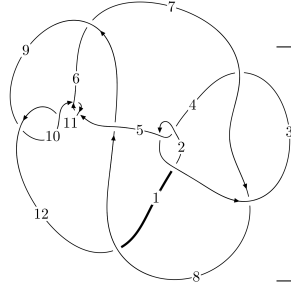
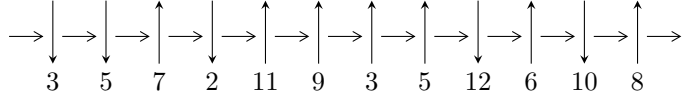


12n₀₁₆₀ (K12n₀₁₆₀)



A knot diagram¹

Linearized knot diagram



Solving Sequence

$$6,10 \xrightarrow{c_{10}} 11 \xrightarrow{c_{11}} 12 \xrightarrow{c_5} 3,5 \xrightarrow{c_2} 2 \xrightarrow{c_1} 1 \xrightarrow{c_4} 4 \xrightarrow{c_9} 9 \xrightarrow{c_6} 7 \xrightarrow{c_8} 8 \rightsquigarrow c_3, c_7, c_{12}$$

Ideals for irreducible components² of X_{par}

$$I_1^u = \langle -3u^{34} + 6u^{33} + \dots + b - 3, 3u^{34} - 3u^{33} + \dots + a + 1, u^{35} - 2u^{34} + \dots - 2u^2 - 1 \rangle$$

$$I_2^u = \langle -u^7 - u^5 - 2u^3 + u^2 + b - u, -u^6 - u^4 - 2u^2 + a + u - 1, u^9 + u^8 + 2u^7 + u^6 + 3u^5 + u^4 + 2u^3 + u - 1 \rangle$$

* 2 irreducible components of $\dim_{\mathbb{C}} = 0$, with total 44 representations.

¹The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

²All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

I.

$$I_1^u = \langle -3u^{34} + 6u^{33} + \dots + b - 3, 3u^{34} - 3u^{33} + \dots + a + 1, u^{35} - 2u^{34} + \dots - 2u^2 - 1 \rangle$$

