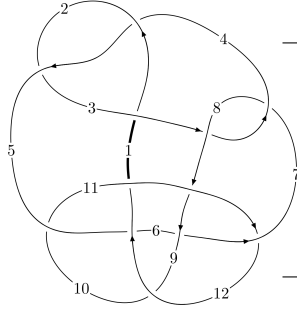
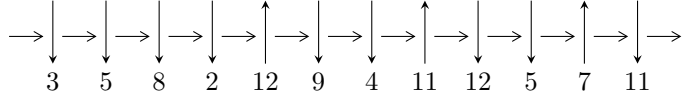


12n<sub>0176</sub> (K12n<sub>0176</sub>)



A knot diagram<sup>1</sup>

**Linearized knot diagram**



**Solving Sequence**

$$4,7 \xrightarrow{c_7} 8,11 \xrightarrow{c_8} 9 \xrightarrow{c_{11}} 12 \xrightarrow{c_{12}} 1 \xrightarrow{c_3} 3 \xrightarrow{c_1} 2 \xrightarrow{c_6} 6 \xrightarrow{c_5} 5 \xrightarrow{c_{10}} 10 \twoheadrightarrow c_2, c_4, c_9$$

**Ideals for irreducible components<sup>2</sup> of  $X_{\text{par}}$**

$$I_1^u = \langle 3.05361 \times 10^{37} u^{37} - 6.31699 \times 10^{37} u^{36} + \dots + 7.79069 \times 10^{38} b - 1.45053 \times 10^{39}, \\ 6.57951 \times 10^{37} u^{37} - 1.30883 \times 10^{38} u^{36} + \dots + 7.79069 \times 10^{38} a + 3.29567 \times 10^{39}, u^{38} - 2u^{37} + \dots - 16u + 1 \rangle$$

$$I_2^u = \langle -u^{11} - 2u^9 - 2u^7 + u^3 + b, -u^{11} + u^{10} - 3u^9 + 3u^8 - 4u^7 + 5u^6 - 2u^5 + 4u^4 + u^3 + 2u^2 + a + u + 1, \\ u^{12} + 3u^{10} + 5u^8 + 4u^6 + 2u^4 + u^2 + 1 \rangle$$

$$I_3^u = \langle -a^2 u^2 - 4a^2 u - 2a^2 + b + 4u + 2, -4a^2 u^2 + a^3 - 2a^2 u + 16u^2 a - 6a^2 + 7au - 8u^2 + 27a - 3u - 15, \\ u^3 + u^2 + 2u + 1 \rangle$$

$$I_1^v = \langle a, -2v^3 - 3v^2 + 4b - 8v - 3, 2v^4 + v^3 + 5v^2 - v + 1 \rangle$$

\* 4 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 63 representations.

<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\mathbf{I. } I_1^u = \langle 3.05 \times 10^{37} u^{37} - 6.32 \times 10^{37} u^{36} + \dots + 7.79 \times 10^{38} b - 1.45 \times 10^{39}, 6.58 \times 10^{37} u^{37} - 1.31 \times 10^{38} u^{36} + \dots + 7.79 \times 10^{38} a + 3.30 \times 10^{39}, u^{38} - 2u^{37} + \dots - 16u + 64 \rangle$$

