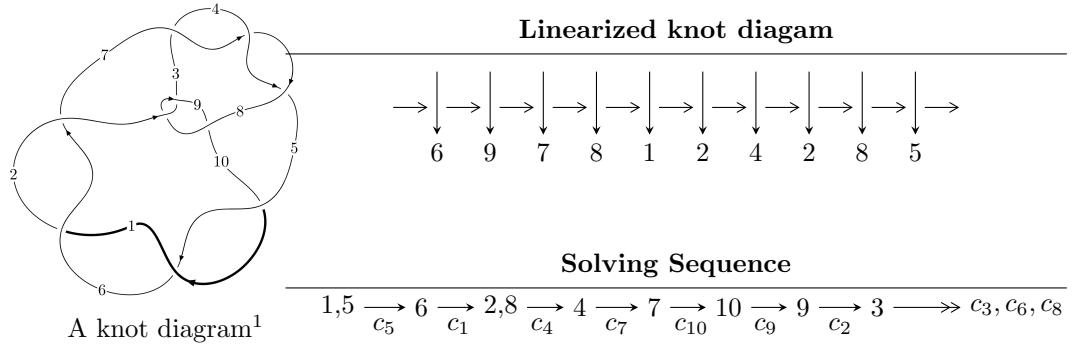


10₁₃₉ ($K10n_{27}$)



Ideals for irreducible components² of X_{par}

$$I_1^u = \langle -u^3 - 3u^2 + b - 2u + 1, -u^3 - 2u^2 + 2a - 2u, u^4 + 4u^3 + 6u^2 + 2u - 2 \rangle$$

$$I_2^u = \langle b + 1, 2a - u + 2, u^2 - 2 \rangle$$

$$I_1^v = \langle a, b - 1, v + 1 \rangle$$

* 3 irreducible components of $\dim_{\mathbb{C}} = 0$, with total 7 representations.

¹The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/math/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

²All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$I_1^u = \langle -u^3 - 3u^2 + b - 2u + 1, \ -u^3 - 2u^2 + 2a - 2u, \ u^4 + 4u^3 + 6u^2 + 2u - 2 \rangle$$

(i) **Arc colorings**

$$a_1 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -u \\ -u^3 + u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} \frac{1}{2}u^3 + u^2 + u \\ u^3 + 3u^2 + 2u - 1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -\frac{1}{2}u^3 - u^2 + 1 \\ -2u^2 - 2u + 1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -u^2 + 1 \\ 4u^3 + 8u^2 + 2u - 2 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} u \\ u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} \frac{3}{2}u^3 + 5u^2 + 4u - 2 \\ -3u^3 - 5u^2 + u + 1 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} \frac{3}{2}u^3 + u^2 - 2u \\ 8u^3 + 28u^2 + 16u - 11 \end{pmatrix}$$

(ii) **Obstruction class** = -1

(iii) **Cusp Shapes** = $-2u - 16$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1, c_5, c_6 c_{10}	$u^4 - 4u^3 + 6u^2 - 2u - 2$
c_2, c_3, c_4 c_7, c_8	$u^4 + 2u^3 + 4u^2 - 2u - 1$
c_9	$u^4 - 4u^3 + 22u^2 + 12u + 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1, c_5, c_6 c_{10}	$y^4 - 4y^3 + 16y^2 - 28y + 4$
c_2, c_3, c_4 c_7, c_8	$y^4 + 4y^3 + 22y^2 - 12y + 1$
c_9	$y^4 + 28y^3 + 582y^2 - 100y + 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.47463$		
$a = -0.903408$	-6.80412	-13.0510
$b = -0.632293$		
$u = 0.395337$		
$a = 0.582522$	-0.588647	-16.7910
$b = 0.321336$		
$u = -1.46036 + 1.13932I$		
$a = 0.660443 + 0.716885I$	$4.51885 + 4.85117I$	$-13.07929 - 2.27864I$
$b = 1.15548 - 1.89385I$		
$u = -1.46036 - 1.13932I$		
$a = 0.660443 - 0.716885I$	$4.51885 - 4.85117I$	$-13.07929 + 2.27864I$
$b = 1.15548 + 1.89385I$		

$$\text{II. } I_2^u = \langle b+1, 2a-u+2, u^2-2 \rangle$$

(i) **Arc colorings**

$$\begin{aligned} a_1 &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_5 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_6 &= \begin{pmatrix} 1 \\ 2 \end{pmatrix} \\ a_2 &= \begin{pmatrix} -u \\ -u \end{pmatrix} \\ a_8 &= \begin{pmatrix} \frac{1}{2}u-1 \\ -1 \end{pmatrix} \\ a_4 &= \begin{pmatrix} \frac{1}{2}u \\ -1 \end{pmatrix} \\ a_7 &= \begin{pmatrix} -1 \\ 0 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} u \\ u \end{pmatrix} \\ a_9 &= \begin{pmatrix} \frac{3}{2}u-1 \\ u-1 \end{pmatrix} \\ a_3 &= \begin{pmatrix} \frac{1}{2}u-1 \\ -1 \end{pmatrix} \end{aligned}$$

(ii) **Obstruction class** = 1

(iii) **Cusp Shapes** = -20

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1, c_5, c_6 c_{10}	$u^2 - 2$
c_2, c_7	$(u - 1)^2$
c_3, c_4, c_8 c_9	$(u + 1)^2$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1, c_5, c_6 c_{10}	$(y - 2)^2$
c_2, c_3, c_4 c_7, c_8, c_9	$(y - 1)^2$

(vi) Complex Volumes and Cusp Shapes

Solutions to I_2^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.41421$		
$a = -0.292893$	-8.22467	-20.0000
$b = -1.00000$		
$u = -1.41421$		
$a = -1.70711$	-8.22467	-20.0000
$b = -1.00000$		

$$\text{III. } I_1^v = \langle a, b - 1, v + 1 \rangle$$

(i) Arc colorings

$$a_1 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -1 \\ 1 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = -12

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1, c_5, c_6 c_{10}	u
c_2, c_7, c_9	$u + 1$
c_3, c_4, c_8	$u - 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1, c_5, c_6 c_{10}	y
c_2, c_3, c_4 c_7, c_8, c_9	$y - 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to I_1^v	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$v = -1.00000$		
$a = 0$	-3.28987	-12.0000
$b = 1.00000$		

IV. u-Polynomials

Crossings	u-Polynomials at each crossing
c_1, c_5, c_6 c_{10}	$u(u^2 - 2)(u^4 - 4u^3 + 6u^2 - 2u - 2)$
c_2, c_7	$(u - 1)^2(u + 1)(u^4 + 2u^3 + 4u^2 - 2u - 1)$
c_3, c_4, c_8	$(u - 1)(u + 1)^2(u^4 + 2u^3 + 4u^2 - 2u - 1)$
c_9	$(u + 1)^3(u^4 - 4u^3 + 22u^2 + 12u + 1)$

V. Riley Polynomials

Crossings	Riley Polynomials at each crossing
c_1, c_5, c_6 c_{10}	$y(y - 2)^2(y^4 - 4y^3 + 16y^2 - 28y + 4)$
c_2, c_3, c_4 c_7, c_8	$(y - 1)^3(y^4 + 4y^3 + 22y^2 - 12y + 1)$
c_9	$(y - 1)^3(y^4 + 28y^3 + 582y^2 - 100y + 1)$