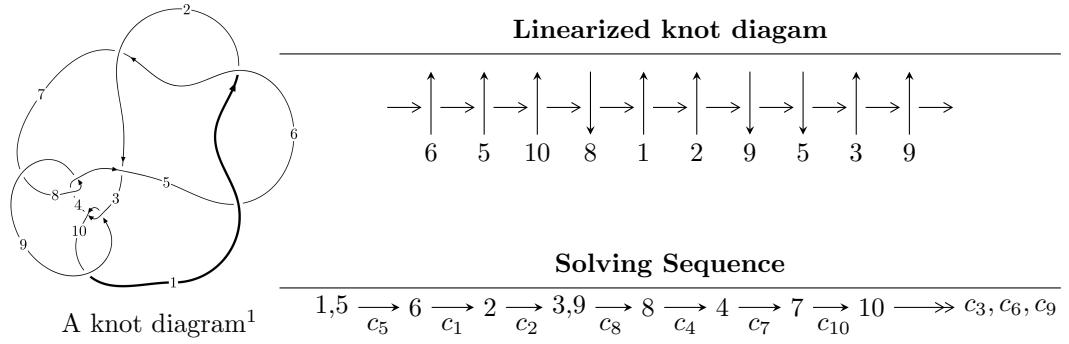


10<sub>143</sub> ( $K10n_{26}$ )



### Ideals for irreducible components<sup>2</sup> of $X_{\text{par}}$

$$I_1^u = \langle 2u^{12} - 2u^{11} - 9u^{10} + 10u^9 + 12u^8 - 18u^7 + 7u^6 + 4u^5 - 25u^4 + 18u^3 + 4u^2 + 4b - 2u + 2, \\ - u^{11} + 4u^9 - 5u^7 - u^5 + 2u^4 + 6u^3 - 2u^2 + 4a + 2u - 4, \\ u^{13} - 2u^{12} - 3u^{11} + 9u^{10} - u^9 - 12u^8 + 14u^7 - 7u^6 - 11u^5 + 23u^4 - 12u^3 + 2u^2 - 2 \rangle$$

$$I_2^u = \langle b + 1, 2a + u, u^2 - 2 \rangle$$

$$I_3^u = \langle -a^2 + b + a, a^3 - 2a^2 + a - 1, u + 1 \rangle$$

$$I_1^v = \langle a, b - 1, v - 1 \rangle$$

\* 4 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 19 representations.

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<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/math/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$I_1^u = \langle 2u^{12} - 2u^{11} + \dots + 4b + 2, -u^{11} + 4u^9 + \dots + 4a - 4, u^{13} - 2u^{12} + \dots + 2u^2 - 2 \rangle$$

(i) **Arc colorings**

$$a_1 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} u \\ -u^3 + u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -u^3 + 2u \\ -u^3 + u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} \frac{1}{4}u^{11} - u^9 + \dots - \frac{1}{2}u + 1 \\ -\frac{1}{2}u^{12} + \frac{1}{2}u^{11} + \dots + \frac{1}{2}u - \frac{1}{2} \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -\frac{1}{2}u^{12} + \frac{3}{4}u^{11} + \dots - \frac{1}{2}u^2 + \frac{1}{2} \\ -\frac{1}{2}u^{12} + \frac{1}{2}u^{11} + \dots + \frac{1}{2}u - \frac{1}{2} \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -\frac{1}{4}u^{11} + u^9 + \dots - \frac{3}{2}u + 1 \\ -\frac{1}{4}u^{11} + u^9 + \dots - \frac{1}{2}u^2 - \frac{1}{2}u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -u^2 + 1 \\ u^4 - 2u^2 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -\frac{1}{4}u^{10} + u^8 + \dots - \frac{1}{2}u + \frac{1}{2} \\ \frac{1}{2}u^7 - \frac{3}{2}u^5 + \frac{1}{2}u^4 + u^3 - u^2 + u \end{pmatrix}$$

