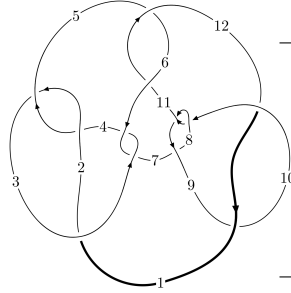
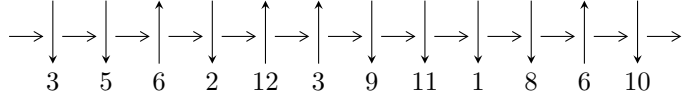


$12n_{0131}$  ( $K12n_{0131}$ )



A knot diagram<sup>1</sup>

**Linearized knot diagram**



**Solving Sequence**

$$3,5 \xrightarrow{c_2} 2 \xrightarrow{c_1} 1 \xrightarrow{c_4} 4,10 \xrightarrow{c_9} 9 \xrightarrow{c_{12}} 12 \xrightarrow{c_5} 6 \xrightarrow{c_6} 7 \xrightarrow{c_{11}} 11 \xrightarrow{c_8} 8 \rightarrow c_3, c_7, c_{10}$$

**Ideals for irreducible components<sup>2</sup> of  $X_{\text{par}}$**

$$I_1^u = \langle 2.86219 \times 10^{101} u^{65} + 3.04230 \times 10^{102} u^{64} + \dots + 1.07604 \times 10^{101} b - 6.59997 \times 10^{101}, \\ 1.26922 \times 10^{102} u^{65} + 1.35759 \times 10^{103} u^{64} + \dots + 2.15207 \times 10^{101} a - 2.45951 \times 10^{103}, \\ u^{66} + 11u^{65} + \dots - 184u - 1 \rangle$$

$$I_2^u = \langle -2a^8 + 3a^7 - 6a^6 + 5a^5 - 9a^4 + 6a^3 - 8a^2 + b + 3a - 4, a^9 - a^8 + 2a^7 - a^6 + 3a^5 - a^4 + 2a^3 + a + 1, u - \dots \rangle$$

$$I_3^u = \langle u^4 + u^3 - u^2 + b - 2u - 1, -u^5 - u^4 + u^3 + u^2 + a - u - 1, u^6 + u^5 - u^4 - 2u^3 + u + 1 \rangle$$

\* 3 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 81 representations.

<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\mathbf{I. } I_1^u = \langle 2.86 \times 10^{101} u^{65} + 3.04 \times 10^{102} u^{64} + \dots + 1.08 \times 10^{101} b - 6.60 \times 10^{101}, 1.27 \times 10^{102} u^{65} + 1.36 \times 10^{103} u^{64} + \dots + 2.15 \times 10^{101} a - 2.46 \times 10^{103}, u^{66} + 11u^{65} + \dots - 184u - 1 \rangle$$

