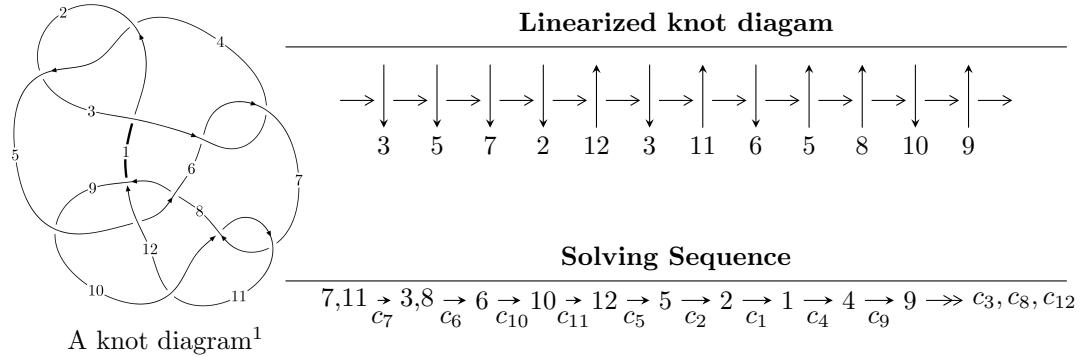


$12n_{0122}$  ( $K12n_{0122}$ )



Ideals for irreducible components<sup>2</sup> of  $X_{\text{par}}$

$$\begin{aligned}
 I_1^u &= \langle -5.51787 \times 10^{81} u^{67} + 2.11041 \times 10^{82} u^{66} + \dots + 3.86959 \times 10^{83} b + 2.32790 \times 10^{83}, \\
 &\quad 2.89477 \times 10^{83} u^{67} - 1.45377 \times 10^{84} u^{66} + \dots + 3.86959 \times 10^{83} a + 1.55319 \times 10^{85}, u^{68} - 5u^{67} + \dots + 61u + \\
 I_2^u &= \langle b, -u^8 + 2u^7 - 3u^6 + 2u^5 - 3u^4 + 2u^3 - 2u^2 + a - 1, u^9 - u^8 + 2u^7 - u^6 + 3u^5 - u^4 + 2u^3 + u + 1 \rangle \\
 I_3^u &= \langle -120a^2u - 76a^2 - 865au + 691b - 663a + 177u + 43, a^3 - a^2u + 7a^2 - 4au - 3a - 5u - 12, \\
 &\quad u^2 + u + 1 \rangle
 \end{aligned}$$

\* 3 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 83 representations.

<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/math/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\text{I. } I_1^u = \langle -5.52 \times 10^{81}u^{67} + 2.11 \times 10^{82}u^{66} + \dots + 3.87 \times 10^{83}b + 2.33 \times 10^{83}, \ 2.89 \times 10^{83}u^{67} - 1.45 \times 10^{84}u^{66} + \dots + 3.87 \times 10^{83}a + 1.55 \times 10^{85}, \ u^{68} - 5u^{67} + \dots + 61u + 1 \rangle$$

(i) **Arc colorings**

$$\begin{aligned} a_7 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_{11} &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_3 &= \begin{pmatrix} -0.748081u^{67} + 3.75690u^{66} + \dots + 210.979u - 40.1384 \\ 0.0142596u^{67} - 0.0545384u^{66} + \dots - 3.15431u - 0.601589 \end{pmatrix} \\ a_8 &= \begin{pmatrix} 1 \\ -u^2 \end{pmatrix} \\ a_6 &= \begin{pmatrix} -0.341935u^{67} + 1.84496u^{66} + \dots + 122.527u - 21.0582 \\ -0.0113435u^{67} + 0.205218u^{66} + \dots + 3.86731u - 0.239724 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} -u \\ u^3 + u \end{pmatrix} \\ a_{12} &= \begin{pmatrix} -u^3 \\ u^5 + u^3 + u \end{pmatrix} \\ a_5 &= \begin{pmatrix} -0.338281u^{67} + 1.62581u^{66} + \dots + 112.042u - 21.2277 \\ 0.0236591u^{67} - 0.0564694u^{66} + \dots + 3.36495u - 0.255517 \end{pmatrix} \\ a_2 &= \begin{pmatrix} -0.330587u^{67} + 1.67938u^{66} + \dots + 116.221u - 23.6818 \\ 0.0236591u^{67} - 0.0564694u^{66} + \dots + 3.36495u - 0.255517 \end{pmatrix} \\ a_1 &= \begin{pmatrix} 0.0416035u^{67} - 0.370846u^{66} + \dots - 11.8634u + 0.807059 \\ 0.0469200u^{67} - 0.282851u^{66} + \dots - 0.607431u + 0.0154252 \end{pmatrix} \\ a_4 &= \begin{pmatrix} -0.762341u^{67} + 3.81144u^{66} + \dots + 214.133u - 39.5368 \\ 0.0142596u^{67} - 0.0545384u^{66} + \dots - 3.15431u - 0.601589 \end{pmatrix} \\ a_9 &= \begin{pmatrix} 0.105467u^{67} - 0.401649u^{66} + \dots - 40.5394u + 7.48605 \\ -0.151780u^{67} + 0.736790u^{66} + \dots + 7.94430u + 0.222620 \end{pmatrix} \end{aligned}$$

