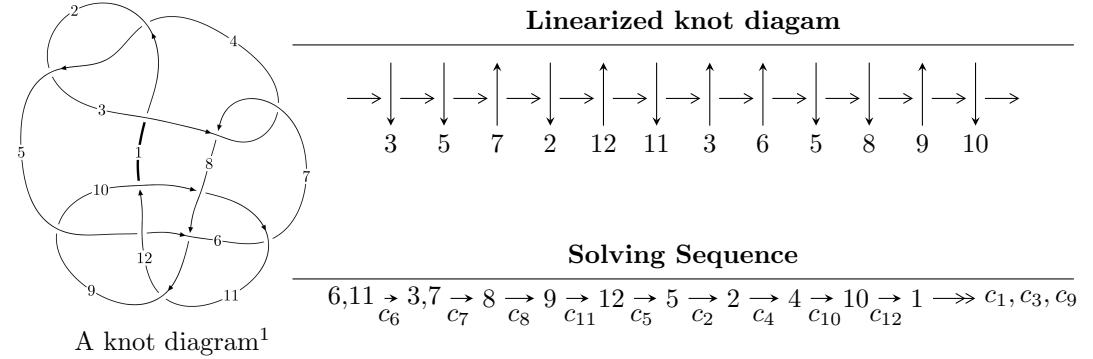


## $12n_{0173}$ ( $K12n_{0173}$ )



### Ideals for irreducible components<sup>2</sup> of $X_{\text{par}}$

$$\begin{aligned}
 I_1^u &= \langle -3.58032 \times 10^{67} u^{39} + 2.06674 \times 10^{67} u^{38} + \dots + 9.73803 \times 10^{65} b - 1.02729 \times 10^{69}, \\
 &\quad 5.45075 \times 10^{69} u^{39} - 3.75387 \times 10^{69} u^{38} + \dots + 1.65547 \times 10^{67} a + 1.34484 \times 10^{71}, u^{40} - 4u^{38} + \dots + 97u + \\
 I_2^u &= \langle 9.27676 \times 10^{169} u^{45} - 2.27749 \times 10^{170} u^{44} + \dots + 9.75406 \times 10^{172} b + 4.16059 \times 10^{173}, \\
 &\quad 9.42080 \times 10^{173} u^{45} - 2.43360 \times 10^{174} u^{44} + \dots + 2.48046 \times 10^{176} a + 3.47623 \times 10^{177}, \\
 &\quad u^{46} - 2u^{45} + \dots + 9446u + 2543 \rangle \\
 I_3^u &= \langle u^3 + 3u^2 + 4b + 2u + 1, -3u^3 - u^2 + 4a - 2u + 5, u^4 + u^2 - u + 1 \rangle \\
 I_4^u &= \langle -4u^{14} - 2u^{13} + \dots + b - 5, \\
 &\quad -2u^{14} - u^{13} + 5u^{12} - 3u^{11} - 10u^{10} + 11u^9 + 10u^8 - 14u^7 - 3u^6 + 14u^5 + u^4 - 8u^3 + u^2 + a + 3u - 1, \\
 &\quad u^{15} - 3u^{13} + 3u^{12} + 5u^{11} - 9u^{10} - 3u^9 + 12u^8 - 2u^7 - 11u^6 + 4u^5 + 7u^4 - 5u^3 - 2u^2 + 3u - 1 \rangle \\
 I_5^u &= \langle -u^5 - u^4 - 2u^3 - 2u^2 + b - u - 1, -u^5 - 2u^3 - u^2 + a - 2u - 2, u^6 + u^5 + 2u^4 + 2u^3 + 2u^2 + 2u + 1 \rangle
 \end{aligned}$$

\* 5 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 111 representations.

<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/math/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\text{I. } I_1^u = \langle -3.58 \times 10^{67}u^{39} + 2.07 \times 10^{67}u^{38} + \dots + 9.74 \times 10^{65}b - 1.03 \times 10^{69}, 5.45 \times 10^{69}u^{39} - 3.75 \times 10^{69}u^{38} + \dots + 1.66 \times 10^{67}a + 1.34 \times 10^{71}, u^{40} - 4u^{38} + \dots + 97u + 17 \rangle$$

(i) **Arc colorings**

$$\begin{aligned} a_6 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_{11} &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_3 &= \begin{pmatrix} -329.258u^{39} + 226.756u^{38} + \dots - 34572.1u - 8123.67 \\ 36.7664u^{39} - 21.2234u^{38} + \dots + 4276.56u + 1054.93 \end{pmatrix} \\ a_7 &= \begin{pmatrix} 1 \\ u^2 \end{pmatrix} \\ a_8 &= \begin{pmatrix} -79.7827u^{39} + 49.4021u^{38} + \dots - 8924.80u - 2162.21 \\ -83.0595u^{39} + 59.0553u^{38} + \dots - 8544.73u - 1992.63 \end{pmatrix} \\ a_9 &= \begin{pmatrix} -162.842u^{39} + 108.457u^{38} + \dots - 17469.5u - 4154.84 \\ -83.0595u^{39} + 59.0553u^{38} + \dots - 8544.73u - 1992.63 \end{pmatrix} \\ a_{12} &= \begin{pmatrix} -398.430u^{39} + 268.461u^{38} + \dots - 42420.9u - 10043.8 \\ -83.0595u^{39} + 59.0553u^{38} + \dots - 8544.73u - 1992.63 \end{pmatrix} \\ a_5 &= \begin{pmatrix} 8.75622u^{39} - 10.8797u^{38} + \dots + 451.374u + 56.6766 \\ -120.738u^{39} + 80.3482u^{38} + \dots - 12927.2u - 3059.02 \end{pmatrix} \\ a_2 &= \begin{pmatrix} -90.2726u^{39} + 62.6721u^{38} + \dots - 9459.34u - 2231.28 \\ 87.9281u^{39} - 59.6344u^{38} + \dots + 9289.11u + 2178.55 \end{pmatrix} \\ a_4 &= \begin{pmatrix} 136.341u^{39} - 97.9644u^{38} + \dots + 13897.5u + 3213.89 \\ -122.755u^{39} + 78.6483u^{38} + \dots - 13489.8u - 3244.38 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} -151.962u^{39} + 97.3994u^{38} + \dots - 16676.8u - 4005.99 \\ -163.408u^{39} + 112.006u^{38} + \dots - 17197.3u - 4045.18 \end{pmatrix} \\ a_1 &= \begin{pmatrix} -107.859u^{39} + 79.5764u^{38} + \dots - 10793.0u - 2477.92 \\ 152.528u^{39} - 100.948u^{38} + \dots + 16405.7u + 3896.33 \end{pmatrix} \end{aligned}$$

(ii) **Obstruction class** = -1

(iii) **Cusp Shapes** =  $-185.230u^{39} + 123.975u^{38} + \dots - 19743.3u - 4644.59$

**(iv) u-Polynomials at the component**

| Crossings        | u-Polynomials at each crossing             |
|------------------|--|
| $c_1$            | $u^{40} + 41u^{39} + \cdots + 8641u + 256$ |
| $c_2, c_4$       | $u^{40} - 7u^{39} + \cdots - 81u + 16$     |
| $c_3, c_7$       | $u^{40} - 5u^{39} + \cdots + 1632u + 256$  |
| $c_5, c_8$       | $u^{40} + u^{39} + \cdots + 2u + 1$        |
| $c_6, c_9$       | $u^{40} - 4u^{38} + \cdots - 97u + 17$     |
| $c_{10}, c_{12}$ | $u^{40} + 4u^{39} + \cdots - 3u + 1$       |
| $c_{11}$         | $u^{40} + 25u^{39} + \cdots + 36u + 4$     |