(i) Arc colorings

$$a_6 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} u^2 + 1 \\ -u^2 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -3u^{34} + 3u^{33} + \dots - 2u - 1 \\ 3u^{34} - 6u^{33} + \dots + u + 3 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -u \\ u^3 + u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -2u^{34} + 2u^{33} + \dots - 2u - 1 \\ 2u^{34} - 4u^{33} + \dots + 7u^2 + 2 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -u^{20} - 3u^{18} - 7u^{16} - 10u^{14} - 10u^{12} - 7u^{10} - u^8 + 2u^6 + 3u^4 + u^2 - 1 \\ u^{22} + 4u^{20} + \dots + 2u^4 + u^2 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -u^{34} + u^{33} + \dots + 3u^2 - 3u \\ u^{34} - 2u^{33} + \dots + 4u^2 + 1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} u^4 + u^2 + 1 \\ -u^4 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} u^9 + 2u^7 + 3u^5 + 2u^3 + u \\ -u^9 - u^7 - u^5 + u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -u^8 - u^6 - u^4 + 1 \\ u^{10} + 2u^8 + 3u^6 + 2u^4 + u^2 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes = $4u^{34} - 2u^{33} + 24u^{32} - 8u^{31} + 92u^{30} - 18u^{29} + 247u^{28} - 13u^{27} + 523u^{26} + 50u^{25} + 904u^{24} + 221u^{23} + 1321u^{22} + 524u^{21} + 1669u^{20} + 895u^{19} + 1845u^{18} + 1222u^{17} + 1810u^{16} + 1360u^{15} + 1576u^{14} + 1256u^{13} + 1216u^{12} + 958u^{11} + 820u^{10} + 594u^9 + 460u^8 + 299u^7 + 205u^6 + 110u^5 + 63u^4 + 27u^3 + 5u^2 + 4u - 2$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1	$u^{35} + 52u^{34} + \dots + 32u + 1$
c_2, c_4	$u^{35} - 10u^{34} + \dots + 12u - 1$
c_3, c_7	$u^{35} - u^{34} + \dots - 1024u - 512$
c_5, c_{10}	$u^{35} - 2u^{34} + \dots - 2u^2 - 1$
c_6	$u^{35} + 10u^{34} + \dots - 206u - 31$
c_8	$u^{35} - 2u^{34} + \dots - 412u - 241$
c_9, c_{11}	$u^{35} + 12u^{34} + \dots - 4u - 1$
c_{12}	$u^{35} + 36u^{33} + \dots - 2u - 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1	$y^{35} - 128y^{34} + \dots + 420y - 1$
c_2, c_4	$y^{35} - 52y^{34} + \dots + 32y - 1$
c_3, c_7	$y^{35} + 57y^{34} + \dots + 2621440y - 262144$
c_5, c_{10}	$y^{35} + 12y^{34} + \dots - 4y - 1$
c_6	$y^{35} + 12y^{34} + \dots - 10140y - 961$
c_8	$y^{35} + 12y^{34} + \dots - 1095024y - 58081$
c_9, c_{11}	$y^{35} + 24y^{34} + \dots - 16y - 1$
c_{12}	$y^{35} + 72y^{34} + \dots - 4y - 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.737220 + 0.648144I$ $a = 1.74315 - 1.73886I$ $b = -2.41211 + 0.15211I$	$-0.58521 - 2.05799I$	$0.94554 + 1.75994I$
$u = 0.737220 - 0.648144I$ $a = 1.74315 + 1.73886I$ $b = -2.41211 - 0.15211I$	$-0.58521 + 2.05799I$	$0.94554 - 1.75994I$
$u = 0.101201 + 0.967150I$ $a = -0.223398 - 0.378771I$ $b = -0.343721 + 0.254391I$	$-2.08113 + 1.70930I$	$0.77222 - 3.96512I$
$u = 0.101201 - 0.967150I$ $a = -0.223398 + 0.378771I$ $b = -0.343721 - 0.254391I$	$-2.08113 - 1.70930I$	$0.77222 + 3.96512I$
$u = 0.678017 + 0.796351I$ $a = -1.63124 - 0.26748I$ $b = 0.89300 + 1.48039I$	$1.40101 + 2.20417I$	$3.92249 - 4.39905I$
$u = 0.678017 - 0.796351I$ $a = -1.63124 + 0.26748I$ $b = 0.89300 - 1.48039I$	$1.40101 - 2.20417I$	$3.92249 + 4.39905I$
$u = -0.030827 + 1.048300I$ $a = 0.987634 + 0.536168I$ $b = 0.592511 - 1.018810I$	$-6.06605 - 1.60204I$	$-6.58193 + 1.49646I$
$u = -0.030827 - 1.048300I$ $a = 0.987634 - 0.536168I$ $b = 0.592511 + 1.018810I$	$-6.06605 + 1.60204I$	$-6.58193 - 1.49646I$
$u = 0.838636 + 0.644982I$ $a = -0.76138 + 2.67985I$ $b = 2.36698 - 1.75635I$	$-10.48130 - 6.27093I$	$0.94475 + 1.94965I$
$u = 0.838636 - 0.644982I$ $a = -0.76138 - 2.67985I$ $b = 2.36698 + 1.75635I$	$-10.48130 + 6.27093I$	$0.94475 - 1.94965I$

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.781183 + 0.727089I$		
$a = -0.051887 + 0.135238I$	$3.78767 + 1.08265I$	$9.73080 - 0.41634I$
$b = 0.057797 + 0.143372I$		
$u = -0.781183 - 0.727089I$		
$a = -0.051887 - 0.135238I$	$3.78767 - 1.08265I$	$9.73080 + 0.41634I$
$b = 0.057797 - 0.143372I$		
$u = -0.632282 + 0.665654I$		
$a = 0.152240 - 0.624708I$	$-1.37778 - 0.83460I$	$0.396623 + 0.019030I$
$b = -0.319580 - 0.496331I$		
$u = -0.632282 - 0.665654I$		
$a = 0.152240 + 0.624708I$	$-1.37778 + 0.83460I$	$0.396623 - 0.019030I$
$b = -0.319580 + 0.496331I$		
$u = -0.121893 + 1.112050I$		
$a = -1.224660 - 0.088950I$	$-17.1086 - 5.6948I$	$-5.50780 + 3.28741I$
$b = -0.248194 + 1.351040I$		
$u = -0.121893 - 1.112050I$		
$a = -1.224660 + 0.088950I$	$-17.1086 + 5.6948I$	$-5.50780 - 3.28741I$
$b = -0.248194 - 1.351040I$		
$u = 0.660177 + 0.922712I$		
$a = 0.183127 - 1.365060I$	$1.00684 + 2.97409I$	$3.31167 - 1.92596I$
$b = -1.38045 + 0.73221I$		
$u = 0.660177 - 0.922712I$		
$a = 0.183127 + 1.365060I$	$1.00684 - 2.97409I$	$3.31167 + 1.92596I$
$b = -1.38045 - 0.73221I$		
$u = -0.518083 + 1.034140I$		
$a = -0.493003 + 0.558538I$	$-14.7020 - 1.1608I$	$-3.27320 + 2.65041I$
$b = 0.322191 + 0.799204I$		
$u = -0.518083 - 1.034140I$		
$a = -0.493003 - 0.558538I$	$-14.7020 + 1.1608I$	$-3.27320 - 2.65041I$
$b = 0.322191 - 0.799204I$		

