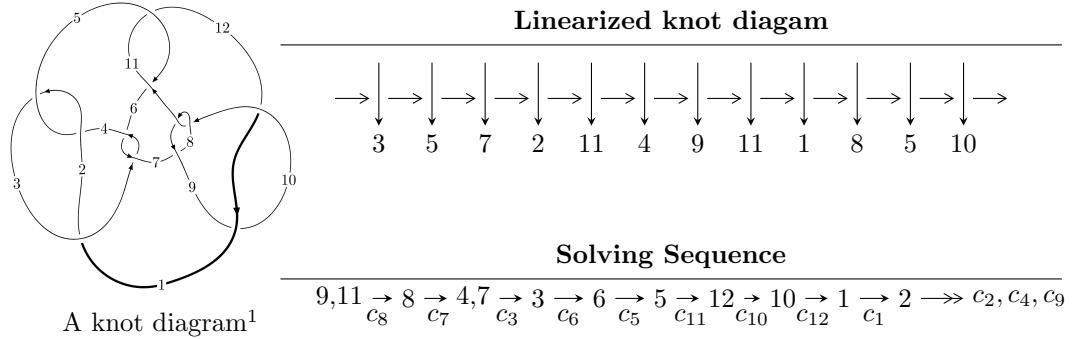


$12n_{0133}$  ( $K12n_{0133}$ )



### Ideals for irreducible components<sup>2</sup> of $X_{\text{par}}$

$$\begin{aligned}
 I_1^u &= \langle 2u^{13} + 5u^{12} - 2u^{11} - 16u^{10} - 10u^9 + 16u^8 + 28u^7 + 10u^6 - 19u^5 - 25u^4 - 7u^3 + 6u^2 + 2b + 5u, \\
 &\quad - u^{13} - 4u^{12} - 3u^{11} + 8u^{10} + 14u^9 - 18u^7 - 21u^6 - 5u^5 + 16u^4 + 17u^3 + 4u^2 + 2a - 4u - 5, \\
 &\quad u^{14} + 3u^{13} - 9u^{11} - 8u^{10} + 8u^9 + 18u^8 + 9u^7 - 10u^6 - 18u^5 - 6u^4 + 6u^3 + 6u^2 + 2u - 1 \rangle \\
 I_2^u &= \langle -1.17690 \times 10^{65}u^{57} - 3.97295 \times 10^{65}u^{56} + \dots + 3.56133 \times 10^{64}b - 4.96718 \times 10^{63}, \\
 &\quad - 6.29210 \times 10^{64}u^{57} - 8.59795 \times 10^{64}u^{56} + \dots + 7.12266 \times 10^{64}a - 4.18226 \times 10^{65}, u^{58} + 4u^{57} + \dots - 5u + \dots \rangle \\
 I_3^u &= \langle u^2 + b + u - 1, a + u, u^3 + u^2 - 1 \rangle \\
 I_4^u &= \langle 4u^2a + 6au + b + 4a + 1, -2u^2a + a^2 - au - 2u^2 + 2a - u + 2, u^3 + u^2 - 1 \rangle \\
 I_5^u &= \langle b - u - 2, a + 2u + 3, u^2 + u - 1 \rangle \\
 I_6^u &= \langle b - 2a + 2, a^2 - a - 1, u - 1 \rangle
 \end{aligned}$$

\* 6 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 85 representations.

<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/math/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\text{I. } I_1^u = \langle 2u^{13} + 5u^{12} + \dots + 2b + 5u, -u^{13} - 4u^{12} + \dots + 2a - 5, u^{14} + 3u^{13} + \dots + 2u - 1 \rangle$$

(i) **Arc colorings**

$$a_9 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} \frac{1}{2}u^{13} + 2u^{12} + \dots + 2u + \frac{5}{2} \\ -u^{13} - \frac{5}{2}u^{12} + \dots - 3u^2 - \frac{3}{2}u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -u^2 + 1 \\ -u^2 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} \frac{1}{2}u^{13} + \frac{3}{2}u^{12} + \dots + \frac{5}{2}u + 2 \\ -\frac{1}{2}u^{13} - 2u^{12} + \dots - u - \frac{1}{2} \end{pmatrix}$$

$$a_6 = \begin{pmatrix} \frac{1}{2}u^{13} + \frac{3}{2}u^{12} + \dots + \frac{3}{2}u + 2 \\ -\frac{1}{2}u^{12} - \frac{3}{2}u^{11} + \dots - \frac{1}{2}u - \frac{1}{2} \end{pmatrix}$$

