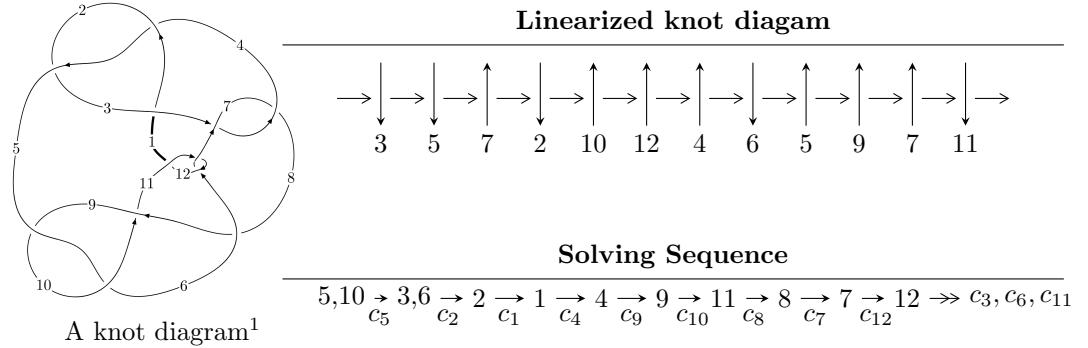


$12n_{0184}$  ( $K12n_{0184}$ )



Ideals for irreducible components<sup>2</sup> of  $X_{\text{par}}$

$$\begin{aligned}
 I_1^u &= \langle -4.91771 \times 10^{36} u^{41} - 1.79820 \times 10^{38} u^{40} + \dots + 2.88772 \times 10^{39} b + 4.22720 \times 10^{39}, \\
 &\quad 9.16076 \times 10^{39} u^{41} - 6.73128 \times 10^{39} u^{40} + \dots + 4.90913 \times 10^{40} a + 8.21058 \times 10^{40}, u^{42} - 2u^{41} + \dots + 16u - \\
 I_2^u &= \langle b + 1, -2u^8 + u^7 + 5u^6 - 3u^5 - 4u^4 + 3u^3 - 2u^2 + a + 2, u^9 - u^8 - 2u^7 + 3u^6 + u^5 - 3u^4 + 2u^3 - u + 1 \rangle \\
 I_3^u &= \langle 33u^3a^2 - 5a^2u^2 - 4u^3a - 30a^2u + 106u^2a + 89u^3 - 19a^2 + 7au + 28u^2 + 185b - 19a - 54u - 160, \\
 &\quad - a^2u^2 - 5u^3a + a^3 + 3a^2u + 4u^2a - a^2 + 4au + 6u^2 - a - u + 1, u^4 - u^2 + 1 \rangle
 \end{aligned}$$

\* 3 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 63 representations.

<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/math/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\text{I. } I_1^u = \langle -4.92 \times 10^{36}u^{41} - 1.80 \times 10^{38}u^{40} + \dots + 2.89 \times 10^{39}b + 4.23 \times 10^{39}, 9.16 \times 10^{39}u^{41} - 6.73 \times 10^{39}u^{40} + \dots + 4.91 \times 10^{40}a + 8.21 \times 10^{40}, u^{42} - 2u^{41} + \dots + 16u - 17 \rangle$$

(i) **Arc colorings**

$$a_5 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -0.186607u^{41} + 0.137118u^{40} + \dots + 5.29366u - 1.67251 \\ 0.00170297u^{41} + 0.0622705u^{40} + \dots - 0.201147u - 1.46385 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -0.184904u^{41} + 0.199388u^{40} + \dots + 5.09252u - 3.13636 \\ 0.00170297u^{41} + 0.0622705u^{40} + \dots - 0.201147u - 1.46385 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 0.0588482u^{41} - 0.261568u^{40} + \dots + 3.71273u + 4.22681 \\ 0.266107u^{41} - 0.115441u^{40} + \dots - 1.21463u + 2.00517 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 0.0875371u^{41} - 0.115951u^{40} + \dots + 5.83351u + 3.00873 \\ 0.0353514u^{41} - 0.0574630u^{40} + \dots - 0.374380u - 0.0632026 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -u \\ u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} u^3 \\ -u^3 + u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -u^3 \\ u^5 - u^3 + u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -0.596514u^{41} + 0.435647u^{40} + \dots + 2.54867u - 8.20884 \\ 0.687055u^{41} - 0.666732u^{40} + \dots - 0.496210u + 10.8635 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 0.589024u^{41} - 0.658891u^{40} + \dots + 2.42549u + 11.2674 \\ 0.0500035u^{41} + 0.0678910u^{40} + \dots - 1.20598u - 1.53919 \end{pmatrix}$$