(ii) **Obstruction class** = -1

(iii) **Cusp Shapes** =  $-0.145860u^{67} + 0.285659u^{66} + \dots + 33.4674u - 8.97504$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1$	$u^{68} + 72u^{67} + \cdots - 116u + 1$
$c_2, c_4$	$u^{68} - 12u^{67} + \cdots + 4u - 1$
$c_3, c_6$	$u^{68} + 3u^{67} + \cdots + 2048u + 512$
$c_5$	$u^{68} + 4u^{67} + \cdots + 20u^2 - 1$
$c_7, c_{10}$	$u^{68} + 5u^{67} + \cdots - 61u + 1$
$c_8$	$u^{68} - 8u^{67} + \cdots - 679u + 1423$
$c_9$	$u^{68} - 4u^{67} + \cdots - 1569175u - 179693$
$c_{11}$	$u^{68} + 33u^{67} + \cdots - 4365u + 1$
$c_{12}$	$u^{68} + 6u^{67} + \cdots - 992u + 64$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1$	$y^{68} - 140y^{67} + \cdots + 13088y + 1$
$c_2, c_4$	$y^{68} - 72y^{67} + \cdots + 116y + 1$
$c_3, c_6$	$y^{68} - 51y^{67} + \cdots - 1048576y + 262144$
$c_5$	$y^{68} - 16y^{67} + \cdots - 40y + 1$
$c_7, c_{10}$	$y^{68} + 33y^{67} + \cdots - 4365y + 1$
$c_8$	$y^{68} - 68y^{67} + \cdots + 88237y + 2024929$
$c_9$	$y^{68} - 20y^{67} + \cdots - 70781434415y + 32289574249$
$c_{11}$	$y^{68} + 9y^{67} + \cdots - 19115909y + 1$
$c_{12}$	$y^{68} + 30y^{67} + \cdots - 332800y + 4096$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.424757 + 0.915138I$		
$a = -1.40780 + 0.30590I$	$2.67134 + 4.86258I$	$-14.4423 - 3.8383I$
$b = -0.22825 + 1.49715I$		
$u = 0.424757 - 0.915138I$		
$a = -1.40780 - 0.30590I$	$2.67134 - 4.86258I$	$-14.4423 + 3.8383I$
$b = -0.22825 - 1.49715I$		
$u = -0.485295 + 0.862009I$		
$a = -6.44205 + 2.64222I$	$-1.10951 - 2.08005I$	$43.7323 + 52.4587I$
$b = -0.604973 + 0.042933I$		
$u = -0.485295 - 0.862009I$		
$a = -6.44205 - 2.64222I$	$-1.10951 + 2.08005I$	$43.7323 - 52.4587I$
$b = -0.604973 - 0.042933I$		
$u = 0.731003 + 0.711801I$		
$a = 0.461608 + 0.068557I$	$3.23957 - 1.57241I$	$8.29788 + 4.00370I$
$b = -0.061104 - 0.642060I$		
$u = 0.731003 - 0.711801I$		
$a = 0.461608 - 0.068557I$	$3.23957 + 1.57241I$	$8.29788 - 4.00370I$
$b = -0.061104 + 0.642060I$		
$u = -0.532729 + 0.793838I$		
$a = -4.58885 - 1.30458I$	$-1.11507 - 2.15821I$	$-17.5757 + 1.3433I$
$b = -0.430627 + 0.271631I$		
$u = -0.532729 - 0.793838I$		
$a = -4.58885 + 1.30458I$	$-1.11507 + 2.15821I$	$-17.5757 - 1.3433I$
$b = -0.430627 - 0.271631I$		
$u = 0.005378 + 0.951686I$		
$a = 0.387546 - 0.444818I$	$-1.99133 - 1.66625I$	$-3.10323 + 3.30828I$
$b = -0.238112 - 0.586278I$		
$u = 0.005378 - 0.951686I$		
$a = 0.387546 + 0.444818I$	$-1.99133 + 1.66625I$	$-3.10323 - 3.30828I$
$b = -0.238112 + 0.586278I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.408970 + 0.857975I$	$-1.07758 - 1.62874I$	$1.55460 + 6.14952I$
$a = -0.45960 - 1.92882I$		
$b = -0.637620 + 0.101517I$		
$u = -0.408970 - 0.857975I$	$-1.07758 + 1.62874I$	$1.55460 - 6.14952I$
$a = -0.45960 + 1.92882I$		
$b = -0.637620 - 0.101517I$		
$u = -0.766786 + 0.740371I$	$1.02080 - 2.73193I$	0
$a = 0.651267 - 0.131314I$		
$b = 0.615638 + 0.219403I$		
$u = -0.766786 - 0.740371I$	$1.02080 + 2.73193I$	0
$a = 0.651267 + 0.131314I$		
$b = 0.615638 - 0.219403I$		
$u = 0.864126 + 0.313585I$	$-1.42714 - 5.94125I$	$-1.80038 + 5.00917I$
$a = 0.309844 + 0.093672I$		
$b = 1.37366 + 0.34187I$		
$u = 0.864126 - 0.313585I$	$-1.42714 + 5.94125I$	$-1.80038 - 5.00917I$
$a = 0.309844 - 0.093672I$		
$b = 1.37366 - 0.34187I$		