$$a_5 = \begin{pmatrix} \frac{1}{2}u^{13} + \frac{3}{2}u^{12} + \dots + \frac{3}{2}u + 2 \\ -u^{12} - \frac{5}{2}u^{11} + \dots - u - \frac{1}{2} \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -u^{11} - u^{10} + 3u^9 + 4u^8 - 3u^7 - 6u^6 - 2u^5 + 3u^4 + 5u^3 + u^2 - 2u - 1 \\ u^{13} + \frac{3}{2}u^{12} + \dots + 3u^2 + \frac{3}{2}u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} u \\ -u^3 + u \end{pmatrix}$$

$$a_1 = \begin{pmatrix} \frac{1}{2}u^{13} + u^{12} + \dots - u - \frac{3}{2} \\ \frac{1}{2}u^{13} + u^{12} + \dots + \frac{7}{2}u^2 + u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -\frac{1}{2}u^{13} - \frac{3}{2}u^{12} + \dots - \frac{3}{2}u - \frac{3}{2} \\ -\frac{1}{2}u^{13} - \frac{1}{2}u^{12} + \dots + \frac{1}{2}u + \frac{1}{2} \end{pmatrix}$$

(ii) **Obstruction class** = -1

(iii) **Cusp Shapes**

$$= 3u^{13} + 3u^{12} - 15u^{11} - 24u^{10} + 14u^9 + 44u^8 + 18u^7 - 27u^6 - 52u^5 - 25u^4 + 14u^3 + 10u^2 + 3u - 11$$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_7$	$u^{14} + 9u^{13} + \dots + 16u + 1$
$c_2, c_4, c_8$ $c_{10}$	$u^{14} - 3u^{13} + \dots - 2u - 1$
$c_3, c_6, c_9$ $c_{12}$	$u^{14} - u^{13} + \dots - 4u - 1$
$c_5, c_{11}$	$u^{14} - 7u^{13} + \dots - 24u + 8$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_7$	$y^{14} - 5y^{13} + \cdots - 208y + 1$
$c_2, c_4, c_8$ $c_{10}$	$y^{14} - 9y^{13} + \cdots - 16y + 1$
$c_3, c_6, c_9$ $c_{12}$	$y^{14} + 3y^{13} + \cdots - 8y + 1$
$c_5, c_{11}$	$y^{14} - 7y^{13} + \cdots + 384y + 64$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.242991 + 0.933745I$		
$a = -0.20291 + 1.67953I$	$1.33116 - 5.50874I$	$-7.69545 + 3.70076I$
$b = -0.821533 + 0.270883I$		
$u = -0.242991 - 0.933745I$		
$a = -0.20291 - 1.67953I$	$1.33116 + 5.50874I$	$-7.69545 - 3.70076I$
$b = -0.821533 - 0.270883I$		
$u = 0.951606 + 0.107631I$		
$a = -0.80680 + 1.21543I$	$-2.88995 - 0.46660I$	$-33.6526 - 15.6404I$
$b = 3.80232 + 0.74412I$		
$u = 0.951606 - 0.107631I$		
$a = -0.80680 - 1.21543I$	$-2.88995 + 0.46660I$	$-33.6526 + 15.6404I$
$b = 3.80232 - 0.74412I$		
$u = -0.389011 + 0.665748I$		
$a = 0.507976 + 0.255319I$	$3.75566 + 0.17244I$	$-4.31674 - 1.33622I$
$b = 0.587054 + 0.784524I$		
$u = -0.389011 - 0.665748I$		
$a = 0.507976 - 0.255319I$	$3.75566 - 0.17244I$	$-4.31674 + 1.33622I$
$b = 0.587054 - 0.784524I$		
$u = -1.217360 + 0.433191I$		
$a = -0.051195 + 0.233560I$	$-1.53918 + 8.57795I$	$-13.9694 - 8.6920I$
$b = 0.695133 + 0.745943I$		
$u = -1.217360 - 0.433191I$		
$a = -0.051195 - 0.233560I$	$-1.53918 - 8.57795I$	$-13.9694 + 8.6920I$
$b = 0.695133 - 0.745943I$		
$u = 1.208510 + 0.461890I$		
$a = 1.195780 - 0.437447I$	$-7.24910 - 2.92807I$	$-16.0849 + 1.6852I$
$b = 1.55260 - 0.60463I$		
$u = 1.208510 - 0.461890I$		
$a = 1.195780 + 0.437447I$	$-7.24910 + 2.92807I$	$-16.0849 - 1.6852I$
$b = 1.55260 + 0.60463I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.31782$		
$a = 0.941660$	-10.4546	-24.6220
$b = 0.882448$		
$u = -1.28364 + 0.61767I$		
$a = -1.46437 - 0.09958I$	$-4.9818 + 17.0516I$	$-13.2441 - 9.4300I$
$b = -2.38982 - 1.44096I$		
$u = -1.28364 - 0.61767I$		
$a = -1.46437 + 0.09958I$	$-4.9818 - 17.0516I$	$-13.2441 + 9.4300I$
$b = -2.38982 + 1.44096I$		
$u = 0.263596$		
$a = 2.70137$	-0.942520	-9.45120
$b = -0.733954$		