**(v) Riley Polynomials at the component**

| Crossings        | Riley Polynomials at each crossing              |
|------------------|---|
| $c_1$            | $y^{40} - 77y^{39} + \cdots - 6662529y + 65536$ |
| $c_2, c_4$       | $y^{40} - 41y^{39} + \cdots - 8641y + 256$      |
| $c_3, c_7$       | $y^{40} + 27y^{39} + \cdots - 226304y + 65536$  |
| $c_5, c_8$       | $y^{40} + 17y^{39} + \cdots + 40y + 1$          |
| $c_6, c_9$       | $y^{40} - 8y^{39} + \cdots - 4275y + 289$       |
| $c_{10}, c_{12}$ | $y^{40} - 40y^{39} + \cdots - 15y + 1$          |
| $c_{11}$         | $y^{40} - y^{39} + \cdots + 1144y + 16$         |

(vi) Complex Volumes and Cusp Shapes

| Solutions to $I_1^u$        | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape             |
|-----------------------------|---------------------------------------|------------------------|
| $u = -0.916795 + 0.271284I$ |                                       |                        |
| $a = 0.07185 - 2.25689I$    | $-4.61460 + 4.21677I$                 | $-10.36400 - 7.96016I$ |
| $b = -0.886132 - 0.556013I$ |                                       |                        |
| $u = -0.916795 - 0.271284I$ |                                       |                        |
| $a = 0.07185 + 2.25689I$    | $-4.61460 - 4.21677I$                 | $-10.36400 + 7.96016I$ |
| $b = -0.886132 + 0.556013I$ |                                       |                        |
| $u = -0.257747 + 1.059350I$ |                                       |                        |
| $a = -1.51427 + 1.70732I$   | $-2.65950 + 0.01537I$                 | $-10.44302 + 0.45727I$ |
| $b = 2.53555 - 1.59062I$    |                                       |                        |
| $u = -0.257747 - 1.059350I$ |                                       |                        |
| $a = -1.51427 - 1.70732I$   | $-2.65950 - 0.01537I$                 | $-10.44302 - 0.45727I$ |
| $b = 2.53555 + 1.59062I$    |                                       |                        |
| $u = -0.773206 + 0.447559I$ |                                       |                        |
| $a = 0.294992 - 0.155460I$  | $1.37570 + 6.93076I$                  | $-8.7508 - 11.5757I$   |
| $b = 1.237270 + 0.037085I$  |                                       |                        |
| $u = -0.773206 - 0.447559I$ |                                       |                        |
| $a = 0.294992 + 0.155460I$  | $1.37570 - 6.93076I$                  | $-8.7508 + 11.5757I$   |
| $b = 1.237270 - 0.037085I$  |                                       |                        |
| $u = 0.843869 + 0.116958I$  |                                       |                        |
| $a = 0.699504 + 0.268479I$  | $-6.65685 - 1.58265I$                 | $-10.51643 + 4.50982I$ |
| $b = -0.806806 + 0.392167I$ |                                       |                        |
| $u = 0.843869 - 0.116958I$  |                                       |                        |
| $a = 0.699504 - 0.268479I$  | $-6.65685 + 1.58265I$                 | $-10.51643 - 4.50982I$ |
| $b = -0.806806 - 0.392167I$ |                                       |                        |
| $u = -0.742457 + 0.416076I$ |                                       |                        |
| $a = -1.13504 + 1.53730I$   | $-10.74610 + 5.03761I$                | $-8.95297 - 0.57470I$  |
| $b = -0.146732 - 0.117931I$ |                                       |                        |
| $u = -0.742457 - 0.416076I$ |                                       |                        |
| $a = -1.13504 - 1.53730I$   | $-10.74610 - 5.03761I$                | $-8.95297 + 0.57470I$  |
| $b = -0.146732 + 0.117931I$ |                                       |                        |

| Solutions to $I_1^u$         | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape            |
|------------------------------|---------------------------------------|-----------------------|
| $u = -0.596745 + 1.034040I$  |                                       |                       |
| $a = 0.0958413 - 0.0250611I$ | $1.35612 + 7.74333I$                  | $9.28204 - 10.17690I$ |
| $b = 0.457567 - 0.044691I$   |                                       |                       |
| $u = -0.596745 - 1.034040I$  |                                       |                       |
| $a = 0.0958413 + 0.0250611I$ | $1.35612 - 7.74333I$                  | $9.28204 + 10.17690I$ |
| $b = 0.457567 + 0.044691I$   |                                       |                       |
| $u = 0.515825 + 1.095850I$   |                                       |                       |
| $a = 0.699738 + 0.145025I$   | $-5.33600 - 3.23521I$                 | 0                     |
| $b = -0.618119 - 0.598353I$  |                                       |                       |
| $u = 0.515825 - 1.095850I$   |                                       |                       |
| $a = 0.699738 - 0.145025I$   | $-5.33600 + 3.23521I$                 | 0                     |
| $b = -0.618119 + 0.598353I$  |                                       |                       |
| $u = 0.297740 + 0.729548I$   |                                       |                       |
| $a = -0.726912 - 0.545199I$  | $0.08293 - 1.53752I$                  | $0.71639 + 4.76389I$  |
| $b = 0.205553 + 0.589406I$   |                                       |                       |
| $u = 0.297740 - 0.729548I$   |                                       |                       |
| $a = -0.726912 + 0.545199I$  | $0.08293 + 1.53752I$                  | $0.71639 - 4.76389I$  |
| $b = 0.205553 - 0.589406I$   |                                       |                       |
| $u = 0.594134 + 0.510868I$   |                                       |                       |
| $a = -0.461994 + 0.161353I$  | $-1.25513 - 1.56952I$                 | $-2.17390 + 4.23177I$ |
| $b = 0.337579 - 0.191190I$   |                                       |                       |
| $u = 0.594134 - 0.510868I$   |                                       |                       |
| $a = -0.461994 - 0.161353I$  | $-1.25513 + 1.56952I$                 | $-2.17390 - 4.23177I$ |
| $b = 0.337579 + 0.191190I$   |                                       |                       |
| $u = -1.178420 + 0.383003I$  |                                       |                       |
| $a = -0.27016 + 1.72025I$    | $-11.7135 + 8.0385I$                  | $-13.2209 - 9.1027I$  |
| $b = 0.672757 + 0.873454I$   |                                       |                       |
| $u = -1.178420 - 0.383003I$  |                                       |                       |
| $a = -0.27016 - 1.72025I$    | $-11.7135 - 8.0385I$                  | $-13.2209 + 9.1027I$  |
| $b = 0.672757 - 0.873454I$   |                                       |                       |

