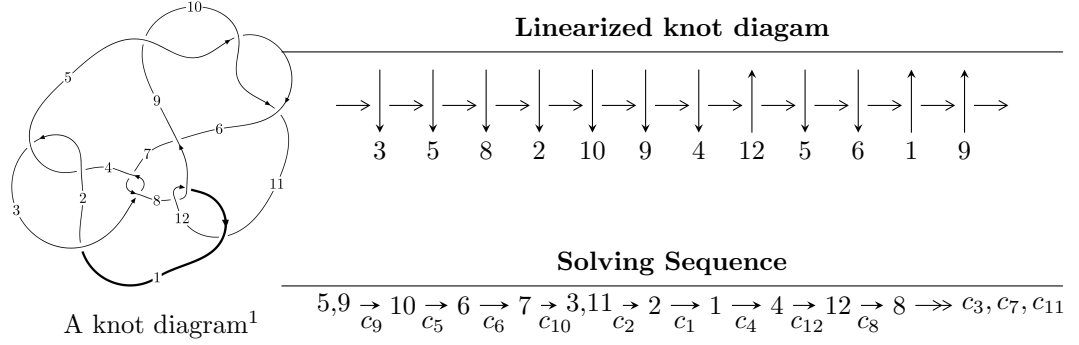


12n<sub>0188</sub> (K12n<sub>0188</sub>)



**Ideals for irreducible components<sup>2</sup> of  $X_{\text{par}}$**

$$I_1^u = \langle 1.51544 \times 10^{40} u^{40} + 2.56027 \times 10^{40} u^{39} + \dots + 1.06321 \times 10^{41} b + 4.21643 \times 10^{41}, \\ 6.97778 \times 10^{40} u^{40} + 1.95337 \times 10^{41} u^{39} + \dots + 2.12642 \times 10^{41} a - 9.27571 \times 10^{40}, u^{41} + 3u^{40} + \dots - 8u - 8 \rangle$$

$$I_2^u = \langle -2a^2 - au + b - 2a - u - 1, 4a^3 + 2a^2u - u, u^2 - 2 \rangle$$

$$I_1^v = \langle a, b + v + 2, v^3 + 3v^2 + 2v - 1 \rangle$$

\* 3 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 50 representations.

<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

I.

$$I_1^u = \langle 1.52 \times 10^{40} u^{40} + 2.56 \times 10^{40} u^{39} + \dots + 1.06 \times 10^{41} b + 4.22 \times 10^{41}, 6.98 \times 10^{40} u^{40} + 1.95 \times 10^{41} u^{39} + \dots + 2.13 \times 10^{41} a - 9.28 \times 10^{40}, u^{41} + 3u^{40} + \dots - 8u - 8 \rangle$$