(i) Arc colorings

$$a_3 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -u^2 + 1 \\ -u^2 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} u \\ -u^3 + u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -5.89768u^{65} - 63.0828u^{64} + \dots + 2827.10u + 114.286 \\ -2.65994u^{65} - 28.2732u^{64} + \dots + 1025.61u + 6.13360 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -8.52453u^{65} - 90.7723u^{64} + \dots + 3834.57u + 120.324 \\ -2.57433u^{65} - 27.0269u^{64} + \dots + 862.488u + 5.23234 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -8.72655u^{65} - 89.2240u^{64} + \dots + 1798.25u - 38.9602 \\ -5.28403u^{65} - 54.4051u^{64} + \dots + 1316.97u + 6.95585 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -3.83893u^{65} - 41.0224u^{64} + \dots + 1345.05u - 6.03327 \\ -1.51701u^{65} - 16.1400u^{64} + \dots + 494.366u + 2.63312 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -5.35594u^{65} - 57.1624u^{64} + \dots + 1839.41u - 3.40015 \\ -1.51701u^{65} - 16.1400u^{64} + \dots + 494.366u + 2.63312 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 13.7708u^{65} + 144.182u^{64} + \dots - 4481.24u - 77.0429 \\ 0.429501u^{65} + 4.69148u^{64} + \dots - 219.153u - 1.47738 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -7.65340u^{65} - 81.3957u^{64} + \dots + 3054.18u + 72.2685 \\ -5.10197u^{65} - 53.2822u^{64} + \dots + 1553.54u + 8.78813 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes =  $7.00145u^{65} + 70.4042u^{64} + \dots - 636.383u - 12.3310$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1$	$u^{66} + 21u^{65} + \dots + 31524u + 1$
$c_2, c_4$	$u^{66} - 11u^{65} + \dots + 184u - 1$
$c_3, c_6$	$u^{66} + 8u^{65} + \dots - 7168u + 512$
$c_5, c_{11}$	$u^{66} + 3u^{65} + \dots - 2u - 1$
$c_7$	$u^{66} + 28u^{65} + \dots - 143u + 1$
$c_8, c_{10}$	$u^{66} - 8u^{65} + \dots - 11u + 1$
$c_9, c_{12}$	$u^{66} - 2u^{65} + \dots + 192u + 64$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1$	$y^{66} + 59y^{65} + \dots - 992297680y + 1$
$c_2, c_4$	$y^{66} - 21y^{65} + \dots - 31524y + 1$
$c_3, c_6$	$y^{66} - 60y^{65} + \dots - 76021760y + 262144$
$c_5, c_{11}$	$y^{66} + 15y^{65} + \dots - 20y + 1$
$c_7$	$y^{66} + 28y^{65} + \dots - 12229y + 1$
$c_8, c_{10}$	$y^{66} - 28y^{65} + \dots + 143y + 1$
$c_9, c_{12}$	$y^{66} + 42y^{65} + \dots + 77824y + 4096$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.00537$ $a = 0.406767$ $b = -11.0855$	$-2.82917$	$365.350$
$u = 0.687723 + 0.687263I$ $a = -1.353200 - 0.228510I$ $b = -1.300520 + 0.290425I$	$-2.23471 - 2.98196I$	$0$
$u = 0.687723 - 0.687263I$ $a = -1.353200 + 0.228510I$ $b = -1.300520 - 0.290425I$	$-2.23471 + 2.98196I$	$0$
$u = 1.028820 + 0.216167I$ $a = 0.012733 + 0.445672I$ $b = 0.438763 + 0.902849I$	$-1.91057 - 0.79816I$	$0$
$u = 1.028820 - 0.216167I$ $a = 0.012733 - 0.445672I$ $b = 0.438763 - 0.902849I$	$-1.91057 + 0.79816I$	$0$
$u = 0.783333 + 0.429567I$ $a = 2.12816 + 1.63033I$ $b = 2.36643 - 1.94607I$	$-3.21013 - 1.26950I$	$-4.00000 + 7.64083I$
$u = 0.783333 - 0.429567I$ $a = 2.12816 - 1.63033I$ $b = 2.36643 + 1.94607I$	$-3.21013 + 1.26950I$	$-4.00000 - 7.64083I$
$u = 1.125970 + 0.056995I$ $a = 0.023922 - 0.599547I$ $b = 0.36398 + 1.57344I$	$0.81136 + 2.64313I$	$0$
$u = 1.125970 - 0.056995I$ $a = 0.023922 + 0.599547I$ $b = 0.36398 - 1.57344I$	$0.81136 - 2.64313I$	$0$
$u = -0.824004 + 0.171548I$ $a = -1.143160 + 0.689270I$ $b = -0.151706 + 0.583718I$	$-4.86194 + 7.45999I$	$-0.96246 - 11.41011I$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.824004 - 0.171548I$ $a = -1.143160 - 0.689270I$ $b = -0.151706 - 0.583718I$	$-4.86194 - 7.45999I$	$-0.96246 + 11.41011I$
$u = 0.515278 + 1.048940I$ $a = -1.36638 - 1.36297I$ $b = -1.375720 + 0.022642I$	$2.19847 - 2.32521I$	0
$u = 0.515278 - 1.048940I$ $a = -1.36638 + 1.36297I$ $b = -1.375720 - 0.022642I$	$2.19847 + 2.32521I$	0
$u = -0.745847 + 0.910266I$ $a = -1.20178 + 2.28035I$ $b = -2.03130 + 0.52431I$	$2.17496 - 0.19887I$	0
$u = -0.745847 - 0.910266I$ $a = -1.20178 - 2.28035I$ $b = -2.03130 - 0.52431I$	$2.17496 + 0.19887I$	0
$u = -0.760288 + 0.928501I$ $a = 1.67368 - 0.06126I$ $b = 1.88450 + 0.90427I$	$7.72304 - 2.79945I$	0
$u = -0.760288 - 0.928501I$ $a = 1.67368 + 0.06126I$ $b = 1.88450 - 0.90427I$	$7.72304 + 2.79945I$	0
$u = 0.668448 + 0.397576I$ $a = 0.003744 - 1.234270I$ $b = -1.38255 + 1.28759I$	$2.07274 - 4.10478I$	$-2.27198 - 0.09641I$
$u = 0.668448 - 0.397576I$ $a = 0.003744 + 1.234270I$ $b = -1.38255 - 1.28759I$	$2.07274 + 4.10478I$	$-2.27198 + 0.09641I$
$u = -0.856203 + 0.882898I$ $a = 0.290557 + 1.073450I$ $b = 0.231042 + 0.438928I$	$3.57906 + 2.47635I$	0