$u = 1.039310 + 0.373209I$	$-8.36607 - 10.64720I$	0
$a = -0.065636 + 0.281257I$		
$b = -1.54296 - 0.70662I$		
$u = 1.039310 - 0.373209I$	$-8.36607 + 10.64720I$	0
$a = -0.065636 - 0.281257I$		
$b = -1.54296 + 0.70662I$		
$u = -0.626101 + 0.914760I$	$0.59153 - 2.55241I$	0
$a = 0.325312 - 0.028892I$		
$b = 0.152283 - 0.264499I$		
$u = -0.626101 - 0.914760I$	$0.59153 + 2.55241I$	0
$a = 0.325312 + 0.028892I$		
$b = 0.152283 + 0.264499I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.400472 + 1.043800I$		
$a = 0.03414 - 1.47370I$	$-2.78363 - 2.76140I$	0
$b = 0.099037 + 0.659391I$		
$u = -0.400472 - 1.043800I$		
$a = 0.03414 + 1.47370I$	$-2.78363 + 2.76140I$	0
$b = 0.099037 - 0.659391I$		
$u = 0.476376 + 0.736339I$		
$a = 1.265560 - 0.103489I$	$3.20421 - 1.15270I$	$2.54366 + 10.12386I$
$b = 0.004351 - 1.233950I$		
$u = 0.476376 - 0.736339I$		
$a = 1.265560 + 0.103489I$	$3.20421 + 1.15270I$	$2.54366 - 10.12386I$
$b = 0.004351 + 1.233950I$		
$u = 0.811711 + 0.324295I$		
$a = -0.395948 - 0.346003I$	$-9.06891 - 3.72651I$	$-4.60990 + 1.47067I$
$b = 1.49081 + 0.62148I$		
$u = 0.811711 - 0.324295I$		
$a = -0.395948 + 0.346003I$	$-9.06891 + 3.72651I$	$-4.60990 - 1.47067I$
$b = 1.49081 - 0.62148I$		
$u = -0.512874 + 1.037760I$		
$a = 1.84313 - 2.43983I$	$-9.13954 - 3.03771I$	0
$b = 1.60245 + 0.14929I$		
$u = -0.512874 - 1.037760I$		
$a = 1.84313 + 2.43983I$	$-9.13954 + 3.03771I$	0
$b = 1.60245 - 0.14929I$		
$u = -0.625197 + 0.558754I$		
$a = -0.748140 + 0.492702I$	$-7.66872 - 1.43842I$	$-12.36030 + 1.63046I$
$b = 1.46358 + 0.03079I$		
$u = -0.625197 - 0.558754I$		
$a = -0.748140 - 0.492702I$	$-7.66872 + 1.43842I$	$-12.36030 - 1.63046I$
$b = 1.46358 - 0.03079I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.788749 + 0.201384I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = -0.513368 - 1.264270I$	$-3.90942 - 3.06813I$	$-3.25697 + 2.62072I$
$b = -0.132527 + 1.397610I$		
$u = 0.788749 - 0.201384I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = -0.513368 + 1.264270I$	$-3.90942 + 3.06813I$	$-3.25697 - 2.62072I$
$b = -0.132527 - 1.397610I$		
$u = 0.255427 + 1.176880I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = 1.79250 + 1.07133I$	$-13.78770 - 0.65730I$	0
$b = 1.90837 + 0.50499I$		
$u = 0.255427 - 1.176880I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = 1.79250 - 1.07133I$	$-13.78770 + 0.65730I$	0
$b = 1.90837 - 0.50499I$		
$u = 0.416558 + 1.131590I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = -1.83787 - 1.06821I$	$-5.18749 + 3.49319I$	0
$b = -1.42336 + 0.58360I$		
$u = 0.416558 - 1.131590I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = -1.83787 + 1.06821I$	$-5.18749 - 3.49319I$	0
$b = -1.42336 - 0.58360I$		
$u = 0.698400 + 0.990081I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = -0.386699 + 0.027385I$	$2.39963 + 7.06465I$	0
$b = 0.004017 + 0.573210I$		
$u = 0.698400 - 0.990081I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = -0.386699 - 0.027385I$	$2.39963 - 7.06465I$	0
$b = 0.004017 - 0.573210I$		
$u = -1.22213$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = -0.185084$	$-4.25382$	0
$b = -1.38307$		
$u = 0.473990 + 1.133450I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = -1.74243 - 1.06594I$	$-4.78405 + 4.34186I$	0
