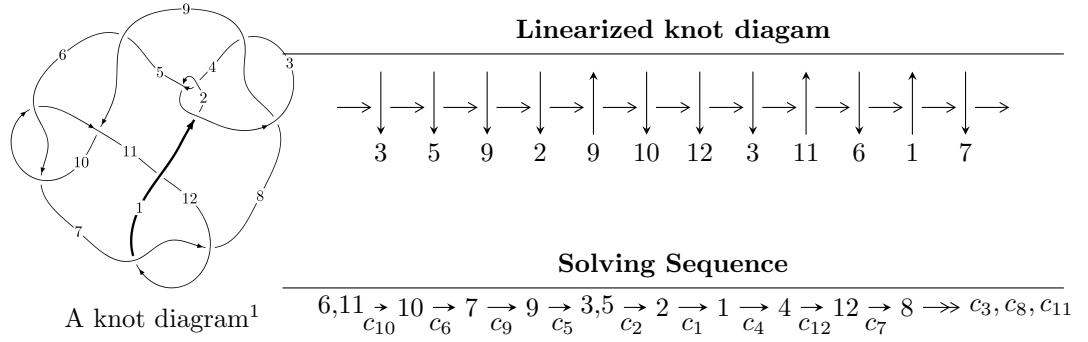


## $12n_{0157}$ ( $K12n_{0157}$ )



### Ideals for irreducible components<sup>2</sup> of $X_{\text{par}}$

$$\begin{aligned}
 I_1^u &= \langle u^{16} - 3u^{15} + 6u^{14} - 8u^{13} + 12u^{12} - 12u^{11} + 12u^{10} - 3u^9 - 3u^8 + 5u^7 - 9u^6 + 9u^5 - 5u^4 - 6u^3 + 8b - u - 3 \\
 &\quad - 3u^{16} + 5u^{15} + \dots + 4a - 7, u^{17} + 5u^{15} + \dots + 2u - 1 \rangle \\
 I_2^u &= \langle -92905u^{29} + 216359u^{28} + \dots + 130935b + 251026, \\
 &\quad 263141u^{29} - 444141u^{28} + \dots + 130935a - 340714, u^{30} - 2u^{29} + \dots - 2u + 1 \rangle \\
 I_3^u &= \langle -u^3 - u^2 + 2b - 1, u^3 + a + u + 1, u^4 + u^2 + u + 1 \rangle \\
 I_4^u &= \langle u^4 - u^3 + u^2 + b - u + 1, u^5 - u^4 + 2u^3 - 2u^2 + a + 2u - 2, u^6 - u^5 + 2u^4 - 2u^3 + 2u^2 - 2u + 1 \rangle
 \end{aligned}$$

\* 4 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 57 representations.

<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$I_1^u = \langle u^{16} - 3u^{15} + \dots + 8b - 3, -3u^{16} + 5u^{15} + \dots + 4a - 7, u^{17} + 5u^{15} + \dots + 2u - 1 \rangle^{\text{I.}}$$