| Solutions to $I_1^u$        | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape            |
|-----------------------------|---------------------------------------|-----------------------|
| $u = 0.668836 + 0.264877I$  |                                       |                       |
| $a = 0.282272 + 1.160020I$  | $-1.90192 + 1.40153I$                 | $-6.20748 - 1.19828I$ |
| $b = 0.135893 - 0.315911I$  |                                       |                       |
| $u = 0.668836 - 0.264877I$  |                                       |                       |
| $a = 0.282272 - 1.160020I$  | $-1.90192 - 1.40153I$                 | $-6.20748 + 1.19828I$ |
| $b = 0.135893 + 0.315911I$  |                                       |                       |
| $u = -0.679465 + 0.012974I$ |                                       |                       |
| $a = 0.90700 - 2.42772I$    | $-4.35694 + 0.92822I$                 | $-9.14930 + 0.28573I$ |
| $b = 0.690272 + 0.025224I$  |                                       |                       |
| $u = -0.679465 - 0.012974I$ |                                       |                       |
| $a = 0.90700 + 2.42772I$    | $-4.35694 - 0.92822I$                 | $-9.14930 - 0.28573I$ |
| $b = 0.690272 - 0.025224I$  |                                       |                       |
| $u = -0.423175 + 0.521589I$ |                                       |                       |
| $a = 1.35188 + 1.41277I$    | $-2.35252 + 0.61317I$                 | $-4.61633 + 3.05486I$ |
| $b = 1.03242 - 1.13997I$    |                                       |                       |
| $u = -0.423175 - 0.521589I$ |                                       |                       |
| $a = 1.35188 - 1.41277I$    | $-2.35252 - 0.61317I$                 | $-4.61633 - 3.05486I$ |
| $b = 1.03242 + 1.13997I$    |                                       |                       |
| $u = -0.663180 + 0.080866I$ |                                       |                       |
| $a = -0.505742 + 0.206401I$ | $2.64301 + 1.48294I$                  | $-4.81453 + 7.72547I$ |
| $b = -1.384640 - 0.132216I$ |                                       |                       |
| $u = -0.663180 - 0.080866I$ |                                       |                       |
| $a = -0.505742 - 0.206401I$ | $2.64301 - 1.48294I$                  | $-4.81453 - 7.72547I$ |
| $b = -1.384640 + 0.132216I$ |                                       |                       |
| $u = 1.31926 + 0.81503I$    |                                       |                       |
| $a = -0.254068 - 1.123980I$ | $-5.42435 - 5.89974I$                 | 0                     |
| $b = 2.08311 - 0.15702I$    |                                       |                       |
| $u = 1.31926 - 0.81503I$    |                                       |                       |
| $a = -0.254068 + 1.123980I$ | $-5.42435 + 5.89974I$                 | 0                     |
| $b = 2.08311 + 0.15702I$    |                                       |                       |

| Solutions to $I_1^u$        | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|-----------------------------|---------------------------------------|------------|
| $u = -1.33509 + 1.00004I$   |                                       |            |
| $a = -0.103766 + 0.191805I$ | $-7.28442 + 9.37900I$                 | 0          |
| $b = -1.191910 + 0.700889I$ |                                       |            |
| $u = -1.33509 - 1.00004I$   |                                       |            |
| $a = -0.103766 - 0.191805I$ | $-7.28442 - 9.37900I$                 | 0          |
| $b = -1.191910 - 0.700889I$ |                                       |            |
| $u = 1.64955 + 0.34859I$    |                                       |            |
| $a = 0.041797 + 0.918280I$  | $-14.3131 - 1.3284I$                  | 0          |
| $b = -1.41260 + 0.58964I$   |                                       |            |
| $u = 1.64955 - 0.34859I$    |                                       |            |
| $a = 0.041797 - 0.918280I$  | $-14.3131 + 1.3284I$                  | 0          |
| $b = -1.41260 - 0.58964I$   |                                       |            |
| $u = 1.25011 + 1.13972I$    |                                       |            |
| $a = 0.537152 + 1.115220I$  | $-4.50733 - 12.55940I$                | 0          |
| $b = -2.58218 + 0.30646I$   |                                       |            |
| $u = 1.25011 - 1.13972I$    |                                       |            |
| $a = 0.537152 - 1.115220I$  | $-4.50733 + 12.55940I$                | 0          |
| $b = -2.58218 - 0.30646I$   |                                       |            |
| $u = -0.82513 + 1.61273I$   |                                       |            |
| $a = 0.619679 - 0.520496I$  | $-10.55600 + 0.42655I$                | 0          |
| $b = -2.49695 + 0.94026I$   |                                       |            |
| $u = -0.82513 - 1.61273I$   |                                       |            |
| $a = 0.619679 + 0.520496I$  | $-10.55600 - 0.42655I$                | 0          |
| $b = -2.49695 - 0.94026I$   |                                       |            |
| $u = 1.25209 + 1.40579I$    |                                       |            |
| $a = -0.710628 - 0.936920I$ | $-11.2981 - 17.8760I$                 | 0          |
| $b = 2.76309 - 0.57698I$    |                                       |            |
| $u = 1.25209 - 1.40579I$    |                                       |            |
| $a = -0.710628 + 0.936920I$ | $-11.2981 + 17.8760I$                 | 0          |
| $b = 2.76309 + 0.57698I$    |                                       |            |

$$\text{III. } I_2^u = \langle 9.28 \times 10^{169} u^{45} - 2.28 \times 10^{170} u^{44} + \dots + 9.75 \times 10^{172} b + 4.16 \times 10^{173}, 9.42 \times 10^{173} u^{45} - 2.43 \times 10^{174} u^{44} + \dots + 2.48 \times 10^{176} a + 3.48 \times 10^{177}, u^{46} - 2u^{45} + \dots + 9446u + 2543 \rangle$$

(i) **Arc colorings**

$$\begin{aligned} a_6 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_{11} &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_3 &= \begin{pmatrix} -0.00379801u^{45} + 0.00981109u^{44} + \dots - 43.1222u - 14.0145 \\ -0.000951066u^{45} + 0.00233492u^{44} + \dots - 8.80677u - 4.26549 \end{pmatrix} \\ a_7 &= \begin{pmatrix} 1 \\ u^2 \end{pmatrix} \\ a_8 &= \begin{pmatrix} 0.000716237u^{45} - 0.00105546u^{44} + \dots + 4.58476u + 9.05145 \\ 0.00144541u^{45} - 0.00363803u^{44} + \dots + 12.3847u + 6.56682 \end{pmatrix} \\ a_9 &= \begin{pmatrix} 0.00216165u^{45} - 0.00469349u^{44} + \dots + 16.9695u + 15.6183 \\ 0.00144541u^{45} - 0.00363803u^{44} + \dots + 12.3847u + 6.56682 \end{pmatrix} \\ a_{12} &= \begin{pmatrix} -0.00398318u^{45} + 0.00931129u^{44} + \dots - 34.5587u - 20.7912 \\ -0.000496329u^{45} + 0.000994531u^{44} + \dots - 6.30884u - 5.67547 \end{pmatrix} \\ a_5 &= \begin{pmatrix} 0.00412015u^{45} - 0.0103795u^{44} + \dots + 41.9047u + 14.6677 \\ 0.000976621u^{45} - 0.00236780u^{44} + \dots + 11.0461u + 5.89430 \end{pmatrix} \\ a_2 &= \begin{pmatrix} -0.00289423u^{45} + 0.00709969u^{44} + \dots - 29.5330u - 10.4974 \\ -0.000537120u^{45} + 0.00126553u^{44} + \dots - 6.34240u - 3.78873 \end{pmatrix} \\ a_4 &= \begin{pmatrix} 0.00382997u^{45} - 0.00995571u^{44} + \dots + 40.6638u + 12.6470 \\ 0.00116221u^{45} - 0.00292917u^{44} + \dots + 9.48770u + 4.47069 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} -0.00461706u^{45} + 0.0113680u^{44} + \dots - 34.2999u - 16.9762 \\ 0.00113021u^{45} - 0.00305123u^{44} + \dots + 8.04999u + 1.86051 \end{pmatrix} \\ a_1 &= \begin{pmatrix} -0.00527624u^{45} + 0.0130113u^{44} + \dots - 46.7854u - 17.7735 \\ 0.000580431u^{45} - 0.00159375u^{44} + \dots + 1.15606u - 0.758198 \end{pmatrix} \end{aligned}$$

(ii) **Obstruction class** = -1

(iii) **Cusp Shapes** =  $0.00495504u^{45} - 0.00970261u^{44} + \dots + 38.8323u + 37.7445$

