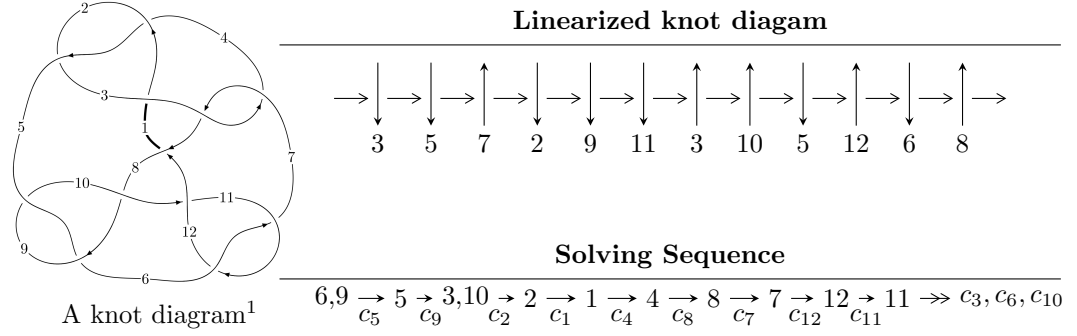


12n₀₂₁₁ (K12n₀₂₁₁)



Ideals for irreducible components² of X_{par}

$$I_1^u = \langle 13u^{16} + 9u^{15} + \dots + 32b + 15, 21u^{16} - 15u^{15} + \dots + 32a - 41, \\ u^{17} + 3u^{15} + 2u^{14} + 9u^{13} + 4u^{12} + 15u^{11} + 9u^{10} + 23u^9 + 6u^8 + 23u^7 + 5u^6 + 19u^5 - 3u^4 + 11u^3 + 1 \rangle$$

$$I_2^u = \langle -u^3 + u^2 + 2b + 1, -u^3 - u^2 + 2a - 1, u^4 + u^2 - u + 1 \rangle$$

$$I_3^u = \langle -33675480u^{21} + 230853871u^{20} + \dots + 427516113b + 1988747145, \\ -330664297u^{21} + 1163900912u^{20} + \dots + 1282548339a + 9330160065, \\ u^{22} - 2u^{21} + \dots - 12u + 9 \rangle$$

$$I_4^u = \langle u^5 + u^4 + u^3 + 2u^2 + b + u + 1, u^5 + u^4 + u^3 + u^2 + a + u, u^6 + u^5 + 2u^4 + 2u^3 + 2u^2 + 2u + 1 \rangle$$

$$I_5^u = \langle au + 5b - 3a + u - 3, a^2 + au + 5u - 4, u^2 + 1 \rangle$$

* 5 irreducible components of $\dim_{\mathbb{C}} = 0$, with total 53 representations.

¹The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

²All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\mathbf{I. } I_1^u = \langle 13u^{16} + 9u^{15} + \dots + 32b + 15, 21u^{16} - 15u^{15} + \dots + 32a - 41, u^{17} + 3u^{15} + \dots + 11u^3 + 1 \rangle$$

(i) Arc colorings

$$a_6 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -0.656250u^{16} + 0.468750u^{15} + \dots + 2.90625u + 1.28125 \\ -0.406250u^{16} - 0.281250u^{15} + \dots - 0.343750u - 0.468750 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -u \\ u^3 + u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -0.468750u^{16} + 0.406250u^{15} + \dots + 3.21875u + 0.343750 \\ -0.0937500u^{16} - 0.218750u^{15} + \dots - 0.156250u - 0.531250 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} \frac{1}{2}u^{16} + u^{14} + \dots - \frac{5}{2}u^3 + \frac{5}{2}u \\ \frac{1}{4}u^{16} + \frac{1}{2}u^{14} + \dots - \frac{9}{4}u^3 - \frac{3}{4}u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -0.281250u^{16} + 0.0937500u^{15} + \dots + 2.53125u + 0.156250 \\ -0.531250u^{16} + 0.0937500u^{15} + \dots + 0.281250u + 0.156250 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -u^3 \\ u^5 + u^3 + u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} \frac{1}{4}u^{15} + \frac{1}{2}u^{13} + \dots - \frac{5}{4}u^2 + \frac{5}{4} \\ u^2 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} \frac{1}{4}u^{16} + \frac{1}{2}u^{14} + \dots - \frac{9}{4}u^3 + \frac{9}{4}u \\ -u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} \frac{1}{4}u^{16} + \frac{1}{2}u^{14} + \dots - \frac{9}{4}u^3 + \frac{5}{4}u \\ -u \end{pmatrix}$$

