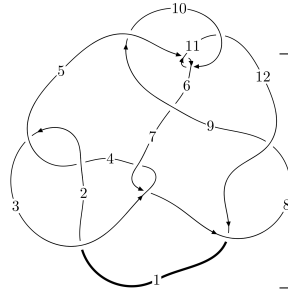
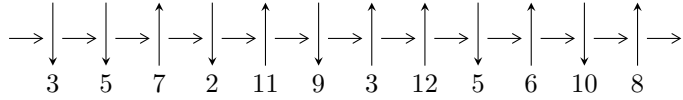


12n₀₁₉₈ (K12n₀₁₉₈)



A knot diagram¹

Linearized knot diagram



Solving Sequence

$$5,11 \xrightarrow{c_5} 3,6 \xrightarrow{c_2} 2 \xrightarrow{c_1} 1 \xrightarrow{c_4} 4 \xrightarrow{c_{10}} 10 \xrightarrow{c_{11}} 12 \xrightarrow{c_9} 9 \xrightarrow{c_6} 7 \xrightarrow{c_8} 8 \rightsquigarrow c_3, c_7, c_{12}$$

Ideals for irreducible components² of X_{par}

$$I_1^u = \langle -u^{21} - u^{20} + \dots + b - u, -u^{21} - u^{20} + \dots - 3u^3 + a, u^{23} + 2u^{22} + \dots + 2u + 1 \rangle$$

$$I_2^u = \langle b + 1, -u^3 + u^2 + a, u^4 + u^2 + u + 1 \rangle$$

$$I_3^u = \langle b + 1, -u^3 + a - u + 1, u^6 - u^5 + 2u^4 - 2u^3 + 2u^2 - 2u + 1 \rangle$$

* 3 irreducible components of $\dim_{\mathbb{C}} = 0$, with total 33 representations.

¹The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

²All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$I_1^u = \langle -u^{21} - u^{20} + \dots + b - u, -u^{21} - u^{20} + \dots - 3u^3 + a, u^{23} + 2u^{22} + \dots + 2u + 1 \rangle \quad \text{I.}$$

(i) Arc colorings

$$a_5 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} u^{21} + u^{20} + \dots + u^4 + 3u^3 \\ u^{21} + u^{20} + \dots + u^2 + u \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 2u^{21} + 2u^{20} + \dots + u^2 + u \\ u^{21} + u^{20} + \dots + u^2 + u \end{pmatrix}$$

$$a_1 = \begin{pmatrix} u^{19} + 4u^{17} + 8u^{15} + 8u^{13} + 3u^{11} - 2u^9 - 2u^7 + u^3 \\ -u^{21} - 5u^{19} + \dots - u^3 - u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 3u^{21} + 3u^{20} + \dots + 3u + 1 \\ u^{21} + u^{20} + \dots + u^2 + 2u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -u \\ u^3 + u \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -u^3 \\ u^5 + u^3 + u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} u^3 \\ u^3 + u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} u^8 + u^6 + u^4 + 1 \\ u^8 + 2u^6 + 2u^4 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -u^{11} - 2u^9 - 2u^7 + u^3 \\ u^{13} + 3u^{11} + 5u^9 + 4u^7 + 2u^5 + u^3 + u \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes

