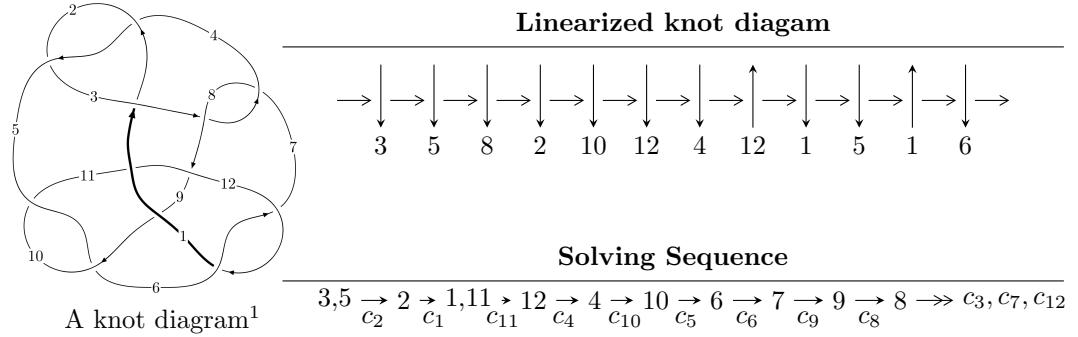


$12n_{0204}$  ( $K12n_{0204}$ )



### Ideals for irreducible components<sup>2</sup> of $X_{\text{par}}$

$$\begin{aligned}
 I_1^u &= \langle -409562441u^{28} - 633138331u^{27} + \dots + 1278981878b + 1495358594, \\
 &\quad - 649542429u^{28} - 1056906370u^{27} + \dots + 2557963756a - 48242973, u^{29} + 2u^{28} + \dots + 5u - 4 \rangle \\
 I_2^u &= \langle u^{14}a - u^{14} + \dots + b - 1, -2u^{14} - u^{13} + \dots - a + 3, \\
 &\quad u^{15} + u^{14} - 4u^{13} - 5u^{12} + 6u^{11} + 10u^{10} - 7u^8 - 8u^7 - 4u^6 + 6u^5 + 8u^4 + 2u^3 - 2u^2 - 2u - 1 \rangle \\
 I_3^u &= \langle u^4a + u^3a - u^4 - u^3 - au + b - a + u, u^5 - 2u^3 + a^2 - u^2 + 2u + 1, u^6 + u^5 - u^4 - 2u^3 + u + 1 \rangle \\
 I_4^u &= \langle 2b + 3, a + 1, u - 1 \rangle
 \end{aligned}$$

\* 4 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 72 representations.

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<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/math/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

I.

$$I_1^u = \langle -4.10 \times 10^8 u^{28} - 6.33 \times 10^8 u^{27} + \dots + 1.28 \times 10^9 b + 1.50 \times 10^9, -6.50 \times 10^8 u^{28} - 1.06 \times 10^9 u^{27} + \dots + 2.56 \times 10^9 a - 4.82 \times 10^7, u^{29} + 2u^{28} + \dots + 5u - 4 \rangle$$

(i) **Arc colorings**

$$a_3 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -u^2 + 1 \\ -u^2 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0.253929u^{28} + 0.413183u^{27} + \dots + 3.78605u + 0.0188599 \\ 0.320225u^{28} + 0.495033u^{27} + \dots + 1.86204u - 1.16918 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 0.253151u^{28} + 0.268291u^{27} + \dots + 2.54838u + 0.206314 \\ 0.0347611u^{28} + 0.0691866u^{27} + \dots - 0.718788u - 0.0155112 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} u \\ -u^3 + u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0.253929u^{28} + 0.413183u^{27} + \dots + 3.78605u + 0.0188599 \\ 0.265953u^{28} + 0.469651u^{27} + \dots + 0.372941u - 0.790474 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -0.241553u^{28} - 0.198421u^{27} + \dots - 2.06949u + 0.135383 \\ 0.0507414u^{28} + 0.0659434u^{27} + \dots + 1.51952u - 0.265184 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -0.482352u^{28} - 0.389873u^{27} + \dots - 4.05885u + 0.333349 \\ 0.0518322u^{28} + 0.0860020u^{27} + \dots + 1.78896u - 0.341645 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0.246071u^{28} + 0.0868173u^{27} + \dots + 1.21395u + 0.481140 \\ -0.0746592u^{28} - 0.176612u^{27} + \dots - 2.68612u + 0.591964 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 0.487395u^{28} + 0.426835u^{27} + \dots + 3.80650u - 0.325257 \\ -0.00202308u^{28} - 0.00908992u^{27} + \dots - 1.92712u + 0.242240 \end{pmatrix}$$