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.645286 + 0.989574I$		
$a = 0.110285 - 0.455498I$	$-2.35824 - 4.23049I$	$-1.64611 + 4.83730I$
$b = -0.379583 - 0.403061I$		
$u = -0.645286 - 0.989574I$		
$a = 0.110285 + 0.455498I$	$-2.35824 + 4.23049I$	$-1.64611 - 4.83730I$
$b = -0.379583 + 0.403061I$		
$u = 0.801511 + 0.879701I$		
$a = 1.77931 + 2.04057I$	$-6.25391 + 2.99402I$	$1.83860 - 2.69092I$
$b = 0.36896 - 3.20080I$		
$u = 0.801511 - 0.879701I$		
$a = 1.77931 - 2.04057I$	$-6.25391 - 2.99402I$	$1.83860 + 2.69092I$
$b = 0.36896 + 3.20080I$		
$u = 0.677300 + 1.008060I$		
$a = -2.02100 + 1.40176I$	$-1.65574 + 7.47330I$	$-0.96819 - 6.53783I$
$b = 2.78188 + 1.08787I$		
$u = 0.677300 - 1.008060I$		
$a = -2.02100 - 1.40176I$	$-1.65574 - 7.47330I$	$-0.96819 + 6.53783I$
$b = 2.78188 - 1.08787I$		
$u = -0.718651 + 0.985154I$		
$a = 0.0048122 + 0.1319630I$	$3.00104 - 6.75637I$	$7.73187 + 5.52332I$
$b = 0.133462 + 0.090095I$		
$u = -0.718651 - 0.985154I$		
$a = 0.0048122 - 0.1319630I$	$3.00104 + 6.75637I$	$7.73187 - 5.52332I$
$b = 0.133462 - 0.090095I$		
$u = -0.715979 + 0.271293I$		
$a = 0.797619 + 0.724413I$	$-12.50660 - 3.28011I$	$0.69781 + 2.19401I$
$b = 0.767607 + 0.302276I$		
$u = -0.715979 - 0.271293I$		
$a = 0.797619 - 0.724413I$	$-12.50660 + 3.28011I$	$0.69781 - 2.19401I$
$b = 0.767607 - 0.302276I$		

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.715761 + 1.041330I$ $a = 2.74535 - 0.31064I$ $b = -2.28849 - 2.63647I$	$-11.6867 + 12.0828I$	$-0.83819 - 6.56234I$
$u = 0.715761 - 1.041330I$ $a = 2.74535 + 0.31064I$ $b = -2.28849 + 2.63647I$	$-11.6867 - 12.0828I$	$-0.83819 + 6.56234I$
$u = -0.268541 + 0.381611I$ $a = 0.20602 - 1.57922I$ $b = -0.547327 - 0.502704I$	$-1.72551 - 0.80413I$	$-2.43242 + 1.76310I$
$u = -0.268541 - 0.381611I$ $a = 0.20602 + 1.57922I$ $b = -0.547327 + 0.502704I$	$-1.72551 + 0.80413I$	$-2.43242 - 1.76310I$
$u = 0.445806$ $a = -0.605941$ $b = 0.270132$	0.870658	11.9110

$$\text{II. } I_2^u = \langle -u^7 - u^5 - 2u^3 + u^2 + b - u, -u^6 - u^4 - 2u^2 + a + u - 1, u^9 + u^8 + 2u^7 + u^6 + 3u^5 + u^4 + 2u^3 + u - 1 \rangle$$