(i) Arc colorings

$$a_4 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -0.0844535u^{37} + 0.168000u^{36} + \dots - 5.59244u - 4.23026 \\ -0.0391956u^{37} + 0.0810838u^{36} + \dots - 11.2341u + 1.86188 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -0.0835952u^{37} + 0.174732u^{36} + \dots - 10.9131u + 0.727986 \\ 0.0870239u^{37} - 0.136889u^{36} + \dots + 10.6763u + 8.29286 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -0.123649u^{37} + 0.249084u^{36} + \dots - 16.8266u - 2.36838 \\ -0.0391956u^{37} + 0.0810838u^{36} + \dots - 11.2341u + 1.86188 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -0.100768u^{37} + 0.165433u^{36} + \dots - 8.51486u - 7.59481 \\ -0.0261741u^{37} + 0.0152352u^{36} + \dots - 1.41664u - 8.18193 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} u \\ u^3 + u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -0.0775401u^{37} + 0.125316u^{36} + \dots - 7.03756u - 7.83004 \\ -0.0160423u^{37} - 0.00551256u^{36} + \dots - 1.32448u - 8.82286 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -0.199765u^{37} + 0.392882u^{36} + \dots - 29.9030u - 7.71626 \\ -0.0575627u^{37} + 0.156935u^{36} + \dots - 18.3766u + 7.51449 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -0.0221640u^{37} + 0.0480035u^{36} + \dots - 1.22673u + 2.89771 \\ 0.0786038u^{37} - 0.117429u^{36} + \dots + 7.28813u + 10.4925 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0.0238166u^{37} - 0.105781u^{36} + \dots + 18.0697u - 10.6973 \\ 0.0874152u^{37} - 0.224299u^{36} + \dots + 22.3080u - 6.95902 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes =  $-0.284536u^{37} + 0.695784u^{36} + \dots - 86.8413u + 36.9834$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1$	$u^{38} + 16u^{37} + \dots + 49u + 16$
$c_2, c_4$	$u^{38} - 4u^{37} + \dots - 35u + 4$
$c_3, c_7$	$u^{38} - 2u^{37} + \dots - 16u + 64$
$c_5$	$u^{38} + 4u^{37} + \dots - 28u + 49$
$c_6, c_{10}$	$u^{38} - 2u^{37} + \dots + 42u + 9$
$c_8$	$u^{38} + 14u^{37} + \dots + 95422u + 43691$
$c_9$	$u^{38} - 8u^{37} + \dots + 235720u + 204268$
$c_{11}$	$u^{38} - 2u^{37} + \dots + 18u + 9$
$c_{12}$	$u^{38} + 2u^{37} + \dots - 576u + 81$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1$	$y^{38} + 16y^{37} + \dots + 137023y + 256$
$c_2, c_4$	$y^{38} - 16y^{37} + \dots - 49y + 16$
$c_3, c_7$	$y^{38} + 24y^{37} + \dots + 78592y + 4096$
$c_5$	$y^{38} - 92y^{37} + \dots - 3136y + 2401$
$c_6, c_{10}$	$y^{38} + 58y^{37} + \dots + 2304y + 81$