(ii) **Obstruction class = -1**

(iii) **Cusp Shapes** =  $\frac{1071754917}{2557963756}u^{28} - \frac{75682913}{2557963756}u^{27} + \dots + \frac{8446888807}{2557963756}u - \frac{9796598069}{639490939}$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1$	$u^{29} + 16u^{28} + \cdots + 209u + 16$
$c_2, c_4$	$u^{29} - 2u^{28} + \cdots + 5u + 4$
$c_3, c_7$	$u^{29} + 3u^{28} + \cdots + 18u + 8$
$c_5, c_6, c_{10}$ $c_{12}$	$u^{29} + u^{28} + \cdots + 2u + 1$
$c_8, c_{11}$	$u^{29} - 5u^{28} + \cdots - 6u + 1$
$c_9$	$u^{29} + 26u^{28} + \cdots + 376832u + 32768$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1$	$y^{29} - 4y^{28} + \cdots + 21313y - 256$
$c_2, c_4$	$y^{29} - 16y^{28} + \cdots + 209y - 16$
$c_3, c_7$	$y^{29} + 9y^{28} + \cdots - 140y - 64$
$c_5, c_6, c_{10}$ $c_{12}$	$y^{29} + 5y^{28} + \cdots - 6y - 1$
$c_8, c_{11}$	$y^{29} + 45y^{28} + \cdots + 6y - 1$
$c_9$	$y^{29} - 16y^{28} + \cdots + 6174015488y - 1073741824$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.960613 + 0.170294I$		
$a = -1.129440 - 0.468149I$	$-3.34627 + 0.60911I$	$-7.67402 - 10.34191I$
$b = -1.63701 - 0.14149I$		
$u = -0.960613 - 0.170294I$		
$a = -1.129440 + 0.468149I$	$-3.34627 - 0.60911I$	$-7.67402 + 10.34191I$
$b = -1.63701 + 0.14149I$		
$u = 0.829481 + 0.498753I$		
$a = 0.851038 + 0.266459I$	$-0.95125 - 3.42018I$	$-9.12436 + 7.13905I$
$b = 1.25630 - 0.93003I$		
$u = 0.829481 - 0.498753I$		
$a = 0.851038 - 0.266459I$	$-0.95125 + 3.42018I$	$-9.12436 - 7.13905I$
$b = 1.25630 + 0.93003I$		
$u = -0.555934 + 0.787790I$		
$a = -0.385011 + 0.878403I$	$3.91212 - 3.07296I$	$-3.58580 + 5.16956I$
$b = -0.547815 - 0.259593I$		
$u = -0.555934 - 0.787790I$		
$a = -0.385011 - 0.878403I$	$3.91212 + 3.07296I$	$-3.58580 - 5.16956I$
$b = -0.547815 + 0.259593I$		
$u = -0.133622 + 0.942757I$		
$a = -1.05744 + 1.03712I$	$-3.40148 - 10.10230I$	$-5.65840 + 6.34779I$
$b = -0.400359 - 0.621002I$		
$u = -0.133622 - 0.942757I$		
$a = -1.05744 - 1.03712I$	$-3.40148 + 10.10230I$	$-5.65840 - 6.34779I$
$b = -0.400359 + 0.621002I$		
$u = -0.482129 + 0.757528I$		
$a = 0.760914 - 0.157398I$	$3.66760 - 0.05333I$	$-4.59541 - 3.69602I$
$b = 0.683226 + 0.243077I$		
$u = -0.482129 - 0.757528I$		
$a = 0.760914 + 0.157398I$	$3.66760 + 0.05333I$	$-4.59541 + 3.69602I$
$b = 0.683226 - 0.243077I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.819144 + 0.362327I$		
