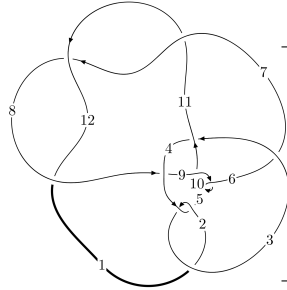
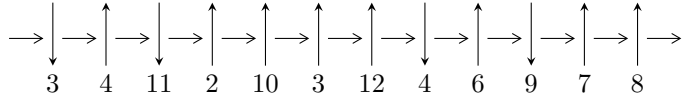


12n<sub>0144</sub> (K12n<sub>0144</sub>)



A knot diagram<sup>1</sup>

**Linearized knot diagram**



**Solving Sequence**

$$7, 11 \xrightarrow{c_{11}} 12 \xrightarrow{c_7} 4, 8 \xrightarrow{c_8} 9 \xrightarrow{c_{12}} 1 \xrightarrow{c_3} 3 \xrightarrow{c_2} 2 \xrightarrow{c_4} 5 \xrightarrow{c_6} 6 \xrightarrow{c_{10}} 10 \rightsquigarrow c_1, c_5, c_9$$

**Ideals for irreducible components<sup>2</sup> of  $X_{\text{par}}$**

$$I_1^u = \langle 7.34372 \times 10^{20} u^{43} + 1.60104 \times 10^{21} u^{42} + \dots + 6.28525 \times 10^{21} b + 5.02483 \times 10^{21}, \\ 1.42649 \times 10^{20} u^{43} + 6.11830 \times 10^{20} u^{42} + \dots + 3.14262 \times 10^{21} a - 1.33924 \times 10^{20}, u^{44} + 4u^{43} + \dots + 32u + \dots \rangle$$

$$I_2^u = \langle 4b + 2a - u + 2, 2a^2 - 2au + 7, u^2 - 2 \rangle$$

$$I_3^u = \langle au + 7b + 4a + u + 4, 2a^2 + au - 3u + 7, u^2 - 2 \rangle$$

$$I_4^u = \langle 3a^4 - 4a^3 + 24a^2 + 2b - 25a + 8, a^5 - 2a^4 + 9a^3 - 14a^2 + 9a - 2, u - 1 \rangle$$

$$I_1^v = \langle a, b - v - 1, v^2 + v + 1 \rangle$$

$$I_2^v = \langle a, b^2 - b + 1, v - 1 \rangle$$

\* 6 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 61 representations.

<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\mathbf{I. } I_1^u = \langle 7.34 \times 10^{20} u^{43} + 1.60 \times 10^{21} u^{42} + \dots + 6.29 \times 10^{21} b + 5.02 \times 10^{21}, 1.43 \times 10^{20} u^{43} + 6.12 \times 10^{20} u^{42} + \dots + 3.14 \times 10^{21} a - 1.34 \times 10^{20}, u^{44} + 4u^{43} + \dots + 32u + 16 \rangle$$