(i) Arc colorings

$$\begin{aligned} a_6 &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_{11} &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} 1 \\ -u^2 \end{pmatrix} \\ a_7 &= \begin{pmatrix} -u \\ u^3 + u \end{pmatrix} \\ a_9 &= \begin{pmatrix} u^2 + 1 \\ -u^2 \end{pmatrix} \\ a_3 &= \begin{pmatrix} \frac{3}{4}u^{16} - \frac{5}{4}u^{15} + \dots - \frac{15}{4}u + \frac{7}{4} \\ -\frac{1}{8}u^{16} + \frac{3}{8}u^{15} + \dots + \frac{1}{8}u + \frac{3}{8} \end{pmatrix} \\ a_5 &= \begin{pmatrix} -u^5 - 2u^3 - u \\ u^5 + u^3 + u \end{pmatrix} \\ a_2 &= \begin{pmatrix} \frac{3}{4}u^{16} - \frac{1}{4}u^{15} + \dots - \frac{15}{4}u + \frac{7}{4} \\ -\frac{3}{8}u^{16} + \frac{1}{8}u^{15} + \dots + \frac{3}{8}u + \frac{1}{8} \end{pmatrix} \\ a_1 &= \begin{pmatrix} u^{15} + 4u^{13} + \dots - 2u^2 + 2u \\ u^2 \end{pmatrix} \\ a_4 &= \begin{pmatrix} \frac{3}{4}u^{16} - \frac{9}{4}u^{15} + \dots - \frac{19}{4}u + \frac{7}{4} \\ \frac{3}{8}u^{16} + \frac{7}{8}u^{15} + \dots - \frac{11}{8}u + \frac{7}{8} \end{pmatrix} \\ a_{12} &= \begin{pmatrix} u^{15} + 4u^{13} + \dots - u^2 + 2u \\ -u^4 \end{pmatrix} \\ a_8 &= \begin{pmatrix} -u^{16} - 4u^{14} + \dots - 2u^2 - u \\ u^5 + u^3 + u \end{pmatrix} \end{aligned}$$

(ii) Obstruction class = -1

$$(iii) \text{ Cusp Shapes} = -\frac{31}{16}u^{16} - \frac{43}{16}u^{15} - \frac{73}{16}u^{14} - \frac{29}{16}u^{13} - \frac{107}{4}u^{12} - \frac{145}{4}u^{11} - \frac{177}{4}u^{10} - \frac{851}{16}u^9 - \frac{835}{16}u^8 - \frac{763}{16}u^7 - \frac{625}{16}u^6 - \frac{487}{16}u^5 - \frac{477}{16}u^4 - \frac{127}{8}u^3 - 7u^2 - \frac{97}{16}u - \frac{115}{16}$$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1$	$u^{17} + 3u^{16} + \cdots + 209u + 16$
$c_2, c_4$	$u^{17} - 3u^{16} + \cdots - 15u + 4$
$c_3, c_8$	$u^{17} + 3u^{16} + \cdots + 144u + 64$
$c_5$	$u^{17} - 6u^{16} + \cdots + 4u + 4$
$c_6, c_7, c_{10}$ $c_{12}$	$u^{17} + 5u^{15} + \cdots + 2u + 1$
$c_9, c_{11}$	$u^{17} - 10u^{16} + \cdots + 2u + 1$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1$	$y^{17} + 25y^{16} + \cdots + 9953y - 256$
$c_2, c_4$	$y^{17} - 3y^{16} + \cdots + 209y - 16$
$c_3, c_8$	$y^{17} + 21y^{16} + \cdots - 28416y - 4096$
$c_5$	$y^{17} - 20y^{16} + \cdots + 8y - 16$
$c_6, c_7, c_{10}$ $c_{12}$	$y^{17} + 10y^{16} + \cdots + 2y - 1$