$a = 0.087730 - 0.590172I$	$-0.751059 - 0.353134I$	$-9.39424 - 1.40493I$
$b = -0.776429 + 0.138255I$		
$u = 0.819144 - 0.362327I$		
$a = 0.087730 + 0.590172I$	$-0.751059 + 0.353134I$	$-9.39424 + 1.40493I$
$b = -0.776429 - 0.138255I$		
$u = 0.121290 + 0.842756I$		
$a = -1.00456 - 1.22447I$	$-4.45862 + 3.60692I$	$-7.22386 - 2.01130I$
$b = -0.539181 + 0.622092I$		
$u = 0.121290 - 0.842756I$		
$a = -1.00456 + 1.22447I$	$-4.45862 - 3.60692I$	$-7.22386 + 2.01130I$
$b = -0.539181 - 0.622092I$		
$u = -1.002290 + 0.666485I$		
$a = 0.794138 - 0.363712I$	$2.60025 + 8.50017I$	$-5.17138 - 9.83055I$
$b = 1.64106 + 0.14073I$		
$u = -1.002290 - 0.666485I$		
$a = 0.794138 + 0.363712I$	$2.60025 - 8.50017I$	$-5.17138 + 9.83055I$
$b = 1.64106 - 0.14073I$		
$u = -1.064380 + 0.598303I$		
$a = -0.159509 + 0.533064I$	$1.93242 + 5.18468I$	$-8.47176 - 2.14374I$
$b = -0.638339 - 0.004258I$		
$u = -1.064380 - 0.598303I$		
$a = -0.159509 - 0.533064I$	$1.93242 - 5.18468I$	$-8.47176 + 2.14374I$
$b = -0.638339 + 0.004258I$		
$u = 1.230540 + 0.053330I$		
$a = -0.440769 + 0.411058I$	$-2.23909 + 1.32557I$	$-7.93584 - 5.22491I$
$b = -1.154760 + 0.333664I$		
$u = 1.230540 - 0.053330I$		
$a = -0.440769 - 0.411058I$	$-2.23909 - 1.32557I$	$-7.93584 + 5.22491I$
$b = -1.154760 - 0.333664I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.243450 + 0.397204I$		
$a = -0.541600 - 0.973717I$	$-8.59540 + 0.64697I$	$-11.02522 - 1.67463I$
$b = -1.67988 - 0.94005I$		
$u = -1.243450 - 0.397204I$		
$a = -0.541600 + 0.973717I$	$-8.59540 - 0.64697I$	$-11.02522 + 1.67463I$
$b = -1.67988 + 0.94005I$		
$u = 1.215230 + 0.518861I$		
$a = 0.943218 + 0.506066I$	$-7.70776 - 8.57292I$	$-9.65881 + 5.33629I$
$b = 2.90492 + 0.42900I$		
$u = 1.215230 - 0.518861I$		
$a = 0.943218 - 0.506066I$	$-7.70776 + 8.57292I$	$-9.65881 - 5.33629I$
$b = 2.90492 - 0.42900I$		
$u = -1.252950 + 0.545209I$		
$a = 0.925713 - 0.557598I$	$-6.8135 + 15.4607I$	$-8.47000 - 9.06787I$
$b = 2.79765 - 0.77731I$		
$u = -1.252950 - 0.545209I$		
$a = 0.925713 + 0.557598I$	$-6.8135 - 15.4607I$	$-8.47000 + 9.06787I$
$b = 2.79765 + 0.77731I$		
$u = 1.313260 + 0.385635I$		
$a = -0.416958 + 0.934515I$	$-8.00289 + 5.49028I$	$-9.85377 - 4.12172I$
$b = -1.47424 + 1.05397I$		
$u = 1.313260 - 0.385635I$		
$a = -0.416958 - 0.934515I$	$-8.00289 - 5.49028I$	$-9.85377 + 4.12172I$
$b = -1.47424 - 1.05397I$		
$u = 0.332840$		
$a = 1.29507$	$-0.777392$	$-12.5640$
$b = -0.370297$		