$$= 4u^{22} + 12u^{21} + 34u^{20} + 68u^{19} + 118u^{18} + 192u^{17} + 251u^{16} + 335u^{15} + 353u^{14} + 392u^{13} + 355u^{12} + 316u^{11} + 243u^{10} + 163u^9 + 106u^8 + 46u^7 + 14u^6 + 11u^5 + 15u^4 + 30u^3 + 15u^2 + 13u + 6$$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1	$u^{23} + 47u^{22} + \dots - 11u + 1$
c_2, c_4	$u^{23} - 11u^{22} + \dots - 9u + 1$
c_3, c_7	$u^{23} - u^{22} + \dots + 2048u + 1024$
c_5, c_{10}	$u^{23} - 2u^{22} + \dots + 2u - 1$
c_6	$u^{23} - 10u^{22} + \dots + 120u - 31$
c_8, c_{12}	$u^{23} + 24u^{21} + \dots + 2u + 1$
c_9	$u^{23} + 2u^{22} + \dots - 15u^2 - 8$
c_{11}	$u^{23} + 12u^{22} + \dots - 2u - 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1	$y^{23} - 211y^{22} + \dots - 215y - 1$
c_2, c_4	$y^{23} - 47y^{22} + \dots - 11y - 1$
c_3, c_7	$y^{23} + 63y^{22} + \dots + 8912896y - 1048576$
c_5, c_{10}	$y^{23} + 12y^{22} + \dots - 2y - 1$
c_6	$y^{23} - 12y^{22} + \dots - 6122y - 961$
c_8, c_{12}	$y^{23} + 48y^{22} + \dots - 2y - 1$
c_9	$y^{23} - 12y^{22} + \dots - 240y - 64$
c_{11}	$y^{23} + 24y^{21} + \dots + 2y - 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.695674 + 0.794301I$		
$a = -0.38303 + 1.50526I$	$-15.4705 + 2.6332I$	$-1.74115 - 2.82837I$
$b = 2.14604 - 0.04602I$		
$u = 0.695674 - 0.794301I$		
$a = -0.38303 - 1.50526I$	$-15.4705 - 2.6332I$	$-1.74115 + 2.82837I$
$b = 2.14604 + 0.04602I$		
$u = -0.851428 + 0.257921I$		
$a = 0.102425 + 0.901741I$	$-18.5278 + 5.0308I$	$-2.42173 - 1.77619I$
$b = 2.23097 - 0.23648I$		
$u = -0.851428 - 0.257921I$		
$a = 0.102425 - 0.901741I$	$-18.5278 - 5.0308I$	$-2.42173 + 1.77619I$
$b = 2.23097 + 0.23648I$		
$u = -0.483954 + 1.020520I$		
$a = 0.825387 - 0.274069I$	$-0.56646 - 3.01940I$	$3.36749 + 3.11832I$
$b = 0.223453 + 0.115878I$		
$u = -0.483954 - 1.020520I$		
$a = 0.825387 + 0.274069I$	$-0.56646 + 3.01940I$	$3.36749 - 3.11832I$
$b = 0.223453 - 0.115878I$		
$u = 0.364715 + 1.105530I$		
$a = 0.392472 - 0.466255I$	$-3.74014 + 1.10612I$	$-5.73854 - 0.32981I$
$b = -0.334457 - 0.705017I$		
$u = 0.364715 - 1.105530I$		
$a = 0.392472 + 0.466255I$	$-3.74014 - 1.10612I$	$-5.73854 + 0.32981I$
$b = -0.334457 + 0.705017I$		
$u = 0.518947 + 1.123690I$		
$a = -0.425430 + 0.139303I$	$-2.62716 + 6.50806I$	$-2.44317 - 6.43144I$
$b = 0.028115 + 0.688429I$		
$u = 0.518947 - 1.123690I$		
$a = -0.425430 - 0.139303I$	$-2.62716 - 6.50806I$	$-2.44317 + 6.43144I$
$b = 0.028115 - 0.688429I$		

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.213623 + 0.731187I$ $a = -0.66221 - 1.37892I$ $b = -0.994946 + 0.319082I$	$-2.09274 + 1.02920I$	$-5.56905 - 0.54720I$
$u = 0.213623 - 0.731187I$ $a = -0.66221 + 1.37892I$ $b = -0.994946 - 0.319082I$	$-2.09274 - 1.02920I$	$-5.56905 + 0.54720I$
$u = -0.449726 + 1.155180I$ $a = -2.55174 + 1.46474I$ $b = -1.68340 - 0.16500I$	$-6.16024 - 4.07736I$	$-6.51340 + 3.55333I$
$u = -0.449726 - 1.155180I$ $a = -2.55174 - 1.46474I$ $b = -1.68340 + 0.16500I$	$-6.16024 + 4.07736I$	$-6.51340 - 3.55333I$
$u = -0.490965 + 0.550455I$ $a = 0.503661 + 0.280792I$ $b = 0.106838 - 0.230098I$	$0.861404 - 1.022110I$	$5.67905 + 4.33251I$
$u = -0.490965 - 0.550455I$ $a = 0.503661 - 0.280792I$ $b = 0.106838 + 0.230098I$	$0.861404 + 1.022110I$	$5.67905 - 4.33251I$
$u = -0.276568 + 1.232250I$ $a = 2.87251 - 0.51904I$ $b = 2.32781 - 0.18898I$	$16.1704 + 1.4493I$	$-7.34390 + 0.38241I$
$u = -0.276568 - 1.232250I$ $a = 2.87251 + 0.51904I$ $b = 2.32781 + 0.18898I$	$16.1704 - 1.4493I$	$-7.34390 - 0.38241I$
$u = 0.653892 + 0.258897I$ $a = 0.330772 + 0.501247I$ $b = -0.038798 - 0.528699I$	$-0.16241 - 1.94681I$	$1.33418 + 3.65595I$
$u = 0.653892 - 0.258897I$ $a = 0.330772 - 0.501247I$ $b = -0.038798 + 0.528699I$	$-0.16241 + 1.94681I$	$1.33418 - 3.65595I$