### II.

$$I_2^u = \langle -1.18 \times 10^{65}u^{57} - 3.97 \times 10^{65}u^{56} + \dots + 3.56 \times 10^{64}b - 4.97 \times 10^{63}, -6.29 \times 10^{64}u^{57} - 8.60 \times 10^{64}u^{56} + \dots + 7.12 \times 10^{64}a - 4.18 \times 10^{65}, u^{58} + 4u^{57} + \dots - 5u + 1 \rangle$$

(i) **Arc colorings**

$$a_9 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 0.883391u^{57} + 1.20713u^{56} + \dots - 9.91542u + 5.87176 \\ 3.30467u^{57} + 11.1558u^{56} + \dots - 6.41751u + 0.139475 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -u^2 + 1 \\ -u^2 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 0.793575u^{57} + 0.365747u^{56} + \dots - 3.89250u + 4.38523 \\ 1.32573u^{57} + 4.64753u^{56} + \dots + 4.91950u - 1.75010 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 1.70888u^{57} + 4.42480u^{56} + \dots - 6.68595u + 4.41639 \\ 2.56867u^{57} + 8.73466u^{56} + \dots - 12.4165u + 1.63075 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 1.70888u^{57} + 4.42480u^{56} + \dots - 6.68595u + 4.41639 \\ 0.322307u^{57} + 1.39608u^{56} + \dots + 1.34584u - 0.779945 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 1.31808u^{57} + 3.67421u^{56} + \dots + 1.92169u - 2.00892 \\ 0.489553u^{57} + 1.26691u^{56} + \dots - 0.411200u + 0.625023 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} u \\ -u^3 + u \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 2.12433u^{57} + 5.66107u^{56} + \dots + 3.12772u - 2.10774 \\ -0.0988242u^{57} - 1.20154u^{56} + \dots + 7.79161u - 0.711908 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -0.453494u^{57} - 0.227312u^{56} + \dots + 6.41674u - 3.64552 \\ -2.66084u^{57} - 9.70894u^{56} + \dots + 11.5745u - 1.08534 \end{pmatrix}$$

