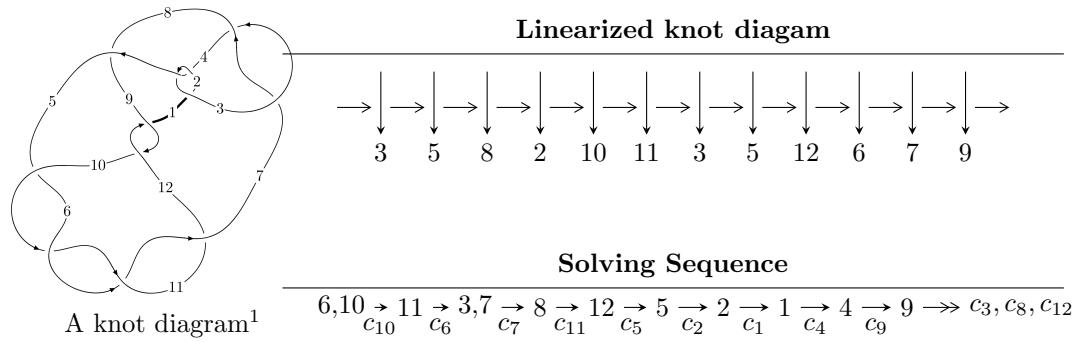


$12n_{0166} \ (K12n_{0166})$



Ideals for irreducible components² of X_{par}

$$I_1^u = \langle u^{25} - 14u^{23} + \cdots + b - 1, 2u^{25} - u^{24} + \cdots + a - 5u, u^{26} - 2u^{25} + \cdots + 3u + 1 \rangle$$

$$I_2^u = \langle u^4 - 2u^2 + b + u, -u^5 + 3u^3 + a - u + 1, u^6 + u^5 - 3u^4 - 2u^3 + 2u^2 - u - 1 \rangle$$

* 2 irreducible components of $\dim_{\mathbb{C}} = 0$, with total 32 representations.

¹The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/math/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

²All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$I_1^u = \langle u^{25} - 14u^{23} + \cdots + b - 1, \ 2u^{25} - u^{24} + \cdots + a - 5u, \ u^{26} - 2u^{25} + \cdots + 3u + 1 \rangle^{\mathbf{I}_1}$$

(i) **Arc colorings**

$$\begin{aligned} a_6 &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_{10} &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_{11} &= \begin{pmatrix} 1 \\ u^2 \end{pmatrix} \\ a_3 &= \begin{pmatrix} -2u^{25} + u^{24} + \cdots + 9u^2 + 5u \\ -u^{25} + 14u^{23} + \cdots + 4u + 1 \end{pmatrix} \\ a_7 &= \begin{pmatrix} -u \\ -u^3 + u \end{pmatrix} \\ a_8 &= \begin{pmatrix} -u^{10} + 5u^8 - 8u^6 + 5u^4 - 3u^2 + 1 \\ -u^{10} + 4u^8 - 3u^6 - 2u^4 - u^2 \end{pmatrix} \\ a_{12} &= \begin{pmatrix} -u^2 + 1 \\ -u^4 + 2u^2 \end{pmatrix} \\ a_5 &= \begin{pmatrix} u \\ u \end{pmatrix} \\ a_2 &= \begin{pmatrix} -u^{25} + u^{24} + \cdots + u - 1 \\ u^{22} - 12u^{20} + \cdots - 4u^3 - 3u^2 \end{pmatrix} \\ a_1 &= \begin{pmatrix} u^{10} - 5u^8 + 8u^6 - 5u^4 + 3u^2 - 1 \\ u^{12} - 6u^{10} + 12u^8 - 8u^6 + u^4 - 2u^2 \end{pmatrix} \\ a_4 &= \begin{pmatrix} u^{24} - 13u^{22} + \cdots - u - 1 \\ u^{25} - 14u^{23} + \cdots - 3u - 1 \end{pmatrix} \\ a_9 &= \begin{pmatrix} -u^6 + 3u^4 - 2u^2 + 1 \\ -u^8 + 4u^6 - 4u^4 \end{pmatrix} \end{aligned}$$

(ii) **Obstruction class** = -1

$$(iii) \text{ Cusp Shapes} = -4u^{25} + 5u^{24} + 51u^{23} - 62u^{22} - 269u^{21} + 312u^{20} + 760u^{19} - 813u^{18} - 1264u^{17} + 1176u^{16} + 1341u^{15} - 1013u^{14} - 1049u^{13} + 682u^{12} + 692u^{11} - 399u^{10} - 430u^9 + 65u^8 + 311u^7 - 6u^6 - 115u^5 - 18u^4 + 50u^3 + 9u^2 - 6u - 18$$

