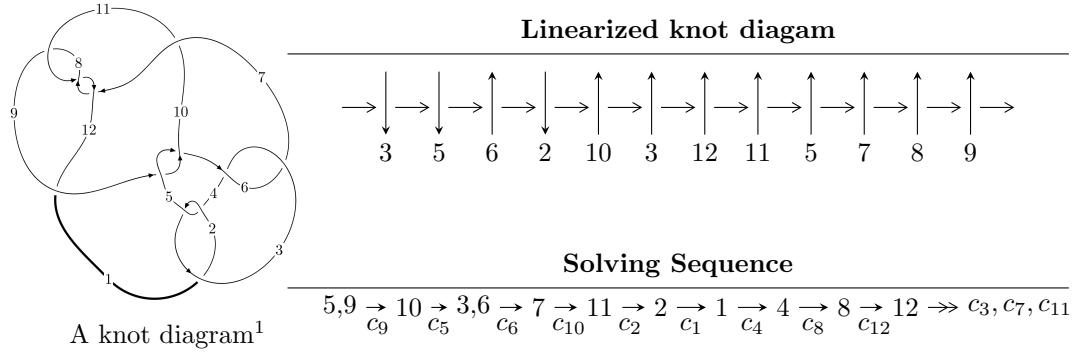


$12n_{0116}$  ( $K12n_{0116}$ )



Ideals for irreducible components<sup>2</sup> of  $X_{\text{par}}$

$$I_1^u = \langle -1.49041 \times 10^{48} u^{40} - 1.63923 \times 10^{48} u^{39} + \dots + 4.94994 \times 10^{48} b + 1.35928 \times 10^{48}, \\ - 1.49041 \times 10^{48} u^{40} - 1.63923 \times 10^{48} u^{39} + \dots + 4.94994 \times 10^{48} a + 1.35928 \times 10^{48}, u^{41} + 2u^{40} + \dots - u - 1 \rangle$$

$$I_2^u = \langle -u^5 + u^4 + 3u^3 - 2u^2 + b - u - 1, -u^5 + u^4 + 3u^3 - 2u^2 + a - 2u - 1, u^6 - u^5 - 3u^4 + 2u^3 + 2u^2 + u - 1 \rangle$$

\* 2 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 47 representations.

<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/math/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

**I.**

$$I_1^u = \langle -1.49 \times 10^{48} u^{40} - 1.64 \times 10^{48} u^{39} + \dots + 4.95 \times 10^{48} b + 1.36 \times 10^{48}, -1.49 \times 10^{48} u^{40} - 1.64 \times 10^{48} u^{39} + \dots + 4.95 \times 10^{48} a + 1.36 \times 10^{48}, u^{41} + 2u^{40} + \dots - u - 1 \rangle$$

(i) **Arc colorings**

$$a_5 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 0.301096u^{40} + 0.331162u^{39} + \dots + 2.34511u - 0.274605 \\ 0.301096u^{40} + 0.331162u^{39} + \dots + 3.34511u - 0.274605 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} u \\ -u^3 + u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -0.501619u^{40} - 0.639447u^{39} + \dots + 0.896473u + 0.455440 \\ -0.458393u^{40} - 0.639616u^{39} + \dots + 0.799469u + 0.637044 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -0.205384u^{40} - 0.351951u^{39} + \dots + 0.606975u + 1.47006 \\ -0.559530u^{40} - 0.970963u^{39} + \dots + 1.39792u + 1.11199 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 0.301096u^{40} + 0.331162u^{39} + \dots + 2.34511u - 0.274605 \\ 0.0224886u^{40} - 0.0444496u^{39} + \dots + 3.31504u - 0.00357471 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 0.110835u^{40} - 0.0229094u^{39} + \dots - 0.234831u + 0.545396 \\ -0.390784u^{40} - 0.662356u^{39} + \dots + 0.661642u + 1.00084 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 0.257870u^{40} + 0.331331u^{39} + \dots + 2.44211u - 0.456209 \\ 0.313467u^{40} + 0.443108u^{39} + \dots + 3.39872u - 0.542830 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -0.659770u^{40} - 1.09530u^{39} + \dots + 1.32120u + 1.69134 \\ -0.119568u^{40} + 0.0303721u^{39} + \dots - 0.186514u - 1.02623 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 0.501619u^{40} + 0.639447u^{39} + \dots - 0.896473u - 0.455440 \\ -0.390784u^{40} - 0.662356u^{39} + \dots + 0.661642u + 1.00084 \end{pmatrix}$$