$c_9, c_{11}$	$y^{17} - 2y^{16} + \cdots + 62y - 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.322169 + 0.932839I$		
$a = 1.62275 - 0.13510I$	$0.45185 - 4.10615I$	$-5.36541 + 8.40411I$
$b = -0.887795 - 0.139754I$		
$u = 0.322169 - 0.932839I$		
$a = 1.62275 + 0.13510I$	$0.45185 + 4.10615I$	$-5.36541 - 8.40411I$
$b = -0.887795 + 0.139754I$		
$u = -0.942204 + 0.079923I$		
$a = 0.14770 - 2.09951I$	$5.75170 - 3.64530I$	$-7.03668 + 2.07740I$
$b = 0.10264 + 1.92963I$		
$u = -0.942204 - 0.079923I$		
$a = 0.14770 + 2.09951I$	$5.75170 + 3.64530I$	$-7.03668 - 2.07740I$
$b = 0.10264 - 1.92963I$		
$u = 0.644046 + 0.585914I$		
$a = 0.110639 - 0.237693I$	$-1.54328 - 1.26290I$	$-4.69916 + 2.78148I$
$b = 0.141114 + 0.412958I$		
$u = 0.644046 - 0.585914I$		
$a = 0.110639 + 0.237693I$	$-1.54328 + 1.26290I$	$-4.69916 - 2.78148I$
$b = 0.141114 - 0.412958I$		
$u = -0.365355 + 1.127480I$		
$a = -0.001951 + 1.108840I$	$5.03884 + 6.08356I$	$-0.37752 - 7.44095I$
$b = -0.461535 + 0.413910I$		
$u = -0.365355 - 1.127480I$		
$a = -0.001951 - 1.108840I$	$5.03884 - 6.08356I$	$-0.37752 + 7.44095I$
$b = -0.461535 - 0.413910I$		
$u = -0.603603 + 1.090260I$		
$a = -0.576964 + 0.057793I$	$1.68715 + 8.69176I$	$-1.96939 - 9.35770I$
$b = -0.208622 - 0.448687I$		
$u = -0.603603 - 1.090260I$		
$a = -0.576964 - 0.057793I$	$1.68715 - 8.69176I$	$-1.96939 + 9.35770I$
$b = -0.208622 + 0.448687I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.204874 + 0.705829I$		
$a = -1.11943 - 2.16921I$	$-1.27035 + 1.28580I$	$-7.39957 - 4.02248I$
$b = 0.782082 - 0.120438I$		
$u = -0.204874 - 0.705829I$		
$a = -1.11943 + 2.16921I$	$-1.27035 - 1.28580I$	$-7.39957 + 4.02248I$
$b = 0.782082 + 0.120438I$		
$u = 0.445712 + 1.288030I$		
$a = -1.82989 - 0.01952I$	$14.2142 - 5.9853I$	$-0.22003 + 3.96763I$
$b = 0.74942 + 2.06882I$		
$u = 0.445712 - 1.288030I$		
$a = -1.82989 + 0.01952I$	$14.2142 + 5.9853I$	$-0.22003 - 3.96763I$
$b = 0.74942 - 2.06882I$		
$u = 0.524102 + 1.283480I$		
$a = 1.78460 + 0.35804I$	$13.1143 - 14.2375I$	$-1.63337 + 7.74538I$
$b = -0.69769 - 2.47703I$		
$u = 0.524102 - 1.283480I$		
$a = 1.78460 - 0.35804I$	$13.1143 + 14.2375I$	$-1.63337 - 7.74538I$
$b = -0.69769 + 2.47703I$		
$u = 0.360012$		
$a = 0.725098$	$-0.866858$	$-11.8480$
$b = 0.460755$		