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.856203 - 0.882898I$ $a = 0.290557 - 1.073450I$ $b = 0.231042 - 0.438928I$	$3.57906 - 2.47635I$	0
$u = -1.118290 + 0.517016I$ $a = 0.122393 - 0.353509I$ $b = -0.055274 - 0.183449I$	$-1.20228 + 5.48361I$	0
$u = -1.118290 - 0.517016I$ $a = 0.122393 + 0.353509I$ $b = -0.055274 + 0.183449I$	$-1.20228 - 5.48361I$	0
$u = -0.690354 + 1.028160I$ $a = -0.438411 - 1.018090I$ $b = -0.341152 - 0.391855I$	$4.03833 - 2.66127I$	0
$u = -0.690354 - 1.028160I$ $a = -0.438411 + 1.018090I$ $b = -0.341152 + 0.391855I$	$4.03833 + 2.66127I$	0
$u = 1.274370 + 0.103527I$ $a = 0.09874 + 1.51084I$ $b = 1.63942 + 2.71558I$	$-4.31795 - 0.78820I$	0
$u = 1.274370 - 0.103527I$ $a = 0.09874 - 1.51084I$ $b = 1.63942 - 2.71558I$	$-4.31795 + 0.78820I$	0
$u = -0.983683 + 0.830782I$ $a = 0.570504 + 0.494511I$ $b = 0.437347 + 0.006156I$	$3.17239 + 3.89822I$	0
$u = -0.983683 - 0.830782I$ $a = 0.570504 - 0.494511I$ $b = 0.437347 - 0.006156I$	$3.17239 - 3.89822I$	0
$u = -0.894353 + 0.951169I$ $a = -1.78516 + 0.28107I$ $b = -2.14588 - 0.82546I$	$9.29382 + 3.78649I$	0

