5.7611I$
$u = 1.10890 + 1.13111I$ $a = -0.839564 - 0.595930I$ $b = 1.78058 - 0.11270I$	$18.9482 + 3.1990I$	$-14.9528 - 0.8134I$
$u = 1.10890 - 1.13111I$ $a = -0.839564 + 0.595930I$ $b = 1.78058 + 0.11270I$	$18.9482 - 3.1990I$	$-14.9528 + 0.8134I$
$u = 1.14879 + 1.10311I$ $a = -0.592413 - 0.839025I$ $b = 1.68896 + 0.17655I$	$-8.95243 - 4.17612I$	$-10.28879 + 2.37984I$
$u = 1.14879 - 1.10311I$ $a = -0.592413 + 0.839025I$ $b = 1.68896 - 0.17655I$	$-8.95243 + 4.17612I$	$-10.28879 - 2.37984I$
$u = -1.13279 + 1.12536I$ $a = -0.701441 + 0.703233I$ $b = 1.71752 - 0.02970I$	$-11.62970 - 0.31954I$	$-13.41116 + 1.33191I$
$u = -1.13279 - 1.12536I$ $a = -0.701441 - 0.703233I$ $b = 1.71752 + 0.02970I$	$-11.62970 + 0.31954I$	$-13.41116 - 1.33191I$
$u = 0.385892$ $a = 1.12146$ $b = 0.0212520$	$-0.763627$	$-13.0190$

**II.**

$$I_2^u = \langle b+1, u^5 + 2u^4 + 4u^3 + 5u^2 + a + 4u + 3, u^6 + u^5 + 3u^4 + 2u^3 + 2u^2 + u - 1 \rangle$$

**(i) Arc colorings**

$$a_5 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -u^5 - 2u^4 - 4u^3 - 5u^2 - 4u - 3 \\ -1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -u \\ u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -u^3 - 2u \\ -u^5 - u^3 + u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -u^5 - 2u^4 - 4u^3 - 5u^2 - 4u - 4 \\ -1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -u^5 - 2u^4 - 4u^3 - 5u^2 - 4u - 3 \\ -1 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -u^2 - 1 \\ u^2 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} u^5 + 2u^3 + u \\ -u^5 - u^3 + u \end{pmatrix}$$

**(ii) Obstruction class = 1**

$$\text{(iii) Cusp Shapes} = -7u^5 - 15u^4 - 29u^3 - 33u^2 - 28u - 32$$



(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_2$	$(u - 1)^6$
$c_3, c_6$	$u^6$
$c_4$	$(u + 1)^6$
$c_5$	$u^6 + u^5 + 3u^4 + 2u^3 + 2u^2 + u - 1$
$c_7, c_8$	$u^6 - u^5 - 3u^4 + 2u^3 + 2u^2 + u - 1$
$c_9, c_{12}$	$u^6 - u^5 + 3u^4 - 2u^3 + 2u^2 - u - 1$
$c_{10}, c_{11}$	$u^6 + u^5 - 3u^4 - 2u^3 + 2u^2 - u - 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_4$	$(y - 1)^6$
$c_3, c_6$	$y^6$
$c_5, c_9, c_{12}$	$y^6 + 5y^5 + 9y^4 + 4y^3 - 6y^2 - 5y + 1$
$c_7, c_8, c_{10}$ $c_{11}$	$y^6 - 7y^5 + 17y^4 - 16y^3 + 6y^2 - 5y + 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.873214$ $a = -1.31147$ $b = -1.00000$	-9.30502	-18.5710
$u = 0.138835 + 1.234450I$ $a = 0.631845 + 0.143944I$ $b = -1.00000$	$1.31531 - 1.97241I$	$-11.10050 + 4.53432I$
$u = 0.138835 - 1.234450I$ $a = 0.631845 - 0.143944I$ $b = -1.00000$	$1.31531 + 1.97241I$	$-11.10050 - 4.53432I$
$u = -0.408802 + 1.276380I$ $a = 0.453123 - 0.323434I$ $b = -1.00000$	$-5.34051 + 4.59213I$	$-13.7303 - 5.9632I$
$u = -0.408802 - 1.276380I$ $a = 0.453123 + 0.323434I$ $b = -1.00000$	$-5.34051 - 4.59213I$	$-13.7303 + 5.9632I$
$u = 0.413150$ $a = -5.85846$ $b = -1.00000$	-2.38379	-51.7680

### III. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1$	$((u-1)^6)(u^{29} + 39u^{28} + \dots + 2258u + 1)$
$c_2$	$((u-1)^6)(u^{29} - 7u^{28} + \dots - 54u + 1)$
$c_3, c_6$	$u^6(u^{29} + 5u^{28} + \dots + 384u + 64)$
$c_4$	$((u+1)^6)(u^{29} - 7u^{28} + \dots - 54u + 1)$
$c_5$	$(u^6 + u^5 + 3u^4 + 2u^3 + 2u^2 + u - 1)(u^{29} + 2u^{28} + \dots - u - 1)$
$c_7, c_8$	$(u^6 - u^5 - 3u^4 + 2u^3 + 2u^2 + u - 1)(u^{29} + 2u^{28} + \dots + 5u + 1)$
$c_9$	$(u^6 - u^5 + 3u^4 - 2u^3 + 2u^2 - u - 1)(u^{29} + 2u^{28} + \dots - u - 1)$
$c_{10}, c_{11}$	$(u^6 + u^5 - 3u^4 - 2u^3 + 2u^2 - u - 1)(u^{29} + 2u^{28} + \dots + 5u + 1)$
$c_{12}$	$(u^6 - u^5 + 3u^4 - 2u^3 + 2u^2 - u - 1)(u^{29} - 12u^{28} + \dots + 3529u + 937)$

#### IV. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1$	$((y - 1)^6)(y^{29} - 91y^{28} + \dots + 4903026y - 1)$
$c_2, c_4$	$((y - 1)^6)(y^{29} - 39y^{28} + \dots + 2258y - 1)$
$c_3, c_6$	$y^6(y^{29} + 39y^{28} + \dots + 212992y - 4096)$
$c_5, c_9$	$(y^6 + 5y^5 + \dots - 5y + 1)(y^{29} + 30y^{27} + \dots + 13y - 1)$
$c_7, c_8, c_{10}$ $c_{11}$	$(y^6 - 7y^5 + \dots - 5y + 1)(y^{29} - 36y^{28} + \dots + 13y - 1)$
$c_{12}$	$(y^6 + 5y^5 + 9y^4 + 4y^3 - 6y^2 - 5y + 1)$ $\cdot (y^{29} - 36y^{28} + \dots + 62137329y - 877969)$