$b = -1.70619 + 0.02634I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.473990 - 1.133450I$	$-4.78405 - 4.34186I$	0
$a = -1.74243 + 1.06594I$		
$b = -1.70619 - 0.02634I$		
$u = 0.330229 + 1.197830I$	$-8.15277 + 0.56922I$	0
$a = -0.598268 + 0.608886I$		
$b = 0.36448 + 1.47439I$		
$u = 0.330229 - 1.197830I$	$-8.15277 - 0.56922I$	0
$a = -0.598268 - 0.608886I$		
$b = 0.36448 - 1.47439I$		
$u = 0.219337 + 1.224320I$	$-6.53057 - 2.65488I$	0
$a = 1.99373 + 0.73372I$		
$b = 1.390620 - 0.107878I$		
$u = 0.219337 - 1.224320I$	$-6.53057 + 2.65488I$	0
$a = 1.99373 - 0.73372I$		
$b = 1.390620 + 0.107878I$		
$u = -0.523934 + 1.144670I$	$-1.26231 - 4.39904I$	0
$a = 1.74807 - 0.40921I$		
$b = 0.856476 + 0.079544I$		
$u = -0.523934 - 1.144670I$	$-1.26231 + 4.39904I$	0
$a = 1.74807 + 0.40921I$		
$b = 0.856476 - 0.079544I$		
$u = 0.532228 + 1.170640I$	$-6.75213 + 7.96693I$	0
$a = 0.919867 - 0.607693I$		
$b = -0.24571 - 1.71682I$		
$u = 0.532228 - 1.170640I$	$-6.75213 - 7.96693I$	0
$a = 0.919867 + 0.607693I$		
$b = -0.24571 + 1.71682I$		
$u = 0.580858 + 1.155040I$	$-11.5445 + 8.9372I$	0
$a = 1.64375 + 1.15261I$		
$b = 1.50003 - 0.88828I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.580858 - 1.155040I$		
$a = 1.64375 - 1.15261I$	$-11.5445 - 8.9372I$	0
$b = 1.50003 + 0.88828I$		
$u = 0.590895 + 1.169050I$		
$a = 1.76142 + 1.12256I$	$-4.00028 + 11.30660I$	0
$b = 1.59367 - 0.43143I$		
$u = 0.590895 - 1.169050I$		
$a = 1.76142 - 1.12256I$	$-4.00028 - 11.30660I$	0
$b = 1.59367 + 0.43143I$		
$u = -0.637144 + 0.213090I$		
$a = 0.983394 - 0.020692I$	$1.45198 - 0.17538I$	$6.99722 - 1.18140I$
$b = 0.436473 - 0.303668I$		
$u = -0.637144 - 0.213090I$		
$a = 0.983394 + 0.020692I$	$1.45198 + 0.17538I$	$6.99722 + 1.18140I$
$b = 0.436473 + 0.303668I$		
$u = -0.272566 + 0.576168I$		
$a = -2.41405 - 1.00736I$	$-1.175210 - 0.433161I$	$-4.73090 + 4.14534I$
$b = -0.635817 - 0.458472I$		
$u = -0.272566 - 0.576168I$		
$a = -2.41405 + 1.00736I$	$-1.175210 + 0.433161I$	$-4.73090 - 4.14534I$
$b = -0.635817 + 0.458472I$		
$u = 0.670259 + 1.215250I$		
$a = -1.67768 - 1.18901I$	$-10.9823 + 16.7933I$	0
$b = -1.58802 + 0.84313I$		
$u = 0.670259 - 1.215250I$		
$a = -1.67768 + 1.18901I$	$-10.9823 - 16.7933I$	0
$b = -1.58802 - 0.84313I$		
$u = 0.603559 + 0.095740I$		
$a = 0.085973 - 0.820052I$	$-1.98118 - 0.16998I$	$-3.50308 + 0.05920I$
$b = -1.250030 + 0.072344I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.603559 - 0.095740I$		
$a = 0.085973 + 0.820052I$	$-1.98118 + 0.16998I$	$-3.50308 - 0.05920I$
$b = -1.250030 - 0.072344I$		
$u = -1.095700 + 0.886640I$		
$a = -0.177881 + 0.508174I$	$-5.26056 - 3.80306I$	0
$b = -1.41985 - 0.12337I$		
$u = -1.095700 - 0.886640I$		
$a = -0.177881 - 0.508174I$	$-5.26056 + 3.80306I$	0
$b = -1.41985 + 0.12337I$		
$u = 0.11898 + 1.44090I$		
$a = -1.66657 - 0.44374I$	$-14.9486 - 6.6050I$	0
$b = -1.71694 - 0.48047I$		
$u = 0.11898 - 1.44090I$		
$a = -1.66657 + 0.44374I$	$-14.9486 + 6.6050I$	0
$b = -1.71694 + 0.48047I$		
$u = -0.62573 + 1.38215I$		
$a = -1.24381 + 0.74714I$	$-8.52431 - 6.48393I$	0
$b = -1.52635 - 0.26330I$		
$u = -0.62573 - 1.38215I$		
$a = -1.24381 - 0.74714I$	$-8.52431 + 6.48393I$	0
$b = -1.52635 + 0.26330I$		
$u = -0.0151235$		
$a = -43.4959$	$-1.12640$	$-9.50710$
$b = -0.551958$		