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.894353 - 0.951169I$ $a = -1.78516 - 0.28107I$ $b = -2.14588 + 0.82546I$	$9.29382 - 3.78649I$	0
$u = -1.062290 + 0.802217I$ $a = 2.22217 - 0.70557I$ $b = 2.85845 + 0.87099I$	$1.18870 + 6.56344I$	0
$u = -1.062290 - 0.802217I$ $a = 2.22217 + 0.70557I$ $b = 2.85845 - 0.87099I$	$1.18870 - 6.56344I$	0
$u = -1.057290 + 0.809211I$ $a = -0.51219 + 1.44953I$ $b = -1.79007 + 0.34040I$	$6.78475 + 9.23321I$	0
$u = -1.057290 - 0.809211I$ $a = -0.51219 - 1.44953I$ $b = -1.79007 - 0.34040I$	$6.78475 - 9.23321I$	0
$u = -0.620743 + 0.209791I$ $a = 1.51472 - 0.44133I$ $b = 0.351541 - 0.610430I$	$-1.43375 + 2.91518I$	$0.46506 - 4.85019I$
$u = -0.620743 - 0.209791I$ $a = 1.51472 + 0.44133I$ $b = 0.351541 + 0.610430I$	$-1.43375 - 2.91518I$	$0.46506 + 4.85019I$
$u = -0.597235 + 0.259408I$ $a = -0.28543 + 1.39421I$ $b = -0.011224 + 0.406559I$	$1.17931 - 1.63015I$	$3.12613 + 3.30141I$
$u = -0.597235 - 0.259408I$ $a = -0.28543 - 1.39421I$ $b = -0.011224 - 0.406559I$	$1.17931 + 1.63015I$	$3.12613 - 3.30141I$
$u = -0.994697 + 0.913978I$ $a = 0.79592 - 1.57410I$ $b = 1.87674 - 0.36992I$	$8.98485 + 3.05406I$	0



Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.994697 - 0.913978I$ $a = 0.79592 + 1.57410I$ $b = 1.87674 + 0.36992I$	$8.98485 - 3.05406I$	0
$u = 0.784334 + 1.103720I$ $a = 1.32414 + 1.54204I$ $b = 1.68117 + 0.18497I$	$1.02644 - 7.74901I$	0
$u = 0.784334 - 1.103720I$ $a = 1.32414 - 1.54204I$ $b = 1.68117 - 0.18497I$	$1.02644 + 7.74901I$	0
$u = -0.634943 + 0.050863I$ $a = -1.58118 - 0.94089I$ $b = -0.349515 - 0.878817I$	$-5.23148 + 1.44469I$	$-2.19147 - 1.36304I$
$u = -0.634943 - 0.050863I$ $a = -1.58118 + 0.94089I$ $b = -0.349515 + 0.878817I$	$-5.23148 - 1.44469I$	$-2.19147 + 1.36304I$
$u = 0.601289 + 0.105594I$ $a = 0.258323 + 0.970497I$ $b = 1.215100 - 0.178401I$	$-1.82059 + 0.01526I$	$-7.87182 - 0.48568I$
$u = 0.601289 - 0.105594I$ $a = 0.258323 - 0.970497I$ $b = 1.215100 + 0.178401I$	$-1.82059 - 0.01526I$	$-7.87182 + 0.48568I$
$u = -1.127320 + 0.826259I$ $a = -0.431491 - 0.571092I$ $b = -0.399530 - 0.114576I$	$2.66554 + 9.42263I$	0
$u = -1.127320 - 0.826259I$ $a = -0.431491 + 0.571092I$ $b = -0.399530 + 0.114576I$	$2.66554 - 9.42263I$	0
$u = -0.147109 + 0.577451I$ $a = -1.41532 - 0.01491I$ $b = -0.366040 + 0.326712I$	$1.31523 - 1.27199I$	$3.06090 + 2.68907I$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.147109 - 0.577451I$ $a = -1.41532 + 0.01491I$ $b = -0.366040 - 0.326712I$	$1.31523 + 1.27199I$	$3.06090 - 2.68907I$
$u = -0.723739 + 1.209940I$ $a = 1.67771 - 1.53567I$ $b = 2.06140 - 0.32997I$	$9.83371 - 2.67210I$	0
$u = -0.723739 - 1.209940I$ $a = 1.67771 + 1.53567I$ $b = 2.06140 + 0.32997I$	$9.83371 + 2.67210I$	0
$u = 0.411231 + 0.411306I$ $a = 0.32779 + 1.74947I$ $b = 0.97919 - 1.06319I$	$2.74552 + 1.51786I$	$-0.89722 - 4.70084I$
$u = 0.411231 - 0.411306I$ $a = 0.32779 - 1.74947I$ $b = 0.97919 + 1.06319I$	$2.74552 - 1.51786I$	$-0.89722 + 4.70084I$
$u = -0.60092 + 1.28586I$ $a = -1.89989 + 1.40726I$ $b = -2.07450 + 0.29742I$	$8.19227 - 8.99833I$	0
$u = -0.60092 - 1.28586I$ $a = -1.89989 - 1.40726I$ $b = -2.07450 - 0.29742I$	$8.19227 + 8.99833I$	0
$u = -1.19778 + 0.88601I$ $a = -1.78025 + 0.89840I$ $b = -2.69078 - 0.32973I$	$8.24876 + 10.14770I$	0
$u = -1.19778 - 0.88601I$ $a = -1.78025 - 0.89840I$ $b = -2.69078 + 0.32973I$	$8.24876 - 10.14770I$	0
$u = -1.26526 + 0.84227I$ $a = 1.68547 - 1.04922I$ $b = 2.75955 + 0.13511I$	$5.9981 + 16.5072I$	0