### II.

$$I_2^u = \langle -9.29 \times 10^4 u^{29} + 2.16 \times 10^5 u^{28} + \dots + 1.31 \times 10^5 b + 2.51 \times 10^5, 2.63 \times 10^5 u^{29} - 4.44 \times 10^5 u^{28} + \dots + 1.31 \times 10^5 a - 3.41 \times 10^5, u^{30} - 2u^{29} + \dots - 2u + 1 \rangle$$

(i) Arc colorings

$$\begin{aligned} a_6 &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_{11} &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} 1 \\ -u^2 \end{pmatrix} \\ a_7 &= \begin{pmatrix} -u \\ u^3 + u \end{pmatrix} \\ a_9 &= \begin{pmatrix} u^2 + 1 \\ -u^2 \end{pmatrix} \\ a_3 &= \begin{pmatrix} -2.00971u^{29} + 3.39207u^{28} + \dots - 5.34987u + 2.60216 \\ 0.709551u^{29} - 1.65242u^{28} + \dots + 4.31412u - 1.91718 \end{pmatrix} \\ a_5 &= \begin{pmatrix} -u^5 - 2u^3 - u \\ u^5 + u^3 + u \end{pmatrix} \\ a_2 &= \begin{pmatrix} -0.985413u^{29} + 2.58805u^{28} + \dots - 1.73251u + 0.970054 \\ -0.0934739u^{29} - 1.15465u^{28} + \dots + 1.36986u - 0.724375 \end{pmatrix} \\ a_1 &= \begin{pmatrix} -1.10899u^{29} + 2.08162u^{28} + \dots + 7.36940u + 0.914484 \\ 0.581747u^{29} - 0.918028u^{28} + \dots - 0.836285u - 1.13635 \end{pmatrix} \\ a_4 &= \begin{pmatrix} -3.03400u^{29} + 4.19610u^{28} + \dots - 9.96723u + 4.23427 \\ 1.30708u^{29} - 2.17849u^{28} + \dots + 5.03852u - 2.49276 \end{pmatrix} \\ a_{12} &= \begin{pmatrix} -1.69073u^{29} + 2.99965u^{28} + \dots + 8.20569u + 1.05083 \\ 1.96604u^{29} - 2.83797u^{28} + \dots - 1.76339u - 1.51817 \end{pmatrix} \\ a_8 &= \begin{pmatrix} -1.24547u^{29} + 1.68839u^{28} + \dots - 2.02714u + 2.58175 \\ 0.712292u^{29} - 1.03145u^{28} + \dots - 0.916722u - 0.275305 \end{pmatrix} \end{aligned}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes =  $\frac{240791}{130935}u^{29} - \frac{162874}{43645}u^{28} + \dots - \frac{489788}{43645}u - \frac{735898}{130935}$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1$	$(u^{15} + 2u^{14} + \cdots - 3u + 1)^2$
$c_2, c_4$	$(u^{15} - 4u^{14} + \cdots - 3u + 1)^2$
$c_3, c_8$	$(u^{15} - u^{14} + \cdots + 12u - 8)^2$
$c_5$	$(u^{15} + 2u^{14} + \cdots + 2u - 1)^2$
$c_6, c_7, c_{10}$ $c_{12}$	$u^{30} + 2u^{29} + \cdots + 2u + 1$
$c_9, c_{11}$	$u^{30} - 18u^{29} + \cdots + 20u^2 + 1$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1$	$(y^{15} + 26y^{14} + \cdots - 3y - 1)^2$
$c_2, c_4$	$(y^{15} - 2y^{14} + \cdots - 3y - 1)^2$
$c_3, c_8$	$(y^{15} + 21y^{14} + \cdots - 48y - 64)^2$
$c_5$	$(y^{15} - 20y^{14} + \cdots + 20y - 1)^2$
$c_6, c_7, c_{10}$ $c_{12}$	$y^{30} + 18y^{29} + \cdots + 20y^2 + 1$
$c_9, c_{11}$	$y^{30} - 14y^{29} + \cdots + 40y + 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.113884 + 1.019270I$		
$a = 0.083302 - 0.745556I$	2.02375	$-13.41313 + 0.I$
$b = -3.08095 + 2.65889I$		
$u = 0.113884 - 1.019270I$		
$a = 0.083302 + 0.745556I$	2.02375	$-13.41313 + 0.I$
$b = -3.08095 - 2.65889I$		
$u = 0.968195 + 0.069474I$		
$a = 0.13797 - 2.33358I$	9.38409 + 8.90152I	$-4.37309 - 5.02376I$
$b = -0.34781 + 2.07950I$		
$u = 0.968195 - 0.069474I$		
$a = 0.13797 + 2.33358I$	9.38409 - 8.90152I	$-4.37309 + 5.02376I$
$b = -0.34781 - 2.07950I$		
$u = 0.919318 + 0.052871I$		
$a = -0.58314 - 2.24993I$	10.07630 - 1.17157I	$-3.47853 + 0.84051I$
$b = 0.20945 + 2.09210I$		
$u = 0.919318 - 0.052871I$		
$a = -0.58314 + 2.24993I$	10.07630 + 1.17157I	$-3.47853 - 0.84051I$
$b = 0.20945 - 2.09210I$		
$u = -0.382683 + 1.019330I$		
$a = -0.100174 + 0.245215I$	4.66000 + 0.70150I	$1.29100 - 2.23884I$
$b = -1.043020 + 0.299494I$		
$u = -0.382683 - 1.019330I$		
$a = -0.100174 - 0.245215I$	4.66000 - 0.70150I	$1.29100 + 2.23884I$
$b = -1.043020 - 0.299494I$		
$u = -0.205921 + 0.850565I$		
$a = -1.04297 - 1.20710I$	-1.01332 + 1.14653I	$-7.69630 + 0.14216I$
$b = 1.238940 - 0.251605I$		
$u = -0.205921 - 0.850565I$		
$a = -1.04297 + 1.20710I$	-1.01332 - 1.14653I	$-7.69630 - 0.14216I$
$b = 1.238940 + 0.251605I$		