(ii) Obstruction class = -1

$$\text{(iii) Cusp Shapes} = \frac{25}{64}u^{16} + \frac{61}{64}u^{15} + \dots + \frac{639}{64}u - \frac{133}{64}$$

(iv) u-Polynomials at the component

| Crossings | u-Polynomials at each crossing |
|-----------------------------|--|
| c_1 | $u^{17} + 25u^{16} + \dots - 31u + 16$ |
| c_2, c_4 | $u^{17} - 5u^{16} + \dots - u + 4$ |
| c_3, c_7 | $u^{17} - 3u^{16} + \dots + 176u + 64$ |
| c_5, c_6, c_9 c_{11} | $u^{17} + 3u^{15} + \dots + 11u^3 - 1$ |
| c_8, c_{10} | $u^{17} - 6u^{16} + \dots - 6u^2 + 1$ |
| c_{12} | $u^{17} + 19u^{15} + \dots - 5u^2 + 4$ |

(v) Riley Polynomials at the component

| Crossings | Riley Polynomials at each crossing |
|-----------------------------|--|
| c_1 | $y^{17} - 61y^{16} + \dots - 15103y - 256$ |
| c_2, c_4 | $y^{17} - 25y^{16} + \dots - 31y - 16$ |
| c_3, c_7 | $y^{17} + 27y^{16} + \dots + 4352y - 4096$ |
| c_5, c_6, c_9 c_{11} | $y^{17} + 6y^{16} + \dots + 6y^2 - 1$ |
| c_8, c_{10} | $y^{17} + 18y^{16} + \dots + 12y - 1$ |
| c_{12} | $y^{17} + 38y^{16} + \dots + 40y - 16$ |

(vi) Complex Volumes and Cusp Shapes

| Solutions to I_1^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|-----------------------------|---------------------------------------|-----------------------|
| $u = 0.609453 + 0.805159I$ | | |
| $a = 0.854862 - 0.986654I$ | $-0.52072 - 2.33309I$ | $-2.02167 + 3.26936I$ |
| $b = -0.766890 - 0.457544I$ | | |
| $u = 0.609453 - 0.805159I$ | | |
| $a = 0.854862 + 0.986654I$ | $-0.52072 + 2.33309I$ | $-2.02167 - 3.26936I$ |
| $b = -0.766890 + 0.457544I$ | | |
| $u = 0.230202 + 0.870288I$ | | |
| $a = -2.22993 - 0.26645I$ | $-6.16563 - 1.02177I$ | $-6.84477 + 7.08191I$ |
| $b = -0.119488 + 0.657240I$ | | |
| $u = 0.230202 - 0.870288I$ | | |
| $a = -2.22993 + 0.26645I$ | $-6.16563 + 1.02177I$ | $-6.84477 - 7.08191I$ |
| $b = -0.119488 - 0.657240I$ | | |
| $u = -0.773626 + 0.937847I$ | | |
| $a = 0.606886 - 0.071826I$ | $-4.38989 + 4.09446I$ | $-5.30008 - 4.36784I$ |
| $b = -1.190660 + 0.370945I$ | | |
| $u = -0.773626 - 0.937847I$ | | |
| $a = 0.606886 + 0.071826I$ | $-4.38989 - 4.09446I$ | $-5.30008 + 4.36784I$ |
| $b = -1.190660 - 0.370945I$ | | |
| $u = -1.050610 + 0.636095I$ | | |
| $a = -0.407370 + 0.267779I$ | $-17.5984 - 0.0758I$ | $-7.31042 - 1.57550I$ |
| $b = 1.93722 - 0.60149I$ | | |
| $u = -1.050610 - 0.636095I$ | | |
| $a = -0.407370 - 0.267779I$ | $-17.5984 + 0.0758I$ | $-7.31042 + 1.57550I$ |
| $b = 1.93722 + 0.60149I$ | | |
| $u = -0.576669 + 1.098490I$ | | |
| $a = -0.263264 - 0.069567I$ | $1.86747 + 7.21175I$ | $3.72852 - 5.27936I$ |
| $b = 0.341659 - 0.129445I$ | | |
| $u = -0.576669 - 1.098490I$ | | |
| $a = -0.263264 + 0.069567I$ | $1.86747 - 7.21175I$ | $3.72852 + 5.27936I$ |
| $b = 0.341659 + 0.129445I$ | | |

