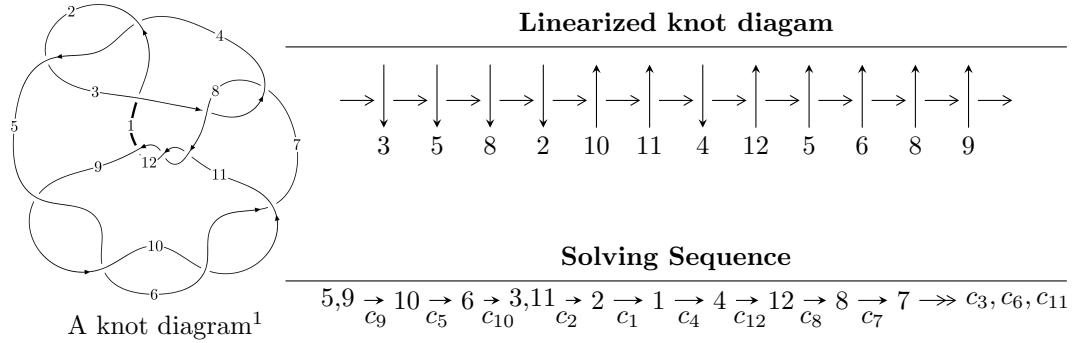


$12n_{0192}$ ($K12n_{0192}$)



Ideals for irreducible components² of X_{par}

$$\begin{aligned}
 I_1^u &= \langle -3.17034 \times 10^{19} u^{22} + 2.06027 \times 10^{19} u^{21} + \dots + 1.07970 \times 10^{20} b + 1.66107 \times 10^{20}, \\
 &\quad - 9.79843 \times 10^{18} u^{22} - 2.69589 \times 10^{19} u^{21} + \dots + 2.15940 \times 10^{20} a - 7.11427 \times 10^{20}, \\
 &\quad u^{23} - 2u^{22} + \dots - 24u + 8 \rangle \\
 I_2^u &= \langle -2a^2 - au + b - 2a - u - 1, 4a^3 + 2a^2u - u, u^2 - 2 \rangle \\
 I_3^u &= \langle b + u - 1, u^2 + a - u - 2, u^3 - u^2 - 2u + 1 \rangle
 \end{aligned}$$

$$I_1^v = \langle a, b + v + 2, v^3 + 3v^2 + 2v - 1 \rangle$$

* 4 irreducible components of $\dim_{\mathbb{C}} = 0$, with total 35 representations.

¹The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/math/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

²All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\text{I. } I_1^u = \langle -3.17 \times 10^{19}u^{22} + 2.06 \times 10^{19}u^{21} + \dots + 1.08 \times 10^{20}b + 1.66 \times 10^{20}, -9.80 \times 10^{18}u^{22} - 2.70 \times 10^{19}u^{21} + \dots + 2.16 \times 10^{20}a - 7.11 \times 10^{20}, u^{23} - 2u^{22} + \dots - 24u + 8 \rangle$$

(i) Arc colorings

$$\begin{aligned} a_5 &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_9 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} 1 \\ -u^2 \end{pmatrix} \\ a_6 &= \begin{pmatrix} u \\ -u^3 + u \end{pmatrix} \\ a_3 &= \begin{pmatrix} 0.0453756u^{22} + 0.124844u^{21} + \dots + 6.96611u + 3.29455 \\ 0.293631u^{22} - 0.190818u^{21} + \dots + 6.03607u - 1.53845 \end{pmatrix} \\ a_{11} &= \begin{pmatrix} -u^2 + 1 \\ u^4 - 2u^2 \end{pmatrix} \\ a_2 &= \begin{pmatrix} 0.0453756u^{22} + 0.124844u^{21} + \dots + 6.96611u + 3.29455 \\ -0.0606713u^{22} + 0.0493494u^{21} + \dots + 1.22479u + 0.186315 \end{pmatrix} \\ a_1 &= \begin{pmatrix} 0.00815407u^{22} + 0.0581561u^{21} + \dots + 0.816899u + 0.942300 \\ 0.167916u^{22} - 0.134620u^{21} + \dots + 3.19264u - 1.46520 \end{pmatrix} \\ a_4 &= \begin{pmatrix} -0.318134u^{22} + 0.323483u^{21} + \dots + 1.70680u + 4.47989 \\ 0.354835u^{22} - 0.251401u^{21} + \dots + 7.02928u - 1.98143 \end{pmatrix} \\ a_{12} &= \begin{pmatrix} -0.159762u^{22} + 0.192776u^{21} + \dots - 2.37574u + 2.40750 \\ 0.167916u^{22} - 0.134620u^{21} + \dots + 3.19264u - 1.46520 \end{pmatrix} \\ a_8 &= \begin{pmatrix} -0.231610u^{22} + 0.238881u^{21} + \dots - 3.80455u + 2.85872 \\ 0.190322u^{22} - 0.136611u^{21} + \dots + 2.10246u - 1.34349 \end{pmatrix} \\ a_7 &= \begin{pmatrix} u^3 - 2u \\ -u^5 + 3u^3 - u \end{pmatrix} \end{aligned}$$

