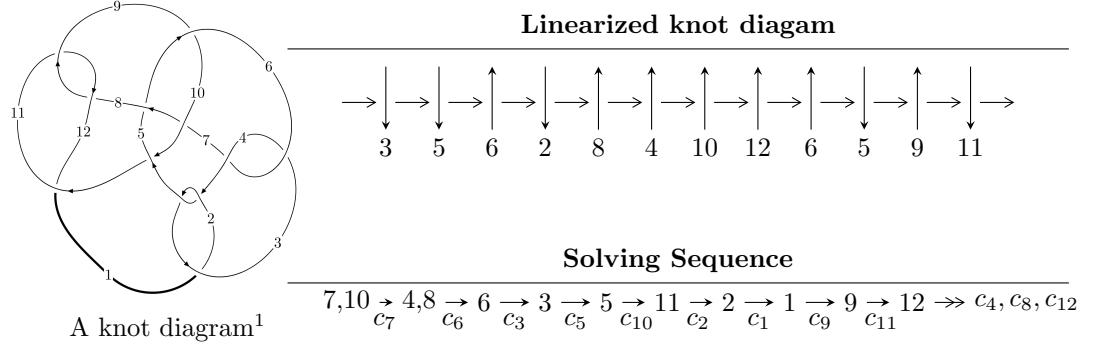


$12n_{0129}$  ( $K12n_{0129}$ )



### Ideals for irreducible components<sup>2</sup> of $X_{\text{par}}$

$$I_1^u = \langle 7.80956 \times 10^{63}u^{23} - 1.02547 \times 10^{64}u^{22} + \dots + 2.29425 \times 10^{67}b - 5.89286 \times 10^{67}, \\ 1.97576 \times 10^{64}u^{23} - 3.89917 \times 10^{64}u^{22} + \dots + 4.58851 \times 10^{67}a - 3.71378 \times 10^{68}, \\ u^{24} - 2u^{23} + \dots - 28672u + 4096 \rangle$$

$$I_2^u = \langle b, -u^8 + 2u^7 + 2u^6 - 5u^5 - u^4 + 5u^3 - u^2 + a, u^9 - u^8 - 2u^7 + 3u^6 + u^5 - 3u^4 + 2u^3 - u + 1 \rangle$$

$$I_1^v = \langle a, -164522v^{11} - 355934v^{10} + \dots + 707733b + 176501, \\ v^{12} + 3v^{11} + 3v^{10} + 18v^9 + 31v^8 - 29v^7 - 31v^6 - 9v^5 + 19v^4 + 5v^3 - 4v^2 + v + 1 \rangle$$

\* 3 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 45 representations.

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<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/math/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\text{I. } I_1^u = \\ \langle 7.81 \times 10^{63} u^{23} - 1.03 \times 10^{64} u^{22} + \dots + 2.29 \times 10^{67} b - 5.89 \times 10^{67}, 1.98 \times 10^{64} u^{23} - 3.90 \times 10^{64} u^{22} + \dots + 4.59 \times 10^{67} a - 3.71 \times 10^{68}, u^{24} - 2u^{23} + \dots - 28672u + 4096 \rangle$$

(i) **Arc colorings**

$$a_7 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -0.000430588u^{23} + 0.000849769u^{22} + \dots - 30.4322u + 8.09365 \\ -0.000340396u^{23} + 0.000446971u^{22} + \dots - 15.0993u + 2.56853 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -0.000770690u^{23} + 0.000886997u^{22} + \dots - 28.3683u + 4.83639 \\ 0.0000627821u^{23} - 2.14799 \times 10^{-6}u^{22} + \dots + 0.966055u - 0.729487 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -0.000177123u^{23} + 0.000316023u^{22} + \dots - 20.9747u + 7.59248 \\ -0.000440550u^{23} + 0.000737374u^{22} + \dots - 27.4672u + 4.56426 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -0.000247524u^{23} + 0.000151248u^{22} + \dots - 13.7287u + 2.88552 \\ -0.0000743622u^{23} + 0.000208018u^{22} + \dots - 5.79607u + 0.542658 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0.00108442u^{23} - 0.00207040u^{22} + \dots + 62.2122u - 10.2669 \\ 0.000158575u^{23} + 0.0000350829u^{22} + \dots - 7.95177u + 2.38129 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -0.000349715u^{23} + 0.000929736u^{22} + \dots - 27.5141u + 7.63549 \\ -0.000471953u^{23} + 0.000545981u^{22} + \dots - 19.0997u + 3.40520 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -0.000974598u^{23} + 0.00198880u^{22} + \dots - 59.8532u + 10.2543 \\ -0.000406712u^{23} + 0.000387216u^{22} + \dots - 5.12759u + 0.162234 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0.00105057u^{23} - 0.00167229u^{22} + \dots + 45.4181u - 7.13094 \\ -0.000133803u^{23} + 0.000328867u^{22} + \dots - 13.2158u + 2.91448 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 0.00207530u^{23} - 0.00334512u^{22} + \dots + 88.7435u - 14.5857 \\ 0.000298832u^{23} - 0.0000705567u^{22} + \dots - 4.27903u + 1.62940 \end{pmatrix}$$