(i) Arc colorings

$$\begin{aligned} a_7 &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_{11} &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_{12} &= \begin{pmatrix} 1 \\ -u^2 \end{pmatrix} \\ a_4 &= \begin{pmatrix} -0.0453917u^{43} - 0.194688u^{42} + \dots - 0.0781355u + 0.0426155 \\ -0.116841u^{43} - 0.254730u^{42} + \dots - 2.09430u - 0.799464 \end{pmatrix} \\ a_8 &= \begin{pmatrix} u \\ -u^3 + u \end{pmatrix} \\ a_9 &= \begin{pmatrix} 0.191388u^{43} + 0.550760u^{42} + \dots + 3.38008u + 3.58656 \\ -0.0541941u^{43} - 0.188082u^{42} + \dots - 0.273250u - 1.13238 \end{pmatrix} \\ a_1 &= \begin{pmatrix} -u^2 + 1 \\ u^4 - 2u^2 \end{pmatrix} \\ a_3 &= \begin{pmatrix} -0.162232u^{43} - 0.449417u^{42} + \dots - 2.17243u - 0.756849 \\ -0.116841u^{43} - 0.254730u^{42} + \dots - 2.09430u - 0.799464 \end{pmatrix} \\ a_2 &= \begin{pmatrix} -0.459894u^{43} - 1.20645u^{42} + \dots - 7.93846u - 3.69776 \\ 0.319896u^{43} + 0.993797u^{42} + \dots + 4.40818u + 5.01424 \end{pmatrix} \\ a_5 &= \begin{pmatrix} 0.873473u^{43} + 2.49705u^{42} + \dots + 13.0049u + 12.6274 \\ u^4 - 2u^2 \end{pmatrix} \\ a_6 &= \begin{pmatrix} -0.776380u^{43} - 2.07570u^{42} + \dots - 12.3449u - 8.51440 \\ 0.297158u^{43} + 0.926397u^{42} + \dots + 6.35873u + 4.85216 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} -0.335109u^{43} - 1.04952u^{42} + \dots - 6.89963u - 4.51774 \\ -0.185846u^{43} - 0.499407u^{42} + \dots - 2.65438u - 1.59651 \end{pmatrix} \end{aligned}$$