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.26526 - 0.84227I$ $a = 1.68547 + 1.04922I$ $b = 2.75955 - 0.13511I$	$5.9981 - 16.5072I$	0
$u = 1.42330 + 0.57117I$ $a = -0.920325 + 0.724904I$ $b = -1.27403 + 1.04616I$	$-1.42259 + 0.46359I$	0
$u = 1.42330 - 0.57117I$ $a = -0.920325 - 0.724904I$ $b = -1.27403 - 1.04616I$	$-1.42259 - 0.46359I$	0
$u = 1.59839 + 0.34758I$ $a = 0.832676 - 0.993612I$ $b = 1.38737 - 1.32476I$	$-1.87995 - 4.31692I$	0
$u = 1.59839 - 0.34758I$ $a = 0.832676 + 0.993612I$ $b = 1.38737 + 1.32476I$	$-1.87995 + 4.31692I$	0
$u = -0.00563429$ $a = 98.6949$ $b = 0.501097$	$-1.20362$	$-8.91660$

**II.**

$$I_2^u = \langle -2a^8 + b + \dots + 3a - 4, a^9 - a^8 + 2a^7 - a^6 + 3a^5 - a^4 + 2a^3 + a + 1, u - 1 \rangle$$

**(i) Arc colorings**

$$a_3 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} a \\ 2a^8 - 3a^7 + 6a^6 - 5a^5 + 9a^4 - 6a^3 + 8a^2 - 3a + 4 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} a \\ 2a^8 - 3a^7 + 6a^6 - 5a^5 + 9a^4 - 6a^3 + 8a^2 - 4a + 4 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -a^2 \\ a^8 - 2a^7 + 3a^6 - 3a^5 + 4a^4 - 4a^3 + 3a^2 - 2a + 1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} a^4 \\ 0 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} a^4 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -a^6 - a^2 \\ a^8 - 2a^7 + 3a^6 - 3a^5 + 4a^4 - 4a^3 + 3a^2 - 2a + 1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -a^6 - a^2 \\ a^8 - 2a^7 + 4a^6 - 3a^5 + 6a^4 - 4a^3 + 6a^2 - 2a + 3 \end{pmatrix}$$