(ii) **Obstruction class = -1**

(iii) **Cusp Shapes** =  $8.86204u^{57} + 41.6548u^{56} + \dots + 50.2522u - 23.8526$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_7$	$u^{58} + 32u^{57} + \cdots + 25u + 1$
$c_2, c_4, c_8$ $c_{10}$	$u^{58} - 4u^{57} + \cdots + 5u + 1$
$c_3, c_6, c_9$ $c_{12}$	$u^{58} - 4u^{57} + \cdots + 32u - 4$
$c_5, c_{11}$	$(u^{29} + 2u^{28} + \cdots - 28u - 8)^2$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_7$	$y^{58} - 8y^{57} + \cdots + 195y + 1$
$c_2, c_4, c_8$ $c_{10}$	$y^{58} - 32y^{57} + \cdots - 25y + 1$
$c_3, c_6, c_9$ $c_{12}$	$y^{58} + 18y^{57} + \cdots - 984y + 16$
$c_5, c_{11}$	$(y^{29} - 28y^{28} + \cdots + 2896y - 64)^2$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.988988$		
$a = -0.481132$	-2.67255	-211.680
$b = -5.97136$		
$u = -0.852515 + 0.455377I$		
$a = 0.096402 + 0.221595I$	$4.34822 + 5.30129I$	$-10.14110 - 5.91971I$
$b = 1.14950 + 1.39220I$		
$u = -0.852515 - 0.455377I$		
$a = 0.096402 - 0.221595I$	$4.34822 - 5.30129I$	$-10.14110 + 5.91971I$
$b = 1.14950 - 1.39220I$		
$u = -0.875378 + 0.395680I$		
$a = -1.17395 - 1.12502I$	-1.15248 + 2.97907I	-9.53425 - 4.84429I
$b = -0.55207 - 1.63441I$		
$u = -0.875378 - 0.395680I$		
$a = -1.17395 + 1.12502I$	-1.15248 - 2.97907I	-9.53425 + 4.84429I
$b = -0.55207 + 1.63441I$		
$u = 0.382222 + 0.979860I$		
$a = 0.37822 + 1.49048I$	-4.05295 + 3.42058I	-12.00000 - 4.03802I
$b = 0.968996 + 0.458325I$		
$u = 0.382222 - 0.979860I$		
$a = 0.37822 - 1.49048I$	-4.05295 - 3.42058I	-12.00000 + 4.03802I
$b = 0.968996 - 0.458325I$		
$u = -1.06017$		
$a = 1.48801$	-10.6310	-48.5360
$b = 1.19467$		
$u = -0.216051 + 1.075610I$		
$a = 0.49789 - 1.82352I$	-1.66044 - 11.01250I	-12.00000 + 0.I
$b = 0.930330 - 0.518578I$		
$u = -0.216051 - 1.075610I$		
$a = 0.49789 + 1.82352I$	-1.66044 + 11.01250I	-12.00000 + 0.I
$b = 0.930330 + 0.518578I$		

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.994844 + 0.502352I$	$-0.488787 + 0.370462I$	0
$a = -0.026325 - 0.357537I$		
$b = -1.077780 - 0.102508I$		
$u = 0.994844 - 0.502352I$	$-0.488787 - 0.370462I$	0
$a = -0.026325 + 0.357537I$		
$b = -1.077780 + 0.102508I$		
$u = -0.108845 + 0.869895I$	$-3.19564 - 4.35308I$	$-12.04263 + 3.74313I$
$a = 0.31064 + 1.79296I$		
$b = 0.569231 + 0.371365I$		
$u = -0.108845 - 0.869895I$	$-3.19564 + 4.35308I$	$-12.04263 - 3.74313I$
$a = 0.31064 - 1.79296I$		
$b = 0.569231 - 0.371365I$		
$u = -1.006590 + 0.537430I$	$2.03816 + 4.43643I$	0
$a = 0.312868 + 0.518025I$		
$b = -0.632775 - 0.100970I$		
$u = -1.006590 - 0.537430I$	$2.03816 - 4.43643I$	0
$a = 0.312868 - 0.518025I$		
$b = -0.632775 + 0.100970I$		
$u = -0.873306 + 0.762690I$	$1.81502 + 2.87998I$	0
$a = 2.26083 + 2.71765I$		
$b = 0.21388 + 2.77675I$		
$u = -0.873306 - 0.762690I$	$1.81502 - 2.87998I$	0
$a = 2.26083 - 2.71765I$		
$b = 0.21388 - 2.77675I$		
$u = 0.836851 + 0.036106I$	$1.81502 - 2.87998I$	$-58.6220 + 17.5185I$
$a = 0.0838767 - 0.0224097I$		
$b = 0.00910 - 4.38592I$		
$u = 0.836851 - 0.036106I$	$1.81502 + 2.87998I$	$-58.6220 - 17.5185I$
$a = 0.0838767 + 0.0224097I$		
$b = 0.00910 + 4.38592I$		