$c_8$	$y^{38} - 48y^{37} + \dots - 15294799908y + 1908903481$
$c_9$	$y^{38} + 70y^{37} + \dots + 426020361080y + 41725415824$
$c_{11}$	$y^{38} + 2y^{37} + \dots - 576y + 81$
$c_{12}$	$y^{38} + 82y^{37} + \dots + 166536y + 6561$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.988171 + 0.101317I$ $a = 0.357719 + 0.096343I$ $b = -0.706300 - 0.532125I$	$0.60571 + 3.27765I$	$-3.71492 - 6.11137I$
$u = 0.988171 - 0.101317I$ $a = 0.357719 - 0.096343I$ $b = -0.706300 + 0.532125I$	$0.60571 - 3.27765I$	$-3.71492 + 6.11137I$
$u = -0.859103 + 0.407305I$ $a = 0.195881 + 0.507732I$ $b = -0.415895 - 0.161770I$	$-0.113764 - 0.661154I$	$-3.22428 + 0.50932I$
$u = -0.859103 - 0.407305I$ $a = 0.195881 - 0.507732I$ $b = -0.415895 + 0.161770I$	$-0.113764 + 0.661154I$	$-3.22428 - 0.50932I$
$u = -0.057356 + 0.905930I$ $a = 0.690281 - 0.347775I$ $b = -0.294609 - 0.999645I$	$-0.317569 + 1.038530I$	$-6.65259 - 1.29718I$
$u = -0.057356 - 0.905930I$ $a = 0.690281 + 0.347775I$ $b = -0.294609 + 0.999645I$	$-0.317569 - 1.038530I$	$-6.65259 + 1.29718I$
$u = 0.513402 + 1.056580I$ $a = -0.548129 - 0.950989I$ $b = 0.629901 - 0.115553I$	$4.15976 - 1.13418I$	$1.31812 + 0.91951I$
$u = 0.513402 - 1.056580I$ $a = -0.548129 + 0.950989I$ $b = 0.629901 + 0.115553I$	$4.15976 + 1.13418I$	$1.31812 - 0.91951I$
$u = 0.499541 + 1.066880I$ $a = 0.678051 + 0.671685I$ $b = -0.123848 + 1.082220I$	$-1.77296 - 5.49964I$	$-11.19640 + 5.85708I$
$u = 0.499541 - 1.066880I$ $a = 0.678051 - 0.671685I$ $b = -0.123848 - 1.082220I$	$-1.77296 + 5.49964I$	$-11.19640 - 5.85708I$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.636697 + 0.515733I$		
$a = 1.48373 + 1.08936I$	$-3.49167 + 1.02692I$	$-15.5440 - 0.4261I$
$b = 0.050362 + 0.915692I$		
$u = 0.636697 - 0.515733I$		
$a = 1.48373 - 1.08936I$	$-3.49167 - 1.02692I$	$-15.5440 + 0.4261I$
$b = 0.050362 - 0.915692I$		
$u = -0.632708 + 1.049740I$		
$a = -0.318350 + 0.929181I$	$1.72214 + 6.04516I$	$-1.25225 - 6.03705I$
$b = 0.386295 + 0.336655I$		
$u = -0.632708 - 1.049740I$		
$a = -0.318350 - 0.929181I$	$1.72214 - 6.04516I$	$-1.25225 + 6.03705I$
$b = 0.386295 - 0.336655I$		
$u = -0.116308 + 0.741636I$		
$a = -1.59041 + 2.36341I$	$-1.04131 - 1.37519I$	$-0.70276 + 2.28236I$
$b = 0.483477 - 0.463055I$		
$u = -0.116308 - 0.741636I$		
$a = -1.59041 - 2.36341I$	$-1.04131 + 1.37519I$	$-0.70276 - 2.28236I$
$b = 0.483477 + 0.463055I$		
$u = -0.120470 + 1.245000I$		
$a = 1.85282 + 0.54192I$	$8.23228 + 3.92903I$	$-3.32062 - 2.35045I$
$b = -1.07360 - 1.05803I$		
$u = -0.120470 - 1.245000I$		
