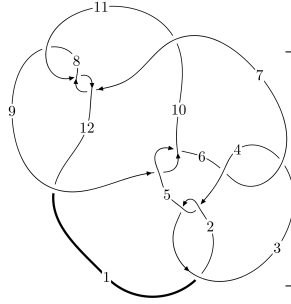
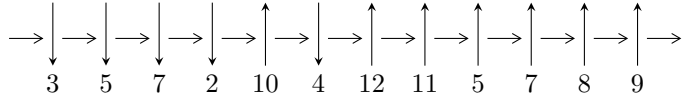


12n₀₁₁₈ (K12n₀₁₁₈)



A knot diagram¹

Linearized knot diagram



Solving Sequence

$$7,12 \xrightarrow{c_7} 4,8 \xrightarrow{c_3} 3 \xrightarrow{c_6} 6 \xrightarrow{c_{11}} 11 \xrightarrow{c_8} 9 \xrightarrow{c_{12}} 1 \xrightarrow{c_{10}} 10 \xrightarrow{c_5} 5 \xrightarrow{c_2} 2 \rightsquigarrow c_1, c_4, c_9$$

Ideals for irreducible components² of X_{par}

$$I_1^u = \langle -647u^{17} + 2375u^{16} + \dots + 9396b - 4651, -6142u^{17} + 31873u^{16} + \dots + 9396a - 63899, u^{18} - 5u^{17} + \dots + 9u + 1 \rangle$$

$$I_2^u = \langle au - u^2 + b + a + u + 1, -2u^2a + a^2 - 2au + 4u^2 - a + 8, u^3 + u^2 + 2u + 1 \rangle$$

$$I_3^u = \langle b, u^5 - 2u^4 + 4u^3 - 4u^2 + a + 3u - 2, u^6 - u^5 + 3u^4 - 2u^3 + 2u^2 - u - 1 \rangle$$

$$I_4^u = \langle b - u, u^2 + a + u + 1, u^3 + u^2 + 2u + 1 \rangle$$

* 4 irreducible components of $\dim_{\mathbb{C}} = 0$, with total 33 representations.

¹The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

²All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\mathbf{I. } I_1^u = \langle -647u^{17} + 2375u^{16} + \dots + 9396b - 4651, -6142u^{17} + 31873u^{16} + \dots + 9396a - 63899, u^{18} - 5u^{17} + \dots + 9u + 1 \rangle$$

(i) Arc colorings

$$a_7 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 0.653682u^{17} - 3.39219u^{16} + \dots - 10.7699u + 6.80066 \\ 0.0688591u^{17} - 0.252767u^{16} + \dots + 0.207322u + 0.494998 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 0.722542u^{17} - 3.64496u^{16} + \dots - 10.5626u + 7.29566 \\ 0.0688591u^{17} - 0.252767u^{16} + \dots + 0.207322u + 0.494998 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 0.257450u^{17} - 0.780438u^{16} + \dots - 0.469455u - 2.80502 \\ -0.357812u^{17} + 1.57620u^{16} + \dots + 3.73297u + 0.156982 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -u \\ u^3 + u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} u^2 + 1 \\ -u^4 - 2u^2 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} u^5 + 2u^3 + u \\ -u^7 - 3u^5 - 2u^3 + u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -u^3 - 2u \\ u^3 + u \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -0.00500213u^{17} + 0.206152u^{16} + \dots + 1.80449u - 2.50234 \\ -0.181141u^{17} + 0.997233u^{16} + \dots + 2.45732u - 0.00500213 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 0.232546u^{17} - 1.30726u^{16} + \dots - 5.17156u + 5.55034 \\ 0.181141u^{17} - 0.997233u^{16} + \dots - 2.45732u + 0.00500213 \end{pmatrix}$$

(ii) Obstruction class = -1

$$\text{(iii) Cusp Shapes} = -\frac{2501}{1566}u^{17} + \frac{12545}{1566}u^{16} + \dots + \frac{44011}{3132}u - \frac{28247}{3132}$$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1	$u^{18} + 10u^{17} + \dots + 526u + 1$
c_2, c_4	$u^{18} - 10u^{17} + \dots + 14u + 1$
c_3, c_6	$u^{18} - 4u^{17} + \dots + 256u - 64$
c_5, c_9	$u^{18} + 9u^{17} + \dots - 2048u - 512$
c_7, c_8, c_{11}	$u^{18} + 5u^{17} + \dots - 9u + 1$
c_{10}, c_{12}	$u^{18} - 5u^{17} + \dots - 497u + 49$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1	$y^{18} + 134y^{17} + \dots - 240078y + 1$
c_2, c_4	$y^{18} - 10y^{17} + \dots - 526y + 1$
c_3, c_6	$y^{18} + 48y^{17} + \dots - 81920y + 4096$
c_5, c_9	$y^{18} - 63y^{17} + \dots - 3014656y + 262144$
c_7, c_8, c_{11}	$y^{18} + 13y^{17} + \dots - 109y + 1$
c_{10}, c_{12}	$y^{18} - 47y^{17} + \dots - 257005y + 2401$