**(iv) u-Polynomials at the component**

| Crossings        | u-Polynomials at each crossing               |
|------------------|--|
| $c_1$            | $(u^{23} + 26u^{22} + \cdots - 7u + 1)^2$    |
| $c_2, c_4$       | $(u^{23} - 4u^{22} + \cdots - 3u - 1)^2$     |
| $c_3, c_7$       | $(u^{23} + 3u^{22} + \cdots + 36u - 8)^2$    |
| $c_5, c_8$       | $u^{46} + 6u^{45} + \cdots + 116u + 17$      |
| $c_6, c_9$       | $u^{46} + 2u^{45} + \cdots - 9446u + 2543$   |
| $c_{10}, c_{12}$ | $u^{46} - 3u^{44} + \cdots - 76140u + 32521$ |
| $c_{11}$         | $(u^{23} - 10u^{22} + \cdots + 4u^2 + 1)^2$  |

**(v) Riley Polynomials at the component**

| Crossings        | Riley Polynomials at each crossing                    |
|------------------|---|
| $c_1$            | $(y^{23} - 54y^{22} + \cdots - 215y - 1)^2$           |
| $c_2, c_4$       | $(y^{23} - 26y^{22} + \cdots - 7y - 1)^2$             |
| $c_3, c_7$       | $(y^{23} + 21y^{22} + \cdots - 48y - 64)^2$           |
| $c_5, c_8$       | $y^{46} - 10y^{45} + \cdots + 3136y + 289$            |
| $c_6, c_9$       | $y^{46} - 10y^{45} + \cdots - 111757896y + 6466849$   |
| $c_{10}, c_{12}$ | $y^{46} - 6y^{45} + \cdots + 636394872y + 1057615441$ |
| $c_{11}$         | $(y^{23} + 20y^{21} + \cdots - 8y - 1)^2$             |

(vi) Complex Volumes and Cusp Shapes

| Solutions to $I_2^u$        | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape             |
|-----------------------------|---------------------------------------|------------------------|
| $u = 0.938998 + 0.344976I$  | $-1.23158 - 3.46001I$                 | $-0.93966 + 11.94434I$ |
| $a = -2.24368 + 0.34394I$   |                                       |                        |
| $b = -2.40240 - 0.99716I$   |                                       |                        |
| $u = 0.938998 - 0.344976I$  | $-1.23158 + 3.46001I$                 | $-0.93966 - 11.94434I$ |
| $a = -2.24368 - 0.34394I$   |                                       |                        |
| $b = -2.40240 + 0.99716I$   |                                       |                        |
| $u = 0.381487 + 0.925362I$  | $0.22577 - 2.35596I$                  | $1.37102 + 5.00512I$   |
| $a = 0.036904 - 0.397055I$  |                                       |                        |
| $b = -0.308362 + 0.632471I$ |                                       |                        |
| $u = 0.381487 - 0.925362I$  | $0.22577 + 2.35596I$                  | $1.37102 - 5.00512I$   |
| $a = 0.036904 + 0.397055I$  |                                       |                        |
| $b = -0.308362 - 0.632471I$ |                                       |                        |
| $u = -0.662967 + 0.741919I$ | $0.22577 - 2.35596I$                  | $1.37102 + 5.00512I$   |
| $a = -0.882738 + 0.492316I$ |                                       |                        |
| $b = 0.019759 + 1.137980I$  |                                       |                        |
| $u = -0.662967 - 0.741919I$ | $0.22577 + 2.35596I$                  | $1.37102 - 5.00512I$   |
| $a = -0.882738 - 0.492316I$ |                                       |                        |
| $b = 0.019759 - 1.137980I$  |                                       |                        |
| $u = -0.776430 + 0.599101I$ | $-9.93186 + 9.38993I$                 | $-5.00822 - 8.89816I$  |
| $a = 0.64174 - 1.41107I$    |                                       |                        |
| $b = -0.331275 + 0.637663I$ |                                       |                        |
| $u = -0.776430 - 0.599101I$ | $-9.93186 - 9.38993I$                 | $-5.00822 + 8.89816I$  |
| $a = 0.64174 + 1.41107I$    |                                       |                        |
| $b = -0.331275 - 0.637663I$ |                                       |                        |
| $u = -0.347658 + 0.962709I$ | $3.29942$                             | $11.64034 + 0.I$       |
| $a = -0.094250 - 0.137661I$ |                                       |                        |
| $b = -0.617430 + 0.174037I$ |                                       |                        |
| $u = -0.347658 - 0.962709I$ | $3.29942$                             | $11.64034 + 0.I$       |
| $a = -0.094250 + 0.137661I$ |                                       |                        |
| $b = -0.617430 - 0.174037I$ |                                       |                        |

| Solutions to $I_2^u$        | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape             |
|-----------------------------|---------------------------------------|------------------------|
| $u = 0.363894 + 0.859272I$  |                                       |                        |
| $a = 0.961328 - 0.913318I$  | $0.07682 - 4.67687I$                  | $-2.82043 + 11.56965I$ |
| $b = 0.081085 + 0.409837I$  |                                       |                        |
| $u = 0.363894 - 0.859272I$  |                                       |                        |
| $a = 0.961328 + 0.913318I$  | $0.07682 + 4.67687I$                  | $-2.82043 - 11.56965I$ |
| $b = 0.081085 - 0.409837I$  |                                       |                        |
| $u = -0.576444 + 0.916663I$ |                                       |                        |
| $a = -3.57574 + 2.35289I$   | $-1.23158 + 3.46001I$                 | $-0.93966 - 11.94434I$ |
| $b = 3.83467 + 2.38953I$    |                                       |                        |
| $u = -0.576444 - 0.916663I$ |                                       |                        |
| $a = -3.57574 - 2.35289I$   | $-1.23158 - 3.46001I$                 | $-0.93966 + 11.94434I$ |
| $b = 3.83467 - 2.38953I$    |                                       |                        |
| $u = 0.091395 + 1.210170I$  |                                       |                        |
| $a = -0.143737 + 0.825821I$ | $-6.90053 - 6.33030I$                 | $-5.55743 + 6.60020I$  |
| $b = -0.195131 + 0.246758I$ |                                       |                        |
| $u = 0.091395 - 1.210170I$  |                                       |                        |
| $a = -0.143737 - 0.825821I$ | $-6.90053 + 6.33030I$                 | $-5.55743 - 6.60020I$  |
| $b = -0.195131 - 0.246758I$ |                                       |                        |
| $u = -0.642034 + 0.452369I$ |                                       |                        |
| $a = -0.21983 + 1.87152I$   | $-4.25470 + 2.83401I$                 | $-16.2136 - 5.6542I$   |
| $b = 1.23526 - 0.94866I$    |                                       |                        |
| $u = -0.642034 - 0.452369I$ |                                       |                        |
| $a = -0.21983 - 1.87152I$   | $-4.25470 - 2.83401I$                 | $-16.2136 + 5.6542I$   |
| $b = 1.23526 + 0.94866I$    |                                       |                        |
| $u = 0.669574 + 1.086330I$  |                                       |                        |
| $a = -0.208906 - 0.373689I$ | $0.78715 - 2.82758I$                  | $2.28819 - 1.37730I$   |
| $b = 0.927797 + 0.477174I$  |                                       |                        |
| $u = 0.669574 - 1.086330I$  |                                       |                        |
| $a = -0.208906 + 0.373689I$ | $0.78715 + 2.82758I$                  | $2.28819 + 1.37730I$   |
| $b = 0.927797 - 0.477174I$  |                                       |                        |