(ii) Obstruction class = -1

$$\mathbf{(iii) Cusp Shapes} = \frac{1752784223058518261005}{785655665183033765648} u^{43} + \frac{2500993104539143938499}{392827832591516882824} u^{42} + \dots + \frac{1124081559828742593975}{49103479073939610353} u + \frac{1641699334520185355340}{49103479073939610353}$$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1$	$u^{44} + 51u^{43} + \dots - 38168u + 2401$
$c_2, c_4$	$u^{44} - 11u^{43} + \dots - 796u + 49$
$c_3$	$u^{44} + 3u^{43} + \dots - 4u + 7$
$c_5, c_9$	$u^{44} - 3u^{43} + \dots - 14u + 7$
$c_6$	$u^{44} + 2u^{43} + \dots - 7517u + 13159$
$c_7, c_{11}, c_{12}$	$u^{44} + 4u^{43} + \dots + 32u + 16$
$c_8$	$u^{44} - 2u^{43} + \dots - 23256067u + 7050439$
$c_{10}$	$u^{44} + 27u^{43} + \dots + 476u + 49$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1$	$y^{44} - 109y^{43} + \dots - 778696200y + 5764801$
$c_2, c_4$	$y^{44} + 51y^{43} + \dots - 38168y + 2401$
$c_3$	$y^{44} + 11y^{43} + \dots + 796y + 49$
$c_5, c_9$	$y^{44} + 27y^{43} + \dots + 476y + 49$
$c_6$	$y^{44} + 26y^{43} + \dots + 5158564319y + 173159281$
$c_7, c_{11}, c_{12}$	$y^{44} - 36y^{43} + \dots + 1024y + 256$
$c_8$	$y^{44} - 50y^{43} + \dots - 570620658530165y + 49708690092721$
$c_{10}$	$y^{44} - 13y^{43} + \dots + 67816y + 2401$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.053172 + 0.977197I$ $a = -0.726530 - 0.386151I$ $b = -0.881310 + 0.926174I$	$-7.21788 + 3.26048I$	$2.64523 - 2.48280I$
$u = 0.053172 - 0.977197I$ $a = -0.726530 + 0.386151I$ $b = -0.881310 - 0.926174I$	$-7.21788 - 3.26048I$	$2.64523 + 2.48280I$
$u = -0.969991 + 0.414842I$ $a = 0.607490 + 0.368276I$ $b = -0.799478 + 0.075673I$	$-1.73925 - 3.53680I$	$0.98095 + 4.14861I$
$u = -0.969991 - 0.414842I$ $a = 0.607490 - 0.368276I$ $b = -0.799478 - 0.075673I$	$-1.73925 + 3.53680I$	$0.98095 - 4.14861I$
$u = -0.174827 + 1.043030I$ $a = -0.718830 + 0.754972I$ $b = -0.888329 - 1.005910I$	$-11.08430 - 8.59782I$	$0.28005 + 5.55448I$
$u = -0.174827 - 1.043030I$ $a = -0.718830 - 0.754972I$ $b = -0.888329 + 1.005910I$	$-11.08430 + 8.59782I$	$0.28005 - 5.55448I$
$u = 0.074358 + 1.061190I$ $a = -0.353302 + 0.278439I$ $b = -0.957730 - 0.874395I$	$-11.51210 + 1.82027I$	$-0.464174 - 0.761806I$
$u = 0.074358 - 1.061190I$ $a = -0.353302 - 0.278439I$ $b = -0.957730 + 0.874395I$	$-11.51210 - 1.82027I$	$-0.464174 + 0.761806I$
$u = -1.060920 + 0.195318I$ $a = 0.943353 - 0.723894I$ $b = 0.729269 + 0.856189I$	$1.66107 - 5.45145I$	$5.86619 + 6.59616I$
$u = -1.060920 - 0.195318I$ $a = 0.943353 + 0.723894I$ $b = 0.729269 - 0.856189I$	$1.66107 + 5.45145I$	$5.86619 - 6.59616I$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.396864 + 0.675816I$		
$a = 0.320038 - 0.485056I$	$-3.41945 - 0.63164I$	$-2.08485 + 2.40121I$
$b = 0.767519 + 0.420310I$		
$u = -0.396864 - 0.675816I$		
$a = 0.320038 + 0.485056I$	$-3.41945 + 0.63164I$	$-2.08485 - 2.40121I$
$b = 0.767519 - 0.420310I$		
$u = 1.209100 + 0.327502I$		
$a = -0.52561 - 2.57152I$	$1.94616 + 7.53567I$	$4.00000 - 7.30881I$
$b = -0.313533 + 1.159410I$		
$u = 1.209100 - 0.327502I$		
$a = -0.52561 + 2.57152I$	$1.94616 - 7.53567I$	$4.00000 + 7.30881I$
$b = -0.313533 - 1.159410I$		
$u = -1.244840 + 0.163819I$		
$a = -0.40678 + 2.39610I$	$4.81580 - 3.31538I$	$11.03880 + 4.12292I$
$b = -0.306940 - 1.055000I$		
$u = -1.244840 - 0.163819I$		
$a = -0.40678 - 2.39610I$	$4.81580 + 3.31538I$	$11.03880 - 4.12292I$
$b = -0.306940 + 1.055000I$		
$u = -1.193050 + 0.633879I$		
$a = -0.488351 + 0.504147I$	$-7.99420 + 2.74053I$	0
$b = 0.926853 - 0.905761I$		
$u = -1.193050 - 0.633879I$		
$a = -0.488351 - 0.504147I$	$-7.99420 - 2.74053I$	0
$b = 0.926853 + 0.905761I$		
$u = 1.277500 + 0.501120I$		
$a = -0.535158 - 0.270801I$	$-3.43084 + 1.99299I$	0
$b = 0.908252 + 0.813085I$		
$u = 1.277500 - 0.501120I$		
$a = -0.535158 + 0.270801I$	$-3.43084 - 1.99299I$	0
$b = 0.908252 - 0.813085I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.155102 + 0.599275I$ $a = 0.352478 - 1.113320I$ $b = 0.478851 + 1.053130I$	$-1.29319 - 4.02132I$	$-0.30638 + 3.65044I$
$u = 0.155102 - 0.599275I$ $a = 0.352478 + 1.113320I$ $b = 0.478851 - 1.053130I$	$-1.29319 + 4.02132I$	$-0.30638 - 3.65044I$
$u = -1.405870 + 0.102387I$ $a = -0.89393 + 1.77081I$ $b = -0.149374 - 0.798948I$	$6.37799 - 2.69804I$	0
$u = -1.405870 - 0.102387I$ $a = -0.89393 - 1.77081I$ $b = -0.149374 + 0.798948I$	$6.37799 + 2.69804I$	0
$u = 1.286440 + 0.585860I$ $a = 0.43019 + 1.54824I$ $b = 0.898558 - 0.969867I$	$-7.79148 + 3.97595I$	0
$u = 1.286440 - 0.585860I$ $a = 0.43019 - 1.54824I$ $b = 0.898558 + 0.969867I$	$-7.79148 - 3.97595I$	0
$u = 1.41894 + 0.07907I$ $a = -1.13538 - 1.16362I$ $b = -0.065725 + 0.584352I$	$5.49142 - 1.80694I$	0
$u = 1.41894 - 0.07907I$ $a = -1.13538 + 1.16362I$ $b = -0.065725 - 0.584352I$	$5.49142 + 1.80694I$	0
$u = -1.35375 + 0.46551I$ $a = 0.66647 - 1.74497I$ $b = 0.826223 + 1.007890I$	$-2.81404 - 8.41153I$	0
$u = -1.35375 - 0.46551I$ $a = 0.66647 + 1.74497I$ $b = 0.826223 - 1.007890I$	$-2.81404 + 8.41153I$	0