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.654785 + 0.491061I$		
$a = 0.267178 + 0.146980I$	$4.90257 - 1.34329I$	$-7.80264 + 1.36225I$
$b = -0.936070 - 0.955868I$		
$u = -0.654785 - 0.491061I$		
$a = 0.267178 - 0.146980I$	$4.90257 + 1.34329I$	$-7.80264 - 1.36225I$
$b = -0.936070 + 0.955868I$		
$u = -1.141310 + 0.406924I$		
$a = -1.042680 - 0.445981I$	$-4.05295 + 3.42058I$	0
$b = -1.124050 - 0.134041I$		
$u = -1.141310 - 0.406924I$		
$a = -1.042680 + 0.445981I$	$-4.05295 - 3.42058I$	0
$b = -1.124050 + 0.134041I$		
$u = -0.787150 + 0.924733I$		
$a = 1.205180 - 0.532327I$	$4.90257 + 1.34329I$	0
$b = 1.38107 + 0.43654I$		
$u = -0.787150 - 0.924733I$		
$a = 1.205180 + 0.532327I$	$4.90257 - 1.34329I$	0
$b = 1.38107 - 0.43654I$		
$u = 0.000304 + 0.780908I$		
$a = -0.24339 - 2.24468I$	$-3.74876 - 1.54341I$	$-12.07483 + 3.03548I$
$b = 0.267868 - 0.277636I$		
$u = 0.000304 - 0.780908I$		
$a = -0.24339 + 2.24468I$	$-3.74876 + 1.54341I$	$-12.07483 - 3.03548I$
$b = 0.267868 + 0.277636I$		
$u = 1.120680 + 0.529353I$		
$a = 1.175230 - 0.118199I$	$-3.19564 - 4.35308I$	0
$b = 1.86181 - 1.77127I$		
$u = 1.120680 - 0.529353I$		
$a = 1.175230 + 0.118199I$	$-3.19564 + 4.35308I$	0
$b = 1.86181 + 1.77127I$		

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.665448 + 0.320577I$	$-0.488787 + 0.370462I$	$-8.36692 - 2.50640I$
$a = -1.75785 - 0.27970I$		
$b = -0.427413 - 0.048282I$		
$u = -0.665448 - 0.320577I$	$-0.488787 - 0.370462I$	$-8.36692 + 2.50640I$
$a = -1.75785 + 0.27970I$		
$b = -0.427413 + 0.048282I$		
$u = -1.209970 + 0.458074I$	$-7.27243 + 6.00653I$	0
$a = -1.109810 - 0.614505I$		
$b = -2.00916 - 2.00839I$		
$u = -1.209970 - 0.458074I$	$-7.27243 - 6.00653I$	0
$a = -1.109810 + 0.614505I$		
$b = -2.00916 + 2.00839I$		
$u = 1.264110 + 0.277934I$	$-1.15248 - 2.97907I$	0
$a = -0.094671 - 0.217784I$		
$b = 0.589009 + 0.036358I$		
$u = 1.264110 - 0.277934I$	$-1.15248 + 2.97907I$	0
$a = -0.094671 + 0.217784I$		
$b = 0.589009 - 0.036358I$		
$u = 1.278760 + 0.279605I$	$-3.74876 + 1.54341I$	0
$a = -0.874635 + 0.506037I$		
$b = -1.179270 + 0.382768I$		
$u = 1.278760 - 0.279605I$	$-3.74876 - 1.54341I$	0
$a = -0.874635 - 0.506037I$		
$b = -1.179270 - 0.382768I$		
$u = 0.689587$	$-2.67255$	$-211.680$
$a = 6.16946$		
$b = -5.31315$		
$u = 1.251940 + 0.396137I$	$-7.39364$	0
$a = -1.204600 + 0.452476I$		
$b = -2.28308 + 2.02996I$		

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.251940 - 0.396137I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = -1.204600 - 0.452476I$	$-7.39364$	0
$b = -2.28308 - 2.02996I$		
$u = 0.027420 + 0.672723I$		
$a = 0.367381 + 0.017368I$	$2.03816 - 4.43643I$	$-7.12586 + 5.70665I$
$b = -0.180737 - 0.719838I$		
$u = 0.027420 - 0.672723I$		
$a = 0.367381 - 0.017368I$	$2.03816 + 4.43643I$	$-7.12586 - 5.70665I$
$b = -0.180737 + 0.719838I$		
$u = -1.227590 + 0.512752I$		
$a = 1.029830 + 0.433526I$	$-6.56035 + 9.36152I$	0
$b = 1.235900 + 0.213650I$		
$u = -1.227590 - 0.512752I$		
$a = 1.029830 - 0.433526I$	$-6.56035 - 9.36152I$	0
$b = 1.235900 - 0.213650I$		
$u = -0.984255 + 0.909262I$		
$a = -1.077810 + 0.708898I$	$4.34822 + 5.30129I$	0
$b = -1.52408 - 0.24363I$		
$u = -0.984255 - 0.909262I$		
$a = -1.077810 - 0.708898I$	$4.34822 - 5.30129I$	0
$b = -1.52408 + 0.24363I$		
$u = -1.220950 + 0.580073I$		
$a = 1.236460 + 0.202005I$	$-1.66044 + 11.01250I$	0
$b = 2.15316 + 1.56889I$		
$u = -1.220950 - 0.580073I$		
$a = 1.236460 - 0.202005I$	$-1.66044 - 11.01250I$	0
$b = 2.15316 - 1.56889I$		
$u = 1.196500 + 0.654445I$		
$a = -1.393060 + 0.026552I$	$-6.56035 - 9.36152I$	0
$b = -2.02586 + 1.44130I$		