(vi) Complex Volumes and Cusp Shapes

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.405109 + 0.770998I$ $a = -0.291015 - 0.772728I$ $b = 1.202570 + 0.386446I$	$-1.63880 - 0.39759I$	$1.43515 + 1.37331I$
$u = -0.405109 - 0.770998I$ $a = -0.291015 + 0.772728I$ $b = 1.202570 - 0.386446I$	$-1.63880 + 0.39759I$	$1.43515 - 1.37331I$
$u = 0.725373 + 0.450694I$ $a = -1.51182 - 2.82088I$ $b = 0.43981 + 1.86757I$	$4.14833 - 1.63757I$	$3.60384 - 0.80616I$
$u = 0.725373 - 0.450694I$ $a = -1.51182 + 2.82088I$ $b = 0.43981 - 1.86757I$	$4.14833 + 1.63757I$	$3.60384 + 0.80616I$
$u = 1.194030 + 0.232985I$ $a = 1.74711 - 4.55330I$ $b = -1.67536 + 2.69388I$	$-16.4086 + 6.1635I$	$4.05351 - 2.26793I$
$u = 1.194030 - 0.232985I$ $a = 1.74711 + 4.55330I$ $b = -1.67536 - 2.69388I$	$-16.4086 - 6.1635I$	$4.05351 + 2.26793I$
$u = 0.360607 + 1.183990I$ $a = 0.448733 + 1.258690I$ $b = 0.550074 - 0.990997I$	$1.63305 + 5.70935I$	$3.81042 - 6.18784I$
$u = 0.360607 - 1.183990I$ $a = 0.448733 - 1.258690I$ $b = 0.550074 + 0.990997I$	$1.63305 - 5.70935I$	$3.81042 + 6.18784I$
$u = -0.110512 + 1.276710I$ $a = -0.353124 - 0.089950I$ $b = -0.038877 + 0.478514I$	$-3.23015 - 1.96870I$	$3.57157 + 3.68129I$
$u = -0.110512 - 1.276710I$ $a = -0.353124 + 0.089950I$ $b = -0.038877 - 0.478514I$	$-3.23015 + 1.96870I$	$3.57157 - 3.68129I$

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.250746 + 1.287460I$ $a = -1.43169 + 2.15528I$ $b = -0.532012 - 0.309792I$	$-4.27182 - 2.53682I$	$-10.79254 + 3.39126I$
$u = -0.250746 - 1.287460I$ $a = -1.43169 - 2.15528I$ $b = -0.532012 + 0.309792I$	$-4.27182 + 2.53682I$	$-10.79254 - 3.39126I$
$u = -0.456369$ $a = -0.475415$ $b = -0.212377$	0.789107	12.7820
$u = 0.48335 + 1.48077I$ $a = -0.44539 - 2.81436I$ $b = -1.31271 + 2.12200I$	$17.6239 + 12.0475I$	$1.51476 - 4.65853I$
$u = 0.48335 - 1.48077I$ $a = -0.44539 + 2.81436I$ $b = -1.31271 - 2.12200I$	$17.6239 - 12.0475I$	$1.51476 + 4.65853I$
$u = 0.77938 + 1.42726I$ $a = 2.16835 + 3.72673I$ $b = -0.76484 - 3.84358I$	$19.6304 + 0.9404I$	$2.54501 - 0.81034I$
$u = 0.77938 - 1.42726I$ $a = 2.16835 - 3.72673I$ $b = -0.76484 + 3.84358I$	$19.6304 - 0.9404I$	$2.54501 + 0.81034I$
$u = -0.0963755$ $a = 7.81308$ $b = 0.475099$	-1.21816	-10.2650

II.

$$I_2^u = \langle au - u^2 + b + a + u + 1, -2u^2a + a^2 - 2au + 4u^2 - a + 8, u^3 + u^2 + 2u + 1 \rangle$$

(i) Arc colorings

$$a_7 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} a \\ -au + u^2 - a - u - 1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -au + u^2 - u - 1 \\ -au + u^2 - a - u - 1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} u^2a - 3 \\ -u^2a - 2au - a - 3u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -u \\ -u^2 - u - 1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} u^2 + 1 \\ -u^2 - u - 1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} u^2 + 1 \\ -u^2 - u - 1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} u^2a - 3 \\ -u^2a - 2au - a - 3u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -2au - a - 3u - 5 \\ -u^2a - 2au - a - 3u \end{pmatrix}$$