| Solutions to I_1^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|--|---------------------------------------|-----------------------|
| $u = 0.743234 + 1.053510I$ $a = -0.04444 + 2.04366I$ $b = 2.07902 + 0.33370I$ | $-3.55752 - 7.80542I$ | $-4.29962 + 6.17985I$ |
| $u = 0.743234 - 1.053510I$ $a = -0.04444 - 2.04366I$ $b = 2.07902 - 0.33370I$ | $-3.55752 + 7.80542I$ | $-4.29962 - 6.17985I$ |
| $u = 0.71574 + 1.23305I$ $a = -0.99869 - 1.97392I$ $b = -2.63254 + 0.11082I$ | $-13.5091 - 13.2681I$ | $-3.78464 + 6.49717I$ |
| $u = 0.71574 - 1.23305I$ $a = -0.99869 + 1.97392I$ $b = -2.63254 - 0.11082I$ | $-13.5091 + 13.2681I$ | $-3.78464 - 6.49717I$ |
| $u = 0.302591 + 0.411010I$ $a = 0.856584 + 0.998116I$ $b = 0.086217 - 0.461654I$ | $-0.250655 - 1.078620I$ | $-3.32954 + 6.69723I$ |
| $u = 0.302591 - 0.411010I$ $a = 0.856584 - 0.998116I$ $b = 0.086217 + 0.461654I$ | $-0.250655 + 1.078620I$ | $-3.32954 - 6.69723I$ |
| $u = -0.400636$ $a = -1.24927$ $b = -0.969091$ | -2.22247 | -4.42560 |

$$\text{II. } I_2^u = \langle -u^3 + u^2 + 2b + 1, -u^3 - u^2 + 2a - 1, u^4 + u^2 - u + 1 \rangle$$

(i) Arc colorings

$$a_6 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} \frac{1}{2}u^3 + \frac{1}{2}u^2 + \frac{1}{2} \\ \frac{1}{2}u^3 - \frac{1}{2}u^2 - \frac{1}{2} \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -u \\ u^3 + u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} \frac{1}{2}u^3 + \frac{1}{2}u^2 - \frac{1}{2} \\ \frac{1}{2}u^3 + \frac{1}{2}u^2 - \frac{1}{2} \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -1 \\ u^2 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} \frac{1}{2}u^3 + \frac{1}{2}u^2 + \frac{1}{2} \\ \frac{1}{2}u^3 - \frac{1}{2}u^2 - \frac{1}{2} \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -u^3 \\ u^2 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -u^3 \\ u^2 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} u^3 - u^2 - 1 \\ u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} u^3 - u^2 + u - 1 \\ u \end{pmatrix}$$

(ii) Obstruction class = 1

$$\text{(iii) Cusp Shapes} = \frac{11}{4}u^3 + \frac{21}{4}u^2 - \frac{1}{2}u - \frac{17}{4}$$

(iv) u-Polynomials at the component

| Crossings | u-Polynomials at each crossing |
|---------------|--------------------------------|
| c_1, c_2 | $(u - 1)^4$ |
| c_3, c_7 | u^4 |
| c_4 | $(u + 1)^4$ |
| c_5, c_6 | $u^4 + u^2 - u + 1$ |
| c_8, c_{10} | $u^4 + 2u^3 + 3u^2 + u + 1$ |
| c_9, c_{11} | $u^4 + u^2 + u + 1$ |
| c_{12} | $u^4 + 3u^3 + 4u^2 + 3u + 2$ |

(v) Riley Polynomials at the component

| Crossings | Riley Polynomials at each crossing |
|-----------------------------|------------------------------------|
| c_1, c_2, c_4 | $(y - 1)^4$ |
| c_3, c_7 | y^4 |
| c_5, c_6, c_9 c_{11} | $y^4 + 2y^3 + 3y^2 + y + 1$ |
| c_8, c_{10} | $y^4 + 2y^3 + 7y^2 + 5y + 1$ |
| c_{12} | $y^4 - y^3 + 2y^2 + 7y + 4$ |