(ii) **Obstruction class** = -1

(iii) **Cusp Shapes** =  $1.57605u^{41} - 2.80061u^{40} + \dots + 23.4107u + 46.2988$

**(iv) u-Polynomials at the component**

| Crossings     | u-Polynomials at each crossing              |
|---------------|---------------------------------------------|
| $c_1$         | $u^{42} + 2u^{41} + \cdots + 24u + 1$       |
| $c_2, c_4$    | $u^{42} - 14u^{41} + \cdots + 12u - 1$      |
| $c_3, c_7$    | $u^{42} - u^{41} + \cdots + 5632u + 512$    |
| $c_5, c_9$    | $u^{42} - 2u^{41} + \cdots + 16u - 17$      |
| $c_6, c_{11}$ | $u^{42} - 2u^{41} + \cdots - 70u - 49$      |
| $c_8$         | $u^{42} - 6u^{41} + \cdots - 2688u + 2567$  |
| $c_{10}$      | $u^{42} - 28u^{41} + \cdots + 1206u + 289$  |
| $c_{12}$      | $u^{42} + 6u^{41} + \cdots + 26460u + 2401$ |

**(v) Riley Polynomials at the component**

| Crossings     | Riley Polynomials at each crossing                 |
|---------------|----------------------------------------------------|
| $c_1$         | $y^{42} + 90y^{41} + \cdots + 1420y + 1$           |
| $c_2, c_4$    | $y^{42} - 2y^{41} + \cdots - 24y + 1$              |
| $c_3, c_7$    | $y^{42} - 69y^{41} + \cdots - 17301504y + 262144$  |
| $c_5, c_9$    | $y^{42} - 28y^{41} + \cdots + 1206y + 289$         |
| $c_6, c_{11}$ | $y^{42} + 6y^{41} + \cdots + 26460y + 2401$        |
| $c_8$         | $y^{42} + 68y^{41} + \cdots + 1240622y + 6589489$  |
| $c_{10}$      | $y^{42} - 20y^{41} + \cdots - 5069826y + 83521$    |
| $c_{12}$      | $y^{42} + 74y^{41} + \cdots - 29647548y + 5764801$ |

(vi) Complex Volumes and Cusp Shapes

| Solutions to $I_1^u$        | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape           |
|-----------------------------|---------------------------------------|----------------------|
| $u = -0.961799 + 0.311389I$ |                                       |                      |
| $a = 2.02690 - 2.18124I$    | $-1.72797 - 1.37637I$                 | $4.55612 - 0.38965I$ |
| $b = -0.464784 + 0.408421I$ |                                       |                      |
| $u = -0.961799 - 0.311389I$ |                                       |                      |
| $a = 2.02690 + 2.18124I$    | $-1.72797 + 1.37637I$                 | $4.55612 + 0.38965I$ |
| $b = -0.464784 - 0.408421I$ |                                       |                      |
| $u = -0.829534 + 0.589200I$ |                                       |                      |
| $a = 0.947623 + 0.399065I$  | $-1.74074 - 2.33828I$                 | $4.84594 + 5.31700I$ |
| $b = -0.343165 - 0.102736I$ |                                       |                      |
| $u = -0.829534 - 0.589200I$ |                                       |                      |
| $a = 0.947623 - 0.399065I$  | $-1.74074 + 2.33828I$                 | $4.84594 - 5.31700I$ |
| $b = -0.343165 + 0.102736I$ |                                       |                      |
| $u = 0.944203 + 0.228207I$  |                                       |                      |
| $a = -0.16949 + 2.29855I$   | $2.48881 + 3.70265I$                  | $6.29949 - 2.05838I$ |
| $b = 0.993256 - 0.666835I$  |                                       |                      |
| $u = 0.944203 - 0.228207I$  |                                       |                      |
| $a = -0.16949 - 2.29855I$   | $2.48881 - 3.70265I$                  | $6.29949 + 2.05838I$ |
| $b = 0.993256 + 0.666835I$  |                                       |                      |
| $u = 0.835994 + 0.489683I$  |                                       |                      |
| $a = -3.35442 + 8.86991I$   | $-3.34089 + 2.03680I$                 | $95.8127 + 26.5459I$ |
| $b = -1.016890 + 0.004699I$ |                                       |                      |
| $u = 0.835994 - 0.489683I$  |                                       |                      |
| $a = -3.35442 - 8.86991I$   | $-3.34089 - 2.03680I$                 | $95.8127 - 26.5459I$ |
| $b = -1.016890 - 0.004699I$ |                                       |                      |
| $u = 0.965269 + 0.439008I$  |                                       |                      |
| $a = -0.983823 - 0.359781I$ | $2.81421 - 1.00795I$                  | $8.57321 + 1.27913I$ |
| $b = 0.899894 + 0.651256I$  |                                       |                      |
| $u = 0.965269 - 0.439008I$  |                                       |                      |
| $a = -0.983823 + 0.359781I$ | $2.81421 + 1.00795I$                  | $8.57321 - 1.27913I$ |
| $b = 0.899894 - 0.651256I$  |                                       |                      |