| Solutions to $I_2^u$        | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape             |
|-----------------------------|---------------------------------------|------------------------|
| $u = -1.046560 + 0.783431I$ |                                       |                        |
| $a = 0.59848 - 1.43771I$    | $-12.8626 + 6.8428I$                  | $-11.21020 - 4.32033I$ |
| $b = -1.59045 + 0.05140I$   |                                       |                        |
| $u = -1.046560 - 0.783431I$ |                                       |                        |
| $a = 0.59848 + 1.43771I$    | $-12.8626 - 6.8428I$                  | $-11.21020 + 4.32033I$ |
| $b = -1.59045 - 0.05140I$   |                                       |                        |
| $u = 0.625428 + 0.116207I$  |                                       |                        |
| $a = -0.714645 + 0.198843I$ | $-5.87167 + 0.65487I$                 | $-18.5419 - 8.9539I$   |
| $b = 1.353840 - 0.397532I$  |                                       |                        |
| $u = 0.625428 - 0.116207I$  |                                       |                        |
| $a = -0.714645 - 0.198843I$ | $-5.87167 - 0.65487I$                 | $-18.5419 + 8.9539I$   |
| $b = 1.353840 + 0.397532I$  |                                       |                        |
| $u = -0.548542 + 0.193866I$ |                                       |                        |
| $a = -0.45786 + 1.86963I$   | $-2.99002 + 3.94578I$                 | $-4.9106 - 15.5031I$   |
| $b = -0.184586 - 1.004710I$ |                                       |                        |
| $u = -0.548542 - 0.193866I$ |                                       |                        |
| $a = -0.45786 - 1.86963I$   | $-2.99002 - 3.94578I$                 | $-4.9106 + 15.5031I$   |
| $b = -0.184586 + 1.004710I$ |                                       |                        |
| $u = -1.24048 + 0.78112I$   |                                       |                        |
| $a = -0.03322 - 1.87174I$   | $0.07682 + 4.67687I$                  | $0. - 11.56965I$       |
| $b = -3.56571 - 0.92903I$   |                                       |                        |
| $u = -1.24048 - 0.78112I$   |                                       |                        |
| $a = -0.03322 + 1.87174I$   | $0.07682 - 4.67687I$                  | $0. + 11.56965I$       |
| $b = -3.56571 + 0.92903I$   |                                       |                        |
| $u = 0.467204 + 0.217984I$  |                                       |                        |
| $a = 1.94284 + 2.82388I$    | $-4.75468 - 2.62879I$                 | $-2.77736 + 1.99528I$  |
| $b = -0.202604 - 0.456157I$ |                                       |                        |
| $u = 0.467204 - 0.217984I$  |                                       |                        |
| $a = 1.94284 - 2.82388I$    | $-4.75468 + 2.62879I$                 | $-2.77736 - 1.99528I$  |
| $b = -0.202604 + 0.456157I$ |                                       |                        |

| Solutions to $I_2^u$         | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape           |
|------------------------------|---------------------------------------|----------------------|
| $u = -0.428413 + 0.172818I$  |                                       |                      |
| $a = 3.71471 - 1.22148I$     | $0.78715 + 2.82758I$                  | $2.28819 + 1.37730I$ |
| $b = 0.621273 - 1.245390I$   |                                       |                      |
| $u = -0.428413 - 0.172818I$  |                                       |                      |
| $a = 3.71471 + 1.22148I$     | $0.78715 - 2.82758I$                  | $2.28819 - 1.37730I$ |
| $b = 0.621273 + 1.245390I$   |                                       |                      |
| $u = 0.35071 + 1.65209I$     |                                       |                      |
| $a = 0.0912328 + 0.0808853I$ | $-4.75468 - 2.62879I$                 | 0                    |
| $b = -0.29070 - 1.43919I$    |                                       |                      |
| $u = 0.35071 - 1.65209I$     |                                       |                      |
| $a = 0.0912328 - 0.0808853I$ | $-4.75468 + 2.62879I$                 | 0                    |
| $b = -0.29070 + 1.43919I$    |                                       |                      |
| $u = -1.85979 + 1.16230I$    |                                       |                      |
| $a = -0.246221 + 0.939586I$  | $-6.90053 + 6.33030I$                 | 0                    |
| $b = 3.32130 + 1.56395I$     |                                       |                      |
| $u = -1.85979 - 1.16230I$    |                                       |                      |
| $a = -0.246221 - 0.939586I$  | $-6.90053 - 6.33030I$                 | 0                    |
| $b = 3.32130 - 1.56395I$     |                                       |                      |
| $u = 1.70741 + 1.40554I$     |                                       |                      |
| $a = 0.358502 + 0.842210I$   | $-4.25470 + 2.83401I$                 | 0                    |
| $b = -3.51166 + 1.04732I$    |                                       |                      |
| $u = 1.70741 - 1.40554I$     |                                       |                      |
| $a = 0.358502 - 0.842210I$   | $-4.25470 - 2.83401I$                 | 0                    |
| $b = -3.51166 - 1.04732I$    |                                       |                      |
| $u = 1.43109 + 1.69613I$     |                                       |                      |
| $a = 0.593848 + 0.717598I$   | $-9.93186 - 9.38993I$                 | 0                    |
| $b = -3.15094 + 0.70927I$    |                                       |                      |
| $u = 1.43109 - 1.69613I$     |                                       |                      |
| $a = 0.593848 - 0.717598I$   | $-9.93186 + 9.38993I$                 | 0                    |
| $b = -3.15094 - 0.70927I$    |                                       |                      |

| Solutions to $I_2^u$        | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|-----------------------------|---------------------------------------|------------|
| $u = 1.76806 + 1.35630I$    |                                       |            |
| $a = -0.392722 - 0.812608I$ | $-2.99002 - 3.94578I$                 | 0          |
| $b = 2.93041 - 1.33454I$    |                                       |            |
| $u = 1.76806 - 1.35630I$    |                                       |            |
| $a = -0.392722 + 0.812608I$ | $-2.99002 + 3.94578I$                 | 0          |
| $b = 2.93041 + 1.33454I$    |                                       |            |
| $u = 2.24798 + 0.96891I$    |                                       |            |
| $a = -0.049286 - 0.718312I$ | $-12.8626 + 6.8428I$                  | 0          |
| $b = 3.40524 - 1.44518I$    |                                       |            |
| $u = 2.24798 - 0.96891I$    |                                       |            |
| $a = -0.049286 + 0.718312I$ | $-12.8626 - 6.8428I$                  | 0          |
| $b = 3.40524 + 1.44518I$    |                                       |            |
| $u = -1.91392 + 1.52870I$   |                                       |            |
| $a = 0.405621 - 0.097399I$  | $-5.87167 + 0.65487I$                 | 0          |
| $b = 1.62062 - 2.87145I$    |                                       |            |
| $u = -1.91392 - 1.52870I$   |                                       |            |
| $a = 0.405621 + 0.097399I$  | $-5.87167 - 0.65487I$                 | 0          |
| $b = 1.62062 + 2.87145I$    |                                       |            |

$$\text{III. } I_3^u = \langle u^3 + 3u^2 + 4b + 2u + 1, -3u^3 - u^2 + 4a - 2u + 5, u^4 + u^2 - u + 1 \rangle$$

(i) Arc colorings

$$a_6 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} \frac{3}{4}u^3 + \frac{1}{4}u^2 + \frac{1}{2}u - \frac{5}{4} \\ -\frac{1}{4}u^3 - \frac{3}{4}u^2 - \frac{1}{2}u - \frac{1}{4} \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} u^2 + 1 \\ u^2 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} u^3 + u^2 \\ u^2 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -u^3 \\ -u^2 + u - 1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} \frac{7}{4}u^3 + \frac{1}{4}u^2 + \frac{1}{2}u - \frac{5}{4} \\ -\frac{1}{4}u^3 + \frac{1}{4}u^2 - \frac{3}{2}u + \frac{3}{4} \end{pmatrix}$$

$$a_4 = \begin{pmatrix} \frac{3}{4}u^3 + \frac{1}{4}u^2 + \frac{1}{2}u - \frac{5}{4} \\ -\frac{1}{4}u^3 - \frac{3}{4}u^2 - \frac{1}{2}u - \frac{1}{4} \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} u \\ u^3 + u \end{pmatrix}$$

$$a_1 = \begin{pmatrix} u^3 \\ u^2 - u + 1 \end{pmatrix}$$

(ii) Obstruction class = 1

$$(iii) \text{ Cusp Shapes} = \frac{39}{16}u^3 + \frac{77}{16}u^2 + \frac{19}{8}u - \frac{149}{16}$$