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.568317 + 1.180040I$		
$a = 2.01303 - 2.60561I$	$18.1942 - 10.2590I$	$-5.29878 + 5.24355I$
$b = 2.23769 + 0.30194I$		
$u = -0.568317 - 1.180040I$		
$a = 2.01303 + 2.60561I$	$18.1942 + 10.2590I$	$-5.29878 - 5.24355I$
$b = 2.23769 - 0.30194I$		
$u = -0.651787$		
$a = -1.03569$	-3.01079	-2.62200
$b = -1.49862$		

$$\text{II. } I_2^u = \langle b + 1, -u^3 + u^2 + a, u^4 + u^2 + u + 1 \rangle$$

(i) Arc colorings

$$a_5 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} u^3 - u^2 \\ -1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} u^3 - u^2 - 1 \\ -1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} u^3 - u^2 \\ -1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -u \\ u^3 + u \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -u^3 \\ -u^2 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} u^3 \\ u^3 + u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} u^3 + u^2 + u + 1 \\ u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} u^3 + u^2 + u + 1 \\ u \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = $3u^3 - 4u^2 - u - 2$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1, c_2	$(u - 1)^4$
c_3, c_7	u^4
c_4	$(u + 1)^4$
c_5, c_8	$u^4 + u^2 + u + 1$
c_6	$u^4 - 2u^3 + 3u^2 - u + 1$
c_9	$u^4 - 3u^3 + 4u^2 - 3u + 2$
c_{10}, c_{12}	$u^4 + u^2 - u + 1$
c_{11}	$u^4 + 2u^3 + 3u^2 + u + 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1, c_2, c_4	$(y - 1)^4$
c_3, c_7	y^4
c_5, c_8, c_{10} c_{12}	$y^4 + 2y^3 + 3y^2 + y + 1$
c_6, c_{11}	$y^4 + 2y^3 + 7y^2 + 5y + 1$
c_9	$y^4 - y^3 + 2y^2 + 7y + 4$

(vi) Complex Volumes and Cusp Shapes

Solutions to I_2^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.547424 + 0.585652I$ $a = 0.442547 + 0.966840I$ $b = -1.00000$	$-0.66484 - 1.39709I$	$-0.08162 + 2.95607I$
$u = -0.547424 - 0.585652I$ $a = 0.442547 - 0.966840I$ $b = -1.00000$	$-0.66484 + 1.39709I$	$-0.08162 - 2.95607I$
$u = 0.547424 + 1.120870I$ $a = -0.94255 - 1.62772I$ $b = -1.00000$	$-4.26996 + 7.64338I$	$-4.41838 - 7.23121I$
$u = 0.547424 - 1.120870I$ $a = -0.94255 + 1.62772I$ $b = -1.00000$	$-4.26996 - 7.64338I$	$-4.41838 + 7.23121I$

$$\text{III. } I_3^u = \langle b + 1, -u^3 + a - u + 1, u^6 - u^5 + 2u^4 - 2u^3 + 2u^2 - 2u + 1 \rangle$$

(i) Arc colorings

$$a_5 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} u^3 + u - 1 \\ -1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} u^3 + u - 2 \\ -1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} u^3 + u - 1 \\ -1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -u \\ u^3 + u \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -u^3 \\ u^5 + u^3 + u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} u^3 \\ u^3 + u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} u^4 + u^2 - u + 1 \\ u^5 + 2u^3 - u^2 + u - 1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} u^4 + u^2 - u + 1 \\ u^5 + 2u^3 - u^2 + u - 1 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = $u^4 + 3u^3 + u^2 + 4u - 5$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1, c_2	$(u - 1)^6$
c_3, c_7	u^6
c_4	$(u + 1)^6$
c_5, c_8	$u^6 - u^5 + 2u^4 - 2u^3 + 2u^2 - 2u + 1$
c_6	$u^6 - 3u^5 + 4u^4 - 2u^3 + 1$
c_9	$(u^3 + u^2 - 1)^2$
c_{10}, c_{12}	$u^6 + u^5 + 2u^4 + 2u^3 + 2u^2 + 2u + 1$
c_{11}	$u^6 + 3u^5 + 4u^4 + 2u^3 + 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1, c_2, c_4	$(y - 1)^6$
c_3, c_7	y^6
c_5, c_8, c_{10} c_{12}	$y^6 + 3y^5 + 4y^4 + 2y^3 + 1$
c_6, c_{11}	$y^6 - y^5 + 4y^4 - 2y^3 + 8y^2 + 1$
c_9	$(y^3 - y^2 + 2y - 1)^2$