$$I_2^u = \langle b, -u^8 + 2u^7 + \cdots + a - 1, u^9 - u^8 + 2u^7 - u^6 + 3u^5 - u^4 + 2u^3 + u + 1 \rangle^{\text{III.}}$$

(i) **Arc colorings**

$$\begin{aligned} a_7 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_{11} &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_3 &= \begin{pmatrix} u^8 - 2u^7 + 3u^6 - 2u^5 + 3u^4 - 2u^3 + 2u^2 + 1 \\ 0 \end{pmatrix} \\ a_8 &= \begin{pmatrix} 1 \\ -u^2 \end{pmatrix} \\ a_6 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} -u \\ u^3 + u \end{pmatrix} \\ a_{12} &= \begin{pmatrix} -u^3 \\ u^5 + u^3 + u \end{pmatrix} \\ a_5 &= \begin{pmatrix} -u^8 - u^6 - u^4 + 1 \\ u^8 - u^7 + u^6 - 2u^5 + u^4 - 2u^3 - 2u - 1 \end{pmatrix} \\ a_2 &= \begin{pmatrix} 2u^8 - 2u^7 + 4u^6 - 2u^5 + 4u^4 - 2u^3 + 2u^2 \\ -u^8 + u^7 - u^6 + 2u^5 - u^4 + 2u^3 + 2u + 1 \end{pmatrix} \\ a_1 &= \begin{pmatrix} u^8 + u^6 + u^4 - 1 \\ -u^8 + u^7 - u^6 + 2u^5 - u^4 + 2u^3 + 2u + 1 \end{pmatrix} \\ a_4 &= \begin{pmatrix} u^8 - 2u^7 + 3u^6 - 2u^5 + 3u^4 - 2u^3 + 2u^2 + 1 \\ 0 \end{pmatrix} \\ a_9 &= \begin{pmatrix} u^2 + 1 \\ -u^2 \end{pmatrix} \end{aligned}$$

