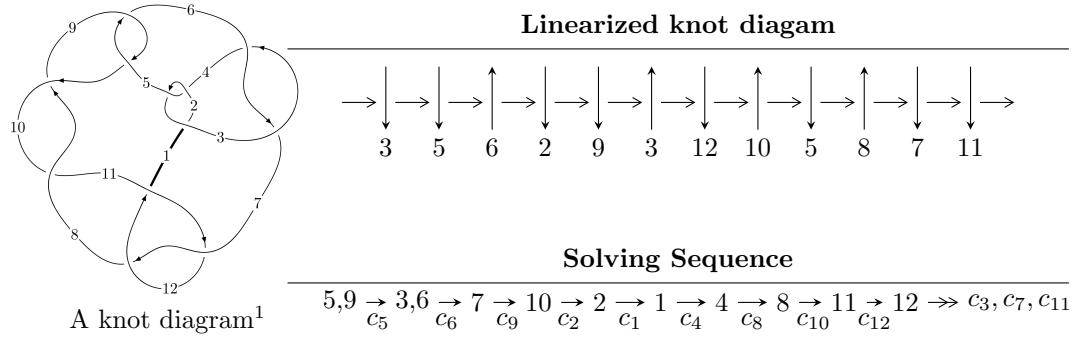


$12n_{0119}$ ($K12n_{0119}$)



Ideals for irreducible components² of X_{par}

$$I_1^u = \langle 6027u^{16} + 12005u^{15} + \dots + 18155b + 3034, 2046u^{16} + 7175u^{15} + \dots + 18155a - 15643,$$

$$u^{17} + 2u^{16} + 2u^{15} + 7u^{13} + 14u^{12} + 14u^{11} + 2u^{10} + 7u^9 + 14u^8 + 14u^7 + 12u^6 + 2u^2 - u - 1 \rangle$$

$$I_2^u = \langle b + 1, u^8 + 2u^7 + 3u^6 + 3u^5 + 4u^4 + 4u^3 + 3u^2 + a + 2u + 1, u^9 + u^8 + 2u^7 + u^6 + 3u^5 + u^4 + 2u^3 + u - 1 \rangle$$

* 2 irreducible components of $\dim_{\mathbb{C}} = 0$, with total 26 representations.

¹The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/math/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

²All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\text{I. } I_1^u = \langle 6027u^{16} + 12005u^{15} + \cdots + 18155b + 3034, 2046u^{16} + 7175u^{15} + \cdots + 18155a - 15643, u^{17} + 2u^{16} + \cdots - u - 1 \rangle$$

(i) **Arc colorings**

$$\begin{aligned} a_5 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_9 &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_3 &= \begin{pmatrix} -0.112696u^{16} - 0.395208u^{15} + \cdots - 0.119581u + 0.861636 \\ -0.331975u^{16} - 0.661250u^{15} + \cdots - 0.611787u - 0.167116 \end{pmatrix} \\ a_6 &= \begin{pmatrix} 1 \\ u^2 \end{pmatrix} \\ a_7 &= \begin{pmatrix} -0.297108u^{16} - 0.860094u^{15} + \cdots - 0.406169u + 0.544313 \\ -0.309777u^{16} - 0.234922u^{15} + \cdots - 0.512476u + 0.102561 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} -u \\ u \end{pmatrix} \\ a_2 &= \begin{pmatrix} -0.444671u^{16} - 1.05646u^{15} + \cdots - 0.731369u + 0.694519 \\ -0.331975u^{16} - 0.661250u^{15} + \cdots - 0.611787u - 0.167116 \end{pmatrix} \\ a_1 &= \begin{pmatrix} -0.389535u^{16} - 1.25558u^{15} + \cdots - 0.355660u + 0.912751 \\ 0.0924263u^{16} + 0.395483u^{15} + \cdots - 0.0505095u - 0.368438 \end{pmatrix} \\ a_4 &= \begin{pmatrix} -0.120848u^{16} - 0.427706u^{15} + \cdots - 0.448857u + 0.864335 \\ -0.283063u^{16} - 0.466263u^{15} + \cdots - 0.636133u - 0.183310 \end{pmatrix} \\ a_8 &= \begin{pmatrix} -u^3 \\ u^3 + u \end{pmatrix} \\ a_{11} &= \begin{pmatrix} -u^5 - u \\ u^5 + u^3 + u \end{pmatrix} \\ a_{12} &= \begin{pmatrix} -0.802534u^{16} - 0.874966u^{15} + \cdots - 0.821261u + 0.711650 \\ 0.114128u^{16} - 0.545029u^{15} + \cdots + 0.609860u - 0.0377857 \end{pmatrix} \end{aligned}$$