**(iv) u-Polynomials at the component**

| Crossings             | u-Polynomials at each crossing |
|-----------------------|--------------------------------|
| $c_1, c_2$            | $(u - 1)^4$                    |
| $c_3, c_7$            | $u^4$                          |
| $c_4$                 | $(u + 1)^4$                    |
| $c_5$                 | $u^4 + 2u^3 + 3u^2 + u + 1$    |
| $c_6$                 | $u^4 + u^2 - u + 1$            |
| $c_8$                 | $u^4 - 2u^3 + 3u^2 - u + 1$    |
| $c_9, c_{10}, c_{12}$ | $u^4 + u^2 + u + 1$            |
| $c_{11}$              | $u^4 + 3u^3 + 4u^2 + 3u + 2$   |

**(v) Riley Polynomials at the component**

| Crossings                      | Riley Polynomials at each crossing |
|--------------------------------|------------------------------------|
| $c_1, c_2, c_4$                | $(y - 1)^4$                        |
| $c_3, c_7$                     | $y^4$                              |
| $c_5, c_8$                     | $y^4 + 2y^3 + 7y^2 + 5y + 1$       |
| $c_6, c_9, c_{10}$<br>$c_{12}$ | $y^4 + 2y^3 + 3y^2 + y + 1$        |
| $c_{11}$                       | $y^4 - y^3 + 2y^2 + 7y + 4$        |

**(vi) Complex Volumes and Cusp Shapes**

| Solutions to $I_3^u$        | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape             |
|-----------------------------|---------------------------------------|------------------------|
| $u = 0.547424 + 0.585652I$  |                                       |                        |
| $a = -1.28654 + 0.69736I$   | $-2.62503 - 1.39709I$                 | $-9.19395 + 5.27044I$  |
| $b = -0.391417 - 0.855136I$ |                                       |                        |
| $u = 0.547424 - 0.585652I$  |                                       |                        |
| $a = -1.28654 - 0.69736I$   | $-2.62503 + 1.39709I$                 | $-9.19395 - 5.27044I$  |
| $b = -0.391417 + 0.855136I$ |                                       |                        |
| $u = -0.547424 + 1.120870I$ |                                       |                        |
| $a = -0.338459 - 0.046758I$ | $0.98010 + 7.64338I$                  | $-10.58730 - 4.22005I$ |
| $b = 0.266417 + 0.460085I$  |                                       |                        |
| $u = -0.547424 - 1.120870I$ |                                       |                        |
| $a = -0.338459 + 0.046758I$ | $0.98010 - 7.64338I$                  | $-10.58730 + 4.22005I$ |
| $b = 0.266417 - 0.460085I$  |                                       |                        |

$$I_4^u = \langle -4u^{14} - 2u^{13} + \dots + b - 5, -2u^{14} - u^{13} + \dots + a - 1, u^{15} - 3u^{13} + \dots + 3u - 1 \rangle$$

(i) Arc colorings

$$\begin{aligned} a_6 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_{11} &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_3 &= \begin{pmatrix} 2u^{14} + u^{13} + \dots - 3u + 1 \\ 4u^{14} + 2u^{13} + \dots - 11u + 5 \end{pmatrix} \\ a_7 &= \begin{pmatrix} 1 \\ u^2 \end{pmatrix} \\ a_8 &= \begin{pmatrix} u \\ -u^{14} + 3u^{12} + \dots + 2u - 3 \end{pmatrix} \\ a_9 &= \begin{pmatrix} -u^{14} + 3u^{12} + \dots + 3u - 3 \\ -u^{14} + 3u^{12} + \dots + 2u - 3 \end{pmatrix} \\ a_{12} &= \begin{pmatrix} u^{14} - 3u^{12} + \dots - 4u + 3 \\ u^{14} - 3u^{12} + \dots - 2u + 3 \end{pmatrix} \\ a_5 &= \begin{pmatrix} 3u^{14} + u^{13} + \dots - 11u + 6 \\ 3u^{14} + u^{13} + \dots - 11u + 7 \end{pmatrix} \\ a_2 &= \begin{pmatrix} 2u^{14} - 6u^{12} + \dots - 6u + 4 \\ 3u^{14} + u^{13} + \dots - 9u + 6 \end{pmatrix} \\ a_4 &= \begin{pmatrix} 5u^{14} + 3u^{13} + \dots - 13u + 5 \\ 4u^{14} + 2u^{13} + \dots - 14u + 7 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} u^3 \\ 0 \end{pmatrix} \\ a_1 &= \begin{pmatrix} u^{14} - 3u^{12} + \dots - 4u + 3 \\ u^{14} - 3u^{12} + \dots - 2u + 3 \end{pmatrix} \end{aligned}$$

(ii) Obstruction class = 1

$$(iii) \text{ Cusp Shapes} = -9u^{14} - 12u^{13} + 18u^{12} + 3u^{11} - 57u^{10} + 9u^9 + 81u^8 - 23u^7 - 69u^6 + 49u^5 + 71u^4 - 33u^3 - 20u^2 + 30u - 2$$

**(iv) u-Polynomials at the component**

| Crossings        | u-Polynomials at each crossing         |
|------------------|--|
| $c_1$            | $u^{15} - 14u^{14} + \cdots + 27u - 1$ |
| $c_2$            | $u^{15} + 4u^{14} + \cdots + 5u - 1$   |
| $c_3$            | $u^{15} - 2u^{14} + \cdots + u - 1$    |
| $c_4$            | $u^{15} - 4u^{14} + \cdots + 5u + 1$   |
| $c_5, c_8$       | $u^{15} - 3u^{14} + \cdots + 3u^2 - 1$ |
| $c_6, c_9$       | $u^{15} - 3u^{13} + \cdots + 3u - 1$   |
| $c_7$            | $u^{15} + 2u^{14} + \cdots + u + 1$    |
| $c_{10}, c_{12}$ | $u^{15} + 6u^{14} + \cdots + 5u + 1$   |
| $c_{11}$         | $u^{15} - 9u^{14} + \cdots - 3u^2 + 1$ |

**(v) Riley Polynomials at the component**

| Crossings        | Riley Polynomials at each crossing      |
|------------------|---|
| $c_1$            | $y^{15} - 22y^{14} + \cdots + 247y - 1$ |
| $c_2, c_4$       | $y^{15} - 14y^{14} + \cdots + 27y - 1$  |
| $c_3, c_7$       | $y^{15} + 6y^{14} + \cdots - 21y - 1$   |
| $c_5, c_8$       | $y^{15} - 5y^{14} + \cdots + 6y - 1$    |
| $c_6, c_9$       | $y^{15} - 6y^{14} + \cdots + 5y - 1$    |
| $c_{10}, c_{12}$ | $y^{15} + 2y^{14} + \cdots - 15y - 1$   |
| $c_{11}$         | $y^{15} - y^{14} + \cdots + 6y - 1$     |