$a = 1.85282 - 0.54192I$	$8.23228 - 3.92903I$	$-3.32062 + 2.35045I$
$b = -1.07360 + 1.05803I$		
$u = 1.330860 + 0.099817I$		
$a = -0.271191 - 0.510477I$	$10.21150 - 1.13879I$	$-3.05135 - 0.25663I$
$b = 1.14380 - 1.00359I$		
$u = 1.330860 - 0.099817I$		
$a = -0.271191 + 0.510477I$	$10.21150 + 1.13879I$	$-3.05135 + 0.25663I$
$b = 1.14380 + 1.00359I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.316680 + 0.320236I$ $a = -0.223799 - 0.516251I$ $b = 1.05336 - 1.13298I$	$9.76921 - 6.87392I$	$-3.78751 + 4.34762I$
$u = -1.316680 - 0.320236I$ $a = -0.223799 + 0.516251I$ $b = 1.05336 + 1.13298I$	$9.76921 + 6.87392I$	$-3.78751 - 4.34762I$
$u = -0.20211 + 1.41718I$ $a = -1.355950 - 0.243842I$ $b = 0.995463 + 0.570318I$	$6.08307 + 2.78224I$	$0. - 2.28655I$
$u = -0.20211 - 1.41718I$ $a = -1.355950 + 0.243842I$ $b = 0.995463 - 0.570318I$	$6.08307 - 2.78224I$	$0. + 2.28655I$
$u = -0.072001 + 0.547844I$ $a = -0.238648 - 0.632863I$ $b = 0.790221 - 0.913835I$	$5.57535 - 2.98438I$	$5.83310 - 0.97501I$
$u = -0.072001 - 0.547844I$ $a = -0.238648 + 0.632863I$ $b = 0.790221 + 0.913835I$	$5.57535 + 2.98438I$	$5.83310 + 0.97501I$
$u = 0.52721 + 1.38450I$ $a = -1.43906 - 0.13679I$ $b = 0.974228 - 0.765508I$	$4.71055 - 8.92356I$	$-6.00000 + 7.15584I$
$u = 0.52721 - 1.38450I$ $a = -1.43906 + 0.13679I$ $b = 0.974228 + 0.765508I$	$4.71055 + 8.92356I$	$-6.00000 - 7.15584I$
$u = -0.194741 + 0.457992I$ $a = 0.933635 - 0.070105I$ $b = -0.245714 - 0.786744I$	$-0.451389 + 1.231000I$	$-5.01122 - 5.21291I$
$u = -0.194741 - 0.457992I$ $a = 0.933635 + 0.070105I$ $b = -0.245714 + 0.786744I$	$-0.451389 - 1.231000I$	$-5.01122 + 5.21291I$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.74805 + 1.38740I$ $a = 1.46219 - 0.60021I$ $b = -0.96971 - 1.27489I$	$13.1525 + 14.1820I$	0
$u = -0.74805 - 1.38740I$ $a = 1.46219 + 0.60021I$ $b = -0.96971 + 1.27489I$	$13.1525 - 14.1820I$	0
$u = 0.53207 + 1.50578I$ $a = 1.45703 + 0.26277I$ $b = -1.06014 + 1.24087I$	$15.4688 - 7.6978I$	0
$u = 0.53207 - 1.50578I$ $a = 1.45703 - 0.26277I$ $b = -1.06014 - 1.24087I$	$15.4688 + 7.6978I$	0
$u = 0.64254 + 1.50454I$ $a = 0.570332 + 0.670108I$ $b = -1.32203 - 0.83464I$	$14.6938 - 5.9617I$	0
$u = 0.64254 - 1.50454I$ $a = 0.570332 - 0.670108I$ $b = -1.32203 + 0.83464I$	$14.6938 + 5.9617I$	0
$u = -0.35097 + 1.60847I$ $a = 0.866365 - 0.578189I$ $b = -1.29525 + 0.97186I$	$16.4349 - 0.8014I$	0
$u = -0.35097 - 1.60847I$ $a = 0.866365 + 0.578189I$ $b = -1.29525 - 0.97186I$	$16.4349 + 0.8014I$	0