| Solutions to $I_1^u$        | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape            |
|-----------------------------|---------------------------------------|-----------------------|
| $u = -0.726987 + 0.560951I$ |                                       |                       |
| $a = 0.802280 + 0.067898I$  | $-1.85016 - 2.19168I$                 | $2.73443 + 3.94919I$  |
| $b = 0.101623 + 0.134205I$  |                                       |                       |
| $u = -0.726987 - 0.560951I$ |                                       |                       |
| $a = 0.802280 - 0.067898I$  | $-1.85016 + 2.19168I$                 | $2.73443 - 3.94919I$  |
| $b = 0.101623 - 0.134205I$  |                                       |                       |
| $u = 0.205294 + 1.093670I$  |                                       |                       |
| $a = -0.50667 - 1.38304I$   | $11.4259 - 8.4418I$                   | $2.24860 + 3.75985I$  |
| $b = 1.23869 + 1.08212I$    |                                       |                       |
| $u = 0.205294 - 1.093670I$  |                                       |                       |
| $a = -0.50667 + 1.38304I$   | $11.4259 + 8.4418I$                   | $2.24860 - 3.75985I$  |
| $b = 1.23869 - 1.08212I$    |                                       |                       |
| $u = 0.053594 + 1.137510I$  |                                       |                       |
| $a = -0.59511 + 1.46169I$   | $12.15940 + 0.20639I$                 | $3.10494 - 0.07106I$  |
| $b = 1.05760 - 1.28040I$    |                                       |                       |
| $u = 0.053594 - 1.137510I$  |                                       |                       |
| $a = -0.59511 - 1.46169I$   | $12.15940 - 0.20639I$                 | $3.10494 + 0.07106I$  |
| $b = 1.05760 + 1.28040I$    |                                       |                       |
| $u = 0.232942 + 0.816588I$  |                                       |                       |
| $a = 0.184697 - 0.861641I$  | $1.95152 + 0.96411I$                  | $4.49813 - 1.84965I$  |
| $b = 0.151638 + 0.884654I$  |                                       |                       |
| $u = 0.232942 - 0.816588I$  |                                       |                       |
| $a = 0.184697 + 0.861641I$  | $1.95152 - 0.96411I$                  | $4.49813 + 1.84965I$  |
| $b = 0.151638 - 0.884654I$  |                                       |                       |
| $u = -1.18461$              |                                       |                       |
| $a = 1.51253$               | 0.934538                              | 7.24150               |
| $b = -1.40973$              |                                       |                       |
| $u = -1.126130 + 0.490429I$ |                                       |                       |
| $a = -0.039913 - 1.285050I$ | $2.33209 - 7.91667I$                  | $6.88839 + 11.06602I$ |
| $b = 0.828323 + 0.354167I$  |                                       |                       |