(iv) u-Polynomials at the component

| Crossings | u-Polynomials at each crossing |
|--------------------------------|--|
| c_1 | $u^{26} + 37u^{25} + \cdots + 76u + 1$ |
| c_2, c_4 | $u^{26} - 7u^{25} + \cdots - 2u - 1$ |
| c_3, c_7 | $u^{26} - u^{25} + \cdots - 128u - 64$ |
| c_5, c_6, c_{10} c_{11} | $u^{26} - 2u^{25} + \cdots + 3u + 1$ |
| c_8 | $u^{26} + 2u^{25} + \cdots + 3u + 1$ |
| c_9, c_{12} | $u^{26} - 6u^{25} + \cdots - 21u - 9$ |

(v) Riley Polynomials at the component

| Crossings | Riley Polynomials at each crossing |
|--------------------------------|--|
| c_1 | $y^{26} - 89y^{25} + \cdots - 2892y + 1$ |
| c_2, c_4 | $y^{26} - 37y^{25} + \cdots - 76y + 1$ |
| c_3, c_7 | $y^{26} - 39y^{25} + \cdots - 12288y + 4096$ |
| c_5, c_6, c_{10} c_{11} | $y^{26} - 30y^{25} + \cdots - 11y + 1$ |
| c_8 | $y^{26} - 54y^{25} + \cdots - 11y + 1$ |
| c_9, c_{12} | $y^{26} + 6y^{25} + \cdots - 531y + 81$ |

(vi) Complex Volumes and Cusp Shapes

| Solutions to I_1^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|-----------------------------|---------------------------------------|------------------------|
| $u = -0.681707 + 0.582351I$ | | |
| $a = -0.132311 + 0.107455I$ | $-10.93830 + 7.21103I$ | $-16.0759 - 5.4438I$ |
| $b = -1.80048 - 0.98897I$ | | |
| $u = -0.681707 - 0.582351I$ | | |
| $a = -0.132311 - 0.107455I$ | $-10.93830 - 7.21103I$ | $-16.0759 + 5.4438I$ |
| $b = -1.80048 + 0.98897I$ | | |
| $u = 1.175060 + 0.078346I$ | | |
| $a = 0.222046 + 0.015295I$ | $-14.2898 + 0.0080I$ | $-18.3523 + 0.3239I$ |
| $b = 1.71753 - 0.10327I$ | | |
| $u = 1.175060 - 0.078346I$ | | |
| $a = 0.222046 - 0.015295I$ | $-14.2898 - 0.0080I$ | $-18.3523 - 0.3239I$ |
| $b = 1.71753 + 0.10327I$ | | |
| $u = -0.615423 + 0.435220I$ | | |
| $a = 0.006046 + 0.650453I$ | $-1.64268 + 3.44770I$ | $-15.9366 - 6.5929I$ |
| $b = 1.43706 + 0.60644I$ | | |
| $u = -0.615423 - 0.435220I$ | | |
| $a = 0.006046 - 0.650453I$ | $-1.64268 - 3.44770I$ | $-15.9366 + 6.5929I$ |
| $b = 1.43706 - 0.60644I$ | | |
| $u = 0.492369 + 0.545154I$ | | |
| $a = 0.033687 + 0.462693I$ | $2.35945 - 1.88336I$ | $-5.73263 + 3.81073I$ |
| $b = 0.322628 + 0.025417I$ | | |
| $u = 0.492369 - 0.545154I$ | | |
| $a = 0.033687 - 0.462693I$ | $2.35945 + 1.88336I$ | $-5.73263 - 3.81073I$ |
| $b = 0.322628 - 0.025417I$ | | |
| $u = -0.265310 + 0.672765I$ | | |
| $a = 0.80138 + 1.96514I$ | $-9.70379 - 2.98173I$ | $-13.78370 + 0.17341I$ |
| $b = 0.117100 - 0.374073I$ | | |
| $u = -0.265310 - 0.672765I$ | | |
| $a = 0.80138 - 1.96514I$ | $-9.70379 + 2.98173I$ | $-13.78370 - 0.17341I$ |
| $b = 0.117100 + 0.374073I$ | | |