**(ii) Obstruction class = 1**

**(iii) Cusp Shapes =  $-45a^8 + 71a^7 - 127a^6 + 112a^5 - 192a^4 + 149a^3 - 165a^2 + 83a - 97$**

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_2$	$(u - 1)^9$
$c_3, c_6$	$u^9$
$c_4$	$(u + 1)^9$
$c_5$	$u^9 + 3u^8 + 8u^7 + 13u^6 + 17u^5 + 17u^4 + 12u^3 + 6u^2 + u - 1$
$c_7$	$u^9 - 5u^8 + 12u^7 - 15u^6 + 9u^5 + u^4 - 4u^3 + 2u^2 + u - 1$
$c_8$	$u^9 + u^8 - 2u^7 - 3u^6 + u^5 + 3u^4 + 2u^3 - u - 1$
$c_9$	$u^9 + u^8 + 2u^7 + u^6 + 3u^5 + u^4 + 2u^3 + u - 1$
$c_{10}$	$u^9 - u^8 - 2u^7 + 3u^6 + u^5 - 3u^4 + 2u^3 - u + 1$
$c_{11}$	$u^9 - 3u^8 + 8u^7 - 13u^6 + 17u^5 - 17u^4 + 12u^3 - 6u^2 + u + 1$
$c_{12}$	$u^9 - u^8 + 2u^7 - u^6 + 3u^5 - u^4 + 2u^3 + u + 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_4$	$(y - 1)^9$
$c_3, c_6$	$y^9$
$c_5, c_{11}$	$y^9 + 7y^8 + 20y^7 + 25y^6 + 5y^5 - 15y^4 + 22y^2 + 13y - 1$
$c_7$	$y^9 - y^8 + 12y^7 - 7y^6 + 37y^5 + y^4 - 10y^2 + 5y - 1$
$c_8, c_{10}$	$y^9 - 5y^8 + 12y^7 - 15y^6 + 9y^5 + y^4 - 4y^3 + 2y^2 + y - 1$
$c_9, c_{12}$	$y^9 + 3y^8 + 8y^7 + 13y^6 + 17y^5 + 17y^4 + 12y^3 + 6y^2 + y - 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.00000$ $a = -0.140343 + 0.966856I$ $b = -0.302374 + 0.039314I$	$0.13850 + 2.09337I$	$-4.31028 - 3.82038I$
$u = 1.00000$ $a = -0.140343 - 0.966856I$ $b = -0.302374 - 0.039314I$	$0.13850 - 2.09337I$	$-4.31028 + 3.82038I$
$u = 1.00000$ $a = -0.628449 + 0.875112I$ $b = -0.223063 + 0.988364I$	$-2.26187 + 2.45442I$	$-6.95900 - 1.69416I$
$u = 1.00000$ $a = -0.628449 - 0.875112I$ $b = -0.223063 - 0.988364I$	$-2.26187 - 2.45442I$	$-6.95900 + 1.69416I$
$u = 1.00000$ $a = 0.796005 + 0.733148I$ $b = -0.194585 + 1.248300I$	$-6.01628 + 1.33617I$	$-13.56769 - 0.26615I$
$u = 1.00000$ $a = 0.796005 - 0.733148I$ $b = -0.194585 - 1.248300I$	$-6.01628 - 1.33617I$	$-13.56769 + 0.26615I$
$u = 1.00000$ $a = 0.728966 + 0.986295I$ $b = 0.026651 + 0.835796I$	$-5.24306 - 7.08493I$	$-11.54551 + 1.34000I$
$u = 1.00000$ $a = 0.728966 - 0.986295I$ $b = 0.026651 - 0.835796I$	$-5.24306 + 7.08493I$	$-11.54551 - 1.34000I$
$u = 1.00000$ $a = -0.512358$ $b = 9.38674$	$-2.84338$	$-223.240$

$$\text{III. } I_3^u = \langle u^4 + u^3 - u^2 + b - 2u - 1, -u^5 - u^4 + u^3 + u^2 + a - u - 1, u^6 + u^5 - u^4 - 2u^3 + u + 1 \rangle$$