(ii) **Obstruction class** = -1

(iii) **Cusp Shapes** =  $-4.91398u^{40} - 6.25021u^{39} + \dots - 14.4903u + 31.2535$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1$	$u^{41} + 47u^{40} + \cdots + 296u + 1$
$c_2, c_4$	$u^{41} - 7u^{40} + \cdots - 12u + 1$
$c_3, c_6$	$u^{41} + 7u^{40} + \cdots + 640u - 64$
$c_5, c_9$	$u^{41} + 2u^{40} + \cdots - u - 1$
$c_7, c_8, c_{11}$	$u^{41} + 2u^{40} + \cdots + u + 1$
$c_{10}, c_{12}$	$u^{41} - 2u^{40} + \cdots - 47u + 17$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1$	$y^{41} - 99y^{40} + \cdots + 111528y - 1$
$c_2, c_4$	$y^{41} - 47y^{40} + \cdots + 296y - 1$
$c_3, c_6$	$y^{41} + 39y^{40} + \cdots + 90112y - 4096$
$c_5, c_9$	$y^{41} + 42y^{39} + \cdots + 7y - 1$
$c_7, c_8, c_{11}$	$y^{41} + 36y^{40} + \cdots + 7y - 1$
$c_{10}, c_{12}$	$y^{41} - 12y^{40} + \cdots - 2041y - 289$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.546127 + 0.811291I$		
$a = 0.743645 - 1.202480I$	$-4.83591 - 7.62929I$	$1.63110 + 8.21040I$
$b = 0.197518 - 0.391191I$		
$u = -0.546127 - 0.811291I$		
$a = 0.743645 + 1.202480I$	$-4.83591 + 7.62929I$	$1.63110 - 8.21040I$
$b = 0.197518 + 0.391191I$		
$u = 0.559771 + 0.753240I$		
$a = -0.624352 - 1.085930I$	$0.18158 + 4.25829I$	$7.22708 - 8.04646I$
$b = -0.064581 - 0.332685I$		
$u = 0.559771 - 0.753240I$		
$a = -0.624352 + 1.085930I$	$0.18158 - 4.25829I$	$7.22708 + 8.04646I$
$b = -0.064581 + 0.332685I$		
$u = -0.664122 + 0.603424I$		
$a = 0.468587 - 0.663053I$	$-2.14123 - 1.43316I$	$6.02200 + 3.64151I$
$b = -0.195535 - 0.059628I$		
$u = -0.664122 - 0.603424I$		
$a = 0.468587 + 0.663053I$	$-2.14123 + 1.43316I$	$6.02200 - 3.64151I$
$b = -0.195535 + 0.059628I$		
$u = 0.350975 + 0.790999I$		
$a = -0.39756 - 1.62860I$	$-6.73300 + 0.22938I$	$-2.25086 - 2.33731I$
$b = -0.046582 - 0.837603I$		
$u = 0.350975 - 0.790999I$		
$a = -0.39756 + 1.62860I$	$-6.73300 - 0.22938I$	$-2.25086 + 2.33731I$
$b = -0.046582 + 0.837603I$		
$u = 0.087719 + 0.850756I$		
$a = -0.12108 - 2.10269I$	$-8.03114 + 3.86698I$	$-3.56668 - 3.96784I$
$b = -0.033358 - 1.251940I$		
$u = 0.087719 - 0.850756I$		
$a = -0.12108 + 2.10269I$	$-8.03114 - 3.86698I$	$-3.56668 + 3.96784I$
$b = -0.033358 + 1.251940I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.445566 + 0.616611I$		
$a = 0.112439 - 1.137990I$	$-1.53709 - 1.40851I$	$1.34634 + 3.01002I$
$b = -0.333128 - 0.521377I$		
$u = -0.445566 - 0.616611I$		
$a = 0.112439 + 1.137990I$	$-1.53709 + 1.40851I$	$1.34634 - 3.01002I$
$b = -0.333128 + 0.521377I$		
$u = -0.090722 + 0.752674I$		
$a = 0.05605 - 1.99845I$	$-2.86548 - 1.28813I$	$1.16839 + 4.84793I$
$b = -0.034673 - 1.245770I$		
$u = -0.090722 - 0.752674I$		
$a = 0.05605 + 1.99845I$	$-2.86548 + 1.28813I$	$1.16839 - 4.84793I$
$b = -0.034673 + 1.245770I$		
$u = -0.527293 + 0.436682I$		
$a = -0.973519 - 0.176954I$	$-4.01492 + 3.79256I$	$2.77393 - 0.06472I$
$b = -1.50081 + 0.25973I$		
$u = -0.527293 - 0.436682I$		
