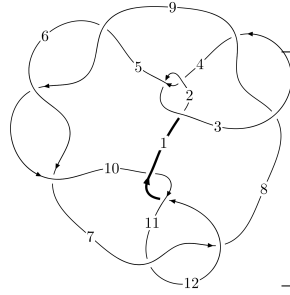
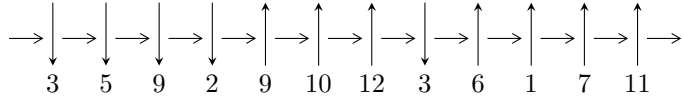


$12n_{0154}$ ($K12n_{0154}$)



A knot diagram¹

Linearized knot diagram



Solving Sequence

$$3,9 \xrightarrow{c_3} 4,5 \xrightarrow{c_5} 6 \xrightarrow{c_9} 10 \xrightarrow{c_6} 7 \xrightarrow{c_2} 2 \xrightarrow{c_1} 1 \xrightarrow{c_{10}} 11 \xrightarrow{c_{12}} 12 \xrightarrow{c_7} 8 \twoheadrightarrow c_4, c_8, c_{11}$$

Ideals for irreducible components² of X_{par}

$$I_1^u = \langle -1.84711 \times 10^{54} u^{30} + 3.00696 \times 10^{54} u^{29} + \dots + 1.54890 \times 10^{57} b + 1.97638 \times 10^{57}, \\ 5.87634 \times 10^{54} u^{30} + 8.97726 \times 10^{53} u^{29} + \dots + 3.09781 \times 10^{57} a - 6.18337 \times 10^{57}, \\ u^{31} + u^{30} + \dots + 128u + 256 \rangle$$

$$I_1^v = \langle a, b - 1, v^8 + v^7 - 3v^6 - 2v^5 + 3v^4 + 2v - 1 \rangle$$

* 2 irreducible components of $\dim_{\mathbb{C}} = 0$, with total 39 representations.

¹The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

²All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\text{I. } I_1^u = \langle -1.85 \times 10^{54} u^{30} + 3.01 \times 10^{54} u^{29} + \dots + 1.55 \times 10^{57} b + 1.98 \times 10^{57}, 5.88 \times 10^{54} u^{30} + 8.98 \times 10^{53} u^{29} + \dots + 3.10 \times 10^{57} a - 6.18 \times 10^{57}, u^{31} + u^{30} + \dots + 128u + 256 \rangle$$