(ii) **Obstruction class = 1**

(iii) **Cusp Shapes** =  $3u^8 - 9u^7 + 12u^6 - 13u^5 + 15u^4 - 15u^3 + 8u^2 - 5u - 3$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_2$	$(u - 1)^9$
$c_3, c_6$	$u^9$
$c_4$	$(u + 1)^9$
$c_5$	$u^9 + 5u^8 + 12u^7 + 15u^6 + 9u^5 - u^4 - 4u^3 - 2u^2 + u + 1$
$c_7$	$u^9 - u^8 + 2u^7 - u^6 + 3u^5 - u^4 + 2u^3 + u + 1$
$c_8, c_{11}$	$u^9 + 3u^8 + 8u^7 + 13u^6 + 17u^5 + 17u^4 + 12u^3 + 6u^2 + u - 1$
$c_9, c_{12}$	$u^9 + u^8 - 2u^7 - 3u^6 + u^5 + 3u^4 + 2u^3 - u - 1$
$c_{10}$	$u^9 + u^8 + 2u^7 + u^6 + 3u^5 + u^4 + 2u^3 + u - 1$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_4$	$(y - 1)^9$
$c_3, c_6$	$y^9$
$c_5$	$y^9 - y^8 + 12y^7 - 7y^6 + 37y^5 + y^4 - 10y^2 + 5y - 1$
$c_7, c_{10}$	$y^9 + 3y^8 + 8y^7 + 13y^6 + 17y^5 + 17y^4 + 12y^3 + 6y^2 + y - 1$
$c_8, c_{11}$	$y^9 + 7y^8 + 20y^7 + 25y^6 + 5y^5 - 15y^4 + 22y^2 + 13y - 1$
$c_9, c_{12}$	$y^9 - 5y^8 + 12y^7 - 15y^6 + 9y^5 + y^4 - 4y^3 + 2y^2 + y - 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.140343 + 0.966856I$		
$a = -0.939568 + 0.981640I$	$-3.42837 - 2.09337I$	$-8.61953 + 2.85927I$
$b = 0$		
$u = -0.140343 - 0.966856I$		
$a = -0.939568 - 0.981640I$	$-3.42837 + 2.09337I$	$-8.61953 - 2.85927I$
$b = 0$		
$u = -0.628449 + 0.875112I$		
$a = 2.26219 + 2.13290I$	$-1.02799 - 2.45442I$	$-5.09778 + 12.45976I$
$b = 0$		
$u = -0.628449 - 0.875112I$		
$a = 2.26219 - 2.13290I$	$-1.02799 + 2.45442I$	$-5.09778 - 12.45976I$
$b = 0$		
$u = 0.796005 + 0.733148I$		
$a = 0.119081 + 0.409451I$	$2.72642 - 1.33617I$	$-5.51122 - 2.15019I$
$b = 0$		
$u = 0.796005 - 0.733148I$		
$a = 0.119081 - 0.409451I$	$2.72642 + 1.33617I$	$-5.51122 + 2.15019I$
$b = 0$		
$u = 0.728966 + 0.986295I$		
$a = -0.016164 - 0.378317I$	$1.95319 + 7.08493I$	$-9.51486 - 6.49599I$
$b = 0$		
$u = 0.728966 - 0.986295I$		
$a = -0.016164 + 0.378317I$	$1.95319 - 7.08493I$	$-9.51486 + 6.49599I$
$b = 0$		
$u = -0.512358$		
$a = 2.14893$	$-0.446489$	$5.48680$
$b = 0$		

$$\text{III. } I_3^u = \langle -120a^2u - 865au + \dots - 663a + 43, a^3 - a^2u + 7a^2 - 4au - 3a - 5u - 12, u^2 + u + 1 \rangle$$