$$\text{II. } I_2^u = \langle -u^{11} - 2u^9 - 2u^7 + u^3 + b, -u^{11} + u^{10} + \dots + a + 1, u^{12} + 3u^{10} + 5u^8 + 4u^6 + 2u^4 + u^2 + 1 \rangle$$

(i) Arc colorings

$$a_4 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} u^{11} - u^{10} + 3u^9 - 3u^8 + 4u^7 - 5u^6 + 2u^5 - 4u^4 - u^3 - 2u^2 - u - 1 \\ u^{11} + 2u^9 + 2u^7 - u^3 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 2u^{11} - u^{10} + 5u^9 - 3u^8 + 6u^7 - 5u^6 + 2u^5 - 4u^4 - 2u^3 - 3u^2 - u - 1 \\ u^{11} + 2u^9 + 2u^7 - u^3 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 2u^{11} - u^{10} + 5u^9 - 3u^8 + 6u^7 - 5u^6 + 2u^5 - 4u^4 - 2u^3 - 2u^2 - u - 1 \\ u^{11} + 2u^9 + 2u^7 - u^3 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} u^{11} + 2u^9 + 2u^7 - u^3 \\ 0 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} u \\ u^3 + u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -u^7 - 2u^5 - 2u^3 \\ -u^7 - u^5 + u \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -u^{11} - u^{10} - 4u^9 - 3u^8 - 6u^7 - 5u^6 - 5u^5 - 4u^4 - u^3 - 2u^2 + 2 \\ 1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} u^9 + 2u^7 + 3u^5 + 2u^3 + u \\ u^{11} + 3u^9 + 4u^7 + 3u^5 + u^3 + u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} u^{11} - u^{10} + 3u^9 - 3u^8 + 4u^7 - 5u^6 + 2u^5 - 4u^4 - u^3 - u^2 - u \\ u^{11} + 2u^9 + 2u^7 - u^3 + u^2 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes =  $4u^{10} + 12u^8 + 16u^6 + 8u^4 - 4$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1$	$(u^6 - 3u^5 + 5u^4 - 4u^3 + 2u^2 - u + 1)^2$
$c_2$	$(u^6 + u^5 - u^4 - 2u^3 + u + 1)^2$
$c_3, c_7$	$u^{12} + 3u^{10} + 5u^8 + 4u^6 + 2u^4 + u^2 + 1$
$c_4$	$(u^6 - u^5 - u^4 + 2u^3 - u + 1)^2$
$c_5$	$u^{12} - 6u^{11} + \dots - 24u + 9$
$c_6, c_{10}, c_{11}$	$(u^2 + 1)^6$
$c_8$	$u^{12} + 12u^{11} + \dots + 60u + 9$
$c_9$	$u^{12} - u^{10} + 5u^8 + 6u^4 - 3u^2 + 1$
$c_{12}$	$(u + 1)^{12}$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1$	$(y^6 + y^5 + 5y^4 + 6y^2 + 3y + 1)^2$
$c_2, c_4$	$(y^6 - 3y^5 + 5y^4 - 4y^3 + 2y^2 - y + 1)^2$
$c_3, c_7$	$(y^6 + 3y^5 + 5y^4 + 4y^3 + 2y^2 + y + 1)^2$
$c_5$	$y^{12} + 14y^{11} + \dots + 108y + 81$
$c_6, c_{10}, c_{11}$	$(y + 1)^{12}$
$c_8$	$y^{12} - 14y^{11} + \dots - 108y + 81$
$c_9$	$(y^6 - y^5 + 5y^4 + 6y^2 - 3y + 1)^2$
$c_{12}$	$(y - 1)^{12}$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.295542 + 1.002190I$ $a = -0.272397 - 0.266417I$ $b = 1.000000I$	$1.89061 - 0.92430I$	$-2.28328 + 0.79423I$
$u = 0.295542 - 1.002190I$ $a = -0.272397 + 0.266417I$ $b = -1.000000I$	$1.89061 + 0.92430I$	$-2.28328 - 0.79423I$
$u = -0.295542 + 1.002190I$ $a = -1.26642 + 0.72760I$ $b = 1.000000I$	$1.89061 + 0.92430I$	$-2.28328 - 0.79423I$
$u = -0.295542 - 1.002190I$ $a = -1.26642 - 0.72760I$ $b = -1.000000I$	$1.89061 - 0.92430I$	$-2.28328 + 0.79423I$
$u = 0.664531 + 0.428243I$ $a = -0.79605 - 3.11811I$ $b = -1.000000I$	$-1.89061 + 0.92430I$	$-9.71672 - 0.79423I$
$u = 0.664531 - 0.428243I$ $a = -0.79605 + 3.11811I$ $b = 1.000000I$	$-1.89061 - 0.92430I$	$-9.71672 + 0.79423I$
$u = -0.664531 + 0.428243I$ $a = 2.11811 - 0.20395I$ $b = -1.000000I$	$-1.89061 - 0.92430I$	$-9.71672 + 0.79423I$
$u = -0.664531 - 0.428243I$ $a = 2.11811 + 0.20395I$ $b = 1.000000I$	$-1.89061 + 0.92430I$	$-9.71672 - 0.79423I$
$u = 0.558752 + 1.073950I$ $a = -0.95037 - 1.16713I$ $b = -1.000000I$	$-5.69302I$	$-6.00000 + 5.51057I$
$u = 0.558752 - 1.073950I$ $a = -0.95037 + 1.16713I$ $b = 1.000000I$	$5.69302I$	$-6.00000 - 5.51057I$

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.558752 + 1.073950I$		
$a = 0.167130 - 0.049626I$	$5.69302I$	$-6.00000 - 5.51057I$
$b = -1.000000I$		
$u = -0.558752 - 1.073950I$		
$a = 0.167130 + 0.049626I$	$-5.69302I$	$-6.00000 + 5.51057I$
$b = 1.000000I$		

$$\text{III. } I_3^u = \langle -a^2u^2 - 4a^2u - 2a^2 + b + 4u + 2, -4a^2u^2 + 16u^2a + \cdots + 27a - 15, u^3 + u^2 + 2u + 1 \rangle$$