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.44498 + 0.10365I$ $a = 0.25589 - 1.83310I$ $b = -0.582379 + 0.972015I$	$4.02565 + 1.74679I$	0
$u = -1.44498 - 0.10365I$ $a = 0.25589 + 1.83310I$ $b = -0.582379 - 0.972015I$	$4.02565 - 1.74679I$	0
$u = -1.38764 + 0.51587I$ $a = -0.717568 + 0.258839I$ $b = 0.967178 - 0.764646I$	$-6.94944 - 7.42595I$	0
$u = -1.38764 - 0.51587I$ $a = -0.717568 - 0.258839I$ $b = 0.967178 + 0.764646I$	$-6.94944 + 7.42595I$	0
$u = -0.353533 + 0.362697I$ $a = 1.81787 + 0.90961I$ $b = -0.443035 + 0.586833I$	$-0.20174 + 3.16277I$	$3.03176 + 0.27471I$
$u = -0.353533 - 0.362697I$ $a = 1.81787 - 0.90961I$ $b = -0.443035 - 0.586833I$	$-0.20174 - 3.16277I$	$3.03176 - 0.27471I$
$u = 0.344360 + 0.354929I$ $a = 1.54824 + 0.67408I$ $b = -0.072149 - 0.658876I$	$0.836056 + 1.038800I$	$7.69659 - 5.53666I$
$u = 0.344360 - 0.354929I$ $a = 1.54824 - 0.67408I$ $b = -0.072149 + 0.658876I$	$0.836056 - 1.038800I$	$7.69659 + 5.53666I$
$u = 1.43633 + 0.46857I$ $a = 0.58445 + 1.94710I$ $b = 0.824013 - 1.059570I$	$-6.0040 + 14.0033I$	0
$u = 1.43633 - 0.46857I$ $a = 0.58445 - 1.94710I$ $b = 0.824013 + 1.059570I$	$-6.0040 - 14.0033I$	0



Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.50906 + 0.09274I$ $a = 0.209822 - 1.305860I$ $b = -0.677586 + 0.683171I$	$3.07707 + 3.14518I$	0
$u = 1.50906 - 0.09274I$ $a = 0.209822 + 1.305860I$ $b = -0.677586 - 0.683171I$	$3.07707 - 3.14518I$	0
$u = 0.221879 + 0.395714I$ $a = 0.765153 + 0.917828I$ $b = 0.310852 - 0.803316I$	$0.452406 + 1.318670I$	$4.68386 - 5.79682I$
$u = 0.221879 - 0.395714I$ $a = 0.765153 - 0.917828I$ $b = 0.310852 + 0.803316I$	$0.452406 - 1.318670I$	$4.68386 + 5.79682I$