(i) Arc colorings

$$a_3 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -0.00189693u^{30} - 0.000289794u^{29} + \dots - 0.486873u + 1.99605 \\ 0.00119253u^{30} - 0.00194134u^{29} + \dots + 0.0270826u - 1.27599 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -0.00189693u^{30} - 0.000289794u^{29} + \dots - 0.486873u + 1.99605 \\ 0.000355948u^{30} - 0.00258740u^{29} + \dots - 0.252818u - 0.864558 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0.00279729u^{30} + 0.00539863u^{29} + \dots + 3.76148u + 1.30472 \\ -0.00152673u^{30} - 0.000485411u^{29} + \dots + 0.810224u + 0.180328 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -0.00639923u^{30} - 0.00401893u^{29} + \dots - 2.31167u + 3.22615 \\ -0.00140881u^{30} - 0.00446228u^{29} + \dots - 0.919581u - 0.559880 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -0.00189693u^{30} - 0.000289794u^{29} + \dots - 0.486873u + 1.99605 \\ -0.000355948u^{30} + 0.00258740u^{29} + \dots + 0.252818u + 0.864558 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -0.00225288u^{30} + 0.00229761u^{29} + \dots - 0.234054u + 2.86060 \\ -0.000355948u^{30} + 0.00258740u^{29} + \dots + 0.252818u + 0.864558 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0.00450141u^{30} + 0.0104443u^{29} + \dots + 7.25496u + 3.10927 \\ -0.00608885u^{30} - 0.00386215u^{29} + \dots - 1.29049u + 0.110126 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 0.00392845u^{30} + 0.00115127u^{29} + \dots + 3.59324u - 2.25231 \\ -0.00318570u^{30} - 0.00674377u^{29} + \dots - 1.03520u - 2.46750 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -u \\ -u \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes = $-0.0199438u^{30} - 0.0268193u^{29} + \dots - 7.14938u - 3.17635$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1	$u^{31} + u^{30} + \dots + 4u + 1$
c_2, c_4	$u^{31} - 9u^{30} + \dots - 6u + 1$
c_3, c_8	$u^{31} + u^{30} + \dots + 128u + 256$
c_5, c_6, c_9	$u^{31} - 2u^{30} + \dots + 2u + 1$
c_7, c_{11}	$u^{31} + 2u^{30} + \dots + 4u + 1$
c_{10}, c_{12}	$u^{31} - 12u^{30} + \dots + 24u - 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1	$y^{31} + 67y^{30} + \dots + 68y - 1$
c_2, c_4	$y^{31} - y^{30} + \dots + 4y - 1$
c_3, c_8	$y^{31} + 51y^{30} + \dots - 344064y - 65536$
c_5, c_6, c_9	$y^{31} - 44y^{30} + \dots + 24y - 1$
c_7, c_{11}	$y^{31} - 12y^{30} + \dots + 24y - 1$
c_{10}, c_{12}	$y^{31} + 16y^{30} + \dots + 264y - 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.161591 + 1.013030I$	$0.69845 + 2.45290I$	$3.48973 - 2.59889I$
$a = 0.773041 - 1.031550I$		
$b = -0.534786 + 0.620785I$		
$u = 0.161591 - 1.013030I$	$0.69845 - 2.45290I$	$3.48973 + 2.59889I$
$a = 0.773041 + 1.031550I$		
$b = -0.534786 - 0.620785I$		
$u = 0.955263 + 0.163453I$	$-1.29160 + 4.22402I$	$2.31530 - 6.13986I$
$a = 0.518313 + 0.144297I$		
$b = 0.790559 - 0.498487I$		
$u = 0.955263 - 0.163453I$	$-1.29160 - 4.22402I$	$2.31530 + 6.13986I$
$a = 0.518313 - 0.144297I$		
$b = 0.790559 + 0.498487I$		
$u = -0.086594 + 1.090170I$	$1.82403 - 7.93866I$	$5.05436 + 7.63782I$
$a = 0.662258 + 1.136950I$		
$b = -0.617467 - 0.656725I$		
$u = -0.086594 - 1.090170I$	$1.82403 + 7.93866I$	$5.05436 - 7.63782I$
$a = 0.662258 - 1.136950I$		
$b = -0.617467 + 0.656725I$		
$u = 0.595270 + 0.941294I$	$1.82341 + 0.25468I$	$4.36583 - 1.12602I$
$a = 0.653949 - 0.621182I$		
$b = -0.196146 + 0.763577I$		
$u = 0.595270 - 0.941294I$	$1.82341 - 0.25468I$	$4.36583 + 1.12602I$
$a = 0.653949 + 0.621182I$		
$b = -0.196146 - 0.763577I$		
$u = -0.766374 + 0.321934I$	$-1.93326 + 0.39687I$	$-0.195239 - 1.308176I$
$a = 0.504447 - 0.092329I$		
$b = 0.918111 + 0.351073I$		
$u = -0.766374 - 0.321934I$	$-1.93326 - 0.39687I$	$-0.195239 + 1.308176I$
$a = 0.504447 + 0.092329I$		
$b = 0.918111 - 0.351073I$		

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.124749 + 0.751932I$		
$a = 0.452240 - 0.011332I$	$-2.89631 - 2.32872I$	$3.99393 + 2.38138I$
$b = 1.209830 + 0.055374I$		
$u = -0.124749 - 0.751932I$		
$a = 0.452240 + 0.011332I$	$-2.89631 + 2.32872I$	$3.99393 - 2.38138I$
$b = 1.209830 - 0.055374I$		
$u = -0.387754 + 1.234260I$		
$a = 0.525560 + 0.831111I$	$6.58495 - 1.93672I$	$10.00855 + 2.44149I$
$b = -0.456481 - 0.859510I$		
$u = -0.387754 - 1.234260I$		
$a = 0.525560 - 0.831111I$	$6.58495 + 1.93672I$	$10.00855 - 2.44149I$
$b = -0.456481 + 0.859510I$		
$u = 0.582153 + 0.326641I$		
$a = 0.779541 - 0.242345I$	$1.172720 + 0.162363I$	$8.67848 - 0.29545I$
$b = 0.169752 + 0.363655I$		
$u = 0.582153 - 0.326641I$		
$a = 0.779541 + 0.242345I$	$1.172720 - 0.162363I$	$8.67848 + 0.29545I$
$b = 0.169752 - 0.363655I$		
$u = -0.770420 + 1.108010I$		
$a = 0.523737 + 0.599489I$	$3.43738 + 4.60020I$	$6.69378 - 4.27348I$
$b = -0.173508 - 0.946032I$		
$u = -0.770420 - 1.108010I$		
$a = 0.523737 - 0.599489I$	$3.43738 - 4.60020I$	$6.69378 + 4.27348I$
$b = -0.173508 + 0.946032I$		
$u = 0.024622 + 0.570476I$		
$a = 1.59020 - 0.12307I$	$-2.59053 + 2.65595I$	$2.84678 - 3.53648I$
$b = -0.374894 + 0.048377I$		
$u = 0.024622 - 0.570476I$		
$a = 1.59020 + 0.12307I$	$-2.59053 - 2.65595I$	$2.84678 + 3.53648I$
$b = -0.374894 - 0.048377I$		