$$I_2^u = \langle u^{14}a - u^{14} + \dots + b - 1, \quad -2u^{14} - u^{13} + \dots - a + 3, \quad u^{15} + u^{14} + \dots - 2u - 1 \rangle^{\text{III.}}$$

(i) **Arc colorings**

$$a_3 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -u^2 + 1 \\ -u^2 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} a \\ -u^{14}a + u^{14} + \dots + u + 1 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} u^6a - 2u^4a + u^2a - u^2 + a + 1 \\ -u^{14}a + u^{14} + \dots + u + 1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} u \\ -u^3 + u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} a \\ -u^{14}a + u^{14} + \dots + u + 1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} u^{14} + u^{13} + \dots - u - 2 \\ -u^{13}a - u^{13} + \dots - a - 1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -u^{11} + 4u^9 - 6u^7 + 2u^5 + 3u^3 - 2u \\ -u^{11} + 3u^9 - 4u^7 + u^5 + u^3 - u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -u^2 + a + 1 \\ -u^{14}a + u^{14} + \dots + u + 1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} u^{14} - 5u^{12} + 10u^{10} - 7u^8 - 4u^6 + 8u^4 - 2u^2 - 1 \\ u^{14} - 4u^{12} + 7u^{10} - 4u^8 - 2u^6 + 4u^4 - u^2 \end{pmatrix}$$

(ii) **Obstruction class** = -1

(iii) **Cusp Shapes**

$$= -4u^{13} + 16u^{11} + 4u^{10} - 28u^9 - 12u^8 + 12u^7 + 16u^6 + 16u^5 - 24u^3 - 8u^2 - 2$$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1$	$(u^{15} + 9u^{14} + \cdots - 4u^2 + 1)^2$
$c_2, c_4$	$(u^{15} - u^{14} + \cdots - 2u + 1)^2$
$c_3, c_7$	$(u^{15} - u^{14} + \cdots + 2u - 1)^2$
$c_5, c_6, c_{10}$ $c_{12}$	$u^{30} - 3u^{29} + \cdots - 30u + 9$
$c_8, c_{11}$	$u^{30} - 11u^{29} + \cdots - 1296u + 81$
$c_9$	$(u - 1)^{30}$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1$	$(y^{15} - 5y^{14} + \cdots + 8y - 1)^2$
$c_2, c_4$	$(y^{15} - 9y^{14} + \cdots + 4y^2 - 1)^2$
$c_3, c_7$	$(y^{15} + 3y^{14} + \cdots + 8y^2 - 1)^2$
$c_5, c_6, c_{10}$ $c_{12}$	$y^{30} + 11y^{29} + \cdots + 1296y + 81$
$c_8, c_{11}$	$y^{30} + 15y^{29} + \cdots - 73224y + 6561$
$c_9$	$(y - 1)^{30}$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.023100 + 0.900040I$		
$a = 0.825316 + 1.129310I$	$-4.73497 - 3.25615I$	$-7.67133 + 2.40088I$
$b = 0.286301 - 0.445204I$		
$u = -0.023100 + 0.900040I$		
$a = 0.98422 - 1.08773I$	$-4.73497 - 3.25615I$	$-7.67133 + 2.40088I$
$b = 0.164746 + 0.352495I$		
$u = -0.023100 - 0.900040I$		
$a = 0.825316 - 1.129310I$	$-4.73497 + 3.25615I$	$-7.67133 - 2.40088I$
$b = 0.286301 + 0.445204I$		
$u = -0.023100 - 0.900040I$		
$a = 0.98422 + 1.08773I$	$-4.73497 + 3.25615I$	$-7.67133 - 2.40088I$
$b = 0.164746 - 0.352495I$		
$u = 0.863978$		
$a = 0.126771 + 1.178080I$	2.03422	-12.4840
$b = 3.66551 - 2.58901I$		
$u = 0.863978$		
$a = 0.126771 - 1.178080I$	2.03422	-12.4840
$b = 3.66551 + 2.58901I$		
$u = 1.093890 + 0.311098I$		
$a = -0.297631 - 0.955829I$	$-0.109911 - 1.108490I$	$-11.51398 + 0.68443I$
$b = -1.62293 - 0.54486I$		
$u = 1.093890 + 0.311098I$		
$a = 0.197813 + 0.275213I$	$-0.109911 - 1.108490I$	$-11.51398 + 0.68443I$
$b = 0.45469 + 1.92439I$		
$u = 1.093890 - 0.311098I$		
$a = -0.297631 + 0.955829I$	$-0.109911 + 1.108490I$	$-11.51398 - 0.68443I$
$b = -1.62293 + 0.54486I$		
$u = 1.093890 - 0.311098I$		
$a = 0.197813 - 0.275213I$	$-0.109911 + 1.108490I$	$-11.51398 - 0.68443I$
$b = 0.45469 - 1.92439I$		