| Solutions to $I_1^u$        | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape            |
|-----------------------------|---------------------------------------|-----------------------|
| $u = -1.126130 - 0.490429I$ |                                       |                       |
| $a = -0.039913 + 1.285050I$ | $2.33209 + 7.91667I$                  | $6.88839 - 11.06602I$ |
| $b = 0.828323 - 0.354167I$  |                                       |                       |
| $u = 1.259460 + 0.006196I$  |                                       |                       |
| $a = -0.97423 - 2.37844I$   | $4.47907 - 1.92884I$                  | $6.47929 + 1.71581I$  |
| $b = 0.506833 + 1.138780I$  |                                       |                       |
| $u = 1.259460 - 0.006196I$  |                                       |                       |
| $a = -0.97423 + 2.37844I$   | $4.47907 + 1.92884I$                  | $6.47929 - 1.71581I$  |
| $b = 0.506833 - 1.138780I$  |                                       |                       |
| $u = 1.072950 + 0.670917I$  |                                       |                       |
| $a = 0.45051 + 1.91983I$    | $4.15910 + 4.29767I$                  | $6.40450 - 3.97494I$  |
| $b = 0.590513 - 1.035150I$  |                                       |                       |
| $u = 1.072950 - 0.670917I$  |                                       |                       |
| $a = 0.45051 - 1.91983I$    | $4.15910 - 4.29767I$                  | $6.40450 + 3.97494I$  |
| $b = 0.590513 + 1.035150I$  |                                       |                       |
| $u = 1.254550 + 0.204489I$  |                                       |                       |
| $a = 1.39168 - 2.27514I$    | $2.23820 + 2.99548I$                  | $5.68648 - 2.96480I$  |
| $b = -1.145780 + 0.655072I$ |                                       |                       |
| $u = 1.254550 - 0.204489I$  |                                       |                       |
| $a = 1.39168 + 2.27514I$    | $2.23820 - 2.99548I$                  | $5.68648 + 2.96480I$  |
| $b = -1.145780 - 0.655072I$ |                                       |                       |
| $u = -0.274846 + 0.651125I$ |                                       |                       |
| $a = 0.435590 + 0.051488I$  | $-0.15519 + 3.49196I$                 | $2.75035 - 5.76254I$  |
| $b = 0.661252 - 0.443712I$  |                                       |                       |
| $u = -0.274846 - 0.651125I$ |                                       |                       |
| $a = 0.435590 - 0.051488I$  | $-0.15519 - 3.49196I$                 | $2.75035 + 5.76254I$  |
| $b = 0.661252 + 0.443712I$  |                                       |                       |
| $u = 0.698771$              |                                       |                       |
| $a = 0.544644$              | 0.929263                              | 11.4390               |
| $b = 0.196513$              |                                       |                       |

| Solutions to $I_1^u$        | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|-----------------------------|---------------------------------------|------------|
| $u = -1.360000 + 0.378690I$ |                                       |            |
| $a = -0.10332 + 2.56500I$   | $6.81382 - 5.26231I$                  | 0          |
| $b = -0.202310 - 1.252300I$ |                                       |            |
| $u = -1.360000 - 0.378690I$ |                                       |            |
| $a = -0.10332 - 2.56500I$   | $6.81382 + 5.26231I$                  | 0          |
| $b = -0.202310 + 1.252300I$ |                                       |            |
| $u = 1.29496 + 0.63382I$    |                                       |            |
| $a = -0.59935 + 2.83045I$   | $14.7912 + 14.5915I$                  | 0          |
| $b = 1.31294 - 0.99932I$    |                                       |            |
| $u = 1.29496 - 0.63382I$    |                                       |            |
| $a = -0.59935 - 2.83045I$   | $14.7912 - 14.5915I$                  | 0          |
| $b = 1.31294 + 0.99932I$    |                                       |            |
| $u = 1.38494 + 0.58465I$    |                                       |            |
| $a = -1.93831 - 1.93197I$   | $16.3124 + 5.9260I$                   | 0          |
| $b = 0.92670 + 1.41166I$    |                                       |            |
| $u = 1.38494 - 0.58465I$    |                                       |            |
| $a = -1.93831 + 1.93197I$   | $16.3124 - 5.9260I$                   | 0          |
| $b = 0.92670 - 1.41166I$    |                                       |            |
| $u = -1.42037 + 0.52003I$   |                                       |            |
| $a = -0.95320 - 2.91761I$   | $16.8335 - 6.1018I$                   | 0          |
| $b = 1.24919 + 1.24050I$    |                                       |            |
| $u = -1.42037 - 0.52003I$   |                                       |            |
| $a = -0.95320 + 2.91761I$   | $16.8335 + 6.1018I$                   | 0          |
| $b = 1.24919 - 1.24050I$    |                                       |            |
| $u = -1.46489 + 0.38079I$   |                                       |            |
| $a = -2.05057 + 2.08335I$   | $16.9282 + 3.1689I$                   | 0          |
| $b = 1.22965 - 1.27108I$    |                                       |            |
| $u = -1.46489 - 0.38079I$   |                                       |            |
| $a = -2.05057 - 2.08335I$   | $16.9282 - 3.1689I$                   | 0          |
| $b = 1.22965 + 1.27108I$    |                                       |            |