$a = -0.973519 + 0.176954I$	$-4.01492 - 3.79256I$	$2.77393 + 0.06472I$
$b = -1.50081 - 0.25973I$		
$u = 0.468495 + 0.464998I$		
$a = 0.622134 - 0.271062I$	$0.599224 - 0.610593I$	$8.50615 - 0.01136I$
$b = 1.090630 + 0.193936I$		
$u = 0.468495 - 0.464998I$		
$a = 0.622134 + 0.271062I$	$0.599224 + 0.610593I$	$8.50615 + 0.01136I$
$b = 1.090630 - 0.193936I$		
$u = -0.325958 + 0.548034I$		
$a = -0.267538 + 0.084708I$	$-2.79420 - 2.18222I$	$4.51636 + 3.99594I$
$b = -0.593496 + 0.632743I$		
$u = -0.325958 - 0.548034I$		
$a = -0.267538 - 0.084708I$	$-2.79420 + 2.18222I$	$4.51636 - 3.99594I$
$b = -0.593496 - 0.632743I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.397250 + 0.182037I$		
$a = -0.506275 - 0.004273I$	$2.57061 + 4.43167I$	$14.03660 + 0.I$
$b = 0.890974 + 0.177764I$		
$u = 1.397250 - 0.182037I$		
$a = -0.506275 + 0.004273I$	$2.57061 - 4.43167I$	$14.03660 + 0.I$
$b = 0.890974 - 0.177764I$		
$u = -1.41231$		
$a = 0.496036$	6.54065	18.5250
$b = -0.916272$		
$u = 0.487776 + 0.155470I$		
$a = 2.02925 - 0.39422I$	$-4.99926 + 2.47497I$	$10.9995 - 16.9397I$
$b = 2.51703 - 0.23875I$		
$u = 0.487776 - 0.155470I$		
$a = 2.02925 + 0.39422I$	$-4.99926 - 2.47497I$	$10.9995 + 16.9397I$
$b = 2.51703 + 0.23875I$		
$u = 0.497461$		
$a = -0.110298$	0.683544	14.8150
$b = 0.387162$		
$u = -1.05090 + 1.14678I$		
$a = 0.504687 + 0.968425I$	$-11.9065 - 13.7324I$	0
$b = -0.54621 + 2.11520I$		
$u = -1.05090 - 1.14678I$		
$a = 0.504687 - 0.968425I$	$-11.9065 + 13.7324I$	0
$b = -0.54621 - 2.11520I$		
$u = 1.05595 + 1.16152I$		
$a = -0.501764 + 0.917028I$	$-6.55369 + 9.57234I$	0
$b = 0.55418 + 2.07855I$		
$u = 1.05595 - 1.16152I$		
$a = -0.501764 - 0.917028I$	$-6.55369 - 9.57234I$	0
$b = 0.55418 - 2.07855I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.10127 + 1.14227I$		
$a = -0.673483 + 0.861835I$	$-16.5464 + 4.1585I$	0
$b = 0.42779 + 2.00411I$		
$u = 1.10127 - 1.14227I$		
$a = -0.673483 - 0.861835I$	$-16.5464 - 4.1585I$	0
$b = 0.42779 - 2.00411I$		
$u = -1.07763 + 1.17451I$		
$a = 0.535143 + 0.849624I$	$-8.52808 - 4.96231I$	0
$b = -0.54248 + 2.02413I$		
$u = -1.07763 - 1.17451I$		
$a = 0.535143 - 0.849624I$	$-8.52808 + 4.96231I$	0
$b = -0.54248 - 2.02413I$		
$u = -1.16301 + 1.12527I$		
$a = 0.754065 + 0.641582I$	$-11.60780 + 5.44383I$	0
$b = -0.40895 + 1.76685I$		
$u = -1.16301 - 1.12527I$		
$a = 0.754065 - 0.641582I$	$-11.60780 - 5.44383I$	0
$b = -0.40895 - 1.76685I$		
$u = -0.373875$		
$a = -2.77728$	$-0.771990$	64.9410
$b = -3.15116$		
$u = -1.13639 + 1.17348I$		
$a = 0.623222 + 0.717077I$	$-8.37413 - 3.52292I$	0
$b = -0.51317 + 1.89056I$		
$u = -1.13639 - 1.17348I$		
$a = 0.623222 - 0.717077I$	$-8.37413 + 3.52292I$	0
$b = -0.51317 - 1.89056I$		
$u = 1.16288 + 1.15013I$		
$a = -0.687885 + 0.655673I$	$-6.27214 - 1.18033I$	0
$b = 0.47499 + 1.80580I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.16288 - 1.15013I$		
$a = -0.687885 - 0.655673I$	$-6.27214 + 1.18033I$	0
$b = 0.47499 - 1.80580I$		