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.437432$ $a = 0.530400$ $b = 0.885369$	-1.27239	-10.1300
$u = 0.48856 + 2.04930I$ $a = -0.125667 + 0.875225I$ $b = -1.16074 - 1.11948I$	$11.66910 - 6.09696I$	0
$u = 0.48856 - 2.04930I$ $a = -0.125667 - 0.875225I$ $b = -1.16074 + 1.11948I$	$11.66910 + 6.09696I$	0
$u = -0.55039 + 2.06488I$ $a = -0.151530 - 0.868888I$ $b = -1.19479 + 1.11693I$	$13.3519 + 11.7446I$	0
$u = -0.55039 - 2.06488I$ $a = -0.151530 + 0.868888I$ $b = -1.19479 - 1.11693I$	$13.3519 - 11.7446I$	0
$u = 0.31189 + 2.12455I$ $a = -0.059513 + 0.836117I$ $b = -1.08470 - 1.18998I$	$11.95390 - 2.34313I$	0
$u = 0.31189 - 2.12455I$ $a = -0.059513 - 0.836117I$ $b = -1.08470 + 1.18998I$	$11.95390 + 2.34313I$	0
$u = -0.27394 + 2.19556I$ $a = -0.052072 - 0.807634I$ $b = -1.07950 + 1.23306I$	$13.7970 - 3.1675I$	0
$u = -0.27394 - 2.19556I$ $a = -0.052072 + 0.807634I$ $b = -1.07950 - 1.23306I$	$13.7970 + 3.1675I$	0
$u = -0.44042 + 2.17097I$ $a = -0.109711 - 0.826235I$ $b = -1.15792 + 1.18934I$	$17.8796 + 4.3535I$	0

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.44042 - 2.17097I$		
$a = -0.109711 + 0.826235I$	$17.8796 - 4.3535I$	0
$b = -1.15792 - 1.18934I$		

$$\text{II. } I_1^v = \langle a, b - 1, v^8 + v^7 - 3v^6 - 2v^5 + 3v^4 + 2v - 1 \rangle$$