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.747479 + 0.391613I$		
$a = 1.023110 - 0.862412I$	$4.53214 + 1.75942I$	$-1.14915 - 5.01461I$
$b = 1.63828 - 1.05509I$		
$u = -0.747479 + 0.391613I$		
$a = -0.42847 + 1.44786I$	$4.53214 + 1.75942I$	$-1.14915 - 5.01461I$
$b = 0.248041 - 0.151767I$		
$u = -0.747479 - 0.391613I$		
$a = 1.023110 + 0.862412I$	$4.53214 - 1.75942I$	$-1.14915 + 5.01461I$
$b = 1.63828 + 1.05509I$		
$u = -0.747479 - 0.391613I$		
$a = -0.42847 - 1.44786I$	$4.53214 - 1.75942I$	$-1.14915 + 5.01461I$
$b = 0.248041 + 0.151767I$		
$u = -1.070290 + 0.443484I$		
$a = -0.592827 + 0.959612I$	$0.87635 + 5.68434I$	$-8.20490 - 7.47679I$
$b = -1.162130 + 0.705596I$		
$u = -1.070290 + 0.443484I$		
$a = 0.643980 - 0.010296I$	$0.87635 + 5.68434I$	$-8.20490 - 7.47679I$
$b = 1.27621 - 1.00477I$		
$u = -1.070290 - 0.443484I$		
$a = -0.592827 - 0.959612I$	$0.87635 - 5.68434I$	$-8.20490 + 7.47679I$
$b = -1.162130 - 0.705596I$		
$u = -1.070290 - 0.443484I$		
$a = 0.643980 + 0.010296I$	$0.87635 - 5.68434I$	$-8.20490 + 7.47679I$
$b = 1.27621 + 1.00477I$		
$u = 1.268720 + 0.457284I$		
$a = -0.923717 - 0.340768I$	$-8.68612 - 1.54935I$	$-11.09602 + 0.66420I$
$b = -2.59581 - 0.49906I$		
$u = 1.268720 + 0.457284I$		
$a = 0.523167 - 0.819566I$	$-8.68612 - 1.54935I$	$-11.09602 + 0.66420I$
$b = 1.44899 - 1.21103I$		