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.779082 + 0.386456I$		
$a = -0.002343 - 0.498402I$	$-0.36549 - 3.51330I$	$-3.79294 + 4.67402I$
$b = -0.087330 + 0.645001I$		
$u = -0.779082 - 0.386456I$		
$a = -0.002343 + 0.498402I$	$-0.36549 + 3.51330I$	$-3.79294 - 4.67402I$
$b = -0.087330 - 0.645001I$		
$u = 0.285236 + 1.100680I$		
$a = 0.248621 + 0.458325I$	$1.96945 - 2.58137I$	$-3.99557 + 4.00241I$
$b = -0.050199 + 0.632654I$		
$u = 0.285236 - 1.100680I$		
$a = 0.248621 - 0.458325I$	$1.96945 + 2.58137I$	$-3.99557 - 4.00241I$
$b = -0.050199 - 0.632654I$		
$u = 0.581753 + 0.981574I$		
$a = 0.378951 + 0.026508I$	$-0.36549 - 3.51330I$	$-3.79294 + 4.67402I$
$b = 0.335458 - 0.088672I$		
$u = 0.581753 - 0.981574I$		
$a = 0.378951 - 0.026508I$	$-0.36549 + 3.51330I$	$-3.79294 - 4.67402I$
$b = 0.335458 + 0.088672I$		
$u = -0.221864 + 1.217690I$		
$a = 0.186395 + 0.139826I$	$4.66000 - 0.70150I$	$1.29100 + 2.23884I$
$b = -0.081740 + 1.033740I$		
$u = -0.221864 - 1.217690I$		
$a = 0.186395 - 0.139826I$	$4.66000 + 0.70150I$	$1.29100 - 2.23884I$
$b = -0.081740 - 1.033740I$		
$u = 0.505703 + 1.263210I$		
$a = 1.53273 + 0.65637I$	$13.7555 - 3.9297I$	$-0.74800 + 2.37642I$
$b = -0.01619 - 2.51545I$		
$u = 0.505703 - 1.263210I$		
$a = 1.53273 - 0.65637I$	$13.7555 + 3.9297I$	$-0.74800 - 2.37642I$
$b = -0.01619 + 2.51545I$		