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.196500 - 0.654445I$		
$a = -1.393060 - 0.026552I$	$-6.56035 + 9.36152I$	0
$b = -2.02586 - 1.44130I$		
$u = 1.44823 + 0.32172I$		
$a = 0.885882 - 0.795017I$	$-7.27243 + 6.00653I$	0
$b = 0.993193 - 0.775693I$		
$u = 1.44823 - 0.32172I$		
$a = 0.885882 + 0.795017I$	$-7.27243 - 6.00653I$	0
$b = 0.993193 + 0.775693I$		
$u = -1.57371$		
$a = 0.372440$	-10.6310	0
$b = 0.379153$		
$u = 0.242019 + 0.246574I$		
$a = 1.39952 - 1.87926I$	-0.942618	$-9.31087 + 0.I$
$b = -0.768573 - 0.066926I$		
$u = 0.242019 - 0.246574I$		
$a = 1.39952 + 1.87926I$	-0.942618	$-9.31087 + 0.I$
$b = -0.768573 + 0.066926I$		
$u = 0.257910 + 0.127141I$		
$a = 2.21702 - 1.31285I$	-0.942376	$-9.38299 + 0.I$
$b = -0.746774 - 0.028572I$		
$u = 0.257910 - 0.127141I$		
$a = 2.21702 + 1.31285I$	-0.942376	$-9.38299 + 0.I$
$b = -0.746774 + 0.028572I$		

$$\text{III. } I_3^u = \langle u^2 + b + u - 1, a + u, u^3 + u^2 - 1 \rangle$$

(i) Arc colorings

$$\begin{aligned} a_9 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_{11} &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_8 &= \begin{pmatrix} 1 \\ -u^2 \end{pmatrix} \\ a_4 &= \begin{pmatrix} -u \\ -u^2 - u + 1 \end{pmatrix} \\ a_7 &= \begin{pmatrix} -u^2 + 1 \\ -u^2 \end{pmatrix} \\ a_3 &= \begin{pmatrix} -1 \\ 0 \end{pmatrix} \\ a_6 &= \begin{pmatrix} 0 \\ -u \end{pmatrix} \\ a_5 &= \begin{pmatrix} 0 \\ -u \end{pmatrix} \\ a_{12} &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_{10} &= \begin{pmatrix} u \\ u^2 + u - 1 \end{pmatrix} \\ a_1 &= \begin{pmatrix} u^2 - 1 \\ u^2 \end{pmatrix} \\ a_2 &= \begin{pmatrix} -1 \\ u^2 \end{pmatrix} \end{aligned}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes =  $-8u - 12$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_3, c_7$ $c_9$	$u^3 - u^2 + 2u - 1$
$c_2, c_8$	$u^3 + u^2 - 1$
$c_4, c_{10}$	$u^3 - u^2 + 1$
$c_5, c_{11}$	$u^3$
$c_6, c_{12}$	$u^3 + u^2 + 2u + 1$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_3, c_6$ $c_7, c_9, c_{12}$	$y^3 + 3y^2 + 2y - 1$
$c_2, c_4, c_8$ $c_{10}$	$y^3 - y^2 + 2y - 1$
$c_5, c_{11}$	$y^3$

**(vi) Complex Volumes and Cusp Shapes**

Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.877439 + 0.744862I$		
$a = 0.877439 - 0.744862I$	$6.04826 + 5.65624I$	$-4.98049 - 5.95889I$
$b = 1.66236 + 0.56228I$		
$u = -0.877439 - 0.744862I$		
$a = 0.877439 + 0.744862I$	$6.04826 - 5.65624I$	$-4.98049 + 5.95889I$
$b = 1.66236 - 0.56228I$		
$u = 0.754878$		
$a = -0.754878$	$-2.22691$	$-18.0390$
$b = -0.324718$		

$$I_4^u = \langle 4u^2a + 6au + b + 4a + 1, -2u^2a + a^2 - au - 2u^2 + 2a - u + 2, u^3 + u^2 - 1 \rangle$$