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.268720 - 0.457284I$		
$a = -0.923717 + 0.340768I$	$-8.68612 + 1.54935I$	$-11.09602 - 0.66420I$
$b = -2.59581 + 0.49906I$		
$u = 1.268720 - 0.457284I$		
$a = 0.523167 + 0.819566I$	$-8.68612 + 1.54935I$	$-11.09602 - 0.66420I$
$b = 1.44899 + 1.21103I$		
$u = -1.260410 + 0.482704I$		
$a = 0.621138 + 0.785123I$	$-8.49724 + 8.19235I$	$-10.69502 - 5.35870I$
$b = 1.74021 + 0.98052I$		
$u = -1.260410 + 0.482704I$		
$a = -0.976755 + 0.431682I$	$-8.49724 + 8.19235I$	$-10.69502 - 5.35870I$
$b = -2.53986 + 0.80421I$		
$u = -1.260410 - 0.482704I$		
$a = 0.621138 - 0.785123I$	$-8.49724 - 8.19235I$	$-10.69502 + 5.35870I$
$b = 1.74021 - 0.98052I$		
$u = -1.260410 - 0.482704I$		
$a = -0.976755 - 0.431682I$	$-8.49724 - 8.19235I$	$-10.69502 + 5.35870I$
$b = -2.53986 - 0.80421I$		
$u = -0.193328 + 0.557909I$		
$a = -0.687123 + 0.933709I$	$3.26563 - 1.73642I$	$-4.42769 + 4.08118I$
$b = 0.869302 - 0.104344I$		
$u = -0.193328 + 0.557909I$		
$a = 1.96101 - 0.71799I$	$3.26563 - 1.73642I$	$-4.42769 + 4.08118I$
$b = 0.628452 - 0.272272I$		
$u = -0.193328 - 0.557909I$		
$a = -0.687123 - 0.933709I$	$3.26563 + 1.73642I$	$-4.42769 - 4.08118I$
$b = 0.869302 + 0.104344I$		
$u = -0.193328 - 0.557909I$		
$a = 1.96101 + 0.71799I$	$3.26563 + 1.73642I$	$-4.42769 - 4.08118I$
$b = 0.628452 + 0.272272I$		

$$\text{III. } I_3^u = \langle u^4a + u^3a - u^4 - u^3 - au + b - a + u, u^5 - 2u^3 + a^2 - u^2 + 2u + 1, u^6 + u^5 - u^4 - 2u^3 + u + 1 \rangle$$

(i) **Arc colorings**

$$\begin{aligned} a_3 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_5 &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_2 &= \begin{pmatrix} 1 \\ -u^2 \end{pmatrix} \\ a_1 &= \begin{pmatrix} -u^2 + 1 \\ -u^2 \end{pmatrix} \\ a_{11} &= \begin{pmatrix} a \\ -u^4a - u^3a + u^4 + u^3 + au + a - u \end{pmatrix} \\ a_{12} &= \begin{pmatrix} -u^2 + a + 1 \\ -u^4a - u^3a + u^4 + u^3 + au - u^2 + a - u \end{pmatrix} \\ a_4 &= \begin{pmatrix} u \\ -u^3 + u \end{pmatrix} \\ a_{10} &= \begin{pmatrix} a \\ -u^4a - u^3a + u^4 - u^2a + u^3 + au + a - u \end{pmatrix} \\ a_6 &= \begin{pmatrix} -u^5 - u^4 + u^3 + 2u^2 - 1 \\ -u^5a - u^4a - u^5 - u^4 + u^2a + u^2 \end{pmatrix} \\ a_7 &= \begin{pmatrix} -u^3a + au \\ -u^3a \end{pmatrix} \\ a_9 &= \begin{pmatrix} u^5a + u^4a - 2u^3a - u^2a + au - u^2 + 2a + 1 \\ u^5a - u^4a - 3u^3a + u^4 - u^2a + u^3 + 2au - u^2 + 2a - u \end{pmatrix} \\ a_8 &= \begin{pmatrix} u^5a + u^4a - 2u^3a - u^2a + au + a \\ u^5a - 2u^3a - u^2a + au + a \end{pmatrix} \end{aligned}$$