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.522779 + 1.269460I$		
$a = -1.59728 + 0.42484I$	$9.38409 + 8.90152I$	$-4.37309 - 5.02376I$
$b = 0.39291 - 2.31888I$		
$u = -0.522779 - 1.269460I$		
$a = -1.59728 - 0.42484I$	$9.38409 - 8.90152I$	$-4.37309 + 5.02376I$
$b = 0.39291 + 2.31888I$		
$u = -0.431128 + 1.304160I$		
$a = 1.54639 - 0.19135I$	$10.07630 + 1.17157I$	$-3.47853 - 0.84051I$
$b = -0.48250 + 1.97368I$		
$u = -0.431128 - 1.304160I$		
$a = 1.54639 + 0.19135I$	$10.07630 - 1.17157I$	$-3.47853 + 0.84051I$
$b = -0.48250 - 1.97368I$		
$u = 0.441120 + 1.321990I$		
$a = -1.55605 - 0.47835I$	$13.7555 + 3.9297I$	$-0.74800 - 2.37642I$
$b = 0.28997 + 2.13261I$		
$u = 0.441120 - 1.321990I$		
$a = -1.55605 + 0.47835I$	$13.7555 - 3.9297I$	$-0.74800 + 2.37642I$
$b = 0.28997 - 2.13261I$		
$u = -0.556485 + 0.018600I$		
$a = 0.802481 - 0.699849I$	$1.96945 - 2.58137I$	$-3.99557 + 4.00241I$
$b = -0.908162 - 0.199648I$		
$u = -0.556485 - 0.018600I$		
$a = 0.802481 + 0.699849I$	$1.96945 + 2.58137I$	$-3.99557 - 4.00241I$
$b = -0.908162 + 0.199648I$		
$u = 0.284735 + 0.297386I$		
$a = 0.96512 - 3.25062I$	$-1.01332 + 1.14653I$	$-7.69630 + 0.14216I$
$b = 0.131164 + 0.467054I$		
$u = 0.284735 - 0.297386I$		
$a = 0.96512 + 3.25062I$	$-1.01332 - 1.14653I$	$-7.69630 - 0.14216I$
$b = 0.131164 - 0.467054I$		

$$\text{III. } I_3^u = \langle -u^3 - u^2 + 2b - 1, \ u^3 + a + u + 1, \ u^4 + u^2 + u + 1 \rangle$$

(i) Arc colorings

$$\begin{aligned} a_6 &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_{11} &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} 1 \\ -u^2 \end{pmatrix} \\ a_7 &= \begin{pmatrix} -u \\ u^3 + u \end{pmatrix} \\ a_9 &= \begin{pmatrix} u^2 + 1 \\ -u^2 \end{pmatrix} \\ a_3 &= \begin{pmatrix} -u^3 - u - 1 \\ \frac{1}{2}u^3 + \frac{1}{2}u^2 + \frac{1}{2} \end{pmatrix} \\ a_5 &= \begin{pmatrix} -u^3 + u^2 \\ -u^2 \end{pmatrix} \\ a_2 &= \begin{pmatrix} -u^2 - u - 1 \\ \frac{1}{2}u^3 + \frac{3}{2}u^2 + \frac{1}{2} \end{pmatrix} \\ a_1 &= \begin{pmatrix} u^3 - u^2 \\ u^2 \end{pmatrix} \\ a_4 &= \begin{pmatrix} -u^3 - u - 1 \\ \frac{1}{2}u^3 + \frac{1}{2}u^2 + \frac{1}{2} \end{pmatrix} \\ a_{12} &= \begin{pmatrix} u^3 \\ u^2 + u + 1 \end{pmatrix} \\ a_8 &= \begin{pmatrix} u^2 + 1 \\ -u^2 \end{pmatrix} \end{aligned}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes =  $-\frac{21}{4}u^3 + \frac{11}{4}u^2 - \frac{1}{2}u - \frac{47}{4}$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_2$	$(u - 1)^4$
$c_3, c_8$	$u^4$
$c_4$	$(u + 1)^4$
$c_5$	$u^4 - 3u^3 + 4u^2 - 3u + 2$
$c_6, c_7$	$u^4 + u^2 - u + 1$
$c_9, c_{11}$	$u^4 + 2u^3 + 3u^2 + u + 1$
$c_{10}, c_{12}$	$u^4 + u^2 + u + 1$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_4$	$(y - 1)^4$
$c_3, c_8$	$y^4$
$c_5$	$y^4 - y^3 + 2y^2 + 7y + 4$
$c_6, c_7, c_{10}$ $c_{12}$	$y^4 + 2y^3 + 3y^2 + y + 1$
$c_9, c_{11}$ $c_{12}$	$y^4 + 2y^3 + 7y^2 + 5y + 1$

