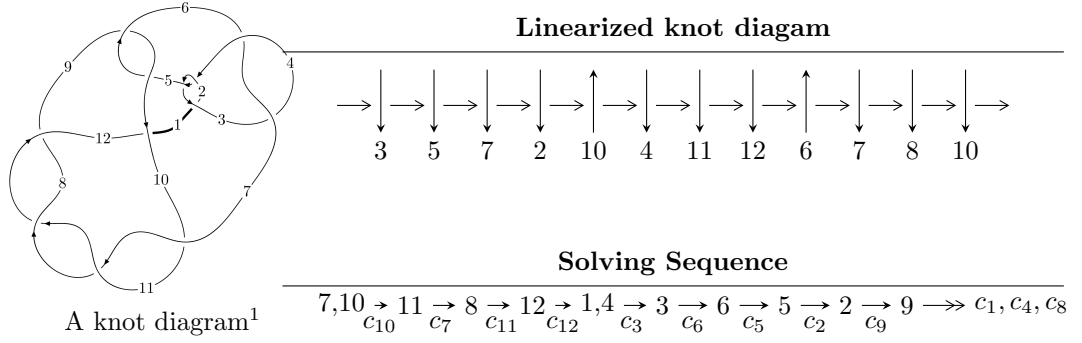


$12n_{0107}$  ( $K12n_{0107}$ )



**Ideals for irreducible components<sup>2</sup> of  $X_{\text{par}}$**

$$I_1^u = \langle 47441368u^{25} + 57693789u^{24} + \dots + 104373924b + 18568285, \\ 120201295u^{25} + 398061213u^{24} + \dots + 104373924a + 783424087, u^{26} + 5u^{25} + \dots + 14u - 1 \rangle$$

$$I_2^u = \langle 2a^2u + a^2 - au + b - a + 2u, a^3 - a^2u + a^2 - 2au + 4a - 2u + 3, u^2 - u - 1 \rangle$$

$$I_3^u = \langle b + 1, a, u + 1 \rangle$$

\* 3 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 33 representations.

<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\mathbf{I. } I_1^u = \langle 4.74 \times 10^7 u^{25} + 5.77 \times 10^7 u^{24} + \dots + 1.04 \times 10^8 b + 1.86 \times 10^7, 1.20 \times 10^8 u^{25} + 3.98 \times 10^8 u^{24} + \dots + 1.04 \times 10^8 a + 7.83 \times 10^8, u^{26} + 5u^{25} + \dots + 14u - 1 \rangle$$

(i) Arc colorings

$$a_7 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -u \\ -u^3 + u \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -u^2 + 1 \\ -u^4 + 2u^2 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} u^4 - 3u^2 + 1 \\ -u^4 + 2u^2 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -1.15164u^{25} - 3.81380u^{24} + \dots - 24.4464u - 7.50594 \\ -0.454533u^{25} - 0.552761u^{24} + \dots + 13.0629u - 0.177902 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -1.15164u^{25} - 3.81380u^{24} + \dots - 24.4464u - 7.50594 \\ 3.33329u^{25} + 11.3654u^{24} + \dots + 41.4363u - 2.12231 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -0.633480u^{25} - 1.36564u^{24} + \dots + 2.69053u + 4.69952 \\ -1.23184u^{25} - 3.55184u^{24} + \dots - 6.61306u + 0.205455 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 0.598359u^{25} + 2.18620u^{24} + \dots + 9.30359u + 4.49406 \\ -1.23184u^{25} - 3.55184u^{24} + \dots - 6.61306u + 0.205455 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -0.598359u^{25} - 2.18620u^{24} + \dots - 9.30359u - 4.49406 \\ -0.203032u^{25} + 0.469119u^{24} + \dots + 15.6624u - 0.533217 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} u^3 - 2u \\ u^5 - 3u^3 + u \end{pmatrix}$$