| Solutions to $I_1^u$        | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape            |
|-----------------------------|---------------------------------------|-----------------------|
| $u = -0.096688 + 0.349533I$ |                                       |                       |
| $a = -0.82299 + 1.83040I$   | $-1.74611 - 0.73385I$                 | $-3.54446 + 0.56735I$ |
| $b = -0.968549 - 0.219170I$ |                                       |                       |
| $u = -0.096688 - 0.349533I$ |                                       |                       |
| $a = -0.82299 - 1.83040I$   | $-1.74611 + 0.73385I$                 | $-3.54446 - 0.56735I$ |
| $b = -0.968549 + 0.219170I$ |                                       |                       |

$$I_2^u = \langle b+1, -2u^8 + u^7 + \dots + a+2, u^9 - u^8 - 2u^7 + 3u^6 + u^5 - 3u^4 + 2u^3 - u + 1 \rangle$$

(i) **Arc colorings**

$$a_5 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 2u^8 - u^7 - 5u^6 + 3u^5 + 4u^4 - 3u^3 + 2u^2 - 2 \\ -1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 2u^8 - u^7 - 5u^6 + 3u^5 + 4u^4 - 3u^3 + 2u^2 - 3 \\ -1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 2u^8 - u^7 - 5u^6 + 3u^5 + 4u^4 - 3u^3 + 2u^2 - 2 \\ -1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -u \\ u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} u^3 \\ -u^3 + u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -u^3 \\ u^5 - u^3 + u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -u^3 \\ u^5 - u^3 + u \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -u^6 + u^4 - 1 \\ u^6 - 2u^4 + u^2 \end{pmatrix}$$

(ii) **Obstruction class** = 1

(iii) **Cusp Shapes** =  $-6u^8 - 5u^7 + 10u^6 + 8u^5 - 10u^4 - 8u^3 - 4u^2 - 8u - 2$

**(iv) u-Polynomials at the component**

| Crossings     | u-Polynomials at each crossing                                     |
|---------------|--------------------------------------------------------------------|
| $c_1, c_2$    | $(u - 1)^9$                                                        |
| $c_3, c_7$    | $u^9$                                                              |
| $c_4$         | $(u + 1)^9$                                                        |
| $c_5$         | $u^9 - u^8 - 2u^7 + 3u^6 + u^5 - 3u^4 + 2u^3 - u + 1$              |
| $c_6$         | $u^9 - u^8 + 2u^7 - u^6 + 3u^5 - u^4 + 2u^3 + u + 1$               |
| $c_8, c_{12}$ | $u^9 + 3u^8 + 8u^7 + 13u^6 + 17u^5 + 17u^4 + 12u^3 + 6u^2 + u - 1$ |
| $c_9$         | $u^9 + u^8 - 2u^7 - 3u^6 + u^5 + 3u^4 + 2u^3 - u - 1$              |
| $c_{10}$      | $u^9 - 5u^8 + 12u^7 - 15u^6 + 9u^5 + u^4 - 4u^3 + 2u^2 + u - 1$    |
| $c_{11}$      | $u^9 + u^8 + 2u^7 + u^6 + 3u^5 + u^4 + 2u^3 + u - 1$               |

**(v) Riley Polynomials at the component**

| Crossings       | Riley Polynomials at each crossing                                    |
|-----------------|-----------------------------------------------------------------------|
| $c_1, c_2, c_4$ | $(y - 1)^9$                                                           |
| $c_3, c_7$      | $y^9$                                                                 |
| $c_5, c_9$      | $y^9 - 5y^8 + 12y^7 - 15y^6 + 9y^5 + y^4 - 4y^3 + 2y^2 + y - 1$       |
| $c_6, c_{11}$   | $y^9 + 3y^8 + 8y^7 + 13y^6 + 17y^5 + 17y^4 + 12y^3 + 6y^2 + y - 1$    |
| $c_8, c_{12}$   | $y^9 + 7y^8 + 20y^7 + 25y^6 + 5y^5 - 15y^4 + 22y^3 + 13y^2 + 13y - 1$ |
| $c_{10}$        | $y^9 - y^8 + 12y^7 - 7y^6 + 37y^5 + y^4 - 10y^2 + 5y - 1$             |