(ii) **Obstruction class** = -1

(iii) **Cusp Shapes**

$$= 2u^{12} - 10u^{10} + 2u^9 + 18u^8 - 8u^7 - 4u^6 + 10u^5 - 26u^4 + 20u^2 - 2u + 8$$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_5, c_6$	$u^{13} + 2u^{12} + \cdots - 2u^2 + 2$
$c_2$	$u^{13} + 3u^{12} + \cdots - 92u + 46$
$c_3, c_9$	$u^{13} - 2u^{12} + \cdots - 3u - 1$
$c_4, c_8$	$u^{13} + 2u^{12} + \cdots + 9u - 1$
$c_7$	$u^{13} + 18u^{12} + \cdots + 65u + 1$
$c_{10}$	$u^{13} - 2u^{12} + \cdots + 17u - 1$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_5, c_6$	$y^{13} - 10y^{12} + \cdots + 8y - 4$
$c_2$	$y^{13} + 23y^{12} + \cdots + 7728y - 2116$
$c_3, c_9$	$y^{13} - 2y^{12} + \cdots + 17y - 1$
$c_4, c_8$	$y^{13} - 18y^{12} + \cdots + 65y - 1$
$c_7$	$y^{13} - 42y^{12} + \cdots + 2989y - 1$
$c_{10}$	$y^{13} + 22y^{12} + \cdots + 205y - 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.116060 + 1.025320I$ $a = -1.94905 - 0.25674I$ $b = -1.69551 + 0.12749I$	$-10.21610 + 3.70097I$	$0.67358 - 2.50956I$
$u = 0.116060 - 1.025320I$ $a = -1.94905 + 0.25674I$ $b = -1.69551 - 0.12749I$	$-10.21610 - 3.70097I$	$0.67358 + 2.50956I$
$u = 1.197110 + 0.332616I$ $a = -0.447636 - 0.899887I$ $b = -0.583119 + 0.809161I$	$1.92578 + 4.88678I$	$6.41460 - 5.91732I$
$u = 1.197110 - 0.332616I$ $a = -0.447636 + 0.899887I$ $b = -0.583119 - 0.809161I$	$1.92578 - 4.88678I$	$6.41460 + 5.91732I$
$u = 1.236960 + 0.573659I$ $a = 0.918969 + 0.882216I$ $b = 1.67219 - 0.07727I$	$-6.78115 + 1.92961I$	$2.66803 - 0.98070I$
$u = 1.236960 - 0.573659I$ $a = 0.918969 - 0.882216I$ $b = 1.67219 + 0.07727I$	$-6.78115 - 1.92961I$	$2.66803 + 0.98070I$
$u = 1.38959$ $a = -0.810069$ $b = -0.135830$	6.53354	13.9760
$u = 0.094132 + 0.586012I$ $a = 0.854196 + 0.075054I$ $b = 0.787240 + 0.445864I$	$-1.38205 - 1.36942I$	$-0.56235 + 3.09698I$
$u = 0.094132 - 0.586012I$ $a = 0.854196 - 0.075054I$ $b = 0.787240 - 0.445864I$	$-1.38205 + 1.36942I$	$-0.56235 - 3.09698I$
$u = -1.45446$ $a = 0.0472843$ $b = -1.10499$	3.37738	1.87580

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.40252 + 0.47847I$		
$a = 0.81193 - 1.16730I$	$-5.44762 - 9.07090I$	$4.16718 + 5.02365I$
$b = 1.62497 + 0.28976I$		
$u = -1.40252 - 0.47847I$		
$a = 0.81193 + 1.16730I$	$-5.44762 + 9.07090I$	$4.16718 - 5.02365I$
$b = 1.62497 - 0.28976I$		
$u = -0.418617$		
$a = 1.38596$	0.992576	11.4260
$b = -0.370722$		

$$\text{II. } I_2^u = \langle b+1, 2a+u, u^2 - 2 \rangle$$

(i) Arc colorings

$$\begin{aligned} a_1 &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_5 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_6 &= \begin{pmatrix} 1 \\ -2 \end{pmatrix} \\ a_2 &= \begin{pmatrix} u \\ -u \end{pmatrix} \\ a_3 &= \begin{pmatrix} 0 \\ -u \end{pmatrix} \\ a_9 &= \begin{pmatrix} -\frac{1}{2}u \\ -1 \end{pmatrix} \\ a_8 &= \begin{pmatrix} -\frac{1}{2}u - 1 \\ -1 \end{pmatrix} \\ a_4 &= \begin{pmatrix} -\frac{1}{2}u \\ -1 \end{pmatrix} \\ a_7 &= \begin{pmatrix} -1 \\ 0 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} -\frac{1}{2}u \\ u - 1 \end{pmatrix} \end{aligned}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = 8

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_2, c_5$ $c_6$	$u^2 - 2$
$c_3, c_4$	$(u + 1)^2$
$c_7, c_8, c_9$ $c_{10}$	$(u - 1)^2$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_5$ $c_6$	$(y - 2)^2$
$c_3, c_4, c_7$ $c_8, c_9, c_{10}$	$(y - 1)^2$