$$\text{III. } I_2^u = \langle -u^5 + u^4 + 3u^3 - 2u^2 + b - u - 1, -u^5 + u^4 + 3u^3 - 2u^2 + a - 2u - 1, u^6 - u^5 - 3u^4 + 2u^3 + 2u^2 + u - 1 \rangle$$

(i) Arc colorings

$$a_5 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} u^5 - u^4 - 3u^3 + 2u^2 + 2u + 1 \\ u^5 - u^4 - 3u^3 + 2u^2 + u + 1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} u \\ -u^3 + u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} u \\ -u^3 + u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -u^2 + 1 \\ u^4 - 2u^2 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} u^5 - u^4 - 3u^3 + 2u^2 + 2u + 1 \\ u^5 - u^4 - 3u^3 + 2u^2 + 1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 0 \\ -u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} u^5 - u^4 - 3u^3 + 2u^2 + 2u + 1 \\ u^5 - u^4 - 3u^3 + 2u^2 + u + 1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -u^5 + 2u^3 + u \\ u^5 - 3u^3 + u \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} u \\ -u \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes =  $-7u^5 + 3u^4 + 19u^3 - 5u^2 - 8u - 6$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_2$	$(u - 1)^6$
$c_3, c_6$	$u^6$
$c_4$	$(u + 1)^6$
$c_5$	$u^6 + u^5 - 3u^4 - 2u^3 + 2u^2 - u - 1$
$c_7, c_8$	$u^6 - u^5 + 3u^4 - 2u^3 + 2u^2 - u - 1$
$c_9, c_{10}, c_{12}$	$u^6 - u^5 - 3u^4 + 2u^3 + 2u^2 + u - 1$
$c_{11}$	$u^6 + u^5 + 3u^4 + 2u^3 + 2u^2 + u - 1$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_4$	$(y - 1)^6$
$c_3, c_6$	$y^6$
$c_5, c_9, c_{10}$ $c_{12}$	$y^6 - 7y^5 + 17y^4 - 16y^3 + 6y^2 - 5y + 1$
$c_7, c_8, c_{11}$	$y^6 + 5y^5 + 9y^4 + 4y^3 - 6y^2 - 5y + 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.493180 + 0.575288I$		
$a = -0.858925 - 1.001920I$	$-4.60518 - 1.97241I$	$3.78159 + 4.50121I$
$b = -0.36575 - 1.57721I$		