**(vi) Complex Volumes and Cusp Shapes**

Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.547424 + 0.585652I$		
$a = -0.851808 - 0.911292I$	$-2.62503 + 1.39709I$	$-13.6914 - 3.7657I$
$b = 0.677958 - 0.157780I$		
$u = -0.547424 - 0.585652I$		
$a = -0.851808 + 0.911292I$	$-2.62503 - 1.39709I$	$-13.6914 + 3.7657I$
$b = 0.677958 + 0.157780I$		
$u = 0.547424 + 1.120870I$		
$a = 0.351808 - 0.720342I$	$0.98010 - 7.64338I$	$-4.68363 + 4.91712I$
$b = -0.927958 + 0.413327I$		
$u = 0.547424 - 1.120870I$		
$a = 0.351808 + 0.720342I$	$0.98010 + 7.64338I$	$-4.68363 - 4.91712I$
$b = -0.927958 - 0.413327I$		

$$\text{IV. } I_4^u = \langle u^4 - u^3 + u^2 + b - u + 1, u^5 - u^4 + 2u^3 - 2u^2 + a + 2u - 2, u^6 - u^5 + 2u^4 - 2u^3 + 2u^2 - 2u + 1 \rangle$$

(i) Arc colorings

$$a_6 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -u \\ u^3 + u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} u^2 + 1 \\ -u^2 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -u^5 + u^4 - 2u^3 + 2u^2 - 2u + 2 \\ -u^4 + u^3 - u^2 + u - 1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -u^5 - 2u^3 - u \\ u^5 + u^3 + u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} u^4 + 2u^2 - u + 2 \\ -u^5 - u^4 - u^2 - 1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} u^5 + 2u^3 + u \\ -u^5 - u^3 - u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -u^5 + u^4 - 2u^3 + 2u^2 - 2u + 2 \\ -u^4 + u^3 - u^2 + u - 1 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 2u^5 + 3u^3 - u^2 + 2u - 1 \\ -2u^5 + u^4 - 3u^3 + 2u^2 - 3u + 2 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} u^2 + 1 \\ -u^2 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes =  $u^5 - 3u^3 - u^2 - 3u - 6$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_2$	$(u - 1)^6$
$c_3, c_8$	$u^6$
$c_4$	$(u + 1)^6$
$c_5$	$(u^3 + u^2 - 1)^2$
$c_6, c_7$	$u^6 + u^5 + 2u^4 + 2u^3 + 2u^2 + 2u + 1$
$c_9, c_{11}$	$u^6 + 3u^5 + 4u^4 + 2u^3 + 1$
$c_{10}, c_{12}$	$u^6 - u^5 + 2u^4 - 2u^3 + 2u^2 - 2u + 1$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_4$	$(y - 1)^6$
$c_3, c_8$	$y^6$
$c_5$	$(y^3 - y^2 + 2y - 1)^2$
$c_6, c_7, c_{10}$ $c_{12}$	$y^6 + 3y^5 + 4y^4 + 2y^3 + 1$
$c_9, c_{11}$	$y^6 - y^5 + 4y^4 - 2y^3 + 8y^2 + 1$

**(vi) Complex Volumes and Cusp Shapes**

Solutions to $I_4^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.498832 + 1.001300I$		
$a = -0.398606 - 0.800120I$	$-1.37919 + 2.82812I$	$-9.17211 - 2.41717I$
$b = 1.060970 + 0.237841I$		
$u = -0.498832 - 1.001300I$		
$a = -0.398606 + 0.800120I$	$-1.37919 - 2.82812I$	$-9.17211 + 2.41717I$
$b = 1.060970 - 0.237841I$		
$u = 0.284920 + 1.115140I$		
$a = 0.215080 - 0.841795I$	2.75839	$-6 - 0.655771 + 0.10I$
$b = -1.53980 + 0.84179I$		
$u = 0.284920 - 1.115140I$		
$a = 0.215080 + 0.841795I$	2.75839	$-6 - 0.655771 + 0.10I$
$b = -1.53980 - 0.84179I$		
$u = 0.713912 + 0.305839I$		
$a = 1.183530 - 0.507021I$	$-1.37919 + 2.82812I$	$-9.17211 - 2.41717I$
$b = -0.521167 - 0.055259I$		
$u = 0.713912 - 0.305839I$		
$a = 1.183530 + 0.507021I$	$-1.37919 - 2.82812I$	$-9.17211 + 2.41717I$
$b = -0.521167 + 0.055259I$		