(ii) Obstruction class = -1

$$\text{(iii) Cusp Shapes} = \frac{158891265015344169787}{765639597674599940106}u^{22} - \frac{49683941378257544770}{26992561435056463973}u^{21} + \dots - \frac{107970245740225855892}{395673949272391412502}u - \frac{26992561435056463973}{26992561435056463973}$$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1	$u^{23} + 23u^{22} + \cdots + 431u + 1$
c_2, c_4	$u^{23} - 7u^{22} + \cdots - 25u - 1$
c_3, c_7	$u^{23} + 2u^{22} + \cdots - 92u + 8$
c_5, c_6, c_9 c_{10}	$u^{23} + 2u^{22} + \cdots - 24u - 8$
c_8, c_{11}, c_{12}	$u^{23} - 5u^{22} + \cdots + 105u - 7$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1	$y^{23} - 39y^{22} + \cdots + 167215y - 1$
c_2, c_4	$y^{23} - 23y^{22} + \cdots + 431y - 1$
c_3, c_7	$y^{23} - 12y^{22} + \cdots + 4048y - 64$
c_5, c_6, c_9 c_{10}	$y^{23} - 18y^{22} + \cdots + 1984y - 64$
c_8, c_{11}, c_{12}	$y^{23} - 3y^{22} + \cdots + 3857y - 49$

(vi) Complex Volumes and Cusp Shapes

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.524450 + 0.823406I$		
$a = 1.198540 - 0.301680I$	$-2.40419 - 0.36830I$	$2.14910 - 0.07440I$
$b = -0.0820455 - 0.0681602I$		
$u = 0.524450 - 0.823406I$		
$a = 1.198540 + 0.301680I$	$-2.40419 + 0.36830I$	$2.14910 + 0.07440I$
$b = -0.0820455 + 0.0681602I$		
$u = 0.647880 + 0.361661I$		
$a = -1.60944 - 0.06303I$	$5.21554 - 2.25150I$	$8.85155 - 0.03890I$
$b = 0.610235 + 0.499402I$		
$u = 0.647880 - 0.361661I$		
$a = -1.60944 + 0.06303I$	$5.21554 + 2.25150I$	$8.85155 + 0.03890I$
$b = 0.610235 - 0.499402I$		
$u = -0.968334 + 0.805177I$		
$a = -0.791369 - 0.993332I$	$-3.71088 - 3.05913I$	$3.40896 + 2.62935I$
$b = 0.30258 - 1.86935I$		
$u = -0.968334 - 0.805177I$		
$a = -0.791369 + 0.993332I$	$-3.71088 + 3.05913I$	$3.40896 - 2.62935I$
$b = 0.30258 + 1.86935I$		
$u = 1.348180 + 0.047266I$		
$a = -0.707662 - 0.573551I$	$7.94226 - 2.99119I$	$5.45880 + 3.25887I$
$b = 0.028918 - 1.035860I$		
$u = 1.348180 - 0.047266I$		
$a = -0.707662 + 0.573551I$	$7.94226 + 2.99119I$	$5.45880 - 3.25887I$
$b = 0.028918 + 1.035860I$		
$u = 1.37411$		
$a = 0.0360037$	6.50526	14.0870
$b = 1.16320$		
$u = -0.596550 + 0.120314I$		
$a = -0.457301 - 0.724116I$	$0.931592 - 0.038203I$	$9.32722 + 1.98466I$
$b = -0.799393 - 0.727747I$		