| Solutions to I_1^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|-----------------------------|---------------------------------------|------------------------|
| $u = 0.589835 + 0.287549I$ | $-2.66891 - 0.88385I$ | $-16.9206 + 6.0063I$ |
| $a = 0.399854 - 1.018310I$ | | |
| $b = -1.126490 + 0.098071I$ | | |
| $u = 0.589835 - 0.287549I$ | $-2.66891 + 0.88385I$ | $-16.9206 - 6.0063I$ |
| $a = 0.399854 + 1.018310I$ | | |
| $b = -1.126490 - 0.098071I$ | | |
| $u = -0.277498 + 0.391559I$ | $-0.683753 - 0.414385I$ | $-12.43905 - 0.47517I$ |
| $a = -0.71760 - 1.38397I$ | | |
| $b = -0.619638 + 0.253799I$ | | |
| $u = -0.277498 - 0.391559I$ | $-0.683753 + 0.414385I$ | $-12.43905 + 0.47517I$ |
| $a = -0.71760 + 1.38397I$ | | |
| $b = -0.619638 - 0.253799I$ | | |
| $u = 1.52883 + 0.05644I$ | $-6.94574 - 0.62089I$ | $-15.5634 - 0.9743I$ |
| $a = 0.949715 - 0.290539I$ | | |
| $b = 0.830011 + 0.081100I$ | | |
| $u = 1.52883 - 0.05644I$ | $-6.94574 + 0.62089I$ | $-15.5634 + 0.9743I$ |
| $a = 0.949715 + 0.290539I$ | | |
| $b = 0.830011 - 0.081100I$ | | |
| $u = -1.52725 + 0.15077I$ | $-4.34854 + 4.33683I$ | $-10.06939 - 2.72465I$ |
| $a = -0.741655 - 0.245504I$ | | |
| $b = -1.002680 - 0.376527I$ | | |
| $u = -1.52725 - 0.15077I$ | $-4.34854 - 4.33683I$ | $-10.06939 + 2.72465I$ |
| $a = -0.741655 + 0.245504I$ | | |
| $b = -1.002680 + 0.376527I$ | | |
| $u = -1.57781 + 0.08698I$ | $-10.09930 + 2.28663I$ | $-19.0760 - 2.3439I$ |
| $a = 2.47671 + 0.53175I$ | | |
| $b = 3.33781 + 0.79397I$ | | |
| $u = -1.57781 - 0.08698I$ | $-10.09930 - 2.28663I$ | $-19.0760 + 2.3439I$ |
| $a = 2.47671 - 0.53175I$ | | |
| $b = 3.33781 - 0.79397I$ | | |

| Solutions to I_1^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|---------------------------|---------------------------------------|----------------------|
| $u = 1.57863 + 0.12294I$ | | |
| $a = -2.06274 + 1.32680I$ | $-9.08260 - 5.47988I$ | $-18.5451 + 4.2333I$ |
| $b = -2.70573 + 0.88516I$ | | |
| $u = 1.57863 - 0.12294I$ | | |
| $a = -2.06274 - 1.32680I$ | $-9.08260 + 5.47988I$ | $-18.5451 - 4.2333I$ |
| $b = -2.70573 - 0.88516I$ | | |
| $u = 1.59730 + 0.17727I$ | | |
| $a = 2.38789 - 2.06908I$ | $-18.6017 - 10.0445I$ | $-18.6964 + 4.4096I$ |
| $b = 3.52206 - 2.02315I$ | | |
| $u = 1.59730 - 0.17727I$ | | |
| $a = 2.38789 + 2.06908I$ | $-18.6017 + 10.0445I$ | $-18.6964 - 4.4096I$ |
| $b = 3.52206 + 2.02315I$ | | |
| $u = -0.383361$ | | |
| $a = -0.709996$ | -0.582197 | -16.9580 |
| $b = -0.351806$ | | |
| $u = -1.65067$ | | |
| $a = -3.53607$ | 15.9598 | -20.6600 |
| $b = -4.70658$ | | |

II.

$$I_2^u = \langle u^4 - 2u^2 + b + u, -u^5 + 3u^3 + a - u + 1, u^6 + u^5 - 3u^4 - 2u^3 + 2u^2 - u - 1 \rangle$$

(i) **Arc colorings**

$$a_6 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} u^5 - 3u^3 + u - 1 \\ -u^4 + 2u^2 - u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -u \\ -u^3 + u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -u \\ -u^3 + u \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -u^2 + 1 \\ -u^4 + 2u^2 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} u \\ u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} u^5 - 3u^3 - 1 \\ -u^4 + 2u^2 - 2u \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -u \\ -u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} u^5 - 3u^3 + u - 1 \\ -u^4 + 2u^2 - u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} u^5 - 2u^3 - u \\ u^5 - 3u^3 + u \end{pmatrix}$$

(ii) **Obstruction class = 1**

(iii) **Cusp Shapes** = $-3u^5 - u^4 + 6u^3 + u^2 + 2u - 14$

(iv) u-Polynomials at the component

| Crossings | u-Polynomials at each crossing |
|------------------|--|
| c_1, c_2 | $(u - 1)^6$ |
| c_3, c_7 | u^6 |
| c_4 | $(u + 1)^6$ |
| c_5, c_6 | $u^6 - u^5 - 3u^4 + 2u^3 + 2u^2 + u - 1$ |
| c_8, c_{12} | $u^6 - u^5 + 3u^4 - 2u^3 + 2u^2 - u - 1$ |
| c_9 | $u^6 + u^5 + 3u^4 + 2u^3 + 2u^2 + u - 1$ |
| c_{10}, c_{11} | $u^6 + u^5 - 3u^4 - 2u^3 + 2u^2 - u - 1$ |