## V. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1$	$((u - 1)^{10})(u^{15} + 2u^{14} + \dots - 3u + 1)^2(u^{17} + 3u^{16} + \dots + 209u + 16)$
$c_2$	$((u - 1)^{10})(u^{15} - 4u^{14} + \dots - 3u + 1)^2(u^{17} - 3u^{16} + \dots - 15u + 4)$
$c_3, c_8$	$u^{10}(u^{15} - u^{14} + \dots + 12u - 8)^2(u^{17} + 3u^{16} + \dots + 144u + 64)$
$c_4$	$((u + 1)^{10})(u^{15} - 4u^{14} + \dots - 3u + 1)^2(u^{17} - 3u^{16} + \dots - 15u + 4)$
$c_5$	$((u^3 + u^2 - 1)^2)(u^4 - 3u^3 + \dots - 3u + 2)(u^{15} + 2u^{14} + \dots + 2u - 1)^2 \cdot (u^{17} - 6u^{16} + \dots + 4u + 4)$
$c_6, c_7$	$(u^4 + u^2 - u + 1)(u^6 + u^5 + 2u^4 + 2u^3 + 2u^2 + 2u + 1) \cdot (u^{17} + 5u^{15} + \dots + 2u + 1)(u^{30} + 2u^{29} + \dots + 2u + 1)$
$c_9, c_{11}$	$(u^4 + 2u^3 + 3u^2 + u + 1)(u^6 + 3u^5 + 4u^4 + 2u^3 + 1) \cdot (u^{17} - 10u^{16} + \dots + 2u + 1)(u^{30} - 18u^{29} + \dots + 20u^2 + 1)$
$c_{10}, c_{12}$	$(u^4 + u^2 + u + 1)(u^6 - u^5 + 2u^4 - 2u^3 + 2u^2 - 2u + 1) \cdot (u^{17} + 5u^{15} + \dots + 2u + 1)(u^{30} + 2u^{29} + \dots + 2u + 1)$

## VI. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1$	$((y - 1)^{10})(y^{15} + 26y^{14} + \dots - 3y - 1)^2$ $\cdot (y^{17} + 25y^{16} + \dots + 9953y - 256)$
$c_2, c_4$	$((y - 1)^{10})(y^{15} - 2y^{14} + \dots - 3y - 1)^2(y^{17} - 3y^{16} + \dots + 209y - 16)$
$c_3, c_8$	$y^{10}(y^{15} + 21y^{14} + \dots - 48y - 64)^2$ $\cdot (y^{17} + 21y^{16} + \dots - 28416y - 4096)$
$c_5$	$(y^3 - y^2 + 2y - 1)^2(y^4 - y^3 + 2y^2 + 7y + 4)$ $\cdot ((y^{15} - 20y^{14} + \dots + 20y - 1)^2)(y^{17} - 20y^{16} + \dots + 8y - 16)$
$c_6, c_7, c_{10}$ $c_{12}$	$(y^4 + 2y^3 + 3y^2 + y + 1)(y^6 + 3y^5 + 4y^4 + 2y^3 + 1)$ $\cdot (y^{17} + 10y^{16} + \dots + 2y - 1)(y^{30} + 18y^{29} + \dots + 20y^2 + 1)$
$c_9, c_{11}$	$(y^4 + 2y^3 + 7y^2 + 5y + 1)(y^6 - y^5 + 4y^4 - 2y^3 + 8y^2 + 1)$ $\cdot (y^{17} - 2y^{16} + \dots + 62y - 1)(y^{30} - 14y^{29} + \dots + 40y + 1)$