(i) Arc colorings

$$a_4 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} a \\ a^2u^2 + 4a^2u + 2a^2 - 4u - 2 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} a^2u^2 + 4a^2u + 2a^2 + a - 4u - 2 \\ a^2u^2 + 4a^2u + 2a^2 - 4u - 2 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} a^2u^2 + 4a^2u + 2a^2 + a - 4u - 2 \\ a^2u^2 + 4a^2u + 2a^2 - 4u - 2 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} u \\ -u^2 - u - 1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} u^2 + 1 \\ u^2 + u + 1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -a^2u^2 + u^2a + a \\ -a^2u^2 - 4a^2u + u^2a - 2a^2 + 4u + 2 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} a^2u^2 + 4a^2u + 2a^2 + a - 4u - 2 \\ a^2u^2 + 4a^2u + 2a^2 - 4u - 2 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes =  $-4u^2 - 4u - 10$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_3, c_7$	$(u^3 + u^2 + 2u + 1)^3$
$c_2, c_4$	$(u^3 - u^2 + 1)^3$
$c_5, c_6, c_{10}$ $c_{11}$	$u^9 + 3u^7 - 3u^6 + 3u^5 - 6u^4 + 3u^3 - 3u^2 + 2u + 1$
$c_8$	$u^9 - 6u^8 + 15u^7 - 15u^6 - 5u^5 + 24u^4 - 9u^3 - 15u^2 + 10u + 1$
$c_9$	$u^9$
$c_{12}$	$u^9 + 6u^8 + 15u^7 + 15u^6 - 5u^5 - 24u^4 - 9u^3 + 15u^2 + 10u - 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_3, c_7$	$(y^3 + 3y^2 + 2y - 1)^3$
$c_2, c_4$	$(y^3 - y^2 + 2y - 1)^3$
$c_5, c_6, c_{10}$ $c_{11}$	$y^9 + 6y^8 + 15y^7 + 15y^6 - 5y^5 - 24y^4 - 9y^3 + 15y^2 + 10y - 1$
$c_8, c_{12}$	$y^9 - 6y^8 + \dots + 130y - 1$
$c_9$	$y^9$



(vi) Complex Volumes and Cusp Shapes

Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.215080 + 1.307140I$ $a = -0.933500 + 0.242758I$ $b = 0.550542 - 1.200360I$	$3.02413 + 2.82812I$	$-2.49024 - 2.97945I$
$u = -0.215080 + 1.307140I$ $a = 1.036610 - 0.079466I$ $b = -0.929255 - 0.157692I$	$3.02413 + 2.82812I$	$-2.49024 - 2.97945I$
$u = -0.215080 + 1.307140I$ $a = -1.182710 + 0.201873I$ $b = 0.378713 + 1.358050I$	$3.02413 + 2.82812I$	$-2.49024 - 2.97945I$
$u = -0.215080 - 1.307140I$ $a = -0.933500 - 0.242758I$ $b = 0.550542 + 1.200360I$	$3.02413 - 2.82812I$	$-2.49024 + 2.97945I$
$u = -0.215080 - 1.307140I$ $a = 1.036610 + 0.079466I$ $b = -0.929255 + 0.157692I$	$3.02413 - 2.82812I$	$-2.49024 + 2.97945I$
$u = -0.215080 - 1.307140I$ $a = -1.182710 - 0.201873I$ $b = 0.378713 - 1.358050I$	$3.02413 - 2.82812I$	$-2.49024 + 2.97945I$
$u = -0.569840$ $a = 0.644489$ $b = 0.298201$	$-1.11345$	$-9.01950$
$u = -0.569840$ $a = 2.75735 + 4.12910I$ $b = -0.149100 + 1.032810I$	$-1.11345$	$-9.01950$
$u = -0.569840$ $a = 2.75735 - 4.12910I$ $b = -0.149100 - 1.032810I$	$-1.11345$	$-9.01950$

$$\text{IV. } I_1^v = \langle a, -2v^3 - 3v^2 + 4b - 8v - 3, 2v^4 + v^3 + 5v^2 - v + 1 \rangle$$