(i) Arc colorings

$$a_3 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} v \\ 0 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} v^2 \\ 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -v^3 + v \\ -v \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -v^4 + 2v^2 \\ -v^2 + 1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -v^3 + v \\ v^3 - 2v \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} v^6 - 2v^4 + v^2 \\ -v^6 + 3v^4 - 2v^2 - 1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} v \\ 0 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = $2v^7 + 7v^6 - 5v^5 - 19v^4 + 8v^3 + 12v^2 - 8v + 10$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1, c_2	$(u - 1)^8$
c_3, c_8	u^8
c_4	$(u + 1)^8$
c_5, c_6	$u^8 - u^7 - 3u^6 + 2u^5 + 3u^4 - 2u - 1$
c_7	$u^8 + u^7 - u^6 - 2u^5 + u^4 + 2u^3 - 2u - 1$
c_9	$u^8 + u^7 - 3u^6 - 2u^5 + 3u^4 + 2u - 1$
c_{10}	$u^8 + 3u^7 + 7u^6 + 10u^5 + 11u^4 + 10u^3 + 6u^2 + 4u + 1$
c_{11}	$u^8 - u^7 - u^6 + 2u^5 + u^4 - 2u^3 + 2u - 1$
c_{12}	$u^8 - 3u^7 + 7u^6 - 10u^5 + 11u^4 - 10u^3 + 6u^2 - 4u + 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1, c_2, c_4	$(y - 1)^8$
c_3, c_8	y^8
c_5, c_6, c_9	$y^8 - 7y^7 + 19y^6 - 22y^5 + 3y^4 + 14y^3 - 6y^2 - 4y + 1$
c_7, c_{11}	$y^8 - 3y^7 + 7y^6 - 10y^5 + 11y^4 - 10y^3 + 6y^2 - 4y + 1$
c_{10}, c_{12}	$y^8 + 5y^7 + 11y^6 + 6y^5 - 17y^4 - 34y^3 - 22y^2 - 4y + 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to I_1^v	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$v = 1.180120 + 0.268597I$ $a = 0$ $b = 1.00000$	$-0.604279 + 1.131230I$	$1.351190 - 0.172290I$
$v = 1.180120 - 0.268597I$ $a = 0$ $b = 1.00000$	$-0.604279 - 1.131230I$	$1.351190 + 0.172290I$
$v = 0.108090 + 0.747508I$ $a = 0$ $b = 1.00000$	$-3.80435 + 2.57849I$	$-5.95120 - 3.90294I$
$v = 0.108090 - 0.747508I$ $a = 0$ $b = 1.00000$	$-3.80435 - 2.57849I$	$-5.95120 + 3.90294I$
$v = -1.37100$ $a = 0$ $b = 1.00000$	4.85780	8.27570
$v = -1.334530 + 0.318930I$ $a = 0$ $b = 1.00000$	$0.73474 - 6.44354I$	$3.58146 + 4.68309I$
$v = -1.334530 - 0.318930I$ $a = 0$ $b = 1.00000$	$0.73474 + 6.44354I$	$3.58146 - 4.68309I$
$v = 0.463640$ $a = 0$ $b = 1.00000$	-0.799899	8.76140

III. u-Polynomials

Crossings	u-Polynomials at each crossing
c_1	$((u-1)^8)(u^{31} + u^{30} + \dots + 4u + 1)$
c_2	$((u-1)^8)(u^{31} - 9u^{30} + \dots - 6u + 1)$
c_3, c_8	$u^8(u^{31} + u^{30} + \dots + 128u + 256)$
c_4	$((u+1)^8)(u^{31} - 9u^{30} + \dots - 6u + 1)$
c_5, c_6	$(u^8 - u^7 - 3u^6 + 2u^5 + 3u^4 - 2u - 1)(u^{31} - 2u^{30} + \dots + 2u + 1)$
c_7	$(u^8 + u^7 + \dots - 2u - 1)(u^{31} + 2u^{30} + \dots + 4u + 1)$
c_9	$(u^8 + u^7 - 3u^6 - 2u^5 + 3u^4 + 2u - 1)(u^{31} - 2u^{30} + \dots + 2u + 1)$
c_{10}	$(u^8 + 3u^7 + 7u^6 + 10u^5 + 11u^4 + 10u^3 + 6u^2 + 4u + 1)$ $\cdot (u^{31} - 12u^{30} + \dots + 24u - 1)$
c_{11}	$(u^8 - u^7 + \dots + 2u - 1)(u^{31} + 2u^{30} + \dots + 4u + 1)$
c_{12}	$(u^8 - 3u^7 + 7u^6 - 10u^5 + 11u^4 - 10u^3 + 6u^2 - 4u + 1)$ $\cdot (u^{31} - 12u^{30} + \dots + 24u - 1)$

IV. Riley Polynomials

Crossings	Riley Polynomials at each crossing
c_1	$((y - 1)^8)(y^{31} + 67y^{30} + \dots + 68y - 1)$
c_2, c_4	$((y - 1)^8)(y^{31} - y^{30} + \dots + 4y - 1)$
c_3, c_8	$y^8(y^{31} + 51y^{30} + \dots - 344064y - 65536)$
c_5, c_6, c_9	$(y^8 - 7y^7 + 19y^6 - 22y^5 + 3y^4 + 14y^3 - 6y^2 - 4y + 1)$ $\cdot (y^{31} - 44y^{30} + \dots + 24y - 1)$
c_7, c_{11}	$(y^8 - 3y^7 + 7y^6 - 10y^5 + 11y^4 - 10y^3 + 6y^2 - 4y + 1)$ $\cdot (y^{31} - 12y^{30} + \dots + 24y - 1)$
c_{10}, c_{12}	$(y^8 + 5y^7 + 11y^6 + 6y^5 - 17y^4 - 34y^3 - 22y^2 - 4y + 1)$ $\cdot (y^{31} + 16y^{30} + \dots + 264y - 1)$