(ii) **Obstruction class = 1**

(iii) **Cusp Shapes** =  $4u^4 - 4u^2 - 4u$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1$	$(u^6 - 3u^5 + 5u^4 - 4u^3 + 2u^2 - u + 1)^2$
$c_2$	$(u^6 + u^5 - u^4 - 2u^3 + u + 1)^2$
$c_3, c_7$	$u^{12} + 3u^{10} + 5u^8 + 4u^6 + 2u^4 + u^2 + 1$
$c_4$	$(u^6 - u^5 - u^4 + 2u^3 - u + 1)^2$
$c_5, c_6, c_{10}$ $c_{12}$	$(u^2 + 1)^6$
$c_8, c_{11}$	$(u + 1)^{12}$
$c_9$	$u^{12} + 12u^{11} + \cdots + 60u + 9$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1$	$(y^6 + y^5 + 5y^4 + 6y^2 + 3y + 1)^2$
$c_2, c_4$	$(y^6 - 3y^5 + 5y^4 - 4y^3 + 2y^2 - y + 1)^2$
$c_3, c_7$	$(y^6 + 3y^5 + 5y^4 + 4y^3 + 2y^2 + y + 1)^2$
$c_5, c_6, c_{10}$ $c_{12}$	$(y + 1)^{12}$
$c_8, c_{11}$	$(y - 1)^{12}$
$c_9$	$y^{12} - 14y^{11} + \cdots - 108y + 81$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.002190 + 0.295542I$		
$a = -0.270708 - 0.917982I$	$1.39926 - 0.92430I$	$-5.71672 + 0.79423I$
$b = -1.49594 + 1.39869I$		
$u = 1.002190 + 0.295542I$		
$a = 0.270708 + 0.917982I$	$1.39926 - 0.92430I$	$-5.71672 + 0.79423I$
$b = 1.95964 + 1.91259I$		
$u = 1.002190 - 0.295542I$		
$a = -0.270708 + 0.917982I$	$1.39926 + 0.92430I$	$-5.71672 - 0.79423I$
$b = -1.49594 - 1.39869I$		
$u = 1.002190 - 0.295542I$		
$a = 0.270708 - 0.917982I$	$1.39926 + 0.92430I$	$-5.71672 - 0.79423I$
$b = 1.95964 - 1.91259I$		
$u = -0.428243 + 0.664531I$		
$a = 1.063260 - 0.685196I$	$5.18047 - 0.92430I$	$1.71672 + 0.79423I$
$b = 1.226020 - 0.214242I$		
$u = -0.428243 + 0.664531I$		
$a = -1.063260 + 0.685196I$	$5.18047 - 0.92430I$	$1.71672 + 0.79423I$
$b = 0.093522 - 0.382665I$		
$u = -0.428243 - 0.664531I$		
$a = 1.063260 + 0.685196I$	$5.18047 + 0.92430I$	$1.71672 - 0.79423I$
$b = 1.226020 + 0.214242I$		
$u = -0.428243 - 0.664531I$		
$a = -1.063260 - 0.685196I$	$5.18047 + 0.92430I$	$1.71672 - 0.79423I$
$b = 0.093522 + 0.382665I$		
$u = -1.073950 + 0.558752I$		
$a = 0.381252 - 0.732786I$	$3.28987 + 5.69302I$	$-2.00000 - 5.51057I$
$b = 1.04838 - 1.16005I$		
$u = -1.073950 + 0.558752I$		
$a = -0.381252 + 0.732786I$	$3.28987 + 5.69302I$	$-2.00000 - 5.51057I$
$b = -0.831626 - 0.477727I$		

Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.073950 - 0.558752I$		
$a = 0.381252 + 0.732786I$	$3.28987 - 5.69302I$	$-2.00000 + 5.51057I$
$b = 1.04838 + 1.16005I$		
$u = -1.073950 - 0.558752I$		
$a = -0.381252 - 0.732786I$	$3.28987 - 5.69302I$	$-2.00000 + 5.51057I$
$b = -0.831626 + 0.477727I$		

$$\text{IV. } I_4^u = \langle 2b+3, a+1, u-1 \rangle$$

(i) Arc colorings

$$a_3 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -1 \\ -1.5 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -1 \\ -0.5 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -1 \\ -0.5 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -1 \\ 0.5 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -2 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -1 \\ 0.5 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -2 \\ 0 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = -9.75