(ii) **Obstruction class = -1**

(iii) **Cusp Shapes** =  $-0.000912531u^{23} + 0.00194308u^{22} + \dots - 44.5011u + 4.80932$

**(iv) u-Polynomials at the component**

| Crossings     | u-Polynomials at each crossing                 |
|---------------|--|
| $c_1$         | $u^{24} + 24u^{23} + \cdots - 179u + 1$        |
| $c_2, c_4$    | $u^{24} - 12u^{23} + \cdots + 17u - 1$         |
| $c_3, c_6$    | $u^{24} + u^{23} + \cdots - 2560u + 512$       |
| $c_5$         | $u^{24} + 4u^{23} + \cdots - 3u - 1$           |
| $c_7$         | $u^{24} + 2u^{23} + \cdots + 28672u + 4096$    |
| $c_8, c_{11}$ | $u^{24} + 8u^{23} + \cdots + 7u + 1$           |
| $c_9$         | $u^{24} + u^{23} + \cdots - 74162u - 19441$    |
| $c_{10}$      | $u^{24} - 5u^{23} + \cdots - 389242u + 249139$ |
| $c_{12}$      | $u^{24} + 20u^{22} + \cdots + 19u + 1$         |

**(v) Riley Polynomials at the component**

| Crossings     | Riley Polynomials at each crossing                          |
|---------------|---|
| $c_1$         | $y^{24} + 204y^{23} + \cdots - 2901y + 1$                   |
| $c_2, c_4$    | $y^{24} - 24y^{23} + \cdots + 179y + 1$                     |
| $c_3, c_6$    | $y^{24} - 63y^{23} + \cdots - 3932160y + 262144$            |
| $c_5$         | $y^{24} + 26y^{22} + \cdots - y + 1$                        |
| $c_7$         | $y^{24} - 90y^{23} + \cdots + 67108864y + 16777216$         |
| $c_8, c_{11}$ | $y^{24} + 20y^{22} + \cdots + 19y + 1$                      |
| $c_9$         | $y^{24} - 61y^{23} + \cdots - 296113128y + 377952481$       |
| $c_{10}$      | $y^{24} + 111y^{23} + \cdots - 469614992544y + 62070241321$ |
| $c_{12}$      | $y^{24} + 40y^{23} + \cdots + 2151y + 1$                    |