$$\text{II. } I_2^u = \langle 4b + 2a - u + 2, 2a^2 - 2au + 7, u^2 - 2 \rangle$$

(i) Arc colorings

$$a_7 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 1 \\ -2 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} a \\ -\frac{1}{2}a + \frac{1}{4}u - \frac{1}{2} \end{pmatrix}$$

$$a_8 = \begin{pmatrix} u \\ -u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -\frac{1}{2}au + \frac{3}{2}a - \frac{3}{4}u \\ -\frac{1}{2}a + \frac{1}{4}u - \frac{1}{2} \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} \frac{1}{2}a + \frac{1}{4}u - \frac{1}{2} \\ -\frac{1}{2}a + \frac{1}{4}u - \frac{1}{2} \end{pmatrix}$$

$$a_2 = \begin{pmatrix} \frac{1}{4}au + \frac{1}{4}u - \frac{9}{4} \\ -\frac{1}{2}a + \frac{1}{4}u + \frac{1}{2} \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} \frac{1}{2}au - a + \frac{1}{2}u + \frac{1}{2} \\ \frac{1}{2}a - \frac{1}{4}u + \frac{1}{2} \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -\frac{1}{4}au + \frac{1}{2}a + \frac{1}{2}u - \frac{5}{4} \\ -\frac{1}{2}a + \frac{1}{4}u + \frac{1}{2} \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes =  $4a - 2u + 8$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_3, c_4$ $c_5$	$(u^2 - u + 1)^2$
$c_2, c_9, c_{10}$	$(u^2 + u + 1)^2$
$c_6$	$u^4 + 4u^3 + 8u^2 + 8u + 7$
$c_7, c_{11}, c_{12}$	$(u^2 - 2)^2$
$c_8$	$u^4 - 4u^3 + 8u^2 - 8u + 7$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_3$ $c_4, c_5, c_9$ $c_{10}$	$(y^2 + y + 1)^2$
$c_6, c_8$	$y^4 + 14y^2 + 48y + 49$
$c_7, c_{11}, c_{12}$	$(y - 2)^4$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.41421$ $a = 0.70711 + 1.73205I$ $b = -0.500000 - 0.866025I$	$4.93480 - 4.05977I$	$8.00000 + 6.92820I$
$u = 1.41421$ $a = 0.70711 - 1.73205I$ $b = -0.500000 + 0.866025I$	$4.93480 + 4.05977I$	$8.00000 - 6.92820I$
$u = -1.41421$ $a = -0.70711 + 1.73205I$ $b = -0.500000 - 0.866025I$	$4.93480 - 4.05977I$	$8.00000 + 6.92820I$
$u = -1.41421$ $a = -0.70711 - 1.73205I$ $b = -0.500000 + 0.866025I$	$4.93480 + 4.05977I$	$8.00000 - 6.92820I$

$$\text{III. } I_3^u = \langle au + 7b + 4a + u + 4, 2a^2 + au - 3u + 7, u^2 - 2 \rangle$$

(i) Arc colorings

$$a_7 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 1 \\ -2 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} a \\ -\frac{1}{7}au - \frac{4}{7}a - \frac{1}{7}u - \frac{4}{7} \end{pmatrix}$$

$$a_8 = \begin{pmatrix} u \\ -u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -\frac{3}{7}au - \frac{5}{7}a - \frac{13}{14}u + \frac{16}{7} \\ \frac{1}{7}au + \frac{4}{7}a + \frac{1}{7}u - \frac{3}{7} \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -\frac{1}{7}au + \frac{3}{7}a - \frac{1}{7}u - \frac{4}{7} \\ -\frac{1}{7}au - \frac{4}{7}a - \frac{1}{7}u - \frac{4}{7} \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -\frac{2}{7}au - \frac{1}{7}a + \frac{3}{14}u - \frac{15}{7} \\ -\frac{1}{7}au - \frac{4}{7}a - \frac{1}{7}u + \frac{3}{7} \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} \frac{2}{7}au + \frac{1}{7}a + \frac{11}{14}u - \frac{13}{7} \\ -\frac{1}{7}au - \frac{4}{7}a - \frac{1}{7}u + \frac{3}{7} \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -\frac{1}{7}au - \frac{11}{7}a - \frac{8}{7}u + \frac{10}{7} \\ \frac{1}{7}au + \frac{4}{7}a + \frac{1}{7}u + \frac{4}{7} \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = 8