(vi) Complex Volumes and Cusp Shapes

Solutions to I_3^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.498832 + 1.001300I$ $a = -0.122561 + 0.744862I$ $b = -1.00000$	$-1.91067 - 2.82812I$	$-4.05004 + 3.74291I$
$u = -0.498832 - 1.001300I$ $a = -0.122561 - 0.744862I$ $b = -1.00000$	$-1.91067 + 2.82812I$	$-4.05004 - 3.74291I$
$u = 0.284920 + 1.115140I$ $a = -1.75488$ $b = -1.00000$	-6.04826	$-7.19479 + 0.27335I$
$u = 0.284920 - 1.115140I$ $a = -1.75488$ $b = -1.00000$	-6.04826	$-7.19479 - 0.27335I$
$u = 0.713912 + 0.305839I$ $a = -0.122561 + 0.744862I$ $b = -1.00000$	$-1.91067 - 2.82812I$	$-1.25517 + 3.34054I$
$u = 0.713912 - 0.305839I$ $a = -0.122561 - 0.744862I$ $b = -1.00000$	$-1.91067 + 2.82812I$	$-1.25517 - 3.34054I$

IV. u-Polynomials

Crossings	u-Polynomials at each crossing
c_1	$((u - 1)^{10})(u^{23} + 47u^{22} + \dots - 11u + 1)$
c_2	$((u - 1)^{10})(u^{23} - 11u^{22} + \dots - 9u + 1)$
c_3, c_7	$u^{10}(u^{23} - u^{22} + \dots + 2048u + 1024)$
c_4	$((u + 1)^{10})(u^{23} - 11u^{22} + \dots - 9u + 1)$
c_5	$(u^4 + u^2 + u + 1)(u^6 - u^5 + 2u^4 - 2u^3 + 2u^2 - 2u + 1)$ $\cdot (u^{23} - 2u^{22} + \dots + 2u - 1)$
c_6	$(u^4 - 2u^3 + 3u^2 - u + 1)(u^6 - 3u^5 + 4u^4 - 2u^3 + 1)$ $\cdot (u^{23} - 10u^{22} + \dots + 120u - 31)$
c_8	$(u^4 + u^2 + u + 1)(u^6 - u^5 + 2u^4 - 2u^3 + 2u^2 - 2u + 1)$ $\cdot (u^{23} + 24u^{21} + \dots + 2u + 1)$
c_9	$((u^3 + u^2 - 1)^2)(u^4 - 3u^3 + \dots - 3u + 2)(u^{23} + 2u^{22} + \dots - 15u^2 - 8)$
c_{10}	$(u^4 + u^2 - u + 1)(u^6 + u^5 + 2u^4 + 2u^3 + 2u^2 + 2u + 1)$ $\cdot (u^{23} - 2u^{22} + \dots + 2u - 1)$
c_{11}	$(u^4 + 2u^3 + 3u^2 + u + 1)(u^6 + 3u^5 + 4u^4 + 2u^3 + 1)$ $\cdot (u^{23} + 12u^{22} + \dots - 2u - 1)$
c_{12}	$(u^4 + u^2 - u + 1)(u^6 + u^5 + 2u^4 + 2u^3 + 2u^2 + 2u + 1)$ $\cdot (u^{23} + 24u^{21} + \dots + 2u + 1)$

V. Riley Polynomials

Crossings	Riley Polynomials at each crossing
c_1	$((y - 1)^{10})(y^{23} - 211y^{22} + \dots - 215y - 1)$
c_2, c_4	$((y - 1)^{10})(y^{23} - 47y^{22} + \dots - 11y - 1)$
c_3, c_7	$y^{10}(y^{23} + 63y^{22} + \dots + 8912896y - 1048576)$
c_5, c_{10}	$(y^4 + 2y^3 + 3y^2 + y + 1)(y^6 + 3y^5 + 4y^4 + 2y^3 + 1)$ $\cdot (y^{23} + 12y^{22} + \dots - 2y - 1)$
c_6	$(y^4 + 2y^3 + 7y^2 + 5y + 1)(y^6 - y^5 + 4y^4 - 2y^3 + 8y^2 + 1)$ $\cdot (y^{23} - 12y^{22} + \dots - 6122y - 961)$
c_8, c_{12}	$(y^4 + 2y^3 + 3y^2 + y + 1)(y^6 + 3y^5 + 4y^4 + 2y^3 + 1)$ $\cdot (y^{23} + 48y^{22} + \dots - 2y - 1)$
c_9	$(y^3 - y^2 + 2y - 1)^2(y^4 - y^3 + 2y^2 + 7y + 4)$ $\cdot (y^{23} - 12y^{22} + \dots - 240y - 64)$
c_{11}	$(y^4 + 2y^3 + 7y^2 + 5y + 1)(y^6 - y^5 + 4y^4 - 2y^3 + 8y^2 + 1)$ $\cdot (y^{23} + 24y^{21} + \dots + 2y - 1)$