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.596550 - 0.120314I$		
$a = -0.457301 + 0.724116I$	$0.931592 + 0.038203I$	$9.32722 - 1.98466I$
$b = -0.799393 + 0.727747I$		
$u = 1.253460 + 0.611260I$		
$a = -0.257061 - 0.819047I$	$-0.01572 + 5.94333I$	$6.39784 - 4.46809I$
$b = -0.178277 - 0.996927I$		
$u = 1.253460 - 0.611260I$		
$a = -0.257061 + 0.819047I$	$-0.01572 - 5.94333I$	$6.39784 + 4.46809I$
$b = -0.178277 + 0.996927I$		
$u = -1.42929$		
$a = -0.686494$	4.96770	-112.550
$b = -12.0652$		
$u = -0.25726 + 1.43341I$		
$a = -0.014716 + 1.238780I$	$-11.10700 - 5.35109I$	$2.30683 + 2.56727I$
$b = -0.02116 + 1.93499I$		
$u = -0.25726 - 1.43341I$		
$a = -0.014716 - 1.238780I$	$-11.10700 + 5.35109I$	$2.30683 - 2.56727I$
$b = -0.02116 - 1.93499I$		
$u = -0.444315$		
$a = -0.534871$	0.878779	12.7060
$b = -0.856360$		
$u = 1.59666 + 0.55985I$		
$a = -0.723361 + 0.626398I$	$-5.20585 + 12.38690I$	$5.26515 - 5.63238I$
$b = 0.55500 + 2.06165I$		
$u = 1.59666 - 0.55985I$		
$a = -0.723361 - 0.626398I$	$-5.20585 - 12.38690I$	$5.26515 + 5.63238I$
$b = 0.55500 - 2.06165I$		
$u = -1.49695 + 0.90558I$		
$a = 0.809749 + 0.607559I$	$-7.48548 - 2.83924I$	$3.01997 + 1.35778I$
$b = -0.42702 + 1.59069I$		

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.49695 - 0.90558I$		
$a = 0.809749 - 0.607559I$	$-7.48548 + 2.83924I$	$3.01997 - 1.35778I$
$b = -0.42702 - 1.59069I$		
$u = 0.244699$		
$a = 3.66585$	-1.28182	-11.3970
$b = 0.520617$		
$u = -1.84826$		
$a = 0.624762$	15.6748	-4.21640
$b = -0.739954$		

$$\text{III. } I_2^u = \langle -2a^2 - au + b - 2a - u - 1, 4a^3 + 2a^2u - u, u^2 - 2 \rangle$$

(i) Arc colorings

$$\begin{aligned} a_5 &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_9 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} 1 \\ -2 \end{pmatrix} \\ a_6 &= \begin{pmatrix} u \\ -u \end{pmatrix} \\ a_3 &= \begin{pmatrix} a \\ 2a^2 + au + 2a + u + 1 \end{pmatrix} \\ a_{11} &= \begin{pmatrix} -1 \\ 0 \end{pmatrix} \\ a_2 &= \begin{pmatrix} a \\ 2a^2 + au + u + 1 \end{pmatrix} \\ a_1 &= \begin{pmatrix} a^2u + a - \frac{1}{2}u \\ 1 \end{pmatrix} \\ a_4 &= \begin{pmatrix} a^2u \\ au + 2a + u + 1 \end{pmatrix} \\ a_{12} &= \begin{pmatrix} a^2u + a - \frac{1}{2}u - 1 \\ 1 \end{pmatrix} \\ a_8 &= \begin{pmatrix} a^2u + a - \frac{1}{2}u \\ 1 \end{pmatrix} \\ a_7 &= \begin{pmatrix} 0 \\ -u \end{pmatrix} \end{aligned}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = $-4au + 8$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1, c_7	$(u^3 - u^2 + 2u - 1)^2$
c_2	$(u^3 + u^2 - 1)^2$
c_3	$(u^3 + u^2 + 2u + 1)^2$
c_4	$(u^3 - u^2 + 1)^2$
c_5, c_6, c_9 c_{10}	$(u^2 - 2)^3$
c_8	$(u - 1)^6$
c_{11}, c_{12}	$(u + 1)^6$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1, c_3, c_7	$(y^3 + 3y^2 + 2y - 1)^2$
c_2, c_4	$(y^3 - y^2 + 2y - 1)^2$
c_5, c_6, c_9 c_{10}	$(y - 2)^6$
c_8, c_{11}, c_{12}	$(y - 1)^6$