(i) **Arc colorings**

$$a_9 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} a \\ -4u^2a - 6au - 4a - 1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -u^2 + 1 \\ -u^2 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -au + u^2 - u \\ -3u^2a - 5au - 3a - u \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 0 \\ -u^2a - 2au + 2u^2 - 2a + 2u + 1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 0 \\ -u^2a - 2au + 2u^2 - 2a + 2u + 1 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} u \\ u^2 + u - 1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} u^2 - 1 \\ u^2 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -au + u^2 - u \\ -u^2a - 2au + 2u^2 - a + u + 2 \end{pmatrix}$$

(ii) **Obstruction class = 1**

(iii) **Cusp Shapes** =  $-16u^2a - 21au - 21a + 11u - 1$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_3, c_7$ $c_9$	$(u^3 - u^2 + 2u - 1)^2$
$c_2, c_8$	$(u^3 + u^2 - 1)^2$
$c_4, c_{10}$	$(u^3 - u^2 + 1)^2$
$c_5, c_{11}$	$u^6$
$c_6, c_{12}$	$(u^3 + u^2 + 2u + 1)^2$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_3, c_6$ $c_7, c_9, c_{12}$	$(y^3 + 3y^2 + 2y - 1)^2$
$c_2, c_4, c_8$ $c_{10}$	$(y^3 - y^2 + 2y - 1)^2$
$c_5, c_{11}$	$y^6$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_4^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.877439 + 0.744862I$		
$a = -1.069840 + 0.424452I$	6.04826	$-6.45445 + 0.I$
$b = -1.75488 - 0.64082I$		
$u = -0.877439 + 0.744862I$		
$a = -1.37744 - 2.29387I$	1.91067 + 2.82812I	$9.7272 + 14.7292I$
$b = 0.18504 - 1.97346I$		
$u = -0.877439 - 0.744862I$		
$a = -1.069840 - 0.424452I$	6.04826	$-6.45445 + 0.I$
$b = -1.75488 + 0.64082I$		
$u = -0.877439 - 0.744862I$		
$a = -1.37744 + 2.29387I$	1.91067 - 2.82812I	$9.7272 - 14.7292I$
$b = 0.18504 + 1.97346I$		
$u = 0.754878$		
$a = -0.052721 + 0.320410I$	1.91067 - 2.82812I	$9.7272 - 14.7292I$
$b = -0.43016 - 3.46319I$		
$u = 0.754878$		
$a = -0.052721 - 0.320410I$	1.91067 + 2.82812I	$9.7272 + 14.7292I$
$b = -0.43016 + 3.46319I$		

$$\mathbf{V}. \quad I_5^u = \langle b - u - 2, \ a + 2u + 3, \ u^2 + u - 1 \rangle$$

(i) Arc colorings

$$\begin{aligned} a_9 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_{11} &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_8 &= \begin{pmatrix} 1 \\ u - 1 \end{pmatrix} \\ a_4 &= \begin{pmatrix} -2u - 3 \\ u + 2 \end{pmatrix} \\ a_7 &= \begin{pmatrix} u \\ u - 1 \end{pmatrix} \\ a_3 &= \begin{pmatrix} -2u - 3 \\ u + 2 \end{pmatrix} \\ a_6 &= \begin{pmatrix} u \\ u - 1 \end{pmatrix} \\ a_5 &= \begin{pmatrix} u \\ -u \end{pmatrix} \\ a_{12} &= \begin{pmatrix} -2u + 1 \\ 3u - 1 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} u \\ -u + 1 \end{pmatrix} \\ a_1 &= \begin{pmatrix} -u \\ u \end{pmatrix} \\ a_2 &= \begin{pmatrix} -3u - 3 \\ 2u + 2 \end{pmatrix} \end{aligned}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = 29

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_2$	$(u - 1)^2$
$c_3, c_6$	$u^2$
$c_4$	$(u + 1)^2$
$c_5, c_7$	$u^2 - 3u + 1$
$c_8, c_9$	$u^2 + u - 1$
$c_{10}, c_{12}$	$u^2 - u - 1$
$c_{11}$	$u^2 + 3u + 1$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_4$	$(y - 1)^2$
$c_3, c_6$	$y^2$
$c_5, c_7, c_{11}$	$y^2 - 7y + 1$
$c_8, c_9, c_{10}$ $c_{12}$	$y^2 - 3y + 1$