(ii) Obstruction class = -1

$$\text{(iii) Cusp Shapes} = -\frac{92088909}{17395654}u^{25} - \frac{188693588}{8697827}u^{24} + \dots - \frac{885802456}{8697827}u - \frac{15795407}{8697827}$$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1$	$u^{26} + 20u^{25} + \dots + 79u + 1$
$c_2, c_4$	$u^{26} - 4u^{25} + \dots - 11u - 1$
$c_3, c_6$	$u^{26} - 3u^{25} + \dots - 6u + 2$
$c_5, c_9$	$u^{26} - 2u^{25} + \dots - 96u + 64$
$c_7, c_8, c_{10}$ $c_{11}$	$u^{26} + 5u^{25} + \dots + 14u - 1$
$c_{12}$	$u^{26} - 21u^{25} + \dots + 52120u + 337$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1$	$y^{26} - 24y^{25} + \dots - 6127y + 1$
$c_2, c_4$	$y^{26} - 20y^{25} + \dots - 79y + 1$
$c_3, c_6$	$y^{26} - 3y^{25} + \dots - 40y + 4$
$c_5, c_9$	$y^{26} + 34y^{25} + \dots - 95232y + 4096$
$c_7, c_8, c_{10}$ $c_{11}$	$y^{26} - 39y^{25} + \dots - 304y + 1$
$c_{12}$	$y^{26} - 123y^{25} + \dots - 2285596764y + 113569$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.476607 + 0.919429I$ $a = -0.688440 - 0.733293I$ $b = 0.227587 + 1.287750I$	$-5.18299 + 2.95142I$	$-14.7696 - 4.0162I$
$u = -0.476607 - 0.919429I$ $a = -0.688440 + 0.733293I$ $b = 0.227587 - 1.287750I$	$-5.18299 - 2.95142I$	$-14.7696 + 4.0162I$
$u = -0.757036$ $a = -0.441343$ $b = 0.637723$	$-1.34161$	$-6.51520$
$u = 1.223650 + 0.232594I$ $a = -0.924838 - 0.484695I$ $b = 0.280314 - 1.358420I$	$-5.77000 - 3.25214I$	$-11.73752 + 3.41900I$
$u = 1.223650 - 0.232594I$ $a = -0.924838 + 0.484695I$ $b = 0.280314 + 1.358420I$	$-5.77000 + 3.25214I$	$-11.73752 - 3.41900I$
$u = -1.329480 + 0.241157I$ $a = 0.277950 + 0.611388I$ $b = 0.308061 + 0.000558I$	$-3.29395 - 1.34186I$	$-11.30499 + 4.69401I$
$u = -1.329480 - 0.241157I$ $a = 0.277950 - 0.611388I$ $b = 0.308061 - 0.000558I$	$-3.29395 + 1.34186I$	$-11.30499 - 4.69401I$
$u = 1.369250 + 0.095489I$ $a = 0.500507 - 0.680570I$ $b = 0.10931 - 1.70719I$	$-9.37037 - 1.40410I$	$-14.8448 + 0.4920I$
$u = 1.369250 - 0.095489I$ $a = 0.500507 + 0.680570I$ $b = 0.10931 + 1.70719I$	$-9.37037 + 1.40410I$	$-14.8448 - 0.4920I$
$u = 1.273730 + 0.536724I$ $a = 0.988931 + 0.204426I$ $b = -0.48656 + 1.60886I$	$-10.60190 - 7.95034I$	$-14.2939 + 5.5201I$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.273730 - 0.536724I$ $a = 0.988931 - 0.204426I$ $b = -0.48656 - 1.60886I$	$-10.60190 + 7.95034I$	$-14.2939 - 5.5201I$
$u = -0.586682 + 0.167108I$ $a = -0.045237 - 0.711969I$ $b = -0.71246 - 2.34576I$	$-2.72200 + 0.36882I$	$-3.94523 + 10.24837I$
$u = -0.586682 - 0.167108I$ $a = -0.045237 + 0.711969I$ $b = -0.71246 + 2.34576I$	$-2.72200 - 0.36882I$	$-3.94523 - 10.24837I$
$u = -0.348677 + 0.367916I$ $a = 1.247060 + 0.371784I$ $b = -0.209352 - 0.864493I$	$-0.636376 + 1.127340I$	$-7.20662 - 6.11077I$
$u = -0.348677 - 0.367916I$ $a = 1.247060 - 0.371784I$ $b = -0.209352 + 0.864493I$	$-0.636376 - 1.127340I$	$-7.20662 + 6.11077I$
$u = 0.424219 + 0.095685I$ $a = 0.07818 + 2.89428I$ $b = -0.1185550 - 0.0289313I$	$2.35620 + 2.67700I$	$3.89989 + 1.35809I$
$u = 0.424219 - 0.095685I$ $a = 0.07818 - 2.89428I$ $b = -0.1185550 + 0.0289313I$	$2.35620 - 2.67700I$	$3.89989 - 1.35809I$
$u = 1.63681$ $a = 0.377195$ $b = -1.87474$	$-9.79249$	$1.55260$
$u = -1.80599 + 0.06787I$ $a = 0.735548 - 0.651435I$ $b = -0.23521 - 1.59914I$	$-16.9214 + 4.6752I$	$0$
$u = -1.80599 - 0.06787I$ $a = 0.735548 + 0.651435I$ $b = -0.23521 + 1.59914I$	$-16.9214 - 4.6752I$	$0$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.81333 + 0.15530I$ $a = -0.732203 + 0.586510I$ $b = 0.50599 + 1.87679I$	$17.8851 + 11.1272I$	0
$u = -1.81333 - 0.15530I$ $a = -0.732203 - 0.586510I$ $b = 0.50599 - 1.87679I$	$17.8851 - 11.1272I$	0
$u = -1.83864 + 0.02244I$ $a = -0.672414 - 0.695929I$ $b = -0.16075 - 1.49337I$	$18.0411 + 1.9797I$	0
$u = -1.83864 - 0.02244I$ $a = -0.672414 + 0.695929I$ $b = -0.16075 + 1.49337I$	$18.0411 - 1.9797I$	0
$u = 1.87792$ $a = -0.655106$ $b = -0.356336$	-16.1049	-16.4270
$u = 0.0594263$ $a = -8.81083$ $b = 0.576606$	-1.19028	-8.21100