(ii) **Obstruction class** = -1

(iii) **Cusp Shapes** = $\frac{25781}{18155}u^{16} + \frac{6669}{3631}u^{15} + \cdots + \frac{4791}{18155}u - \frac{139178}{18155}$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1	$u^{17} + 40u^{16} + \cdots + 501u + 1$
c_2, c_4	$u^{17} - 10u^{16} + \cdots + 25u - 1$
c_3, c_6	$u^{17} + 3u^{16} + \cdots + 512u + 512$
c_5, c_9	$u^{17} + 2u^{16} + \cdots - u - 1$
c_7, c_{11}	$u^{17} - 2u^{16} + \cdots - u - 1$
c_8, c_{10}	$u^{17} + 18u^{15} + \cdots + 5u + 1$
c_{12}	$u^{17} + 12u^{16} + \cdots + 5u + 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1	$y^{17} - 244y^{16} + \cdots + 241285y - 1$
c_2, c_4	$y^{17} - 40y^{16} + \cdots + 501y - 1$
c_3, c_6	$y^{17} + 57y^{16} + \cdots + 6553600y - 262144$
c_5, c_9	$y^{17} + 18y^{15} + \cdots + 5y - 1$
c_7, c_{11}	$y^{17} - 12y^{16} + \cdots + 5y - 1$
c_8, c_{10}	$y^{17} + 36y^{16} + \cdots + 17y - 1$
c_{12}	$y^{17} - 12y^{16} + \cdots + 81y - 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.01926$		
$a = 1.09396$	-7.51678	-13.0910
$b = -2.50941$		
$u = 0.814269 + 0.697849I$		
$a = -0.135222 + 1.183260I$	-3.61218 - 4.89234I	-8.33842 + 5.53487I
$b = -0.021919 - 1.343220I$		
$u = 0.814269 - 0.697849I$		
$a = -0.135222 - 1.183260I$	-3.61218 + 4.89234I	-8.33842 - 5.53487I
$b = -0.021919 + 1.343220I$		
$u = -0.151212 + 0.886118I$		
$a = 0.259000 - 0.151859I$	1.33808 + 1.89910I	2.88769 - 4.28758I
$b = 0.317232 + 0.130128I$		
$u = -0.151212 - 0.886118I$		
$a = 0.259000 + 0.151859I$	1.33808 - 1.89910I	2.88769 + 4.28758I
$b = 0.317232 - 0.130128I$		
$u = -0.524511 + 0.603470I$		
$a = 0.421833 - 0.890237I$	-0.23007 + 1.50880I	-2.26409 - 4.36176I
$b = -0.173796 + 0.509907I$		
$u = -0.524511 - 0.603470I$		
$a = 0.421833 + 0.890237I$	-0.23007 - 1.50880I	-2.26409 + 4.36176I
$b = -0.173796 - 0.509907I$		
$u = 0.413009 + 0.524274I$		
$a = 2.66953 + 0.96171I$	-3.04819 + 0.77610I	-9.75157 + 2.68802I
$b = -0.655191 + 0.306962I$		
$u = 0.413009 - 0.524274I$		
$a = 2.66953 - 0.96171I$	-3.04819 - 0.77610I	-9.75157 - 2.68802I
$b = -0.655191 - 0.306962I$		
$u = 0.568174$		
$a = -1.49974$	-2.38424	-2.38490
$b = -1.19167$		