(i) Arc colorings

$$a_3 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -u^2 + 1 \\ -u^2 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} u \\ -u^3 + u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} u^5 + u^4 - u^3 - u^2 + u + 1 \\ -u^4 - u^3 + u^2 + 2u + 1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} u^5 + u^4 - u^3 - u^2 + u + 1 \\ -u^4 - u^3 + u^2 + 2u + 1 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -u^2 + 1 \\ -u^2 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} u^5 - 2u^3 + u \\ u^5 - u^3 + u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 2u^5 - 3u^3 + 2u \\ u^5 - u^3 + u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -2u^5 + 3u^3 - 2u \\ -u^5 + u^3 - u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 3u^5 + u^4 - 4u^3 - u^2 + 3u + 1 \\ u^5 - u^4 - 2u^3 + u^2 + 3u + 1 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes =  $-3u^5 + u^4 - u^3 - 2u^2 - 3u - 7$



(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_5$	$u^6 - 3u^5 + 5u^4 - 4u^3 + 2u^2 - u + 1$
$c_2, c_6$	$u^6 + u^5 - u^4 - 2u^3 + u + 1$
$c_3, c_4$	$u^6 - u^5 - u^4 + 2u^3 - u + 1$
$c_7, c_8$	$(u - 1)^6$
$c_9, c_{12}$	$u^6$
$c_{10}$	$(u + 1)^6$
$c_{11}$	$u^6 + 3u^5 + 5u^4 + 4u^3 + 2u^2 + u + 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_5, c_{11}$	$y^6 + y^5 + 5y^4 + 6y^2 + 3y + 1$
$c_2, c_3, c_4$ $c_6$	$y^6 - 3y^5 + 5y^4 - 4y^3 + 2y^2 - y + 1$
$c_7, c_8, c_{10}$	$(y - 1)^6$
$c_9, c_{12}$	$y^6$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.002190 + 0.295542I$		
$a = 1.00126 + 1.15863I$	$-3.53554 - 0.92430I$	$-12.60470 - 5.55069I$
$b = 2.68739 - 0.76772I$		
$u = 1.002190 - 0.295542I$		
$a = 1.00126 - 1.15863I$	$-3.53554 + 0.92430I$	$-12.60470 + 5.55069I$
$b = 2.68739 + 0.76772I$		
$u = -0.428243 + 0.664531I$		
$a = -0.001257 + 1.158630I$	$0.245672 - 0.924305I$	$-5.68949 + 0.25702I$
$b = -0.346225 + 0.393823I$		
$u = -0.428243 - 0.664531I$		
$a = -0.001257 - 1.158630I$	$0.245672 + 0.924305I$	$-5.68949 - 0.25702I$
$b = -0.346225 - 0.393823I$		
$u = -1.073950 + 0.558752I$		
$a = 0.500000 - 0.260139I$	$-1.64493 + 5.69302I$	$-11.7058 - 8.3306I$
$b = 0.658836 + 0.177500I$		
$u = -1.073950 - 0.558752I$		
$a = 0.500000 + 0.260139I$	$-1.64493 - 5.69302I$	$-11.7058 + 8.3306I$
$b = 0.658836 - 0.177500I$		