(ii) Obstruction class = 1

$$\text{(iii) Cusp Shapes} = u^2a - 10au + 11u^2 - 4a$$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1, c_3, c_{11}	$(u^3 - u^2 + 2u - 1)^2$
c_2, c_{10}, c_{12}	$(u^3 + u^2 - 1)^2$
c_4	$(u^3 - u^2 + 1)^2$
c_5, c_9	u^6
c_6, c_7, c_8	$(u^3 + u^2 + 2u + 1)^2$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1, c_3, c_6 c_7, c_8, c_{11}	$(y^3 + 3y^2 + 2y - 1)^2$
c_2, c_4, c_{10} c_{12}	$(y^3 - y^2 + 2y - 1)^2$
c_5, c_9	y^6

(vi) Complex Volumes and Cusp Shapes

Solutions to I_2^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.215080 + 1.307140I$ $a = -1.06984 + 1.06527I$ $b = -0.215080 - 1.307140I$	$-5.65624I$	$-0.00556 + 4.66003I$
$u = -0.215080 + 1.307140I$ $a = -1.68504 + 0.42445I$ $b = -0.569840$	$-4.13758 - 2.82812I$	$-6.5820 + 15.2977I$
$u = -0.215080 - 1.307140I$ $a = -1.06984 - 1.06527I$ $b = -0.215080 + 1.307140I$	$5.65624I$	$-0.00556 - 4.66003I$
$u = -0.215080 - 1.307140I$ $a = -1.68504 - 0.42445I$ $b = -0.569840$	$-4.13758 + 2.82812I$	$-6.5820 - 15.2977I$
$u = -0.569840$ $a = 0.25488 + 3.03873I$ $b = -0.215080 - 1.307140I$	$4.13758 - 2.82812I$	$4.08755 + 6.14773I$
$u = -0.569840$ $a = 0.25488 - 3.03873I$ $b = -0.215080 + 1.307140I$	$4.13758 + 2.82812I$	$4.08755 - 6.14773I$

III.

$$I_3^u = \langle b, u^5 - 2u^4 + 4u^3 - 4u^2 + a + 3u - 2, u^6 - u^5 + 3u^4 - 2u^3 + 2u^2 - u - 1 \rangle$$

(i) Arc colorings

$$a_7 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -u^5 + 2u^4 - 4u^3 + 4u^2 - 3u + 2 \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -u^5 + 2u^4 - 4u^3 + 4u^2 - 3u + 2 \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -u \\ u^3 + u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} u^2 + 1 \\ -u^4 - 2u^2 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} u^5 + 2u^3 + u \\ -u^5 + u^4 - 2u^3 + u^2 - u - 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -u^3 - 2u \\ u^3 + u \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -u^5 - 2u^3 - u \\ u^5 - u^4 + 2u^3 - u^2 + u + 1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 2u^4 - 2u^3 + 4u^2 - 2u + 2 \\ -u^5 + u^4 - 2u^3 + u^2 - u - 1 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = $-u^5 + 7u^4 - 13u^3 + 20u^2 - 15u + 13$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1, c_2	$(u - 1)^6$
c_3, c_6	u^6
c_4	$(u + 1)^6$
c_5	$u^6 + u^5 - 3u^4 - 2u^3 + 2u^2 - u - 1$
c_7, c_8	$u^6 - u^5 + 3u^4 - 2u^3 + 2u^2 - u - 1$
c_9, c_{10}, c_{12}	$u^6 - u^5 - 3u^4 + 2u^3 + 2u^2 + u - 1$
c_{11}	$u^6 + u^5 + 3u^4 + 2u^3 + 2u^2 + u - 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1, c_2, c_4	$(y - 1)^6$
c_3, c_6	y^6
c_5, c_9, c_{10} c_{12}	$y^6 - 7y^5 + 17y^4 - 16y^3 + 6y^2 - 5y + 1$
c_7, c_8, c_{11}	$y^6 + 5y^5 + 9y^4 + 4y^3 - 6y^2 - 5y + 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to I_3^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.873214$ $a = 0.422181$ $b = 0$	6.01515	10.0580
$u = -0.138835 + 1.234450I$ $a = -0.26610 + 1.72116I$ $b = 0$	$-4.60518 - 1.97241I$	$-6.63014 + 2.86834I$
$u = -0.138835 - 1.234450I$ $a = -0.26610 - 1.72116I$ $b = 0$	$-4.60518 + 1.97241I$	$-6.63014 - 2.86834I$
$u = 0.408802 + 1.276380I$ $a = 0.417699 - 0.090629I$ $b = 0$	$2.05064 + 4.59213I$	$5.72906 - 1.01197I$
$u = 0.408802 - 1.276380I$ $a = 0.417699 + 0.090629I$ $b = 0$	$2.05064 - 4.59213I$	$5.72906 + 1.01197I$
$u = -0.413150$ $a = 4.27462$ $b = 0$	-0.906083	23.7440

$$\text{IV. } I_4^u = \langle b - u, u^2 + a + u + 1, u^3 + u^2 + 2u + 1 \rangle$$