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_3, c_4$ $c_5$	$(u^2 - u + 1)^2$
$c_2, c_9, c_{10}$	$(u^2 + u + 1)^2$
$c_6$	$u^4 - 2u^3 + 5u^2 - 10u + 7$
$c_7, c_{11}, c_{12}$	$(u^2 - 2)^2$
$c_8$	$u^4 + 2u^3 + 5u^2 + 10u + 7$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_3$ $c_4, c_5, c_9$ $c_{10}$	$(y^2 + y + 1)^2$
$c_6, c_8$	$y^4 + 6y^3 - y^2 - 30y + 49$
$c_7, c_{11}, c_{12}$	$(y - 2)^4$



(vi) Complex Volumes and Cusp Shapes

Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.41421$ $a = -0.353553 + 1.119680I$ $b = -0.500000 - 0.866025I$	4.93480	8.00000
$u = 1.41421$ $a = -0.353553 - 1.119680I$ $b = -0.500000 + 0.866025I$	4.93480	8.00000
$u = -1.41421$ $a = 0.35355 + 2.34442I$ $b = -0.500000 - 0.866025I$	4.93480	8.00000
$u = -1.41421$ $a = 0.35355 - 2.34442I$ $b = -0.500000 + 0.866025I$	4.93480	8.00000

IV.

$$I_4^u = \langle 3a^4 - 4a^3 + 24a^2 + 2b - 25a + 8, a^5 - 2a^4 + 9a^3 - 14a^2 + 9a - 2, u - 1 \rangle$$

(i) Arc colorings

$$a_7 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} a \\ -\frac{3}{2}a^4 + 2a^3 - 12a^2 + \frac{25}{2}a - 4 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -a^4 + \frac{3}{2}a^3 - \frac{17}{2}a^2 + \frac{19}{2}a - 2 \\ -\frac{1}{2}a^3 + \frac{1}{2}a^2 - \frac{7}{2}a + 2 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -\frac{3}{2}a^4 + 2a^3 - 12a^2 + \frac{27}{2}a - 4 \\ -\frac{3}{2}a^4 + 2a^3 - 12a^2 + \frac{25}{2}a - 4 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -2a^4 + \frac{5}{2}a^3 - \frac{31}{2}a^2 + \frac{31}{2}a - 4 \\ -a^4 + a^3 - 8a^2 + 6a - 2 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} a^4 - 2a^3 + 8a^2 - 13a + 5 \\ -1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 2a^4 - \frac{5}{2}a^3 + \frac{31}{2}a^2 - \frac{31}{2}a + 4 \\ a^4 - a^3 + 8a^2 - 6a + 2 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} a^3 - a^2 + 6a - 2 \\ -\frac{3}{2}a^4 + 2a^3 - 12a^2 + \frac{27}{2}a - 4 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes = 6