#### IV. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1$	$(u-1)^9(u^6 - 3u^5 + 5u^4 - 4u^3 + 2u^2 - u + 1)$ $\cdot (u^{66} + 21u^{65} + \dots + 31524u + 1)$
$c_2$	$((u-1)^9)(u^6 + u^5 + \dots + u + 1)(u^{66} - 11u^{65} + \dots + 184u - 1)$
$c_3$	$u^9(u^6 - u^5 + \dots - u + 1)(u^{66} + 8u^{65} + \dots - 7168u + 512)$
$c_4$	$((u+1)^9)(u^6 - u^5 + \dots - u + 1)(u^{66} - 11u^{65} + \dots + 184u - 1)$
$c_5$	$(u^6 - 3u^5 + 5u^4 - 4u^3 + 2u^2 - u + 1)$ $\cdot (u^9 + 3u^8 + 8u^7 + 13u^6 + 17u^5 + 17u^4 + 12u^3 + 6u^2 + u - 1)$ $\cdot (u^{66} + 3u^{65} + \dots - 2u - 1)$
$c_6$	$u^9(u^6 + u^5 + \dots + u + 1)(u^{66} + 8u^{65} + \dots - 7168u + 512)$
$c_7$	$(u-1)^6(u^9 - 5u^8 + 12u^7 - 15u^6 + 9u^5 + u^4 - 4u^3 + 2u^2 + u - 1)$ $\cdot (u^{66} + 28u^{65} + \dots - 143u + 1)$
$c_8$	$(u-1)^6(u^9 + u^8 - 2u^7 - 3u^6 + u^5 + 3u^4 + 2u^3 - u - 1)$ $\cdot (u^{66} - 8u^{65} + \dots - 11u + 1)$
$c_9$	$u^6(u^9 + u^8 + 2u^7 + u^6 + 3u^5 + u^4 + 2u^3 + u - 1)$ $\cdot (u^{66} - 2u^{65} + \dots + 192u + 64)$
$c_{10}$	$(u+1)^6(u^9 - u^8 - 2u^7 + 3u^6 + u^5 - 3u^4 + 2u^3 - u + 1)$ $\cdot (u^{66} - 8u^{65} + \dots - 11u + 1)$
$c_{11}$	$(u^6 + 3u^5 + 5u^4 + 4u^3 + 2u^2 + u + 1)$ $\cdot (u^9 - 3u^8 + 8u^7 - 13u^6 + 17u^5 - 17u^4 + 12u^3 - 6u^2 + u + 1)$ $\cdot (u^{66} + 3u^{65} + \dots - 2u - 1)$
$c_{12}$	$u^6(u^9 - u^8 + 2u^7 - u^6 + 3u^5 - u^4 + 2u^3 + u + 1)$ $\cdot (u^{66} - 2u^{65} + \dots + 192u + 64)$

## V. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1$	$(y-1)^9(y^6 + y^5 + 5y^4 + 6y^2 + 3y + 1)$ $\cdot (y^{66} + 59y^{65} + \dots - 992297680y + 1)$
$c_2, c_4$	$(y-1)^9(y^6 - 3y^5 + 5y^4 - 4y^3 + 2y^2 - y + 1)$ $\cdot (y^{66} - 21y^{65} + \dots - 31524y + 1)$
$c_3, c_6$	$y^9(y^6 - 3y^5 + 5y^4 - 4y^3 + 2y^2 - y + 1)$ $\cdot (y^{66} - 60y^{65} + \dots - 76021760y + 262144)$
$c_5, c_{11}$	$(y^6 + y^5 + 5y^4 + 6y^2 + 3y + 1)$ $\cdot (y^9 + 7y^8 + 20y^7 + 25y^6 + 5y^5 - 15y^4 + 22y^2 + 13y - 1)$ $\cdot (y^{66} + 15y^{65} + \dots - 20y + 1)$
$c_7$	$(y-1)^6(y^9 - y^8 + 12y^7 - 7y^6 + 37y^5 + y^4 - 10y^2 + 5y - 1)$ $\cdot (y^{66} + 28y^{65} + \dots - 12229y + 1)$
$c_8, c_{10}$	$(y-1)^6(y^9 - 5y^8 + 12y^7 - 15y^6 + 9y^5 + y^4 - 4y^3 + 2y^2 + y - 1)$ $\cdot (y^{66} - 28y^{65} + \dots + 143y + 1)$
$c_9, c_{12}$	$y^6(y^9 + 3y^8 + 8y^7 + 13y^6 + 17y^5 + 17y^4 + 12y^3 + 6y^2 + y - 1)$ $\cdot (y^{66} + 42y^{65} + \dots + 77824y + 4096)$