(vi) Complex Volumes and Cusp Shapes

| Solutions to $I_2^u$                                                        | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape            |
|-----------------------------------------------------------------------------|---------------------------------------|-----------------------|
| $u = 0.772920 + 0.510351I$<br>$a = -1.67861 + 2.31573I$<br>$b = -1.00000$   | $-3.42837 + 2.09337I$                 | $-12.6725 - 14.2088I$ |
| $u = 0.772920 - 0.510351I$<br>$a = -1.67861 - 2.31573I$<br>$b = -1.00000$   | $-3.42837 - 2.09337I$                 | $-12.6725 + 14.2088I$ |
| $u = -0.825933$<br>$a = 0.871015$<br>$b = -1.00000$                         | $-0.446489$                           | $1.84400$             |
| $u = -1.173910 + 0.391555I$<br>$a = 0.893484 + 0.630694I$<br>$b = -1.00000$ | $2.72642 - 1.33617I$                  | $6.61905 + 0.64999I$  |
| $u = -1.173910 - 0.391555I$<br>$a = 0.893484 - 0.630694I$<br>$b = -1.00000$ | $2.72642 + 1.33617I$                  | $6.61905 - 0.64999I$  |
| $u = 0.141484 + 0.739668I$<br>$a = -0.309843 + 0.043204I$<br>$b = -1.00000$ | $-1.02799 - 2.45442I$                 | $-0.10038 + 1.90984I$ |
| $u = 0.141484 - 0.739668I$<br>$a = -0.309843 - 0.043204I$<br>$b = -1.00000$ | $-1.02799 + 2.45442I$                 | $-0.10038 - 1.90984I$ |
| $u = 1.172470 + 0.500383I$<br>$a = 0.659464 - 0.874093I$<br>$b = -1.00000$  | $1.95319 + 7.08493I$                  | $3.23178 - 2.93209I$  |
| $u = 1.172470 - 0.500383I$<br>$a = 0.659464 + 0.874093I$<br>$b = -1.00000$  | $1.95319 - 7.08493I$                  | $3.23178 + 2.93209I$  |

### III.

$$I_3^u = \langle 33u^3a^2 - 4u^3a + \dots - 19a - 160, -a^2u^2 - 5u^3a + \dots - a + 1, u^4 - u^2 + 1 \rangle$$

(i) **Arc colorings**

$$a_5 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} a \\ -0.178378a^2u^3 + 0.0216216au^3 + \dots + 0.102703a + 0.864865 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -0.178378a^2u^3 + 0.0216216au^3 + \dots + 1.10270a + 0.864865 \\ -0.178378a^2u^3 + 0.0216216au^3 + \dots + 0.102703a + 0.864865 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 0.156757a^2u^3 - 0.0432432au^3 + \dots - 0.00540541a - 1.32973 \\ -0.232432a^2u^3 - 0.632432au^3 + \dots - 0.0540541a + 2.10270 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} \frac{1}{5}u^3a^2 - \frac{3}{5}u^3a + \dots - \frac{3}{5}a + 1 \\ -0.0540541a^2u^3 - 0.654054au^3 + \dots - 0.156757a + 0.237838 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -u \\ u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} u^3 \\ -u^3 + u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -u^3 \\ 0 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 0.340541a^2u^3 - 0.0594595au^3 + \dots - 0.632432a + 0.421622 \\ -0.194595a^2u^3 + 0.00540541au^3 + \dots + 0.675676a + 1.01622 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 0.156757a^2u^3 - 0.0432432au^3 + \dots - 0.00540541a - 1.32973 \\ -0.232432a^2u^3 - 0.632432au^3 + \dots - 0.0540541a + 2.10270 \end{pmatrix}$$

(ii) **Obstruction class = 1**

$$(iii) \text{ Cusp Shapes} = -\frac{132}{185}u^3a^2 + \frac{4}{37}a^2u^2 + \frac{16}{185}u^3a + \frac{24}{37}a^2u - \frac{424}{185}u^2a - \frac{356}{185}u^3 + \frac{76}{185}a^2 - \frac{28}{185}au - \frac{852}{185}u^2 + \frac{76}{185}a + \frac{216}{185}u + \frac{128}{37}$$

**(iv) u-Polynomials at the component**

| Crossings       | u-Polynomials at each crossing |
|-----------------|--------------------------------|
| $c_1$           | $(u^3 - u^2 + 2u - 1)^4$       |
| $c_2$           | $(u^3 + u^2 - 1)^4$            |
| $c_3, c_7$      | $(u^6 - 3u^4 + 2u^2 + 1)^2$    |
| $c_4$           | $(u^3 - u^2 + 1)^4$            |
| $c_5, c_8, c_9$ | $(u^4 - u^2 + 1)^3$            |
| $c_6, c_{11}$   | $(u^2 + 1)^6$                  |
| $c_{10}$        | $(u^2 - u + 1)^6$              |
| $c_{12}$        | $(u + 1)^{12}$                 |