(i) Arc colorings

$$a_5 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -u \\ -u^3 + u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} u^3 - 2u \\ -u^3 + u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -0.328147u^{40} - 0.918618u^{39} + \dots - 19.5503u + 0.436213 \\ -0.142535u^{40} - 0.240806u^{39} + \dots + 7.40030u - 3.96576 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -u^2 + 1 \\ -u^4 + 2u^2 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -0.328147u^{40} - 0.918618u^{39} + \dots - 19.5503u + 0.436213 \\ 0.0824090u^{40} + 0.163606u^{39} + \dots + 9.49889u - 4.49235 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 0.0838694u^{40} + 0.525518u^{39} + \dots + 23.3356u + 7.39263 \\ -0.124059u^{40} - 0.154000u^{39} + \dots + 5.97827u + 0.0223382 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -0.340779u^{40} - 1.11522u^{39} + \dots - 14.5840u - 9.80822 \\ 0.0747081u^{40} - 0.0614080u^{39} + \dots - 12.3801u + 1.21809 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 0.207928u^{40} + 0.679518u^{39} + \dots + 17.3573u + 7.37029 \\ -0.124059u^{40} - 0.154000u^{39} + \dots + 5.97827u + 0.0223382 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 0.401561u^{40} + 1.01803u^{39} + \dots + 27.2274u + 2.78868 \\ -0.142281u^{40} - 0.206934u^{39} + \dots - 0.775735u + 2.43501 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes =  $-0.588415u^{40} - 0.804243u^{39} + \dots + 87.6228u - 60.0034$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1$	$u^{41} + 26u^{40} + \dots + 206u + 1$
$c_2, c_4$	$u^{41} - 4u^{40} + \dots - 14u - 1$
$c_3, c_7$	$u^{41} + 2u^{40} + \dots + 8u - 1$
$c_5, c_9, c_{10}$	$u^{41} + 3u^{40} + \dots - 8u - 8$
$c_6$	$u^{41} - 9u^{40} + \dots + 10824u + 12200$
$c_8, c_{12}$	$u^{41} - 4u^{40} + \dots + 5u - 7$
$c_{11}$	$u^{41} - 12u^{40} + \dots + 1593u - 49$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1$	$y^{41} - 18y^{40} + \dots + 44086y - 1$
$c_2, c_4$	$y^{41} - 26y^{40} + \dots + 206y - 1$
$c_3, c_7$	$y^{41} + 6y^{40} + \dots + 54y - 1$
$c_5, c_9, c_{10}$	$y^{41} - 55y^{40} + \dots + 2752y - 64$
$c_6$	$y^{41} - 139y^{40} + \dots + 8334688576y - 148840000$
$c_8, c_{12}$	$y^{41} - 12y^{40} + \dots + 1593y - 49$
$c_{11}$	$y^{41} + 44y^{40} + \dots + 664281y - 2401$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.852625 + 0.482864I$		
$a = -0.372803 - 0.780038I$	$-0.75167 - 5.04176I$	$-5.33106 + 6.16840I$
$b = 0.771778 - 0.848460I$		
$u = 0.852625 - 0.482864I$		
$a = -0.372803 + 0.780038I$	$-0.75167 + 5.04176I$	$-5.33106 - 6.16840I$
$b = 0.771778 + 0.848460I$		
$u = -0.003882 + 1.032070I$		
$a = -0.244627 - 1.101450I$	$-1.61122 + 4.08215I$	$-8.92321 - 7.89693I$
$b = 0.500255 + 0.850150I$		
$u = -0.003882 - 1.032070I$		
$a = -0.244627 + 1.101450I$	$-1.61122 - 4.08215I$	$-8.92321 + 7.89693I$
$b = 0.500255 - 0.850150I$		
$u = -0.992946 + 0.343746I$		
$a = 1.196560 + 0.016956I$	$-4.56663 + 3.64468I$	$-10.21223 - 4.25500I$
$b = -0.60773 - 1.75136I$		
$u = -0.992946 - 0.343746I$		
$a = 1.196560 - 0.016956I$	$-4.56663 - 3.64468I$	$-10.21223 + 4.25500I$
$b = -0.60773 + 1.75136I$		
$u = 1.044990 + 0.164135I$		
$a = -1.029770 + 0.479582I$	$-4.59839 - 1.02943I$	$-11.04507 + 3.64044I$
$b = -0.335570 + 0.883151I$		
$u = 1.044990 - 0.164135I$		
$a = -1.029770 - 0.479582I$	$-4.59839 + 1.02943I$	$-11.04507 - 3.64044I$
$b = -0.335570 - 0.883151I$		
$u = -0.848129 + 0.093318I$		
$a = 0.256235 - 0.617893I$	$-1.53932 + 0.15416I$	$-7.41256 - 0.66382I$
$b = 0.429896 - 0.866899I$		
$u = -0.848129 - 0.093318I$		
$a = 0.256235 + 0.617893I$	$-1.53932 - 0.15416I$	$-7.41256 + 0.66382I$
$b = 0.429896 + 0.866899I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.960191 + 0.725231I$ $a = 1.064690 - 0.333931I$ $b = -0.87449 + 1.44326I$	$-4.46221 - 9.77258I$	$-8.72581 + 8.02773I$
$u = 0.960191 - 0.725231I$ $a = 1.064690 + 0.333931I$ $b = -0.87449 - 1.44326I$	$-4.46221 + 9.77258I$	$-8.72581 - 8.02773I$
$u = 0.754982 + 0.217030I$ $a = 0.849726 - 0.921367I$ $b = -0.523840 + 0.308432I$	$3.10105 + 2.13666I$	$-4.09917 - 2.47051I$
$u = 0.754982 - 0.217030I$ $a = 0.849726 + 0.921367I$ $b = -0.523840 - 0.308432I$	$3.10105 - 2.13666I$	$-4.09917 + 2.47051I$
$u = 1.39900$ $a = -0.702767$ $b = -12.5949$	$-4.90374$	$-140.900$
$u = 0.133621 + 0.570297I$ $a = 0.730715 + 0.096398I$ $b = -0.904782 - 0.312265I$	$1.42682 + 1.35308I$	$0.34829 - 2.41862I$
$u = 0.133621 - 0.570297I$ $a = 0.730715 - 0.096398I$ $b = -0.904782 + 0.312265I$	$1.42682 - 1.35308I$	$0.34829 + 2.41862I$
$u = -1.25091 + 0.70431I$ $a = -0.754563 - 0.312340I$ $b = 0.351245 + 0.928373I$	$-5.21609 + 2.28754I$	$0$
$u = -1.25091 - 0.70431I$ $a = -0.754563 + 0.312340I$ $b = 0.351245 - 0.928373I$	$-5.21609 - 2.28754I$	$0$
$u = -1.45442$ $a = 0.0474720$ $b = 1.21109$	$-3.37736$	$0$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.45857 + 0.03382I$ $a = -0.622583 - 0.555978I$ $b = 0.018701 - 1.107830I$	$-1.93777 - 2.95731I$	0
$u = -1.45857 - 0.03382I$ $a = -0.622583 + 0.555978I$ $b = 0.018701 + 1.107830I$	$-1.93777 + 2.95731I$	0
$u = 0.056546 + 0.456890I$ $a = -0.64877 + 2.24584I$ $b = 0.904670 - 0.938053I$	$-1.28446 - 0.76291I$	$-5.31890 - 1.67979I$
$u = 0.056546 - 0.456890I$ $a = -0.64877 - 2.24584I$ $b = 0.904670 + 0.938053I$	$-1.28446 + 0.76291I$	$-5.31890 + 1.67979I$
$u = 0.383174 + 0.054663I$ $a = 2.52375 + 1.73333I$ $b = 0.214376 + 0.665960I$	$4.29502 - 2.99232I$	$-13.6444 + 6.7796I$
$u = 0.383174 - 0.054663I$ $a = 2.52375 - 1.73333I$ $b = 0.214376 - 0.665960I$	$4.29502 + 2.99232I$	$-13.6444 - 6.7796I$
$u = -0.330545$ $a = 1.68251$ $b = 0.579990$	$-0.892017$	$-11.9900$
$u = -1.68875 + 0.14392I$ $a = -0.003537 - 0.668461I$ $b = -0.518040 - 1.262490I$	$-9.61160 + 7.52378I$	0
$u = -1.68875 - 0.14392I$ $a = -0.003537 + 0.668461I$ $b = -0.518040 + 1.262490I$	$-9.61160 - 7.52378I$	0
$u = 1.70883 + 0.02668I$ $a = -0.117584 - 0.623199I$ $b = -0.23211 - 1.39628I$	$-10.81520 - 0.66337I$	0