(i) Arc colorings

$$a_4 = \begin{pmatrix} v \\ 0 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0 \\ \frac{1}{2}v^3 + \frac{3}{4}v^2 + 2v + \frac{3}{4} \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ -\frac{3}{2}v^3 - \frac{5}{4}v^2 - \frac{7}{2}v + \frac{1}{4} \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} \frac{1}{2}v^3 + \frac{3}{4}v^2 + 2v + \frac{3}{4} \\ \frac{1}{2}v^3 + \frac{3}{4}v^2 + 2v + \frac{3}{4} \end{pmatrix}$$

$$a_1 = \begin{pmatrix} \frac{1}{2}v^3 + \frac{3}{4}v^2 + 2v + \frac{3}{4} \\ 2v^3 + v^2 + 5v - 1 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} v \\ 0 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} \frac{1}{2}v^3 + \frac{3}{4}v^2 + 3v + \frac{3}{4} \\ 2v^3 + v^2 + 5v - 1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} \frac{3}{2}v^3 + \frac{5}{4}v^2 + \frac{7}{2}v + \frac{3}{4} \\ v^2 + \frac{1}{2}v + \frac{5}{2} \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -\frac{1}{2}v^3 - \frac{3}{4}v^2 - 2v - \frac{3}{4} \\ -2v^3 - v^2 - 5v + 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} \frac{3}{2}v^3 + \frac{1}{4}v^2 + 3v - \frac{7}{4} \\ -v^2 - \frac{1}{2}v - \frac{5}{2} \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes =  $-6v^3 - 4v^2 - 12v - 10$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_2$	$(u - 1)^4$
$c_3, c_7$	$u^4$
$c_4$	$(u + 1)^4$
$c_5$	$u^4 + 5u^3 + 7u^2 + 2u + 1$
$c_6$	$u^4 - u^3 + 3u^2 - 2u + 1$
$c_8$	$u^4 - u^3 + u^2 + 1$
$c_9$	$u^4 + u^3 + 5u^2 - u + 2$
$c_{10}, c_{12}$	$u^4 + u^3 + 3u^2 + 2u + 1$
$c_{11}$	$u^4 + u^3 + u^2 + 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_4$	$(y - 1)^4$
$c_3, c_7$	$y^4$
$c_5$	$y^4 - 11y^3 + 31y^2 + 10y + 1$
$c_6, c_{10}, c_{12}$	$y^4 + 5y^3 + 7y^2 + 2y + 1$
$c_8, c_{11}$	$y^4 + y^3 + 3y^2 + 2y + 1$
$c_9$	$y^4 + 9y^3 + 31y^2 + 19y + 4$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^v$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$v = 0.130534 + 0.427872I$	$5.14581 + 3.16396I$	$-10.48546 - 5.24252I$
$a = 0$		
$b = 0.851808 + 0.911292I$		
$v = 0.130534 - 0.427872I$	$5.14581 - 3.16396I$	$-10.48546 + 5.24252I$
$a = 0$		
$b = 0.851808 - 0.911292I$		
$v = -0.38053 + 1.53420I$	$-1.85594 - 1.41510I$	$-12.38954 + 3.92814I$
$a = 0$		
$b = -0.351808 + 0.720342I$		
$v = -0.38053 - 1.53420I$	$-1.85594 + 1.41510I$	$-12.38954 - 3.92814I$
$a = 0$		
$b = -0.351808 - 0.720342I$		