(i) Arc colorings

$$a_6 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} u^2 + 1 \\ -u^2 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} u^6 + u^4 + 2u^2 - u + 1 \\ u^7 + u^5 + 2u^3 - u^2 + u \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -u \\ u^3 + u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} u^6 + u^4 + 2u^2 + 1 \\ u^7 + u^5 + u^3 - u^2 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} u \\ -u^3 - u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} u^6 + u^4 + 2u^2 - u + 1 \\ u^7 + u^5 + 2u^3 - u^2 + u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} u^4 + u^2 + 1 \\ -u^4 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -u^8 - u^6 - u^4 + 1 \\ u^8 + u^7 + u^6 + 2u^5 + u^4 + 2u^3 + 2u - 1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -u^8 - u^6 - u^4 + 1 \\ u^8 + u^7 + u^6 + 2u^5 + u^4 + 2u^3 + 2u - 1 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = $4u^7 + 4u^6 + 3u^5 + 3u^4 + 6u^3 + 3u^2 - u + 1$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1, c_2	$(u - 1)^9$
c_3, c_7	u^9
c_4	$(u + 1)^9$
c_5	$u^9 - u^8 + 2u^7 - u^6 + 3u^5 - u^4 + 2u^3 + u + 1$
c_6	$u^9 + 5u^8 + 12u^7 + 15u^6 + 9u^5 - u^4 - 4u^3 - 2u^2 + u + 1$
c_8, c_{12}	$u^9 + u^8 - 2u^7 - 3u^6 + u^5 + 3u^4 + 2u^3 - u - 1$
c_9	$u^9 - 3u^8 + 8u^7 - 13u^6 + 17u^5 - 17u^4 + 12u^3 - 6u^2 + u + 1$
c_{10}	$u^9 + u^8 + 2u^7 + u^6 + 3u^5 + u^4 + 2u^3 + u - 1$
c_{11}	$u^9 + 3u^8 + 8u^7 + 13u^6 + 17u^5 + 17u^4 + 12u^3 + 6u^2 + u - 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1, c_2, c_4	$(y - 1)^9$
c_3, c_7	y^9
c_5, c_{10}	$y^9 + 3y^8 + 8y^7 + 13y^6 + 17y^5 + 17y^4 + 12y^3 + 6y^2 + y - 1$
c_6	$y^9 - y^8 + 12y^7 - 7y^6 + 37y^5 + y^4 - 10y^2 + 5y - 1$
c_8, c_{12}	$y^9 - 5y^8 + 12y^7 - 15y^6 + 9y^5 + y^4 - 4y^3 + 2y^2 + y - 1$
c_9, c_{11}	$y^9 + 7y^8 + 20y^7 + 25y^6 + 5y^5 - 15y^4 + 22y^2 + 13y - 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to I_2^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.140343 + 0.966856I$ $a = -0.770941 - 0.258974I$ $b = 0.142194 - 0.781734I$	$-3.42837 + 2.09337I$	$-5.30979 - 3.87975I$
$u = 0.140343 - 0.966856I$ $a = -0.770941 + 0.258974I$ $b = 0.142194 + 0.781734I$	$-3.42837 - 2.09337I$	$-5.30979 + 3.87975I$
$u = 0.628449 + 0.875112I$ $a = -0.147409 - 0.367985I$ $b = 0.229389 - 0.360259I$	$-1.02799 + 2.45442I$	$0.49381 - 3.35442I$
$u = 0.628449 - 0.875112I$ $a = -0.147409 + 0.367985I$ $b = 0.229389 + 0.360259I$	$-1.02799 - 2.45442I$	$0.49381 + 3.35442I$
$u = -0.796005 + 0.733148I$ $a = 0.24323 - 1.73417I$ $b = 1.07779 + 1.55873I$	$2.72642 + 1.33617I$	$1.53709 - 1.22905I$
$u = -0.796005 - 0.733148I$ $a = 0.24323 + 1.73417I$ $b = 1.07779 - 1.55873I$	$2.72642 - 1.33617I$	$1.53709 + 1.22905I$
$u = -0.728966 + 0.986295I$ $a = 1.62529 - 0.46000I$ $b = -0.73109 + 1.93833I$	$1.95319 - 7.08493I$	$0.02676 + 6.64241I$
$u = -0.728966 - 0.986295I$ $a = 1.62529 + 0.46000I$ $b = -0.73109 - 1.93833I$	$1.95319 + 7.08493I$	$0.02676 - 6.64241I$
$u = 0.512358$ $a = 1.09967$ $b = 0.563422$	-0.446489	2.50430