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.70883 - 0.02668I$ $a = -0.117584 + 0.623199I$ $b = -0.23211 + 1.39628I$	$-10.81520 + 0.66337I$	0
$u = -1.71449 + 0.22965I$ $a = -0.820677 + 0.232700I$ $b = 0.88143 + 1.93236I$	$-13.5365 + 13.6208I$	0
$u = -1.71449 - 0.22965I$ $a = -0.820677 - 0.232700I$ $b = 0.88143 - 1.93236I$	$-13.5365 - 13.6208I$	0
$u = 1.73059 + 0.09206I$ $a = -0.776808 - 0.320765I$ $b = 0.52492 - 1.87002I$	$-14.2793 - 5.4313I$	0
$u = 1.73059 - 0.09206I$ $a = -0.776808 + 0.320765I$ $b = 0.52492 + 1.87002I$	$-14.2793 + 5.4313I$	0
$u = -1.73927 + 0.03941I$ $a = 0.823370 + 0.279136I$ $b = -0.408494 + 0.947607I$	$-14.6346 + 1.8508I$	0
$u = -1.73927 - 0.03941I$ $a = 0.823370 - 0.279136I$ $b = -0.408494 - 0.947607I$	$-14.6346 - 1.8508I$	0
$u = -0.220223$ $a = 3.89905$ $b = -3.25550$	0.393691	-52.4600
$u = 1.79882 + 0.15440I$ $a = 0.795536 + 0.161122I$ $b = -0.531853 + 1.253250I$	$-15.9531 - 5.8349I$	0
$u = 1.79882 - 0.15440I$ $a = 0.795536 - 0.161122I$ $b = -0.531853 - 1.253250I$	$-15.9531 + 5.8349I$	0



Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.84865$		
$a = -0.623981$	$-6.53181$	$0$
$b = 0.738641$		

$$\text{II. } I_2^u = \langle -2a^2 - au + b - 2a - u - 1, 4a^3 + 2a^2u - u, u^2 - 2 \rangle$$

(i) Arc colorings

$$a_5 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ 2 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -u \\ -u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 0 \\ -u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} a \\ 2a^2 + au + 2a + u + 1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} a \\ 2a^2 + au + u + 1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} a^2u + a - \frac{1}{2}u \\ 1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} a^2u \\ au + 2a + u + 1 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} a^2u + a - \frac{1}{2}u - 1 \\ 1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} a^2u + a - \frac{1}{2}u \\ 1 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes =  $-4au - 8$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_7$	$(u^3 - u^2 + 2u - 1)^2$
$c_2$	$(u^3 + u^2 - 1)^2$
$c_3$	$(u^3 + u^2 + 2u + 1)^2$
$c_4$	$(u^3 - u^2 + 1)^2$
$c_5, c_6, c_9$ $c_{10}$	$(u^2 - 2)^3$
$c_8$	$(u - 1)^6$
$c_{11}, c_{12}$	$(u + 1)^6$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_3, c_7$	$(y^3 + 3y^2 + 2y - 1)^2$
$c_2, c_4$	$(y^3 - y^2 + 2y - 1)^2$
$c_5, c_6, c_9$ $c_{10}$	$(y - 2)^6$
$c_8, c_{11}, c_{12}$	$(y - 1)^6$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.41421$ $a = -0.620443 + 0.526697I$ $b = 0.510969 + 0.491114I$	$-0.26574 + 2.82812I$	$-4.49024 - 2.97945I$
$u = 1.41421$ $a = -0.620443 - 0.526697I$ $b = 0.510969 - 0.491114I$	$-0.26574 - 2.82812I$	$-4.49024 + 2.97945I$
$u = 1.41421$ $a = 0.533779$ $b = 4.80649$	$-4.40332$	$-11.0200$
$u = -1.41421$ $a = 0.620443 + 0.526697I$ $b = 0.16431 + 1.61567I$	$-0.26574 - 2.82812I$	$-4.49024 + 2.97945I$
$u = -1.41421$ $a = 0.620443 - 0.526697I$ $b = 0.16431 - 1.61567I$	$-0.26574 + 2.82812I$	$-4.49024 - 2.97945I$
$u = -1.41421$ $a = -0.533779$ $b = -0.157054$	$-4.40332$	$-11.0200$