$u = -0.493180 - 0.575288I$		
$a = -0.858925 + 1.001920I$	$-4.60518 + 1.97241I$	$3.78159 - 4.50121I$
$b = -0.36575 + 1.57721I$		
$u = 0.483672$		
$a = 2.06752$	$-0.906083$	$-8.91030$
$b = 1.58384$		
$u = 1.52087 + 0.16310I$		
$a = 0.650045 - 0.069710I$	$2.05064 + 4.59213I$	$-0.56679 - 5.39767I$
$b = -0.870821 - 0.232805I$		
$u = 1.52087 - 0.16310I$		
$a = 0.650045 + 0.069710I$	$2.05064 - 4.59213I$	$-0.56679 + 5.39767I$
$b = -0.870821 + 0.232805I$		
$u = -1.53904$		
$a = -0.649754$	$6.01515$	$2.48070$
$b = 0.889289$		

### III. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1$	$((u - 1)^6)(u^{41} + 47u^{40} + \dots + 296u + 1)$
$c_2$	$((u - 1)^6)(u^{41} - 7u^{40} + \dots - 12u + 1)$
$c_3, c_6$	$u^6(u^{41} + 7u^{40} + \dots + 640u - 64)$
$c_4$	$((u + 1)^6)(u^{41} - 7u^{40} + \dots - 12u + 1)$
$c_5$	$(u^6 + u^5 - 3u^4 - 2u^3 + 2u^2 - u - 1)(u^{41} + 2u^{40} + \dots - u - 1)$
$c_7, c_8$	$(u^6 - u^5 + 3u^4 - 2u^3 + 2u^2 - u - 1)(u^{41} + 2u^{40} + \dots + u + 1)$
$c_9$	$(u^6 - u^5 - 3u^4 + 2u^3 + 2u^2 + u - 1)(u^{41} + 2u^{40} + \dots - u - 1)$
$c_{10}, c_{12}$	$(u^6 - u^5 - 3u^4 + 2u^3 + 2u^2 + u - 1)(u^{41} - 2u^{40} + \dots - 47u + 17)$
$c_{11}$	$(u^6 + u^5 + 3u^4 + 2u^3 + 2u^2 + u - 1)(u^{41} + 2u^{40} + \dots + u + 1)$

#### IV. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1$	$((y - 1)^6)(y^{41} - 99y^{40} + \dots + 111528y - 1)$
$c_2, c_4$	$((y - 1)^6)(y^{41} - 47y^{40} + \dots + 296y - 1)$
$c_3, c_6$	$y^6(y^{41} + 39y^{40} + \dots + 90112y - 4096)$
$c_5, c_9$	$(y^6 - 7y^5 + \dots - 5y + 1)(y^{41} + 42y^{39} + \dots + 7y - 1)$
$c_7, c_8, c_{11}$	$(y^6 + 5y^5 + \dots - 5y + 1)(y^{41} + 36y^{40} + \dots + 7y - 1)$
$c_{10}, c_{12}$	$(y^6 - 7y^5 + 17y^4 - 16y^3 + 6y^2 - 5y + 1) \\ \cdot (y^{41} - 12y^{40} + \dots - 2041y - 289)$