**II.**

$$I_2^u = \langle 2a^2u + a^2 - au + b - a + 2u, a^3 - a^2u + a^2 - 2au + 4a - 2u + 3, u^2 - u - 1 \rangle$$

**(i) Arc colorings**

$$a_7 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ u + 1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -u \\ -u - 1 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -u \\ -u \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 0 \\ -u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} a \\ -2a^2u - a^2 + au + a - 2u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} a \\ -2a^2u - a^2 - 2u \end{pmatrix}$$

$$a_6 = \begin{pmatrix} a^2u \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} a^2u \\ 0 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} a^2u \\ -2a^2u - a^2 - 2u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

**(ii) Obstruction class = 1**

**(iii) Cusp Shapes =  $-19a^2u - 13a^2 + 9au + a - 8u - 29$**



(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_3$	$(u^3 - u^2 + 2u - 1)^2$
$c_2$	$(u^3 + u^2 - 1)^2$
$c_4$	$(u^3 - u^2 + 1)^2$
$c_5, c_9$	$u^6$
$c_6$	$(u^3 + u^2 + 2u + 1)^2$
$c_7, c_8$	$(u^2 + u - 1)^3$
$c_{10}, c_{11}, c_{12}$	$(u^2 - u - 1)^3$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_3, c_6$	$(y^3 + 3y^2 + 2y - 1)^2$
$c_2, c_4$	$(y^3 - y^2 + 2y - 1)^2$
$c_5, c_9$	$y^6$
$c_7, c_8, c_{10}$ $c_{11}, c_{12}$	$(y^2 - 3y + 1)^3$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.618034$ $a = -0.922021$ $b = 1.08457$	-2.10041	-20.9180
$u = -0.618034$ $a = -0.34801 + 2.11500I$ $b = 0.075747 + 0.460350I$	$2.03717 + 2.82812I$	$-16.9959 - 7.7984I$
$u = -0.618034$ $a = -0.34801 - 2.11500I$ $b = 0.075747 - 0.460350I$	$2.03717 - 2.82812I$	$-16.9959 + 7.7984I$
$u = 1.61803$ $a = 0.132927 + 0.807858I$ $b = -0.198308 + 1.205210I$	$-5.85852 - 2.82812I$	$-12.10059 + 3.17745I$
$u = 1.61803$ $a = 0.132927 - 0.807858I$ $b = -0.198308 - 1.205210I$	$-5.85852 + 2.82812I$	$-12.10059 - 3.17745I$
$u = 1.61803$ $a = 0.352181$ $b = -2.83945$	-9.99610	-41.8890