(vi) Complex Volumes and Cusp Shapes

Solutions to I_2^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.41421$		
$a = -0.620443 + 0.526697I$	$9.60386 + 2.82812I$	$11.50976 - 2.97945I$
$b = 0.510969 + 0.491114I$		
$u = -1.41421$		
$a = -0.620443 - 0.526697I$	$9.60386 - 2.82812I$	$11.50976 + 2.97945I$
$b = 0.510969 - 0.491114I$		
$u = 1.41421$		
$a = 0.533779$	5.46628	4.98050
$b = 4.80649$		
$u = -1.41421$		
$a = 0.620443 + 0.526697I$	$9.60386 - 2.82812I$	$11.50976 + 2.97945I$
$b = 0.16431 + 1.61567I$		
$u = -1.41421$		
$a = 0.620443 - 0.526697I$	$9.60386 + 2.82812I$	$11.50976 - 2.97945I$
$b = 0.16431 - 1.61567I$		
$u = -1.41421$		
$a = -0.533779$	5.46628	4.98050
$b = -0.157054$		

$$\text{III. } I_3^u = \langle b + u - 1, \ u^2 + a - u - 2, \ u^3 - u^2 - 2u + 1 \rangle$$

(i) Arc colorings

$$a_5 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} u \\ -u^2 - u + 1 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -u^2 + u + 2 \\ -u + 1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -u^2 + 1 \\ u^2 + u - 1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -u^2 + u + 2 \\ -2u + 1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 0 \\ -u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -u^2 + u + 2 \\ -u + 1 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} u \\ -u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -u^2 + 1 \\ u^2 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -u^2 + 1 \\ u^2 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = $u^2 + 4u + 12$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1, c_2	$(u - 1)^3$
c_3, c_7	u^3
c_4	$(u + 1)^3$
c_5, c_6, c_8	$u^3 + u^2 - 2u - 1$
c_9, c_{10}, c_{11} c_{12}	$u^3 - u^2 - 2u + 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1, c_2, c_4	$(y - 1)^3$
c_3, c_7	y^3
c_5, c_6, c_8 c_9, c_{10}, c_{11} c_{12}	$y^3 - 5y^2 + 6y - 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to I_3^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.24698$		
$a = -0.801938$	4.69981	8.56700
$b = 2.24698$		
$u = 0.445042$		
$a = 2.24698$	-0.939962	13.9780
$b = 0.554958$		
$u = 1.80194$		
$a = 0.554958$	15.9794	22.4550
$b = -0.801938$		