(i) **Arc colorings**

$$\begin{aligned} a_7 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_{11} &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_3 &= \begin{pmatrix} a \\ 0.173661a^2u + 1.25181au + \dots + 0.959479a - 0.0622287 \end{pmatrix} \\ a_8 &= \begin{pmatrix} 1 \\ u+1 \end{pmatrix} \\ a_6 &= \begin{pmatrix} 0.0274964a^2u - 0.0101302au + \dots + 0.426918a + 0.548480 \\ 0.0709117a^2u + 0.552822au + \dots + 0.416787a + 1.78292 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} -u \\ u+1 \end{pmatrix} \\ a_{12} &= \begin{pmatrix} -1 \\ 0 \end{pmatrix} \\ a_5 &= \begin{pmatrix} -0.0434153a^2u - 0.562952au + \dots + 0.0101302a - 1.23444 \\ 0.0709117a^2u + 0.552822au + \dots + 0.416787a + 1.78292 \end{pmatrix} \\ a_2 &= \begin{pmatrix} 0.0274964a^2u - 0.0101302au + \dots + 0.426918a - 1.45152 \\ 0.0709117a^2u + 0.552822au + \dots + 0.416787a + 1.78292 \end{pmatrix} \\ a_1 &= \begin{pmatrix} -1 \\ 0 \end{pmatrix} \\ a_4 &= \begin{pmatrix} -0.173661a^2u - 1.25181au + \dots + 0.0405210a + 0.0622287 \\ 0.173661a^2u + 1.25181au + \dots + 0.959479a - 0.0622287 \end{pmatrix} \\ a_9 &= \begin{pmatrix} -0.162084a^2u + 0.164978au + \dots - 0.0955137a - 0.0752533 \\ 0 \end{pmatrix} \end{aligned}$$

(ii) **Obstruction class = 1**

$$(iii) \text{ Cusp Shapes} = -\frac{837}{691}a^2u - \frac{461}{691}a^2 + \frac{2345}{691}au - \frac{3467}{691}a + \frac{6538}{691}u + \frac{3634}{691}$$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_3$	$(u^3 - u^2 + 2u - 1)^2$
$c_2$	$(u^3 + u^2 - 1)^2$
$c_4$	$(u^3 - u^2 + 1)^2$
$c_5$	$(u^3 - 3u^2 + 2u + 1)^2$
$c_6$	$(u^3 + u^2 + 2u + 1)^2$
$c_7, c_{11}$	$(u^2 + u + 1)^3$
$c_8, c_9$	$u^6 - 2u^5 + 7u^4 + 8u^3 + 7u^2 + 3u + 1$
$c_{10}$	$(u^2 - u + 1)^3$
$c_{12}$	$u^6$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_3, c_6$	$(y^3 + 3y^2 + 2y - 1)^2$
$c_2, c_4$	$(y^3 - y^2 + 2y - 1)^2$
$c_5$	$(y^3 - 5y^2 + 10y - 1)^2$
$c_7, c_{10}, c_{11}$	$(y^2 + y + 1)^3$
$c_8, c_9$	$y^6 + 10y^5 + 95y^4 + 48y^3 + 15y^2 + 5y + 1$
$c_{12}$	$y^6$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.500000 + 0.866025I$		
$a = -1.159960 - 0.102142I$	$3.02413 - 4.85801I$	$8.78307 + 4.05565I$
$b = -0.215080 - 1.307140I$		
$u = -0.500000 + 0.866025I$		
$a = 1.104070 + 0.474671I$	$3.02413 + 0.79824I$	$-7.24138 + 7.14502I$
$b = -0.215080 + 1.307140I$		
$u = -0.500000 + 0.866025I$		
$a = -7.44411 + 0.49350I$	$-1.11345 - 2.02988I$	$37.9583 - 74.4205I$
$b = -0.569840$		
$u = -0.500000 - 0.866025I$		
$a = -1.159960 + 0.102142I$	$3.02413 + 4.85801I$	$8.78307 - 4.05565I$
$b = -0.215080 + 1.307140I$		
$u = -0.500000 - 0.866025I$		
$a = 1.104070 - 0.474671I$	$3.02413 - 0.79824I$	$-7.24138 - 7.14502I$
$b = -0.215080 - 1.307140I$		
$u = -0.500000 - 0.866025I$		
$a = -7.44411 - 0.49350I$	$-1.11345 + 2.02988I$	$37.9583 + 74.4205I$
$b = -0.569840$		