**(vi) Complex Volumes and Cusp Shapes**

| Solutions to $I_1^u$         | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape            |
|------------------------------|---------------------------------------|-----------------------|
| $u = -0.632443 + 0.726844I$  |                                       |                       |
| $a = 0.114777 + 0.151496I$   | $2.67249 - 0.06243I$                  | $6.49122 - 0.13400I$  |
| $b = 1.063560 + 0.162285I$   |                                       |                       |
| $u = -0.632443 - 0.726844I$  |                                       |                       |
| $a = 0.114777 - 0.151496I$   | $2.67249 + 0.06243I$                  | $6.49122 + 0.13400I$  |
| $b = 1.063560 - 0.162285I$   |                                       |                       |
| $u = 1.201550 + 0.153048I$   |                                       |                       |
| $a = 0.0923620 + 0.0946298I$ | $1.03909 - 7.66938I$                  | $3.58752 + 6.84907I$  |
| $b = -0.828567 + 0.942729I$  |                                       |                       |
| $u = 1.201550 - 0.153048I$   |                                       |                       |
| $a = 0.0923620 - 0.0946298I$ | $1.03909 + 7.66938I$                  | $3.58752 - 6.84907I$  |
| $b = -0.828567 - 0.942729I$  |                                       |                       |
| $u = 0.690057 + 0.202830I$   |                                       |                       |
| $a = 2.59655 - 0.30553I$     | $-1.38798 - 2.82419I$                 | $0.59813 + 2.55909I$  |
| $b = -0.024221 - 0.599362I$  |                                       |                       |
| $u = 0.690057 - 0.202830I$   |                                       |                       |
| $a = 2.59655 + 0.30553I$     | $-1.38798 + 2.82419I$                 | $0.59813 - 2.55909I$  |
| $b = -0.024221 + 0.599362I$  |                                       |                       |
| $u = 0.505730 + 0.448375I$   |                                       |                       |
| $a = 2.58887 - 1.75795I$     | $-2.60567 + 1.37963I$                 | $-1.96914 - 4.05392I$ |
| $b = -0.950717 + 0.074911I$  |                                       |                       |
| $u = 0.505730 - 0.448375I$   |                                       |                       |
| $a = 2.58887 + 1.75795I$     | $-2.60567 - 1.37963I$                 | $-1.96914 + 4.05392I$ |
| $b = -0.950717 - 0.074911I$  |                                       |                       |
| $u = -0.661121$              |                                       |                       |
| $a = 0.510618$               | 1.02845                               | 10.2860               |
| $b = 0.373534$               |                                       |                       |
| $u = 0.049304 + 0.644470I$   |                                       |                       |
| $a = 1.84071 - 0.43802I$     | $0.59509 - 2.36713I$                  | $1.40991 + 3.67925I$  |
| $b = 0.232697 - 0.155126I$   |                                       |                       |

| Solutions to $I_1^u$        | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape            |
|-----------------------------|---------------------------------------|-----------------------|
| $u = 0.049304 - 0.644470I$  |                                       |                       |
| $a = 1.84071 + 0.43802I$    | $0.59509 + 2.36713I$                  | $1.40991 - 3.67925I$  |
| $b = 0.232697 + 0.155126I$  |                                       |                       |
| $u = 1.17039 + 0.90470I$    |                                       |                       |
| $a = 0.319512 - 0.046660I$  | $-1.87950 + 2.72151I$                 | $1.13774 - 4.25269I$  |
| $b = -0.893023 + 0.472118I$ |                                       |                       |
| $u = 1.17039 - 0.90470I$    |                                       |                       |
| $a = 0.319512 + 0.046660I$  | $-1.87950 - 2.72151I$                 | $1.13774 + 4.25269I$  |
| $b = -0.893023 - 0.472118I$ |                                       |                       |
| $u = 0.188201 + 0.357668I$  |                                       |                       |
| $a = 2.01717 - 1.17792I$    | $-1.83062 - 1.07717I$                 | $-2.53581 + 1.58170I$ |
| $b = -0.349958 - 0.812535I$ |                                       |                       |
| $u = 0.188201 - 0.357668I$  |                                       |                       |
| $a = 2.01717 + 1.17792I$    | $-1.83062 + 1.07717I$                 | $-2.53581 - 1.58170I$ |
| $b = -0.349958 + 0.812535I$ |                                       |                       |
| $u = -2.38858 + 1.57335I$   |                                       |                       |
| $a = -0.524904 - 0.425161I$ | $18.8685 - 6.6483I$                   | 0                     |
| $b = 2.09180 - 1.57981I$    |                                       |                       |
| $u = -2.38858 - 1.57335I$   |                                       |                       |
| $a = -0.524904 + 0.425161I$ | $18.8685 + 6.6483I$                   | 0                     |
| $b = 2.09180 + 1.57981I$    |                                       |                       |
| $u = 2.25638 + 1.80466I$    |                                       |                       |
| $a = 0.568423 - 0.488334I$  | $18.7357 + 14.2573I$                  | 0                     |
| $b = -2.24002 - 1.53390I$   |                                       |                       |
| $u = 2.25638 - 1.80466I$    |                                       |                       |
| $a = 0.568423 + 0.488334I$  | $18.7357 - 14.2573I$                  | 0                     |
| $b = -2.24002 + 1.53390I$   |                                       |                       |
| $u = -3.61633$              |                                       |                       |
| $a = -0.660672$             | 0.756608                              | 0                     |
| $b = 2.14769$               |                                       |                       |