$$\text{III. } I_3^u = \langle b + 1, a, u + 1 \rangle$$

(i) Arc colorings

$$a_7 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -1 \\ 1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = -12

(iv) **u**-Polynomials at the component

Crossings	<b>u</b> -Polynomials at each crossing
$c_1, c_2, c_5$ $c_7, c_8$	$u - 1$
$c_3, c_6$	$u$
$c_4, c_9, c_{10}$ $c_{11}, c_{12}$	$u + 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_4$ $c_5, c_7, c_8$ $c_9, c_{10}, c_{11}$ $c_{12}$	$y - 1$
$c_3, c_6$	$y$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.00000$		
$a = 0$	-3.28987	-12.0000
$b = -1.00000$		

#### IV. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1$	$(u - 1)(u^3 - u^2 + 2u - 1)^2(u^{26} + 20u^{25} + \dots + 79u + 1)$
$c_2$	$(u - 1)(u^3 + u^2 - 1)^2(u^{26} - 4u^{25} + \dots - 11u - 1)$
$c_3$	$u(u^3 - u^2 + 2u - 1)^2(u^{26} - 3u^{25} + \dots - 6u + 2)$
$c_4$	$(u + 1)(u^3 - u^2 + 1)^2(u^{26} - 4u^{25} + \dots - 11u - 1)$
$c_5$	$u^6(u - 1)(u^{26} - 2u^{25} + \dots - 96u + 64)$
$c_6$	$u(u^3 + u^2 + 2u + 1)^2(u^{26} - 3u^{25} + \dots - 6u + 2)$
$c_7, c_8$	$(u - 1)(u^2 + u - 1)^3(u^{26} + 5u^{25} + \dots + 14u - 1)$
$c_9$	$u^6(u + 1)(u^{26} - 2u^{25} + \dots - 96u + 64)$
$c_{10}, c_{11}$	$(u + 1)(u^2 - u - 1)^3(u^{26} + 5u^{25} + \dots + 14u - 1)$
$c_{12}$	$(u + 1)(u^2 - u - 1)^3(u^{26} - 21u^{25} + \dots + 52120u + 337)$



### V. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1$	$(y - 1)(y^3 + 3y^2 + 2y - 1)^2(y^{26} - 24y^{25} + \dots - 6127y + 1)$
$c_2, c_4$	$(y - 1)(y^3 - y^2 + 2y - 1)^2(y^{26} - 20y^{25} + \dots - 79y + 1)$
$c_3, c_6$	$y(y^3 + 3y^2 + 2y - 1)^2(y^{26} - 3y^{25} + \dots - 40y + 4)$
$c_5, c_9$	$y^6(y - 1)(y^{26} + 34y^{25} + \dots - 95232y + 4096)$
$c_7, c_8, c_{10}$ $c_{11}$	$(y - 1)(y^2 - 3y + 1)^3(y^{26} - 39y^{25} + \dots - 304y + 1)$
$c_{12}$	$(y - 1)(y^2 - 3y + 1)^3(y^{26} - 123y^{25} + \dots - 2.28560 \times 10^9 y + 113569)$