III. u-Polynomials

Crossings	u-Polynomials at each crossing
c_1	$((u-1)^9)(u^{35} + 52u^{34} + \dots + 32u + 1)$
c_2	$((u-1)^9)(u^{35} - 10u^{34} + \dots + 12u - 1)$
c_3, c_7	$u^9(u^{35} - u^{34} + \dots - 1024u - 512)$
c_4	$((u+1)^9)(u^{35} - 10u^{34} + \dots + 12u - 1)$
c_5	$(u^9 - u^8 + \dots + u + 1)(u^{35} - 2u^{34} + \dots - 2u^2 - 1)$
c_6	$(u^9 + 5u^8 + 12u^7 + 15u^6 + 9u^5 - u^4 - 4u^3 - 2u^2 + u + 1)$ $\cdot (u^{35} + 10u^{34} + \dots - 206u - 31)$
c_8	$(u^9 + u^8 - 2u^7 - 3u^6 + u^5 + 3u^4 + 2u^3 - u - 1)$ $\cdot (u^{35} - 2u^{34} + \dots - 412u - 241)$
c_9	$(u^9 - 3u^8 + 8u^7 - 13u^6 + 17u^5 - 17u^4 + 12u^3 - 6u^2 + u + 1)$ $\cdot (u^{35} + 12u^{34} + \dots - 4u - 1)$
c_{10}	$(u^9 + u^8 + \dots + u - 1)(u^{35} - 2u^{34} + \dots - 2u^2 - 1)$
c_{11}	$(u^9 + 3u^8 + 8u^7 + 13u^6 + 17u^5 + 17u^4 + 12u^3 + 6u^2 + u - 1)$ $\cdot (u^{35} + 12u^{34} + \dots - 4u - 1)$
c_{12}	$(u^9 + u^8 - 2u^7 - 3u^6 + u^5 + 3u^4 + 2u^3 - u - 1)$ $\cdot (u^{35} + 36u^{33} + \dots - 2u - 1)$

IV. Riley Polynomials

Crossings	Riley Polynomials at each crossing
c_1	$((y - 1)^9)(y^{35} - 128y^{34} + \dots + 420y - 1)$
c_2, c_4	$((y - 1)^9)(y^{35} - 52y^{34} + \dots + 32y - 1)$
c_3, c_7	$y^9(y^{35} + 57y^{34} + \dots + 2621440y - 262144)$
c_5, c_{10}	$(y^9 + 3y^8 + 8y^7 + 13y^6 + 17y^5 + 17y^4 + 12y^3 + 6y^2 + y - 1)$ $\cdot (y^{35} + 12y^{34} + \dots - 4y - 1)$
c_6	$(y^9 - y^8 + 12y^7 - 7y^6 + 37y^5 + y^4 - 10y^2 + 5y - 1)$ $\cdot (y^{35} + 12y^{34} + \dots - 10140y - 961)$
c_8	$(y^9 - 5y^8 + 12y^7 - 15y^6 + 9y^5 + y^4 - 4y^3 + 2y^2 + y - 1)$ $\cdot (y^{35} + 12y^{34} + \dots - 1095024y - 58081)$
c_9, c_{11}	$(y^9 + 7y^8 + 20y^7 + 25y^6 + 5y^5 - 15y^4 + 22y^2 + 13y - 1)$ $\cdot (y^{35} + 24y^{34} + \dots - 16y - 1)$
c_{12}	$(y^9 - 5y^8 + 12y^7 - 15y^6 + 9y^5 + y^4 - 4y^3 + 2y^2 + y - 1)$ $\cdot (y^{35} + 72y^{34} + \dots - 4y - 1)$