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.471408$		
$a = 1.15792$	-1.25348	-8.31380
$b = 0.0451202$		
$u = -1.08781 + 1.09421I$		
$a = -1.21553 + 1.53450I$	$15.4466 + 9.8759I$	$-8.70686 - 4.52620I$
$b = 2.42560 - 0.51435I$		
$u = -1.08781 - 1.09421I$		
$a = -1.21553 - 1.53450I$	$15.4466 - 9.8759I$	$-8.70686 + 4.52620I$
$b = 2.42560 + 0.51435I$		
$u = 1.09696 + 1.09725I$		
$a = -1.31679 - 1.21871I$	$19.7302 - 4.0499I$	$-6.15248 + 1.91448I$
$b = 2.40736 + 0.21866I$		
$u = 1.09696 - 1.09725I$		
$a = -1.31679 + 1.21871I$	$19.7302 + 4.0499I$	$-6.15248 - 1.91448I$
$b = 2.40736 - 0.21866I$		
$u = -1.09946 + 1.09842I$		
$a = -1.55889 + 0.97165I$	$15.4312 - 1.7937I$	$-8.77960 + 0.70466I$
$b = 2.52869 + 0.07532I$		
$u = -1.09946 - 1.09842I$		
$a = -1.55889 - 0.97165I$	$15.4312 + 1.7937I$	$-8.77960 - 0.70466I$
$b = 2.52869 - 0.07532I$		

II.

$$I_2^u = \langle b+1, u^8 + 2u^7 + \dots + a+1, u^9 + u^8 + 2u^7 + u^6 + 3u^5 + u^4 + 2u^3 + u - 1 \rangle$$

(i) **Arc colorings**

$$a_5 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -u^8 - 2u^7 - 3u^6 - 3u^5 - 4u^4 - 4u^3 - 3u^2 - 2u - 1 \\ -1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -u \\ u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -u^8 - 2u^7 - 3u^6 - 3u^5 - 4u^4 - 4u^3 - 3u^2 - 2u - 2 \\ -1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -u^8 - 2u^7 - 3u^6 - 3u^5 - 4u^4 - 4u^3 - 3u^2 - 2u - 1 \\ -1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -u^3 \\ u^3 + u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -u^5 - u \\ u^5 + u^3 + u \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -u^7 - 2u^5 - 2u^3 - 2u \\ u^8 + u^7 + u^6 + 2u^5 + u^4 + 2u^3 + 2u - 1 \end{pmatrix}$$

(ii) **Obstruction class** = 1

(iii) **Cusp Shapes** = $-3u^8 - 8u^7 - 12u^6 - 11u^5 - 18u^4 - 17u^3 - 15u^2 - 6u - 16$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1, c_2	$(u - 1)^9$
c_3, c_6	u^9
c_4	$(u + 1)^9$
c_5	$u^9 + u^8 + 2u^7 + u^6 + 3u^5 + u^4 + 2u^3 + u - 1$
c_7	$u^9 + u^8 - 2u^7 - 3u^6 + u^5 + 3u^4 + 2u^3 - u - 1$
c_8	$u^9 + 3u^8 + 8u^7 + 13u^6 + 17u^5 + 17u^4 + 12u^3 + 6u^2 + u - 1$
c_9	$u^9 - u^8 + 2u^7 - u^6 + 3u^5 - u^4 + 2u^3 + u + 1$
c_{10}	$u^9 - 3u^8 + 8u^7 - 13u^6 + 17u^5 - 17u^4 + 12u^3 - 6u^2 + u + 1$
c_{11}	$u^9 - u^8 - 2u^7 + 3u^6 + u^5 - 3u^4 + 2u^3 - u + 1$
c_{12}	$u^9 + 5u^8 + 12u^7 + 15u^6 + 9u^5 - u^4 - 4u^3 - 2u^2 + u + 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1, c_2, c_4	$(y - 1)^9$
c_3, c_6	y^9
c_5, c_9	$y^9 + 3y^8 + 8y^7 + 13y^6 + 17y^5 + 17y^4 + 12y^3 + 6y^2 + y - 1$
c_7, c_{11}	$y^9 - 5y^8 + 12y^7 - 15y^6 + 9y^5 + y^4 - 4y^3 + 2y^2 + y - 1$
c_8, c_{10}	$y^9 + 7y^8 + 20y^7 + 25y^6 + 5y^5 - 15y^4 + 22y^2 + 13y - 1$
c_{12}	$y^9 - y^8 + 12y^7 - 7y^6 + 37y^5 + y^4 - 10y^2 + 5y - 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to I_2^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.140343 + 0.966856I$		
$a = 1.004430 + 0.297869I$	$0.13850 - 2.09337I$	$-5.16894 + 4.06115I$
$b = -1.00000$		
$u = 0.140343 - 0.966856I$		
$a = 1.004430 - 0.297869I$	$0.13850 + 2.09337I$	$-5.16894 - 4.06115I$
$b = -1.00000$		
$u = 0.628449 + 0.875112I$		
$a = 0.275254 + 0.816341I$	$-2.26187 - 2.45442I$	$-4.66498 + 3.27944I$
$b = -1.00000$		
$u = 0.628449 - 0.875112I$		
$a = 0.275254 - 0.816341I$	$-2.26187 + 2.45442I$	$-4.66498 - 3.27944I$
$b = -1.00000$		
$u = -0.796005 + 0.733148I$		
$a = -0.070080 - 0.850995I$	$-6.01628 - 1.33617I$	$-9.21174 + 0.80685I$
$b = -1.00000$		
$u = -0.796005 - 0.733148I$		
$a = -0.070080 + 0.850995I$	$-6.01628 + 1.33617I$	$-9.21174 - 0.80685I$
$b = -1.00000$		
$u = -0.728966 + 0.986295I$		
$a = 0.195086 - 0.635552I$	$-5.24306 + 7.08493I$	$-7.33806 - 6.93476I$
$b = -1.00000$		
$u = -0.728966 - 0.986295I$		
$a = 0.195086 + 0.635552I$	$-5.24306 - 7.08493I$	$-7.33806 + 6.93476I$
$b = -1.00000$		
$u = 0.512358$		
$a = -3.80937$	-2.84338	-27.2330
$b = -1.00000$		