| Solutions to $I_1^u$        | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|-----------------------------|---------------------------------------|------------|
| $u = 4.44102 + 1.22807I$    |                                       |            |
| $a = -0.408012 + 0.133656I$ | $-18.9745 - 1.9748I$                  | 0          |
| $b = 3.93681 + 1.85539I$    |                                       |            |
| $u = 4.44102 - 1.22807I$    |                                       |            |
| $a = -0.408012 - 0.133656I$ | $-18.9745 + 1.9748I$                  | 0          |
| $b = 3.93681 - 1.85539I$    |                                       |            |
| $u = -4.34288 + 2.39260I$   |                                       |            |
| $a = 0.369569 + 0.203301I$  | $-18.5925 - 5.6388I$                  | 0          |
| $b = -3.79897 + 1.84880I$   |                                       |            |
| $u = -4.34288 - 2.39260I$   |                                       |            |
| $a = 0.369569 - 0.203301I$  | $-18.5925 + 5.6388I$                  | 0          |
| $b = -3.79897 - 1.84880I$   |                                       |            |

$$\text{II. } I_2^u = \langle b, -u^8 + 2u^7 + 2u^6 - 5u^5 - u^4 + 5u^3 - u^2 + a, u^9 - u^8 - 2u^7 + 3u^6 + u^5 - 3u^4 + 2u^3 - u + 1 \rangle$$

(i) **Arc colorings**

$$\begin{aligned} a_7 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_4 &= \begin{pmatrix} u^8 - 2u^7 - 2u^6 + 5u^5 + u^4 - 5u^3 + u^2 \\ 0 \end{pmatrix} \\ a_8 &= \begin{pmatrix} 1 \\ -u^2 \end{pmatrix} \\ a_6 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_3 &= \begin{pmatrix} u^8 - 2u^7 - 2u^6 + 5u^5 + u^4 - 5u^3 + u^2 \\ 0 \end{pmatrix} \\ a_5 &= \begin{pmatrix} -u^2 + 1 \\ u^4 \end{pmatrix} \\ a_{11} &= \begin{pmatrix} -u^5 + 2u^3 - u \\ u^7 - u^5 + u \end{pmatrix} \\ a_2 &= \begin{pmatrix} u^8 - 2u^7 - 2u^6 + 5u^5 + u^4 - 5u^3 + 2u^2 - 1 \\ -u^4 \end{pmatrix} \\ a_1 &= \begin{pmatrix} u^2 - 1 \\ -u^4 \end{pmatrix} \\ a_9 &= \begin{pmatrix} -u \\ u \end{pmatrix} \\ a_{12} &= \begin{pmatrix} u^8 - 3u^6 + 3u^4 - 1 \\ -u^8 + u^7 + 3u^6 - 2u^5 - 3u^4 + 2u^3 + 1 \end{pmatrix} \end{aligned}$$

(ii) **Obstruction class = 1**

(iii) **Cusp Shapes** =  $-5u^8 + u^7 + 7u^6 - 6u^5 - 6u^4 + 7u^3 - 5u^2 - 7u + 1$

**(iv) u-Polynomials at the component**

| Crossings        | u-Polynomials at each crossing                                     |
|------------------|--|
| $c_1, c_2$       | $(u - 1)^9$  |
| $c_3, c_6$       | $u^9$  |
| $c_4$            | $(u + 1)^9$  |
| $c_5$            | $u^9 + 5u^8 + 12u^7 + 15u^6 + 9u^5 - u^4 - 4u^3 - 2u^2 + u + 1$    |
| $c_7$            | $u^9 - u^8 - 2u^7 + 3u^6 + u^5 - 3u^4 + 2u^3 - u + 1$              |
| $c_8$            | $u^9 - u^8 + 2u^7 - u^6 + 3u^5 - u^4 + 2u^3 + u + 1$               |
| $c_9$            | $u^9 + u^8 - 2u^7 - 3u^6 + u^5 + 3u^4 + 2u^3 - u - 1$              |
| $c_{10}, c_{12}$ | $u^9 + 3u^8 + 8u^7 + 13u^6 + 17u^5 + 17u^4 + 12u^3 + 6u^2 + u - 1$ |
| $c_{11}$         | $u^9 + u^8 + 2u^7 + u^6 + 3u^5 + u^4 + 2u^3 + u - 1$               |