(v) Riley Polynomials at the component

| Crossings | Riley Polynomials at each crossing |
|--------------------------------|--|
| c_1, c_2, c_4 | $(y - 1)^6$ |
| c_3, c_7 | y^6 |
| c_5, c_6, c_{10} c_{11} | $y^6 - 7y^5 + 17y^4 - 16y^3 + 6y^2 - 5y + 1$ |
| c_8, c_9, c_{12} | $y^6 + 5y^5 + 9y^4 + 4y^3 - 6y^2 - 5y + 1$ |

(vi) Complex Volumes and Cusp Shapes

| Solutions to I_2^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|-----------------------------|---------------------------------------|----------------------|
| $u = 0.493180 + 0.575288I$ | | |
| $a = 0.504580 - 0.342767I$ | $1.31531 - 1.97241I$ | $-14.7121 + 3.8836I$ |
| $b = -0.354346 + 0.659157I$ | | |
| $u = 0.493180 - 0.575288I$ | | |
| $a = 0.504580 + 0.342767I$ | $1.31531 + 1.97241I$ | $-14.7121 - 3.8836I$ |
| $b = -0.354346 - 0.659157I$ | | |
| $u = -0.483672$ | | |
| $a = -1.17069$ | -2.38379 | -15.3880 |
| $b = 0.896823$ | | |
| $u = -1.52087 + 0.16310I$ | | |
| $a = 0.462019 + 1.043570I$ | $-5.34051 + 4.59213I$ | $-18.4963 - 3.9250I$ |
| $b = 1.11206 + 1.11328I$ | | |
| $u = -1.52087 - 0.16310I$ | | |
| $a = 0.462019 - 1.043570I$ | $-5.34051 - 4.59213I$ | $-18.4963 + 3.9250I$ |
| $b = 1.11206 - 1.11328I$ | | |
| $u = 1.53904$ | | |
| $a = -1.76250$ | -9.30502 | -18.1960 |
| $b = -2.41226$ | | |

III. u-Polynomials

| Crossings | u-Polynomials at each crossing |
|------------------|--|
| c_1 | $((u - 1)^6)(u^{26} + 37u^{25} + \dots + 76u + 1)$ |
| c_2 | $((u - 1)^6)(u^{26} - 7u^{25} + \dots - 2u - 1)$ |
| c_3, c_7 | $u^6(u^{26} - u^{25} + \dots - 128u - 64)$ |
| c_4 | $((u + 1)^6)(u^{26} - 7u^{25} + \dots - 2u - 1)$ |
| c_5, c_6 | $(u^6 - u^5 - 3u^4 + 2u^3 + 2u^2 + u - 1)(u^{26} - 2u^{25} + \dots + 3u + 1)$ |
| c_8 | $(u^6 - u^5 + 3u^4 - 2u^3 + 2u^2 - u - 1)(u^{26} + 2u^{25} + \dots + 3u + 1)$ |
| c_9 | $(u^6 + u^5 + 3u^4 + 2u^3 + 2u^2 + u - 1)(u^{26} - 6u^{25} + \dots - 21u - 9)$ |
| c_{10}, c_{11} | $(u^6 + u^5 - 3u^4 - 2u^3 + 2u^2 - u - 1)(u^{26} - 2u^{25} + \dots + 3u + 1)$ |
| c_{12} | $(u^6 - u^5 + 3u^4 - 2u^3 + 2u^2 - u - 1)(u^{26} - 6u^{25} + \dots - 21u - 9)$ |

IV. Riley Polynomials

| Crossings | Riley Polynomials at each crossing |
|--------------------------------|---|
| c_1 | $((y - 1)^6)(y^{26} - 89y^{25} + \dots - 2892y + 1)$ |
| c_2, c_4 | $((y - 1)^6)(y^{26} - 37y^{25} + \dots - 76y + 1)$ |
| c_3, c_7 | $y^6(y^{26} - 39y^{25} + \dots - 12288y + 4096)$ |
| c_5, c_6, c_{10} c_{11} | $(y^6 - 7y^5 + \dots - 5y + 1)(y^{26} - 30y^{25} + \dots - 11y + 1)$ |
| c_8 | $(y^6 + 5y^5 + \dots - 5y + 1)(y^{26} - 54y^{25} + \dots - 11y + 1)$ |
| c_9, c_{12} | $(y^6 + 5y^5 + \dots - 5y + 1)(y^{26} + 6y^{25} + \dots - 531y + 81)$ |