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_2, c_5$ $c_6, c_8, c_9$ $c_{11}$	$u - 1$
$c_3, c_7$	$u$
$c_4, c_{10}, c_{12}$	$u + 1$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_4$	
$c_5, c_6, c_8$	$y - 1$
$c_9, c_{10}, c_{11}$	
$c_{12}$	
$c_3, c_7$	$y$

**(vi) Complex Volumes and Cusp Shapes**

Solutions to $I_4^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.00000$		
$a = -1.00000$	-3.28987	-9.75000
$b = -1.50000$		

## V. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1$	$(u - 1)(u^6 - 3u^5 + 5u^4 - 4u^3 + 2u^2 - u + 1)^2$ $\cdot ((u^{15} + 9u^{14} + \dots - 4u^2 + 1)^2)(u^{29} + 16u^{28} + \dots + 209u + 16)$
$c_2$	$(u - 1)(u^6 + u^5 + \dots + u + 1)^2(u^{15} - u^{14} + \dots - 2u + 1)^2$ $\cdot (u^{29} - 2u^{28} + \dots + 5u + 4)$
$c_3, c_7$	$u(u^{12} + 3u^{10} + \dots + u^2 + 1)(u^{15} - u^{14} + \dots + 2u - 1)^2$ $\cdot (u^{29} + 3u^{28} + \dots + 18u + 8)$
$c_4$	$(u + 1)(u^6 - u^5 + \dots - u + 1)^2(u^{15} - u^{14} + \dots - 2u + 1)^2$ $\cdot (u^{29} - 2u^{28} + \dots + 5u + 4)$
$c_5, c_6$	$(u - 1)(u^2 + 1)^6(u^{29} + u^{28} + \dots + 2u + 1)(u^{30} - 3u^{29} + \dots - 30u + 9)$
$c_8, c_{11}$	$(u - 1)(u + 1)^{12}(u^{29} - 5u^{28} + \dots - 6u + 1)$ $\cdot (u^{30} - 11u^{29} + \dots - 1296u + 81)$
$c_9$	$((u - 1)^{31})(u^{12} + 12u^{11} + \dots + 60u + 9)$ $\cdot (u^{29} + 26u^{28} + \dots + 376832u + 32768)$
$c_{10}, c_{12}$	$(u + 1)(u^2 + 1)^6(u^{29} + u^{28} + \dots + 2u + 1)(u^{30} - 3u^{29} + \dots - 30u + 9)$

## VI. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1$	$(y - 1)(y^6 + y^5 + \dots + 3y + 1)^2(y^{15} - 5y^{14} + \dots + 8y - 1)^2 \\ \cdot (y^{29} - 4y^{28} + \dots + 21313y - 256)$
$c_2, c_4$	$(y - 1)(y^6 - 3y^5 + 5y^4 - 4y^3 + 2y^2 - y + 1)^2 \\ \cdot ((y^{15} - 9y^{14} + \dots + 4y^2 - 1)^2)(y^{29} - 16y^{28} + \dots + 209y - 16)$
$c_3, c_7$	$y(y^6 + 3y^5 + \dots + y + 1)^2(y^{15} + 3y^{14} + \dots + 8y^2 - 1)^2 \\ \cdot (y^{29} + 9y^{28} + \dots - 140y - 64)$
$c_5, c_6, c_{10}$ $c_{12}$	$(y - 1)(y + 1)^{12}(y^{29} + 5y^{28} + \dots - 6y - 1) \\ \cdot (y^{30} + 11y^{29} + \dots + 1296y + 81)$
$c_8, c_{11}$	$((y - 1)^{13})(y^{29} + 45y^{28} + \dots + 6y - 1) \\ \cdot (y^{30} + 15y^{29} + \dots - 73224y + 6561)$
$c_9$	$((y - 1)^{31})(y^{12} - 14y^{11} + \dots - 108y + 81) \\ \cdot (y^{29} - 16y^{28} + \dots + 6174015488y - 1073741824)$