**(v) Riley Polynomials at the component**

| Crossings        | Riley Polynomials at each crossing                                 |
|------------------|--|
| $c_1, c_2, c_4$  | $(y - 1)^9$  |
| $c_3, c_6$       | $y^9$  |
| $c_5$            | $y^9 - y^8 + 12y^7 - 7y^6 + 37y^5 + y^4 - 10y^2 + 5y - 1$          |
| $c_7, c_9$       | $y^9 - 5y^8 + 12y^7 - 15y^6 + 9y^5 + y^4 - 4y^3 + 2y^2 + y - 1$    |
| $c_8, c_{11}$    | $y^9 + 3y^8 + 8y^7 + 13y^6 + 17y^5 + 17y^4 + 12y^3 + 6y^2 + y - 1$ |
| $c_{10}, c_{12}$ | $y^9 + 7y^8 + 20y^7 + 25y^6 + 5y^5 - 15y^4 + 22y^2 + 13y - 1$      |

(vi) Complex Volumes and Cusp Shapes

| Solutions to $I_2^u$        | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape            |
|-----------------------------|---------------------------------------|-----------------------|
| $u = 0.772920 + 0.510351I$  | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ |                       |
| $a = -0.939568 - 0.981640I$ | $-3.42837 + 2.09337I$                 | $-4.41045 - 5.46639I$ |
| $b = 0$                     |                                       |                       |
| $u = 0.772920 - 0.510351I$  | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ |                       |
| $a = -0.939568 + 0.981640I$ | $-3.42837 - 2.09337I$                 | $-4.41045 + 5.46639I$ |
| $b = 0$                     |                                       |                       |
| $u = -0.825933$             | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ |                       |
| $a = 2.14893$               | $-0.446489$                           | $-0.182090$           |
| $b = 0$                     |                                       |                       |
| $u = -1.173910 + 0.391555I$ | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ |                       |
| $a = 0.119081 + 0.409451I$  | $2.72642 - 1.33617I$                  | $8.07941 + 3.55369I$  |
| $b = 0$                     |                                       |                       |
| $u = -1.173910 - 0.391555I$ | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ |                       |
| $a = 0.119081 - 0.409451I$  | $2.72642 + 1.33617I$                  | $8.07941 - 3.55369I$  |
| $b = 0$                     |                                       |                       |
| $u = 0.141484 + 0.739668I$  | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ |                       |
| $a = 2.26219 + 2.13290I$    | $-1.02799 - 2.45442I$                 | $-2.24638 - 6.63381I$ |
| $b = 0$                     |                                       |                       |
| $u = 0.141484 - 0.739668I$  | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ |                       |
| $a = 2.26219 - 2.13290I$    | $-1.02799 + 2.45442I$                 | $-2.24638 + 6.63381I$ |
| $b = 0$                     |                                       |                       |
| $u = 1.172470 + 0.500383I$  | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ |                       |
| $a = -0.016164 - 0.378317I$ | $1.95319 + 7.08493I$                  | $8.66846 - 5.33071I$  |
| $b = 0$                     |                                       |                       |
| $u = 1.172470 - 0.500383I$  | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ |                       |
| $a = -0.016164 + 0.378317I$ | $1.95319 - 7.08493I$                  | $8.66846 + 5.33071I$  |
| $b = 0$                     |                                       |                       |

$$\text{III. } I_1^v = \langle a, -1.65 \times 10^5 v^{11} - 3.56 \times 10^5 v^{10} + \dots + 7.08 \times 10^5 b + 1.77 \times 10^5, v^{12} + 3v^{11} + \dots + v + 1 \rangle$$