**(v) Riley Polynomials at the component**

| Crossings       | Riley Polynomials at each crossing |
|-----------------|------------------------------------|
| $c_1$           | $(y^3 + 3y^2 + 2y - 1)^4$          |
| $c_2, c_4$      | $(y^3 - y^2 + 2y - 1)^4$           |
| $c_3, c_7$      | $(y^3 - 3y^2 + 2y + 1)^4$          |
| $c_5, c_8, c_9$ | $(y^2 - y + 1)^6$                  |
| $c_6, c_{11}$   | $(y + 1)^{12}$                     |
| $c_{10}$        | $(y^2 + y + 1)^6$                  |
| $c_{12}$        | $(y - 1)^{12}$                     |

(vi) Complex Volumes and Cusp Shapes

| Solutions to $I_3^u$        | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape            |
|-----------------------------|---------------------------------------|-----------------------|
| $u = 0.866025 + 0.500000I$  |                                       |                       |
| $a = -0.972493 - 1.013180I$ | $1.37919 - 0.79824I$                  | $1.50976 - 0.48465I$  |
| $b = 0.877439 + 0.744862I$  |                                       |                       |
| $u = 0.866025 + 0.500000I$  |                                       |                       |
| $a = 0.11905 - 1.81610I$    | $-2.75839 + 2.02988I$                 | $-5.01951 - 3.46410I$ |
| $b = -0.754878$             |                                       |                       |
| $u = 0.866025 + 0.500000I$  |                                       |                       |
| $a = -0.24463 + 2.19530I$   | $1.37919 + 4.85801I$                  | $1.50976 - 6.44355I$  |
| $b = 0.877439 - 0.744862I$  |                                       |                       |
| $u = 0.866025 - 0.500000I$  |                                       |                       |
| $a = -0.972493 + 1.013180I$ | $1.37919 + 0.79824I$                  | $1.50976 + 0.48465I$  |
| $b = 0.877439 - 0.744862I$  |                                       |                       |
| $u = 0.866025 - 0.500000I$  |                                       |                       |
| $a = 0.11905 + 1.81610I$    | $-2.75839 - 2.02988I$                 | $-5.01951 + 3.46410I$ |
| $b = -0.754878$             |                                       |                       |
| $u = 0.866025 - 0.500000I$  |                                       |                       |
| $a = -0.24463 - 2.19530I$   | $1.37919 - 4.85801I$                  | $1.50976 + 6.44355I$  |
| $b = 0.877439 + 0.744862I$  |                                       |                       |
| $u = -0.866025 + 0.500000I$ |                                       |                       |
| $a = -0.949962 - 0.298361I$ | $1.37919 + 0.79824I$                  | $1.50976 + 0.48465I$  |
| $b = 0.877439 - 0.744862I$  |                                       |                       |
| $u = -0.866025 + 0.500000I$ |                                       |                       |
| $a = 0.90246 - 1.55905I$    | $1.37919 - 4.85801I$                  | $1.50976 + 6.44355I$  |
| $b = 0.877439 + 0.744862I$  |                                       |                       |
| $u = -0.866025 + 0.500000I$ |                                       |                       |
| $a = 4.14558 - 0.50862I$    | $-2.75839 - 2.02988I$                 | $-5.01951 + 3.46410I$ |
| $b = -0.754878$             |                                       |                       |
| $u = -0.866025 - 0.500000I$ |                                       |                       |
| $a = -0.949962 + 0.298361I$ | $1.37919 - 0.79824I$                  | $1.50976 - 0.48465I$  |
| $b = 0.877439 + 0.744862I$  |                                       |                       |

| Solutions to $I_3^u$        | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape            |
|-----------------------------|---------------------------------------|-----------------------|
| $u = -0.866025 - 0.500000I$ |                                       |                       |
| $a = 0.90246 + 1.55905I$    | $1.37919 + 4.85801I$                  | $1.50976 - 6.44355I$  |
| $b = 0.877439 - 0.744862I$  |                                       |                       |
| $u = -0.866025 - 0.500000I$ |                                       |                       |
| $a = 4.14558 + 0.50862I$    | $-2.75839 + 2.02988I$                 | $-5.01951 - 3.46410I$ |
| $b = -0.754878$             |                                       |                       |