**(vi) Complex Volumes and Cusp Shapes**

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.41421$		
$a = -0.707107$	4.93480	8.00000
$b = -1.00000$		
$u = -1.41421$		
$a = 0.707107$	4.93480	8.00000
$b = -1.00000$		

$$\text{III. } I_3^u = \langle -a^2 + b + a, a^3 - 2a^2 + a - 1, u + 1 \rangle$$

(i) Arc colorings

$$a_1 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} a \\ a^2 - a \end{pmatrix}$$

$$a_8 = \begin{pmatrix} a^2 \\ a^2 - a \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -a^2 \\ -a \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} a^2 \\ a^2 - a \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes = 6

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_5, c_6$	$(u - 1)^3$
$c_2$	$u^3$
$c_3, c_4, c_8$ $c_9$	$u^3 - u + 1$
$c_7$	$u^3 + 2u^2 + u + 1$
$c_{10}$	$u^3 - 2u^2 + u - 1$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_5, c_6$	$(y - 1)^3$
$c_2$	$y^3$
$c_3, c_4, c_8$ $c_9$	$y^3 - 2y^2 + y - 1$
$c_7, c_{10}$	$y^3 - 2y^2 - 3y - 1$

**(vi) Complex Volumes and Cusp Shapes**

Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.00000$		
$a = 0.122561 + 0.744862I$	1.64493	6.00000
$b = -0.662359 - 0.562280I$		
$u = -1.00000$		
$a = 0.122561 - 0.744862I$	1.64493	6.00000
$b = -0.662359 + 0.562280I$		
$u = -1.00000$		
$a = 1.75488$	1.64493	6.00000
$b = 1.32472$		

$$\text{IV. } I_1^v = \langle a, b - 1, v - 1 \rangle$$

(i) **Arc colorings**

$$a_1 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

(ii) **Obstruction class = 1**

(iii) **Cusp Shapes = 0**

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_2, c_5$ $c_6$	$u$
$c_3, c_4, c_7$ $c_{10}$	$u - 1$
$c_8, c_9$	$u + 1$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_5$ $c_6$	$y$
$c_3, c_4, c_7$ $c_8, c_9, c_{10}$	$y - 1$

**(vi) Complex Volumes and Cusp Shapes**

Solutions to $I_1^v$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$v = 1.00000$		
$a = 0$	0	0
$b = 1.00000$		

## V. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1, c_5, c_6$	$u(u - 1)^3(u^2 - 2)(u^{13} + 2u^{12} + \dots - 2u^2 + 2)$
$c_2$	$u^4(u^2 - 2)(u^{13} + 3u^{12} + \dots - 92u + 46)$
$c_3$	$(u - 1)(u + 1)^2(u^3 - u + 1)(u^{13} - 2u^{12} + \dots - 3u - 1)$
$c_4$	$(u - 1)(u + 1)^2(u^3 - u + 1)(u^{13} + 2u^{12} + \dots + 9u - 1)$
$c_7$	$((u - 1)^3)(u^3 + 2u^2 + u + 1)(u^{13} + 18u^{12} + \dots + 65u + 1)$
$c_8$	$((u - 1)^2)(u + 1)(u^3 - u + 1)(u^{13} + 2u^{12} + \dots + 9u - 1)$
$c_9$	$((u - 1)^2)(u + 1)(u^3 - u + 1)(u^{13} - 2u^{12} + \dots - 3u - 1)$
$c_{10}$	$((u - 1)^3)(u^3 - 2u^2 + u - 1)(u^{13} - 2u^{12} + \dots + 17u - 1)$

## VI. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1, c_5, c_6$	$y(y - 2)^2(y - 1)^3(y^{13} - 10y^{12} + \dots + 8y - 4)$
$c_2$	$y^4(y - 2)^2(y^{13} + 23y^{12} + \dots + 7728y - 2116)$
$c_3, c_9$	$((y - 1)^3)(y^3 - 2y^2 + y - 1)(y^{13} - 2y^{12} + \dots + 17y - 1)$
$c_4, c_8$	$((y - 1)^3)(y^3 - 2y^2 + y - 1)(y^{13} - 18y^{12} + \dots + 65y - 1)$
$c_7$	$((y - 1)^3)(y^3 - 2y^2 - 3y - 1)(y^{13} - 42y^{12} + \dots + 2989y - 1)$
$c_{10}$	$((y - 1)^3)(y^3 - 2y^2 - 3y - 1)(y^{13} + 22y^{12} + \dots + 205y - 1)$