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1$	$u^5 + 2u^4 + 3u^3 + 6u^2 + 5u - 1$
$c_2, c_4$	$u^5 - 2u^4 + 3u^3 - 2u^2 + u + 1$
$c_3, c_5, c_8$ $c_9$	$u^5 + u^3 + u - 1$
$c_6$	$u^5 - 2u^4 + 3u^3 - 6u^2 + 5u + 1$
$c_7, c_{11}, c_{12}$	$(u - 1)^5$
$c_{10}$	$u^5 + 2u^4 + 3u^3 + 2u^2 + u - 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_6$	$y^5 + 2y^4 - 5y^3 - 2y^2 + 37y - 1$
$c_2, c_4, c_{10}$	$y^5 + 2y^4 + 3y^3 + 6y^2 + 5y - 1$
$c_3, c_5, c_8$ $c_9$	$y^5 + 2y^4 + 3y^3 + 2y^2 + y - 1$
$c_7, c_{11}, c_{12}$	$(y - 1)^5$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_4^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.00000$ $a = 0.669275 + 0.346167I$ $b = 0.707729 - 0.841955I$	1.64493	6.00000
$u = 1.00000$ $a = 0.669275 - 0.346167I$ $b = 0.707729 + 0.841955I$	1.64493	6.00000
$u = 1.00000$ $a = 0.472355$ $b = -0.636883$	1.64493	6.00000
$u = 1.00000$ $a = 0.09455 + 2.72921I$ $b = -0.389287 - 1.070680I$	1.64493	6.00000
$u = 1.00000$ $a = 0.09455 - 2.72921I$ $b = -0.389287 + 1.070680I$	1.64493	6.00000

$$\mathbf{V. } I_1^v = \langle a, b - v - 1, v^2 + v + 1 \rangle$$

**(i) Arc colorings**

$$a_7 = \begin{pmatrix} v \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 0 \\ v + 1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} v \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} v \\ -v - 1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} v + 1 \\ v + 1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} v + 1 \\ v \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -1 \\ -v - 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0 \\ -v \end{pmatrix}$$

**(ii) Obstruction class = 1**

**(iii) Cusp Shapes =  $8v + 10$**

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_4, c_9$	$u^2 - u + 1$
$c_2, c_3, c_5$ $c_{10}$	$u^2 + u + 1$
$c_6, c_8$	$(u + 1)^2$
$c_7, c_{11}, c_{12}$	$u^2$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_3$ $c_4, c_5, c_9$ $c_{10}$	$y^2 + y + 1$
$c_6, c_8$	$(y - 1)^2$
$c_7, c_{11}, c_{12}$	$y^2$



(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^v$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$v = -0.500000 + 0.866025I$ $a = 0$ $b = 0.500000 + 0.866025I$	$-4.05977I$	$6.00000 + 6.92820I$
$v = -0.500000 - 0.866025I$ $a = 0$ $b = 0.500000 - 0.866025I$	$4.05977I$	$6.00000 - 6.92820I$

$$\text{VI. } I_2^v = \langle a, b^2 - b + 1, v - 1 \rangle$$

(i) Arc colorings

$$a_7 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 0 \\ b \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ b - 1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} b \\ b \end{pmatrix}$$

$$a_2 = \begin{pmatrix} b \\ b - 1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} b \\ b - 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -b + 2 \\ b \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = 0

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_4, c_6$ $c_8, c_9$	$u^2 - u + 1$
$c_2, c_3, c_5$ $c_{10}$	$u^2 + u + 1$
$c_7, c_{11}, c_{12}$	$u^2$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_3$ $c_4, c_5, c_6$ $c_8, c_9, c_{10}$	$y^2 + y + 1$
$c_7, c_{11}, c_{12}$	$y^2$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_2^v$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$v = 1.00000$		
$a = 0$	0	0
$b = 0.500000 + 0.866025I$		
$v = 1.00000$		
$a = 0$	0	0
$b = 0.500000 - 0.866025I$		