(i) **Arc colorings**

$$\begin{aligned} a_7 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} v \\ 0 \end{pmatrix} \\ a_4 &= \begin{pmatrix} 0 \\ 0.232463v^{11} + 0.502921v^{10} + \dots - 0.152902v - 0.249389 \end{pmatrix} \\ a_8 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_6 &= \begin{pmatrix} 1 \\ -1.04198v^{11} - 2.90360v^{10} + \dots + 1.23849v - 0.574544 \end{pmatrix} \\ a_3 &= \begin{pmatrix} -0.232463v^{11} - 0.502921v^{10} + \dots + 0.152902v + 0.249389 \\ -1.00827v^{11} - 2.68986v^{10} + \dots + 1.09637v - 2.28028 \end{pmatrix} \\ a_5 &= \begin{pmatrix} 1.04198v^{11} + 2.90360v^{10} + \dots - 1.23849v + 1.57454 \\ -1.04198v^{11} - 2.90360v^{10} + \dots + 1.23849v - 0.574544 \end{pmatrix} \\ a_{11} &= \begin{pmatrix} -0.126775v^{11} - 0.205966v^{10} + \dots + 2.64946v - 0.819476 \\ 0.349127v^{11} + 0.655942v^{10} + \dots - 1.18202v + 1.86146 \end{pmatrix} \\ a_2 &= \begin{pmatrix} 0.819476v^{11} + 2.33165v^{10} + \dots - 1.01499v + 1.46894 \\ -1.62222v^{11} - 4.40786v^{10} + \dots + 1.83221v - 1.73501 \end{pmatrix} \\ a_1 &= \begin{pmatrix} -1 \\ 0 \end{pmatrix} \\ a_9 &= \begin{pmatrix} 0.222352v^{11} + 0.449976v^{10} + \dots + 1.46744v + 1.04198 \\ 0.349127v^{11} + 0.655942v^{10} + \dots - 1.18202v + 1.86146 \end{pmatrix} \\ a_{12} &= \begin{pmatrix} -0.989917v^{11} - 2.68233v^{10} + \dots + 3.73598v - 2.22768 \\ 0.349127v^{11} + 0.655942v^{10} + \dots - 1.18202v + 0.861460 \end{pmatrix} \end{aligned}$$

(ii) **Obstruction class = 1**

$$(iii) \text{ Cusp Shapes} = \frac{1086197}{235911}v^{11} + \frac{2821982}{235911}v^{10} + \dots - \frac{94285}{235911}v + \frac{2199643}{235911}$$

**(iv) u-Polynomials at the component**

| Crossings     | u-Polynomials at each crossing                |
|---------------|---|
| $c_1$         | $(u^6 - 3u^5 + 5u^4 - 4u^3 + 2u^2 - u + 1)^2$ |
| $c_2, c_6$    | $(u^6 + u^5 - u^4 - 2u^3 + u + 1)^2$          |
| $c_3, c_4$    | $(u^6 - u^5 - u^4 + 2u^3 - u + 1)^2$          |
| $c_5$         | $(u^6 + 3u^5 + 5u^4 + 4u^3 + 2u^2 + u + 1)^2$ |
| $c_7$         | $u^{12}$                                      |
| $c_8, c_{12}$ | $(u^2 + u + 1)^6$                             |
| $c_9, c_{10}$ | $u^{12} - u^{11} + \cdots - 3u + 1$           |
| $c_{11}$      | $(u^2 - u + 1)^6$                             |

**(v) Riley Polynomials at the component**

| Crossings                | Riley Polynomials at each crossing            |
|--------------------------|---|
| $c_1, c_5$               | $(y^6 + y^5 + 5y^4 + 6y^2 + 3y + 1)^2$        |
| $c_2, c_3, c_4$<br>$c_6$ | $(y^6 - 3y^5 + 5y^4 - 4y^3 + 2y^2 - y + 1)^2$ |
| $c_7$                    | $y^{12}$                                      |
| $c_8, c_{11}, c_{12}$    | $(y^2 + y + 1)^6$                             |
| $c_9, c_{10}$            | $y^{12} - 3y^{11} + \cdots - y + 1$           |