$$\text{IV. } I_1^v = \langle a, b + v + 2, v^3 + 3v^2 + 2v - 1 \rangle$$

(i) Arc colorings

$$\begin{aligned} a_5 &= \begin{pmatrix} v \\ 0 \end{pmatrix} \\ a_9 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_6 &= \begin{pmatrix} v \\ 0 \end{pmatrix} \\ a_3 &= \begin{pmatrix} 0 \\ -v - 2 \end{pmatrix} \\ a_{11} &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_2 &= \begin{pmatrix} v^2 + 2v - 1 \\ -v - 2 \end{pmatrix} \\ a_1 &= \begin{pmatrix} v^2 + 2v - 1 \\ -1 \end{pmatrix} \\ a_4 &= \begin{pmatrix} -2v^2 - 2v + 1 \\ -v^2 - 2v - 1 \end{pmatrix} \\ a_{12} &= \begin{pmatrix} v^2 + 2v \\ -1 \end{pmatrix} \\ a_8 &= \begin{pmatrix} -v^2 - 2v + 1 \\ 1 \end{pmatrix} \\ a_7 &= \begin{pmatrix} v \\ 0 \end{pmatrix} \end{aligned}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = $-10v^2 - 22v - 10$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1, c_3	$u^3 - u^2 + 2u - 1$
c_2	$u^3 + u^2 - 1$
c_4	$u^3 - u^2 + 1$
c_5, c_6, c_9 c_{10}	u^3
c_7	$u^3 + u^2 + 2u + 1$
c_8	$(u + 1)^3$
c_{11}, c_{12}	$(u - 1)^3$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1, c_3, c_7	$y^3 + 3y^2 + 2y - 1$
c_2, c_4	$y^3 - y^2 + 2y - 1$
c_5, c_6, c_9 c_{10}	y^3
c_8, c_{11}, c_{12}	$(y - 1)^3$

(vi) Complex Volumes and Cusp Shapes

Solutions to I_1^v	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$v = 0.324718$		
$a = 0$	0.531480	-18.1980
$b = -2.32472$		
$v = -1.66236 + 0.56228I$		
$a = 0$	4.66906 - 2.82812I	2.09911 + 6.32406I
$b = -0.337641 - 0.562280I$		
$v = -1.66236 - 0.56228I$		
$a = 0$	4.66906 + 2.82812I	2.09911 - 6.32406I
$b = -0.337641 + 0.562280I$		

V. u-Polynomials

Crossings	u-Polynomials at each crossing
c_1	$((u - 1)^3)(u^3 - u^2 + 2u - 1)^3(u^{23} + 23u^{22} + \dots + 431u + 1)$
c_2	$((u - 1)^3)(u^3 + u^2 - 1)^3(u^{23} - 7u^{22} + \dots - 25u - 1)$
c_3	$u^3(u^3 - u^2 + 2u - 1)(u^3 + u^2 + 2u + 1)^2(u^{23} + 2u^{22} + \dots - 92u + 8)$
c_4	$((u + 1)^3)(u^3 - u^2 + 1)^3(u^{23} - 7u^{22} + \dots - 25u - 1)$
c_5, c_6	$u^3(u^2 - 2)^3(u^3 + u^2 - 2u - 1)(u^{23} + 2u^{22} + \dots - 24u - 8)$
c_7	$u^3(u^3 - u^2 + 2u - 1)^2(u^3 + u^2 + 2u + 1)(u^{23} + 2u^{22} + \dots - 92u + 8)$
c_8	$((u - 1)^6)(u + 1)^3(u^3 + u^2 - 2u - 1)(u^{23} - 5u^{22} + \dots + 105u - 7)$
c_9, c_{10}	$u^3(u^2 - 2)^3(u^3 - u^2 - 2u + 1)(u^{23} + 2u^{22} + \dots - 24u - 8)$
c_{11}, c_{12}	$((u - 1)^3)(u + 1)^6(u^3 - u^2 - 2u + 1)(u^{23} - 5u^{22} + \dots + 105u - 7)$

VI. Riley Polynomials

Crossings	Riley Polynomials at each crossing
c_1	$((y - 1)^3)(y^3 + 3y^2 + 2y - 1)^3(y^{23} - 39y^{22} + \dots + 167215y - 1)$
c_2, c_4	$((y - 1)^3)(y^3 - y^2 + 2y - 1)^3(y^{23} - 23y^{22} + \dots + 431y - 1)$
c_3, c_7	$y^3(y^3 + 3y^2 + 2y - 1)^3(y^{23} - 12y^{22} + \dots + 4048y - 64)$
c_5, c_6, c_9 c_{10}	$y^3(y - 2)^6(y^3 - 5y^2 + 6y - 1)(y^{23} - 18y^{22} + \dots + 1984y - 64)$
c_8, c_{11}, c_{12}	$((y - 1)^9)(y^3 - 5y^2 + 6y - 1)(y^{23} - 3y^{22} + \dots + 3857y - 49)$