(vi) Complex Volumes and Cusp Shapes

| Solutions to $I_4^u$  | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape            |
|---|---------------------------------------|-----------------------|
| $u = -0.705269 + 0.671023I$<br>$a = -1.91716 - 4.45800I$<br>$b = -4.32167 + 1.98193I$   | $-0.66574 + 3.66922I$                 | $-23.4278 - 4.1308I$  |
| $u = -0.705269 - 0.671023I$<br>$a = -1.91716 + 4.45800I$<br>$b = -4.32167 - 1.98193I$   | $-0.66574 - 3.66922I$                 | $-23.4278 + 4.1308I$  |
| $u = 0.705292 + 0.773370I$<br>$a = -1.49935 - 0.52629I$<br>$b = 0.711264 - 1.062020I$   | $0.41822 - 3.68052I$                  | $-1.64123 + 6.14138I$ |
| $u = 0.705292 - 0.773370I$<br>$a = -1.49935 + 0.52629I$<br>$b = 0.711264 + 1.062020I$   | $0.41822 + 3.68052I$                  | $-1.64123 - 6.14138I$ |
| $u = -1.095560 + 0.159935I$<br>$a = 0.03742 - 1.42622I$<br>$b = -0.305259 - 0.223093I$  | $-3.30273 + 3.15661I$                 | $-6.01525 - 3.84939I$ |
| $u = -1.095560 - 0.159935I$<br>$a = 0.03742 + 1.42622I$<br>$b = -0.305259 + 0.223093I$  | $-3.30273 - 3.15661I$                 | $-6.01525 + 3.84939I$ |
| $u = 1.13479$<br>$a = 0.0880681$<br>$b = -1.41713$                                      | $-5.52469$                            | $-6.90180$            |
| $u = 0.655711 + 0.316603I$<br>$a = 0.319019 - 0.248033I$<br>$b = 1.361690 - 0.044903I$  | $2.79458 - 1.83819I$                  | $3.69149 + 10.41016I$ |
| $u = 0.655711 - 0.316603I$<br>$a = 0.319019 + 0.248033I$<br>$b = 1.361690 + 0.044903I$  | $2.79458 + 1.83819I$                  | $3.69149 - 10.41016I$ |
| $u = 0.713404 + 1.059640I$<br>$a = 0.846522 + 0.167681I$<br>$b = -0.686002 - 0.092107I$ | $-5.32622 - 4.02081I$                 | $-6.72360 + 8.77622I$ |

| Solutions to $I_4^u$        | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape            |
|-----------------------------|---------------------------------------|-----------------------|
| $u = 0.713404 - 1.059640I$  |                                       |                       |
| $a = 0.846522 - 0.167681I$  | $-5.32622 + 4.02081I$                 | $-6.72360 - 8.77622I$ |
| $b = -0.686002 + 0.092107I$ |                                       |                       |
| $u = 0.461092 + 0.464467I$  |                                       |                       |
| $a = -0.605558 + 0.197442I$ | $1.69267 - 6.59893I$                  | $3.21319 + 0.18543I$  |
| $b = -1.113150 + 0.171029I$ |                                       |                       |
| $u = 0.461092 - 0.464467I$  |                                       |                       |
| $a = -0.605558 - 0.197442I$ | $1.69267 + 6.59893I$                  | $3.21319 - 0.18543I$  |
| $b = -1.113150 - 0.171029I$ |                                       |                       |
| $u = -1.302070 + 0.416047I$ |                                       |                       |
| $a = -0.224921 + 1.360520I$ | $-10.94270 + 7.51080I$                | $-5.14589 - 4.08277I$ |
| $b = 0.561688 + 0.716944I$  |                                       |                       |
| $u = -1.302070 - 0.416047I$ |                                       |                       |
| $a = -0.224921 - 1.360520I$ | $-10.94270 - 7.51080I$                | $-5.14589 + 4.08277I$ |
| $b = 0.561688 - 0.716944I$  |                                       |                       |

$$\mathbf{V. } I_5^u = \langle -u^5 - u^4 - 2u^3 - 2u^2 + b - u - 1, -u^5 - 2u^3 - u^2 + a - 2u - 2, u^6 + u^5 + 2u^4 + 2u^3 + 2u^2 + 2u + 1 \rangle$$

(i) **Arc colorings**

$$\begin{aligned} a_6 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_{11} &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_3 &= \begin{pmatrix} u^5 + 2u^3 + u^2 + 2u + 2 \\ u^5 + u^4 + 2u^3 + 2u^2 + u + 1 \end{pmatrix} \\ a_7 &= \begin{pmatrix} 1 \\ u^2 \end{pmatrix} \\ a_8 &= \begin{pmatrix} 1 \\ u^2 \end{pmatrix} \\ a_9 &= \begin{pmatrix} u^2 + 1 \\ u^2 \end{pmatrix} \\ a_{12} &= \begin{pmatrix} u^5 + 2u^3 + u \\ u^5 + u^3 + u \end{pmatrix} \\ a_5 &= \begin{pmatrix} -2u^5 - 3u^3 - u^2 - 2u - 1 \\ -2u^5 - u^4 - 3u^3 - 2u^2 - 3u - 2 \end{pmatrix} \\ a_2 &= \begin{pmatrix} 3u^5 + 5u^3 + 2u^2 + 4u + 3 \\ 3u^5 + 2u^4 + 5u^3 + 4u^2 + 4u + 3 \end{pmatrix} \\ a_4 &= \begin{pmatrix} u^5 + 2u^3 + u^2 + 2u + 2 \\ u^5 + u^4 + 2u^3 + 2u^2 + u + 1 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} u \\ u^3 + u \end{pmatrix} \\ a_1 &= \begin{pmatrix} 2u^5 + 3u^3 + u^2 + 2u + 1 \\ 2u^5 + u^4 + 3u^3 + 2u^2 + 3u + 2 \end{pmatrix} \end{aligned}$$

(ii) **Obstruction class = 1**

(iii) **Cusp Shapes** =  $u^5 + 2u^3 + u^2 + 2u - 3$

**(iv) u-Polynomials at the component**

| Crossings             | u-Polynomials at each crossing            |
|-----------------------|---|
| $c_1, c_2$            | $(u - 1)^6$                               |
| $c_3, c_7$            | $u^6$                                     |
| $c_4$                 | $(u + 1)^6$                               |
| $c_5$                 | $u^6 + 3u^5 + 4u^4 + 2u^3 + 1$            |
| $c_6$                 | $u^6 + u^5 + 2u^4 + 2u^3 + 2u^2 + 2u + 1$ |
| $c_8$                 | $u^6 - 3u^5 + 4u^4 - 2u^3 + 1$            |
| $c_9, c_{10}, c_{12}$ | $u^6 - u^5 + 2u^4 - 2u^3 + 2u^2 - 2u + 1$ |
| $c_{11}$              | $(u^3 - u^2 + 1)^2$                       |

**(v) Riley Polynomials at the component**

| Crossings                      | Riley Polynomials at each crossing   |
|--------------------------------|--------------------------------------|
| $c_1, c_2, c_4$                | $(y - 1)^6$                          |
| $c_3, c_7$                     | $y^6$                                |
| $c_5, c_8$                     | $y^6 - y^5 + 4y^4 - 2y^3 + 8y^2 + 1$ |
| $c_6, c_9, c_{10}$<br>$c_{12}$ | $y^6 + 3y^5 + 4y^4 + 2y^3 + 1$       |
| $c_{11}$                       | $(y^3 - y^2 + 2y - 1)^2$             |