(vi) Complex Volumes and Cusp Shapes

| Solutions to $I_1^v$        | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape            |
|-----------------------------|---------------------------------------|-----------------------|
| $v = 0.834826 + 0.083652I$  |                                       |                       |
| $a = 0$                     | $1.89061 + 1.10558I$                  | $3.63443 - 2.52768I$  |
| $b = 1.002190 - 0.295542I$  |                                       |                       |
| $v = 0.834826 - 0.083652I$  |                                       |                       |
| $a = 0$                     | $1.89061 - 1.10558I$                  | $3.63443 + 2.52768I$  |
| $b = 1.002190 + 0.295542I$  |                                       |                       |
| $v = -0.489858 + 0.681154I$ |                                       |                       |
| $a = 0$                     | $1.89061 - 2.95419I$                  | $6.39280 + 3.57892I$  |
| $b = 1.002190 - 0.295542I$  |                                       |                       |
| $v = -0.489858 - 0.681154I$ |                                       |                       |
| $a = 0$                     | $1.89061 + 2.95419I$                  | $6.39280 - 3.57892I$  |
| $b = 1.002190 + 0.295542I$  |                                       |                       |
| $v = -0.458424 + 0.081263I$ |                                       |                       |
| $a = 0$                     | $-7.72290I$                           | $-2.53591 + 7.46338I$ |
| $b = -1.073950 + 0.558752I$ |                                       |                       |
| $v = -0.458424 - 0.081263I$ |                                       |                       |
| $a = 0$                     | $7.72290I$                            | $-2.53591 - 7.46338I$ |
| $b = -1.073950 - 0.558752I$ |                                       |                       |
| $v = 0.299588 + 0.356375I$  |                                       |                       |
| $a = 0$                     | $-3.66314I$                           | $2.83009 + 6.37777I$  |
| $b = -1.073950 + 0.558752I$ |                                       |                       |
| $v = 0.299588 - 0.356375I$  |                                       |                       |
| $a = 0$                     | $3.66314I$                            | $2.83009 - 6.37777I$  |
| $b = -1.073950 - 0.558752I$ |                                       |                       |
| $v = -2.51133 + 0.49706I$   |                                       |                       |
| $a = 0$                     | $-1.89061 + 2.95419I$                 | $-7.91752 - 1.81989I$ |
| $b = -0.428243 + 0.664531I$ |                                       |                       |
| $v = -2.51133 - 0.49706I$   |                                       |                       |
| $a = 0$                     | $-1.89061 - 2.95419I$                 | $-7.91752 + 1.81989I$ |
| $b = -0.428243 - 0.664531I$ |                                       |                       |

| Solutions to $I_1^v$        | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape           |
|-----------------------------|---------------------------------------|----------------------|
| $v = 0.82520 + 2.42341I$    |                                       |                      |
| $a = 0$                     | $-1.89061 + 1.10558I$                 | $3.59610 - 6.57635I$ |
| $b = -0.428243 - 0.664531I$ |                                       |                      |
| $v = 0.82520 - 2.42341I$    |                                       |                      |
| $a = 0$                     | $-1.89061 - 1.10558I$                 | $3.59610 + 6.57635I$ |
| $b = -0.428243 + 0.664531I$ |                                       |                      |