#### IV. u-Polynomials

| Crossings  | u-Polynomials at each crossing                                                                                                               |
|------------|----------------------------------------------------------------------------------------------------------------------------------------------|
| $c_1$      | $((u - 1)^9)(u^3 - u^2 + 2u - 1)^4(u^{42} + 2u^{41} + \dots + 24u + 1)$                                                                      |
| $c_2$      | $((u - 1)^9)(u^3 + u^2 - 1)^4(u^{42} - 14u^{41} + \dots + 12u - 1)$                                                                          |
| $c_3, c_7$ | $u^9(u^6 - 3u^4 + 2u^2 + 1)^2(u^{42} - u^{41} + \dots + 5632u + 512)$                                                                        |
| $c_4$      | $((u + 1)^9)(u^3 - u^2 + 1)^4(u^{42} - 14u^{41} + \dots + 12u - 1)$                                                                          |
| $c_5$      | $(u^4 - u^2 + 1)^3(u^9 - u^8 - 2u^7 + 3u^6 + u^5 - 3u^4 + 2u^3 - u + 1) \cdot (u^{42} - 2u^{41} + \dots + 16u - 17)$                         |
| $c_6$      | $(u^2 + 1)^6(u^9 - u^8 + 2u^7 - u^6 + 3u^5 - u^4 + 2u^3 + u + 1) \cdot (u^{42} - 2u^{41} + \dots - 70u - 49)$                                |
| $c_8$      | $(u^4 - u^2 + 1)^3 \cdot (u^9 + 3u^8 + 8u^7 + 13u^6 + 17u^5 + 17u^4 + 12u^3 + 6u^2 + u - 1) \cdot (u^{42} - 6u^{41} + \dots - 2688u + 2567)$ |
| $c_9$      | $(u^4 - u^2 + 1)^3(u^9 + u^8 - 2u^7 - 3u^6 + u^5 + 3u^4 + 2u^3 - u - 1) \cdot (u^{42} - 2u^{41} + \dots + 16u - 17)$                         |
| $c_{10}$   | $((u^2 - u + 1)^6)(u^9 - 5u^8 + \dots + u - 1) \cdot (u^{42} - 28u^{41} + \dots + 1206u + 289)$                                              |
| $c_{11}$   | $(u^2 + 1)^6(u^9 + u^8 + 2u^7 + u^6 + 3u^5 + u^4 + 2u^3 + u - 1) \cdot (u^{42} - 2u^{41} + \dots - 70u - 49)$                                |
| $c_{12}$   | $((u + 1)^{12})(u^9 + 3u^8 + \dots + u - 1) \cdot (u^{42} + 6u^{41} + \dots + 26460u + 2401)$                                                |

## V. Riley Polynomials

| Crossings     | Riley Polynomials at each crossing                                                                                                       |
|---------------|------------------------------------------------------------------------------------------------------------------------------------------|
| $c_1$         | $((y - 1)^9)(y^3 + 3y^2 + 2y - 1)^4(y^{42} + 90y^{41} + \dots + 1420y + 1)$                                                              |
| $c_2, c_4$    | $((y - 1)^9)(y^3 - y^2 + 2y - 1)^4(y^{42} - 2y^{41} + \dots - 24y + 1)$                                                                  |
| $c_3, c_7$    | $y^9(y^3 - 3y^2 + 2y + 1)^4(y^{42} - 69y^{41} + \dots - 1.73015 \times 10^7y + 262144)$                                                  |
| $c_5, c_9$    | $((y^2 - y + 1)^6)(y^9 - 5y^8 + \dots + y - 1)$<br>$\cdot (y^{42} - 28y^{41} + \dots + 1206y + 289)$                                     |
| $c_6, c_{11}$ | $((y + 1)^{12})(y^9 + 3y^8 + \dots + y - 1)$<br>$\cdot (y^{42} + 6y^{41} + \dots + 26460y + 2401)$                                       |
| $c_8$         | $((y^2 - y + 1)^6)(y^9 + 7y^8 + \dots + 13y - 1)$<br>$\cdot (y^{42} + 68y^{41} + \dots + 1240622y + 6589489)$                            |
| $c_{10}$      | $(y^2 + y + 1)^6(y^9 - y^8 + 12y^7 - 7y^6 + 37y^5 + y^4 - 10y^2 + 5y - 1)$<br>$\cdot (y^{42} - 20y^{41} + \dots - 5069826y + 83521)$     |
| $c_{12}$      | $(y - 1)^{12}(y^9 + 7y^8 + 20y^7 + 25y^6 + 5y^5 - 15y^4 + 22y^2 + 13y - 1)$<br>$\cdot (y^{42} + 74y^{41} + \dots - 29647548y + 5764801)$ |