(vi) Complex Volumes and Cusp Shapes

| Solutions to $I_5^u$        | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape            |
|-----------------------------|---------------------------------------|-----------------------|
| $u = 0.498832 + 1.001300I$  | $-1.37919 - 2.82812I$                 | $-4.21508 + 1.30714I$ |
| $a = 0.78492 + 1.30714I$    |                                       |                       |
| $b = -1.89744 - 0.20118I$   |                                       |                       |
| $u = 0.498832 - 1.001300I$  | $-1.37919 + 2.82812I$                 | $-4.21508 - 1.30714I$ |
| $a = 0.78492 - 1.30714I$    |                                       |                       |
| $b = -1.89744 + 0.20118I$   |                                       |                       |
| $u = -0.284920 + 1.115140I$ | 2.75839                               | $-4.56984 + 0.I$      |
| $a = 0.430160$              |                                       |                       |
| $b = -0.500000 - 0.273346I$ |                                       |                       |
| $u = -0.284920 - 1.115140I$ | 2.75839                               | $-4.56984 + 0.I$      |
| $a = 0.430160$              |                                       |                       |
| $b = -0.500000 + 0.273346I$ |                                       |                       |
| $u = -0.713912 + 0.305839I$ | $-1.37919 - 2.82812I$                 | $-4.21508 + 1.30714I$ |
| $a = 0.78492 + 1.30714I$    |                                       |                       |
| $b = 0.897438 + 0.201182I$  |                                       |                       |
| $u = -0.713912 - 0.305839I$ | $-1.37919 + 2.82812I$                 | $-4.21508 - 1.30714I$ |
| $a = 0.78492 - 1.30714I$    |                                       |                       |
| $b = 0.897438 - 0.201182I$  |                                       |                       |

## VI. u-Polynomials

| Crossings        | u-Polynomials at each crossing  |
|------------------|---|
| $c_1$            | $((u - 1)^{10})(u^{15} - 14u^{14} + \dots + 27u - 1)(u^{23} + 26u^{22} + \dots - 7u + 1)^2$<br>$\cdot (u^{40} + 41u^{39} + \dots + 8641u + 256)$  |
| $c_2$            | $((u - 1)^{10})(u^{15} + 4u^{14} + \dots + 5u - 1)(u^{23} - 4u^{22} + \dots - 3u - 1)^2$<br>$\cdot (u^{40} - 7u^{39} + \dots - 81u + 16)$   |
| $c_3$            | $u^{10}(u^{15} - 2u^{14} + \dots + u - 1)(u^{23} + 3u^{22} + \dots + 36u - 8)^2$<br>$\cdot (u^{40} - 5u^{39} + \dots + 1632u + 256)$  |
| $c_4$            | $((u + 1)^{10})(u^{15} - 4u^{14} + \dots + 5u + 1)(u^{23} - 4u^{22} + \dots - 3u - 1)^2$<br>$\cdot (u^{40} - 7u^{39} + \dots - 81u + 16)$   |
| $c_5$            | $(u^4 + 2u^3 + 3u^2 + u + 1)(u^6 + 3u^5 + 4u^4 + 2u^3 + 1)$<br>$\cdot (u^{15} - 3u^{14} + \dots + 3u^2 - 1)(u^{40} + u^{39} + \dots + 2u + 1)$<br>$\cdot (u^{46} + 6u^{45} + \dots + 116u + 17)$        |
| $c_6$            | $(u^4 + u^2 - u + 1)(u^6 + u^5 + 2u^4 + 2u^3 + 2u^2 + 2u + 1)$<br>$\cdot (u^{15} - 3u^{13} + \dots + 3u - 1)(u^{40} - 4u^{38} + \dots - 97u + 17)$<br>$\cdot (u^{46} + 2u^{45} + \dots - 9446u + 2543)$ |
| $c_7$            | $u^{10}(u^{15} + 2u^{14} + \dots + u + 1)(u^{23} + 3u^{22} + \dots + 36u - 8)^2$<br>$\cdot (u^{40} - 5u^{39} + \dots + 1632u + 256)$  |
| $c_8$            | $(u^4 - 2u^3 + 3u^2 - u + 1)(u^6 - 3u^5 + 4u^4 - 2u^3 + 1)$<br>$\cdot (u^{15} - 3u^{14} + \dots + 3u^2 - 1)(u^{40} + u^{39} + \dots + 2u + 1)$<br>$\cdot (u^{46} + 6u^{45} + \dots + 116u + 17)$        |
| $c_9$            | $(u^4 + u^2 + u + 1)(u^6 - u^5 + 2u^4 - 2u^3 + 2u^2 - 2u + 1)$<br>$\cdot (u^{15} - 3u^{13} + \dots + 3u - 1)(u^{40} - 4u^{38} + \dots - 97u + 17)$<br>$\cdot (u^{46} + 2u^{45} + \dots - 9446u + 2543)$ |
| $c_{10}, c_{12}$ | $(u^4 + u^2 + u + 1)(u^6 - u^5 + 2u^4 - 2u^3 + 2u^2 - 2u + 1)$<br>$\cdot (u^{15} + 6u^{14} + \dots + 5u + 1)(u^{40} + 4u^{39} + \dots - 3u + 1)$<br>$\cdot (u^{46} - 3u^{44} + \dots - 76140u + 32521)$ |
| $c_{11}$         | $((u^3 - u^2 + 1)^2)(u^4 + 3u^3 + \dots + 3u + 2)(u^{15} - 9u^{14} + \dots - 3u^2 + 1)$<br>$\cdot ((u^{23} - 10u^{22} + \dots + 4u^2 + 1)^2)(u^{40} + 25u^{39} + \dots + 36u + 4)$                      |

## VII. Riley Polynomials

| Crossings        | Riley Polynomials at each crossing   |
|------------------|--|
| $c_1$            | $((y - 1)^{10})(y^{15} - 22y^{14} + \dots + 247y - 1)$<br>$\cdot (y^{23} - 54y^{22} + \dots - 215y - 1)^2$<br>$\cdot (y^{40} - 77y^{39} + \dots - 6662529y + 65536)$   |
| $c_2, c_4$       | $((y - 1)^{10})(y^{15} - 14y^{14} + \dots + 27y - 1)(y^{23} - 26y^{22} + \dots - 7y - 1)^2$<br>$\cdot (y^{40} - 41y^{39} + \dots - 8641y + 256)$   |
| $c_3, c_7$       | $y^{10}(y^{15} + 6y^{14} + \dots - 21y - 1)(y^{23} + 21y^{22} + \dots - 48y - 64)^2$<br>$\cdot (y^{40} + 27y^{39} + \dots - 226304y + 65536)$  |
| $c_5, c_8$       | $(y^4 + 2y^3 + 7y^2 + 5y + 1)(y^6 - y^5 + 4y^4 - 2y^3 + 8y^2 + 1)$<br>$\cdot (y^{15} - 5y^{14} + \dots + 6y - 1)(y^{40} + 17y^{39} + \dots + 40y + 1)$<br>$\cdot (y^{46} - 10y^{45} + \dots + 3136y + 289)$      |
| $c_6, c_9$       | $(y^4 + 2y^3 + 3y^2 + y + 1)(y^6 + 3y^5 + 4y^4 + 2y^3 + 1)$<br>$\cdot (y^{15} - 6y^{14} + \dots + 5y - 1)(y^{40} - 8y^{39} + \dots - 4275y + 289)$<br>$\cdot (y^{46} - 10y^{45} + \dots - 111757896y + 6466849)$ |
| $c_{10}, c_{12}$ | $(y^4 + 2y^3 + 3y^2 + y + 1)(y^6 + 3y^5 + 4y^4 + 2y^3 + 1)$<br>$\cdot (y^{15} + 2y^{14} + \dots - 15y - 1)(y^{40} - 40y^{39} + \dots - 15y + 1)$<br>$\cdot (y^{46} - 6y^{45} + \dots + 636394872y + 1057615441)$ |
| $c_{11}$         | $((y^3 - y^2 + 2y - 1)^2)(y^4 - y^3 + 2y^2 + 7y + 4)(y^{15} - y^{14} + \dots + 6y - 1)$<br>$\cdot ((y^{23} + 20y^{21} + \dots - 8y - 1)^2)(y^{40} - y^{39} + \dots + 1144y + 16)$                                |