#### IV. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1$	$((u - 1)^9)(u^3 - u^2 + 2u - 1)^2(u^{68} + 72u^{67} + \dots - 116u + 1)$
$c_2$	$((u - 1)^9)(u^3 + u^2 - 1)^2(u^{68} - 12u^{67} + \dots + 4u - 1)$
$c_3$	$u^9(u^3 - u^2 + 2u - 1)^2(u^{68} + 3u^{67} + \dots + 2048u + 512)$
$c_4$	$((u + 1)^9)(u^3 - u^2 + 1)^2(u^{68} - 12u^{67} + \dots + 4u - 1)$
$c_5$	$(u^3 - 3u^2 + 2u + 1)^2$ $\cdot (u^9 + 5u^8 + 12u^7 + 15u^6 + 9u^5 - u^4 - 4u^3 - 2u^2 + u + 1)$ $\cdot (u^{68} + 4u^{67} + \dots + 20u^2 - 1)$
$c_6$	$u^9(u^3 + u^2 + 2u + 1)^2(u^{68} + 3u^{67} + \dots + 2048u + 512)$
$c_7$	$(u^2 + u + 1)^3(u^9 - u^8 + 2u^7 - u^6 + 3u^5 - u^4 + 2u^3 + u + 1)$ $\cdot (u^{68} + 5u^{67} + \dots - 61u + 1)$
$c_8$	$(u^6 - 2u^5 + 7u^4 + 8u^3 + 7u^2 + 3u + 1)$ $\cdot (u^9 + 3u^8 + 8u^7 + 13u^6 + 17u^5 + 17u^4 + 12u^3 + 6u^2 + u - 1)$ $\cdot (u^{68} - 8u^{67} + \dots - 679u + 1423)$
$c_9$	$(u^6 - 2u^5 + 7u^4 + 8u^3 + 7u^2 + 3u + 1)$ $\cdot (u^9 + u^8 - 2u^7 - 3u^6 + u^5 + 3u^4 + 2u^3 - u - 1)$ $\cdot (u^{68} - 4u^{67} + \dots - 1569175u - 179693)$
$c_{10}$	$(u^2 - u + 1)^3(u^9 + u^8 + 2u^7 + u^6 + 3u^5 + u^4 + 2u^3 + u - 1)$ $\cdot (u^{68} + 5u^{67} + \dots - 61u + 1)$
$c_{11}$	$(u^2 + u + 1)^3$ $\cdot (u^9 + 3u^8 + 8u^7 + 13u^6 + 17u^5 + 17u^4 + 12u^3 + 6u^2 + u - 1)$ $\cdot (u^{68} + 33u^{67} + \dots - 4365u + 1)$
$c_{12}$	$u^6(u^9 + u^8 - 2u^7 - 3u^{\frac{20}{6}} + u^5 + 3u^4 + 2u^3 - u - 1)$ $\cdot (u^{68} + 6u^{67} + \dots - 992u + 64)$

## V. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1$	$((y - 1)^9)(y^3 + 3y^2 + 2y - 1)^2(y^{68} - 140y^{67} + \dots + 13088y + 1)$
$c_2, c_4$	$((y - 1)^9)(y^3 - y^2 + 2y - 1)^2(y^{68} - 72y^{67} + \dots + 116y + 1)$
$c_3, c_6$	$y^9(y^3 + 3y^2 + 2y - 1)^2(y^{68} - 51y^{67} + \dots - 1048576y + 262144)$
$c_5$	$(y^3 - 5y^2 + 10y - 1)^2$ $\cdot (y^9 - y^8 + 12y^7 - 7y^6 + 37y^5 + y^4 - 10y^2 + 5y - 1)$ $\cdot (y^{68} - 16y^{67} + \dots - 40y + 1)$
$c_7, c_{10}$	$(y^2 + y + 1)^3$ $\cdot (y^9 + 3y^8 + 8y^7 + 13y^6 + 17y^5 + 17y^4 + 12y^3 + 6y^2 + y - 1)$ $\cdot (y^{68} + 33y^{67} + \dots - 4365y + 1)$
$c_8$	$(y^6 + 10y^5 + 95y^4 + 48y^3 + 15y^2 + 5y + 1)$ $\cdot (y^9 + 7y^8 + 20y^7 + 25y^6 + 5y^5 - 15y^4 + 22y^2 + 13y - 1)$ $\cdot (y^{68} - 68y^{67} + \dots + 88237y + 2024929)$
$c_9$	$(y^6 + 10y^5 + 95y^4 + 48y^3 + 15y^2 + 5y + 1)$ $\cdot (y^9 - 5y^8 + 12y^7 - 15y^6 + 9y^5 + y^4 - 4y^3 + 2y^2 + y - 1)$ $\cdot (y^{68} - 20y^{67} + \dots - 70781434415y + 32289574249)$
$c_{11}$	$((y^2 + y + 1)^3)(y^9 + 7y^8 + \dots + 13y - 1)$ $\cdot (y^{68} + 9y^{67} + \dots - 19115909y + 1)$
$c_{12}$	$y^6(y^9 - 5y^8 + 12y^7 - 15y^6 + 9y^5 + y^4 - 4y^3 + 2y^2 + y - 1)$ $\cdot (y^{68} + 30y^{67} + \dots - 332800y + 4096)$