$$\text{III. } I_1^v = \langle a, b + v + 2, v^3 + 3v^2 + 2v - 1 \rangle$$

(i) Arc colorings

$$a_5 = \begin{pmatrix} v \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} v \\ 0 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} v \\ 0 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 0 \\ -v - 2 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} v^2 + 2v - 1 \\ -v - 2 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} v^2 + 2v - 1 \\ -1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -2v^2 - 2v + 1 \\ -v^2 - 2v - 1 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} v^2 + 2v \\ -1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -v^2 - 2v + 1 \\ 1 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes =  $2v^2 + 6v + 10$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_3$	$u^3 - u^2 + 2u - 1$
$c_2$	$u^3 + u^2 - 1$
$c_4$	$u^3 - u^2 + 1$
$c_5, c_6, c_9$ $c_{10}$	$u^3$
$c_7$	$u^3 + u^2 + 2u + 1$
$c_8, c_{11}$	$(u + 1)^3$
$c_{12}$	$(u - 1)^3$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_3, c_7$	$y^3 + 3y^2 + 2y - 1$
$c_2, c_4$	$y^3 - y^2 + 2y - 1$
$c_5, c_6, c_9$ $c_{10}$	$y^3$
$c_8, c_{11}, c_{12}$	$(y - 1)^3$



(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^v$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$v = 0.324718$ $a = 0$ $b = -2.32472$	0.531480	12.1590
$v = -1.66236 + 0.56228I$ $a = 0$ $b = -0.337641 - 0.562280I$	$4.66906 - 2.82812I$	$4.92040 - 0.36516I$
$v = -1.66236 - 0.56228I$ $a = 0$ $b = -0.337641 + 0.562280I$	$4.66906 + 2.82812I$	$4.92040 + 0.36516I$

#### IV. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1$	$((u^3 - u^2 + 2u - 1)^3)(u^{41} + 26u^{40} + \dots + 206u + 1)$
$c_2$	$((u^3 + u^2 - 1)^3)(u^{41} - 4u^{40} + \dots - 14u - 1)$
$c_3$	$(u^3 - u^2 + 2u - 1)(u^3 + u^2 + 2u + 1)^2(u^{41} + 2u^{40} + \dots + 8u - 1)$
$c_4$	$((u^3 - u^2 + 1)^3)(u^{41} - 4u^{40} + \dots - 14u - 1)$
$c_5, c_9, c_{10}$	$u^3(u^2 - 2)^3(u^{41} + 3u^{40} + \dots - 8u - 8)$
$c_6$	$u^3(u^2 - 2)^3(u^{41} - 9u^{40} + \dots + 10824u + 12200)$
$c_7$	$((u^3 - u^2 + 2u - 1)^2)(u^3 + u^2 + 2u + 1)(u^{41} + 2u^{40} + \dots + 8u - 1)$
$c_8$	$((u - 1)^6)(u + 1)^3(u^{41} - 4u^{40} + \dots + 5u - 7)$
$c_{11}$	$((u + 1)^9)(u^{41} - 12u^{40} + \dots + 1593u - 49)$
$c_{12}$	$((u - 1)^3)(u + 1)^6(u^{41} - 4u^{40} + \dots + 5u - 7)$

## V. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1$	$((y^3 + 3y^2 + 2y - 1)^3)(y^{41} - 18y^{40} + \dots + 44086y - 1)$
$c_2, c_4$	$((y^3 - y^2 + 2y - 1)^3)(y^{41} - 26y^{40} + \dots + 206y - 1)$
$c_3, c_7$	$((y^3 + 3y^2 + 2y - 1)^3)(y^{41} + 6y^{40} + \dots + 54y - 1)$
$c_5, c_9, c_{10}$	$y^3(y - 2)^6(y^{41} - 55y^{40} + \dots + 2752y - 64)$
$c_6$	$y^3(y - 2)^6(y^{41} - 139y^{40} + \dots + 8.33469 \times 10^9y - 1.48840 \times 10^8)$
$c_8, c_{12}$	$((y - 1)^9)(y^{41} - 12y^{40} + \dots + 1593y - 49)$
$c_{11}$	$((y - 1)^9)(y^{41} + 44y^{40} + \dots + 664281y - 2401)$