## VII. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1$	$(u^2 - u + 1)^6(u^5 + 2u^4 + 3u^3 + 6u^2 + 5u - 1)$ $\cdot (u^{44} + 51u^{43} + \dots - 38168u + 2401)$
$c_2$	$(u^2 + u + 1)^6(u^5 - 2u^4 + 3u^3 - 2u^2 + u + 1)$ $\cdot (u^{44} - 11u^{43} + \dots - 796u + 49)$
$c_3$	$((u^2 - u + 1)^4)(u^2 + u + 1)^2(u^5 + u^3 + u - 1)(u^{44} + 3u^{43} + \dots - 4u + 7)$
$c_4$	$(u^2 - u + 1)^6(u^5 - 2u^4 + 3u^3 - 2u^2 + u + 1)$ $\cdot (u^{44} - 11u^{43} + \dots - 796u + 49)$
$c_5$	$((u^2 - u + 1)^4)(u^2 + u + 1)^2(u^5 + u^3 + u - 1)(u^{44} - 3u^{43} + \dots - 14u + 7)$
$c_6$	$((u + 1)^2)(u^2 - u + 1)(u^4 - 2u^3 + \dots - 10u + 7)(u^4 + 4u^3 + \dots + 8u + 7)$ $\cdot (u^5 - 2u^4 + 3u^3 - 6u^2 + 5u + 1)(u^{44} + 2u^{43} + \dots - 7517u + 13159)$
$c_7, c_{11}, c_{12}$	$u^4(u - 1)^5(u^2 - 2)^4(u^{44} + 4u^{43} + \dots + 32u + 16)$
$c_8$	$((u + 1)^2)(u^2 - u + 1)(u^4 - 4u^3 + \dots - 8u + 7)(u^4 + 2u^3 + \dots + 10u + 7)$ $\cdot (u^5 + u^3 + u - 1)(u^{44} - 2u^{43} + \dots - 2.32561 \times 10^7 u + 7050439)$
$c_9$	$((u^2 - u + 1)^2)(u^2 + u + 1)^4(u^5 + u^3 + u - 1)(u^{44} - 3u^{43} + \dots - 14u + 7)$
$c_{10}$	$(u^2 + u + 1)^6(u^5 + 2u^4 + 3u^3 + 2u^2 + u - 1)$ $\cdot (u^{44} + 27u^{43} + \dots + 476u + 49)$

### VIII. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1$	$(y^2 + y + 1)^6(y^5 + 2y^4 - 5y^3 - 2y^2 + 37y - 1)$ $\cdot (y^{44} - 109y^{43} + \dots - 778696200y + 5764801)$
$c_2, c_4$	$(y^2 + y + 1)^6(y^5 + 2y^4 + 3y^3 + 6y^2 + 5y - 1)$ $\cdot (y^{44} + 51y^{43} + \dots - 38168y + 2401)$
$c_3$	$(y^2 + y + 1)^6(y^5 + 2y^4 + 3y^3 + 2y^2 + y - 1)$ $\cdot (y^{44} + 11y^{43} + \dots + 796y + 49)$
$c_5, c_9$	$(y^2 + y + 1)^6(y^5 + 2y^4 + 3y^3 + 2y^2 + y - 1)$ $\cdot (y^{44} + 27y^{43} + \dots + 476y + 49)$
$c_6$	$((y - 1)^2)(y^2 + y + 1)(y^4 + 14y^2 + 48y + 49)(y^4 + 6y^3 + \dots - 30y + 49)$ $\cdot (y^5 + 2y^4 - 5y^3 - 2y^2 + 37y - 1)$ $\cdot (y^{44} + 26y^{43} + \dots + 5158564319y + 173159281)$
$c_7, c_{11}, c_{12}$	$y^4(y - 2)^8(y - 1)^5(y^{44} - 36y^{43} + \dots + 1024y + 256)$
$c_8$	$((y - 1)^2)(y^2 + y + 1)(y^4 + 14y^2 + 48y + 49)(y^4 + 6y^3 + \dots - 30y + 49)$ $\cdot (y^5 + 2y^4 + 3y^3 + 2y^2 + y - 1)$ $\cdot (y^{44} - 50y^{43} + \dots - 570620658530165y + 49708690092721)$
$c_{10}$	$(y^2 + y + 1)^6(y^5 + 2y^4 + 3y^3 + 6y^2 + 5y - 1)$ $\cdot (y^{44} - 13y^{43} + \dots + 67816y + 2401)$