(i) Arc colorings

$$a_7 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -u^2 - u - 1 \\ u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -u^2 - 1 \\ u \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -u \\ -u^2 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -u \\ -u^2 - u - 1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} u^2 + 1 \\ -u^2 - u - 1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} u^2 + 1 \\ -u^2 - u - 1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -u \\ -u^2 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -u^2 - u - 2 \\ -u^2 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = $-4u^2 - 3u - 4$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1, c_3, c_{11}	$u^3 - u^2 + 2u - 1$
c_2, c_{10}, c_{12}	$u^3 + u^2 - 1$
c_4	$u^3 - u^2 + 1$
c_5, c_9	u^3
c_6, c_7, c_8	$u^3 + u^2 + 2u + 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1, c_3, c_6 c_7, c_8, c_{11}	$y^3 + 3y^2 + 2y - 1$
c_2, c_4, c_{10} c_{12}	$y^3 - y^2 + 2y - 1$
c_5, c_9	y^3

(vi) Complex Volumes and Cusp Shapes

Solutions to I_4^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.215080 + 1.307140I$ $a = 0.877439 - 0.744862I$ $b = -0.215080 + 1.307140I$	0	$3.29468 - 1.67231I$
$u = -0.215080 - 1.307140I$ $a = 0.877439 + 0.744862I$ $b = -0.215080 - 1.307140I$	0	$3.29468 + 1.67231I$
$u = -0.569840$ $a = -0.754878$ $b = -0.569840$	0	-3.58940

V. u-Polynomials

Crossings	u-Polynomials at each crossing
c_1	$((u-1)^6)(u^3-u^2+2u-1)^3(u^{18}+10u^{17}+\dots+526u+1)$
c_2	$((u-1)^6)(u^3+u^2-1)^3(u^{18}-10u^{17}+\dots+14u+1)$
c_3	$u^6(u^3-u^2+2u-1)^3(u^{18}-4u^{17}+\dots+256u-64)$
c_4	$((u+1)^6)(u^3-u^2+1)^3(u^{18}-10u^{17}+\dots+14u+1)$
c_5	$u^9(u^6+u^5+\dots-u-1)(u^{18}+9u^{17}+\dots-2048u-512)$
c_6	$u^6(u^3+u^2+2u+1)^3(u^{18}-4u^{17}+\dots+256u-64)$
c_7, c_8	$(u^3+u^2+2u+1)^3(u^6-u^5+3u^4-2u^3+2u^2-u-1)$ $\cdot (u^{18}+5u^{17}+\dots-9u+1)$
c_9	$u^9(u^6-u^5+\dots+u-1)(u^{18}+9u^{17}+\dots-2048u-512)$
c_{10}, c_{12}	$(u^3+u^2-1)^3(u^6-u^5-3u^4+2u^3+2u^2+u-1)$ $\cdot (u^{18}-5u^{17}+\dots-497u+49)$
c_{11}	$(u^3-u^2+2u-1)^3(u^6+u^5+3u^4+2u^3+2u^2+u-1)$ $\cdot (u^{18}+5u^{17}+\dots-9u+1)$

VI. Riley Polynomials

Crossings	Riley Polynomials at each crossing
c_1	$((y-1)^6)(y^3+3y^2+2y-1)^3(y^{18}+134y^{17}+\dots-240078y+1)$
c_2, c_4	$((y-1)^6)(y^3-y^2+2y-1)^3(y^{18}-10y^{17}+\dots-526y+1)$
c_3, c_6	$y^6(y^3+3y^2+2y-1)^3(y^{18}+48y^{17}+\dots-81920y+4096)$
c_5, c_9	$y^9(y^6-7y^5+17y^4-16y^3+6y^2-5y+1)$ $\cdot (y^{18}-63y^{17}+\dots-3014656y+262144)$
c_7, c_8, c_{11}	$(y^3+3y^2+2y-1)^3(y^6+5y^5+9y^4+4y^3-6y^2-5y+1)$ $\cdot (y^{18}+13y^{17}+\dots-109y+1)$
c_{10}, c_{12}	$(y^3-y^2+2y-1)^3(y^6-7y^5+17y^4-16y^3+6y^2-5y+1)$ $\cdot (y^{18}-47y^{17}+\dots-257005y+2401)$