#### IV. u-Polynomials

| Crossings | u-Polynomials at each crossing  |
|-----------|---|
| $c_1$     | $(u - 1)^9(u^6 - 3u^5 + 5u^4 - 4u^3 + 2u^2 - u + 1)^2 \cdot (u^{24} + 24u^{23} + \dots - 179u + 1)$   |
| $c_2$     | $((u - 1)^9)(u^6 + u^5 + \dots + u + 1)^2(u^{24} - 12u^{23} + \dots + 17u - 1)$   |
| $c_3$     | $u^9(u^6 - u^5 + \dots - u + 1)^2(u^{24} + u^{23} + \dots - 2560u + 512)$   |
| $c_4$     | $((u + 1)^9)(u^6 - u^5 + \dots - u + 1)^2(u^{24} - 12u^{23} + \dots + 17u - 1)$   |
| $c_5$     | $(u^6 + 3u^5 + 5u^4 + 4u^3 + 2u^2 + u + 1)^2 \cdot (u^9 + 5u^8 + 12u^7 + 15u^6 + 9u^5 - u^4 - 4u^3 - 2u^2 + u + 1) \cdot (u^{24} + 4u^{23} + \dots - 3u - 1)$ |
| $c_6$     | $u^9(u^6 + u^5 + \dots + u + 1)^2(u^{24} + u^{23} + \dots - 2560u + 512)$   |
| $c_7$     | $u^{12}(u^9 - u^8 - 2u^7 + 3u^6 + u^5 - 3u^4 + 2u^3 - u + 1) \cdot (u^{24} + 2u^{23} + \dots + 28672u + 4096)$  |
| $c_8$     | $(u^2 + u + 1)^6(u^9 - u^8 + 2u^7 - u^6 + 3u^5 - u^4 + 2u^3 + u + 1) \cdot (u^{24} + 8u^{23} + \dots + 7u + 1)$   |
| $c_9$     | $(u^9 + u^8 + \dots - u - 1)(u^{12} - u^{11} + \dots - 3u + 1) \cdot (u^{24} + u^{23} + \dots - 74162u - 19441)$  |
| $c_{10}$  | $(u^9 + 3u^8 + 8u^7 + 13u^6 + 17u^5 + 17u^4 + 12u^3 + 6u^2 + u - 1) \cdot (u^{12} - u^{11} + \dots - 3u + 1)(u^{24} - 5u^{23} + \dots - 389242u + 249139)$    |
| $c_{11}$  | $(u^2 - u + 1)^6(u^9 + u^8 + 2u^7 + u^6 + 3u^5 + u^4 + 2u^3 + u - 1) \cdot (u^{24} + 8u^{23} + \dots + 7u + 1)$   |
| $c_{12}$  | $(u^2 + u + 1)^6 \cdot (u^9 + 3u^8 + 8u^7 + 13u^6 + 17u^5 + 17u^4 + 12u^3 + 6u^2 + u - 1) \cdot (u^{24} + 20u^{22} + \dots + 19u + 1)$                        |

## V. Riley Polynomials

| Crossings     | Riley Polynomials at each crossing  |
|---------------|---|
| $c_1$         | $(y - 1)^9(y^6 + y^5 + 5y^4 + 6y^2 + 3y + 1)^2 \cdot (y^{24} + 204y^{23} + \dots - 2901y + 1)$  |
| $c_2, c_4$    | $(y - 1)^9(y^6 - 3y^5 + 5y^4 - 4y^3 + 2y^2 - y + 1)^2 \cdot (y^{24} - 24y^{23} + \dots + 179y + 1)$   |
| $c_3, c_6$    | $y^9(y^6 - 3y^5 + 5y^4 - 4y^3 + 2y^2 - y + 1)^2 \cdot (y^{24} - 63y^{23} + \dots - 3932160y + 262144)$  |
| $c_5$         | $(y^6 + y^5 + 5y^4 + 6y^2 + 3y + 1)^2 \cdot (y^9 - y^8 + 12y^7 - 7y^6 + 37y^5 + y^4 - 10y^2 + 5y - 1) \cdot (y^{24} + 26y^{22} + \dots - y + 1)$                          |
| $c_7$         | $y^{12}(y^9 - 5y^8 + 12y^7 - 15y^6 + 9y^5 + y^4 - 4y^3 + 2y^2 + y - 1) \cdot (y^{24} - 90y^{23} + \dots + 67108864y + 16777216)$  |
| $c_8, c_{11}$ | $(y^2 + y + 1)^6 \cdot (y^9 + 3y^8 + 8y^7 + 13y^6 + 17y^5 + 17y^4 + 12y^3 + 6y^2 + y - 1) \cdot (y^{24} + 20y^{22} + \dots + 19y + 1)$                                    |
| $c_9$         | $(y^9 - 5y^8 + 12y^7 - 15y^6 + 9y^5 + y^4 - 4y^3 + 2y^2 + y - 1) \cdot (y^{12} - 3y^{11} + \dots - y + 1) \cdot (y^{24} - 61y^{23} + \dots - 296113128y + 377952481)$     |
| $c_{10}$      | $(y^9 + 7y^8 + 20y^7 + 25y^6 + 5y^5 - 15y^4 + 22y^2 + 13y - 1) \cdot (y^{12} - 3y^{11} + \dots - y + 1) \cdot (y^{24} + 111y^{23} + \dots - 469614992544y + 62070241321)$ |
| $c_{12}$      | $((y^2 + y + 1)^6)(y^9 + 7y^8 + \dots + 13y - 1) \cdot (y^{24} + 40y^{23} + \dots + 2151y + 1)$   |