**(vi) Complex Volumes and Cusp Shapes**

Solutions to $I_5^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.618034$		
$a = -4.23607$	-2.63189	29.0000
$b = 2.61803$		
$u = -1.61803$		
$a = 0.236068$	-10.5276	29.0000
$b = 0.381966$		

$$\text{VI. } I_6^u = \langle b - 2a + 2, a^2 - a - 1, u - 1 \rangle$$

(i) Arc colorings

$$a_9 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} a \\ 2a - 2 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} a \\ a - 2 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -a - 1 \\ -3 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -a - 1 \\ a - 2 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -3a - 2 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -3a - 2 \\ 0 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -a - 1 \\ -1 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = 29

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_{11}$	$u^2 - 3u + 1$
$c_2, c_3$	$u^2 + u - 1$
$c_4, c_6$	$u^2 - u - 1$
$c_5$	$u^2 + 3u + 1$
$c_7, c_8$	$(u - 1)^2$
$c_9, c_{12}$	$u^2$
$c_{10}$	$(u + 1)^2$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_5, c_{11}$	$y^2 - 7y + 1$
$c_2, c_3, c_4$ $c_6$	$y^2 - 3y + 1$
$c_7, c_8, c_{10}$	$(y - 1)^2$
$c_9, c_{12}$	$y^2$

**(vi) Complex Volumes and Cusp Shapes**

Solutions to $I_6^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.00000$		
$a = -0.618034$	-2.63189	29.0000
$b = -3.23607$		
$u = 1.00000$		
$a = 1.61803$	-10.5276	29.0000
$b = 1.23607$		

## VII. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1, c_7$	$((u - 1)^2)(u^2 - 3u + 1)(u^3 - u^2 + 2u - 1)^3(u^{14} + 9u^{13} + \dots + 16u + 1)$ $\cdot (u^{58} + 32u^{57} + \dots + 25u + 1)$
$c_2, c_8$	$((u - 1)^2)(u^2 + u - 1)(u^3 + u^2 - 1)^3(u^{14} - 3u^{13} + \dots - 2u - 1)$ $\cdot (u^{58} - 4u^{57} + \dots + 5u + 1)$
$c_3, c_9$	$u^2(u^2 + u - 1)(u^3 - u^2 + 2u - 1)^3(u^{14} - u^{13} + \dots - 4u - 1)$ $\cdot (u^{58} - 4u^{57} + \dots + 32u - 4)$
$c_4, c_{10}$	$((u + 1)^2)(u^2 - u - 1)(u^3 - u^2 + 1)^3(u^{14} - 3u^{13} + \dots - 2u - 1)$ $\cdot (u^{58} - 4u^{57} + \dots + 5u + 1)$
$c_5, c_{11}$	$u^9(u^2 - 3u + 1)(u^2 + 3u + 1)(u^{14} - 7u^{13} + \dots - 24u + 8)$ $\cdot (u^{29} + 2u^{28} + \dots - 28u - 8)^2$
$c_6, c_{12}$	$u^2(u^2 - u - 1)(u^3 + u^2 + 2u + 1)^3(u^{14} - u^{13} + \dots - 4u - 1)$ $\cdot (u^{58} - 4u^{57} + \dots + 32u - 4)$

### VIII. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1, c_7$	$((y - 1)^2)(y^2 - 7y + 1)(y^3 + 3y^2 + 2y - 1)^3(y^{14} - 5y^{13} + \dots - 208y + 1)$ $\cdot (y^{58} - 8y^{57} + \dots + 195y + 1)$
$c_2, c_4, c_8$ $c_{10}$	$((y - 1)^2)(y^2 - 3y + 1)(y^3 - y^2 + 2y - 1)^3(y^{14} - 9y^{13} + \dots - 16y + 1)$ $\cdot (y^{58} - 32y^{57} + \dots - 25y + 1)$
$c_3, c_6, c_9$ $c_{12}$	$y^2(y^2 - 3y + 1)(y^3 + 3y^2 + 2y - 1)^3(y^{14} + 3y^{13} + \dots - 8y + 1)$ $\cdot (y^{58} + 18y^{57} + \dots - 984y + 16)$
$c_5, c_{11}$	$y^9(y^2 - 7y + 1)^2(y^{14} - 7y^{13} + \dots + 384y + 64)$ $\cdot (y^{29} - 28y^{28} + \dots + 2896y - 64)^2$