III. u-Polynomials

Crossings	u-Polynomials at each crossing
c_1	$((u - 1)^9)(u^{17} + 40u^{16} + \dots + 501u + 1)$
c_2	$((u - 1)^9)(u^{17} - 10u^{16} + \dots + 25u - 1)$
c_3, c_6	$u^9(u^{17} + 3u^{16} + \dots + 512u + 512)$
c_4	$((u + 1)^9)(u^{17} - 10u^{16} + \dots + 25u - 1)$
c_5	$(u^9 + u^8 + \dots + u - 1)(u^{17} + 2u^{16} + \dots - u - 1)$
c_7	$(u^9 + u^8 + \dots - u - 1)(u^{17} - 2u^{16} + \dots - u - 1)$
c_8	$(u^9 + 3u^8 + 8u^7 + 13u^6 + 17u^5 + 17u^4 + 12u^3 + 6u^2 + u - 1) \cdot (u^{17} + 18u^{15} + \dots + 5u + 1)$
c_9	$(u^9 - u^8 + \dots + u + 1)(u^{17} + 2u^{16} + \dots - u - 1)$
c_{10}	$(u^9 - 3u^8 + 8u^7 - 13u^6 + 17u^5 - 17u^4 + 12u^3 - 6u^2 + u + 1) \cdot (u^{17} + 18u^{15} + \dots + 5u + 1)$
c_{11}	$(u^9 - u^8 + \dots - u + 1)(u^{17} - 2u^{16} + \dots - u - 1)$
c_{12}	$(u^9 + 5u^8 + 12u^7 + 15u^6 + 9u^5 - u^4 - 4u^3 - 2u^2 + u + 1) \cdot (u^{17} + 12u^{16} + \dots + 5u + 1)$

IV. Riley Polynomials

Crossings	Riley Polynomials at each crossing
c_1	$((y - 1)^9)(y^{17} - 244y^{16} + \dots + 241285y - 1)$
c_2, c_4	$((y - 1)^9)(y^{17} - 40y^{16} + \dots + 501y - 1)$
c_3, c_6	$y^9(y^{17} + 57y^{16} + \dots + 6553600y - 262144)$
c_5, c_9	$(y^9 + 3y^8 + 8y^7 + 13y^6 + 17y^5 + 17y^4 + 12y^3 + 6y^2 + y - 1) \cdot (y^{17} + 18y^{15} + \dots + 5y - 1)$
c_7, c_{11}	$(y^9 - 5y^8 + 12y^7 - 15y^6 + 9y^5 + y^4 - 4y^3 + 2y^2 + y - 1) \cdot (y^{17} - 12y^{16} + \dots + 5y - 1)$
c_8, c_{10}	$(y^9 + 7y^8 + 20y^7 + 25y^6 + 5y^5 - 15y^4 + 22y^2 + 13y - 1) \cdot (y^{17} + 36y^{16} + \dots + 17y - 1)$
c_{12}	$(y^9 - y^8 + 12y^7 - 7y^6 + 37y^5 + y^4 - 10y^2 + 5y - 1) \cdot (y^{17} - 12y^{16} + \dots + 81y - 1)$