## V. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1$	$(u-1)^4(u^3+u^2+2u+1)^3(u^6-3u^5+5u^4-4u^3+2u^2-u+1)^2$ $\cdot (u^{38}+16u^{37}+\dots+49u+16)$
$c_2$	$(u-1)^4(u^3-u^2+1)^3(u^6+u^5-u^4-2u^3+u+1)^2$ $\cdot (u^{38}-4u^{37}+\dots-35u+4)$
$c_3, c_7$	$u^4(u^3+u^2+2u+1)^3(u^{12}+3u^{10}+5u^8+4u^6+2u^4+u^2+1)$ $\cdot (u^{38}-2u^{37}+\dots-16u+64)$
$c_4$	$(u+1)^4(u^3-u^2+1)^3(u^6-u^5-u^4+2u^3-u+1)^2$ $\cdot (u^{38}-4u^{37}+\dots-35u+4)$
$c_5$	$(u^4+5u^3+7u^2+2u+1)$ $\cdot (u^9+3u^7-3u^6+3u^5-6u^4+3u^3-3u^2+2u+1)$ $\cdot (u^{12}-6u^{11}+\dots-24u+9)(u^{38}+4u^{37}+\dots-28u+49)$
$c_6$	$(u^2+1)^6(u^4-u^3+3u^2-2u+1)$ $\cdot (u^9+3u^7-3u^6+3u^5-6u^4+3u^3-3u^2+2u+1)$ $\cdot (u^{38}-2u^{37}+\dots+42u+9)$
$c_8$	$(u^4-u^3+u^2+1)$ $\cdot (u^9-6u^8+15u^7-15u^6-5u^5+24u^4-9u^3-15u^2+10u+1)$ $\cdot (u^{12}+12u^{11}+\dots+60u+9)(u^{38}+14u^{37}+\dots+95422u+43691)$
$c_9$	$u^9(u^4+u^3+5u^2-u+2)(u^{12}-u^{10}+5u^8+6u^4-3u^2+1)$ $\cdot (u^{38}-8u^{37}+\dots+235720u+204268)$
$c_{10}$	$(u^2+1)^6(u^4+u^3+3u^2+2u+1)$ $\cdot (u^9+3u^7-3u^6+3u^5-6u^4+3u^3-3u^2+2u+1)$ $\cdot (u^{38}-2u^{37}+\dots+42u+9)$
$c_{11}$	$(u^2+1)^6(u^4+u^3+u^2+1)$ $\cdot (u^9+3u^7-3u^6+3u^5-6u^4+3u^3-3u^2+2u+1)$ $\cdot (u^{38}-2u^{37}+\dots+18u+9)$
$c_{12}$	$(u+1)^{12}(u^4+u^3+3u^2+2u+1)$ $\cdot (u^9+6u^8+15u^7+15u^6-5u^5-24u^4-9u^3+15u^2+10u-1)$ $\cdot (u^{38}+2u^{37}+\dots-576u+81)$

## VI. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1$	$(y-1)^4(y^3+3y^2+2y-1)^3(y^6+y^5+5y^4+6y^2+3y+1)^2$ $\cdot (y^{38}+16y^{37}+\dots+137023y+256)$
$c_2, c_4$	$(y-1)^4(y^3-y^2+2y-1)^3(y^6-3y^5+5y^4-4y^3+2y^2-y+1)^2$ $\cdot (y^{38}-16y^{37}+\dots-49y+16)$
$c_3, c_7$	$y^4(y^3+3y^2+2y-1)^3(y^6+3y^5+5y^4+4y^3+2y^2+y+1)^2$ $\cdot (y^{38}+24y^{37}+\dots+78592y+4096)$
$c_5$	$(y^4-11y^3+31y^2+10y+1)$ $\cdot (y^9+6y^8+15y^7+15y^6-5y^5-24y^4-9y^3+15y^2+10y-1)$ $\cdot (y^{12}+14y^{11}+\dots+108y+81)(y^{38}-92y^{37}+\dots-3136y+2401)$
$c_6, c_{10}$	$(y+1)^{12}(y^4+5y^3+7y^2+2y+1)$ $\cdot (y^9+6y^8+15y^7+15y^6-5y^5-24y^4-9y^3+15y^2+10y-1)$ $\cdot (y^{38}+58y^{37}+\dots+2304y+81)$
$c_8$	$(y^4+y^3+3y^2+2y+1)(y^9-6y^8+\dots+130y-1)$ $\cdot (y^{12}-14y^{11}+\dots-108y+81)$ $\cdot (y^{38}-48y^{37}+\dots-15294799908y+1908903481)$
$c_9$	$y^9(y^4+9y^3+31y^2+19y+4)(y^6-y^5+5y^4+6y^2-3y+1)^2$ $\cdot (y^{38}+70y^{37}+\dots+426020361080y+41725415824)$
$c_{11}$	$(y+1)^{12}(y^4+y^3+3y^2+2y+1)$ $\cdot (y^9+6y^8+15y^7+15y^6-5y^5-24y^4-9y^3+15y^2+10y-1)$ $\cdot (y^{38}+2y^{37}+\dots-576y+81)$
$c_{12}$	$((y-1)^{12})(y^4+5y^3+\dots+2y+1)(y^9-6y^8+\dots+130y-1)$ $\cdot (y^{38}+82y^{37}+\dots+166536y+6561)$