(vi) Complex Volumes and Cusp Shapes

| Solutions to I_2^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|-----------------------------|---------------------------------------|-----------------------|
| $u = 0.547424 + 0.585652I$ | | |
| $a = 0.278726 + 0.483420I$ | $-2.62503 - 1.39709I$ | $-5.84901 + 3.96898I$ |
| $b = -0.677958 - 0.157780I$ | | |
| $u = 0.547424 - 0.585652I$ | | |
| $a = 0.278726 - 0.483420I$ | $-2.62503 + 1.39709I$ | $-5.84901 - 3.96898I$ |
| $b = -0.677958 + 0.157780I$ | | |
| $u = -0.547424 + 1.120870I$ | | |
| $a = 0.971274 - 0.813859I$ | $0.98010 + 7.64338I$ | $-3.77599 - 8.10462I$ |
| $b = 0.927958 + 0.413327I$ | | |
| $u = -0.547424 - 1.120870I$ | | |
| $a = 0.971274 + 0.813859I$ | $0.98010 - 7.64338I$ | $-3.77599 + 8.10462I$ |
| $b = 0.927958 - 0.413327I$ | | |

III.

$$I_3^u = \langle -3.37 \times 10^7 u^{21} + 2.31 \times 10^8 u^{20} + \dots + 4.28 \times 10^8 b + 1.99 \times 10^9, -3.31 \times 10^8 u^{21} + 1.16 \times 10^9 u^{20} + \dots + 1.28 \times 10^9 a + 9.33 \times 10^9, u^{22} - 2u^{21} + \dots - 12u + 9 \rangle$$

(i) Arc colorings

$$\begin{aligned} a_6 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_9 &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_5 &= \begin{pmatrix} 1 \\ -u^2 \end{pmatrix} \\ a_3 &= \begin{pmatrix} 0.257818u^{21} - 0.907491u^{20} + \dots + 8.27519u - 7.27470 \\ 0.0787701u^{21} - 0.539989u^{20} + \dots + 5.17053u - 4.65186 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} -u \\ u^3 + u \end{pmatrix} \\ a_2 &= \begin{pmatrix} 0.0569753u^{21} - 0.732717u^{20} + \dots + 6.42310u - 8.39988 \\ 0.147735u^{21} - 0.732052u^{20} + \dots + 6.08589u - 6.69407 \end{pmatrix} \\ a_1 &= \begin{pmatrix} -0.113449u^{21} - 0.132459u^{20} + \dots + 2.54918u - 1.84329 \\ 0.183373u^{21} - 0.457606u^{20} + \dots + 4.47394u - 2.89558 \end{pmatrix} \\ a_4 &= \begin{pmatrix} -0.325326u^{21} + 0.184523u^{20} + \dots + 0.502711u - 2.87359 \\ -0.383495u^{21} + 0.177086u^{20} + \dots - 0.310468u - 2.63640 \end{pmatrix} \\ a_8 &= \begin{pmatrix} -u^3 \\ u^5 + u^3 + u \end{pmatrix} \\ a_7 &= \begin{pmatrix} -0.264604u^{21} + 0.445061u^{20} + \dots - 3.11735u - 0.705220 \\ -0.121794u^{21} + 0.190645u^{20} + \dots - 0.910828u - 1.28085 \end{pmatrix} \\ a_{12} &= \begin{pmatrix} \frac{1}{9}u^{21} - \frac{2}{9}u^{20} + \dots + \frac{32}{9}u - \frac{4}{3} \\ 0.0312057u^{21} - 0.184205u^{20} + \dots + 2.13810u - 1.28530 \end{pmatrix} \\ a_{11} &= \begin{pmatrix} 0.142317u^{21} - 0.406427u^{20} + \dots + 5.69365u - 2.61863 \\ 0.0312057u^{21} - 0.184205u^{20} + \dots + 2.13810u - 1.28530 \end{pmatrix} \end{aligned}$$

(ii) Obstruction class = -1

$$(iii) \text{ Cusp Shapes} = -\frac{51496451}{142505371}u^{21} + \frac{36892662}{142505371}u^{20} + \dots + \frac{723246262}{142505371}u - \frac{1135221198}{142505371}$$

(iv) u-Polynomials at the component

| Crossings | u-Polynomials at each crossing |
|-----------------------------|--|
| c_1 | $(u^{11} + 18u^{10} + \dots + 31u + 1)^2$ |
| c_2, c_4 | $(u^{11} - 4u^{10} - u^9 + 17u^8 + u^7 - 40u^6 + 3u^5 + 37u^4 - 3u^3 - 9u^2 + 7u - 1)^2$ |
| c_3, c_7 | $(u^{11} + u^{10} + \dots - 4u + 8)^2$ |
| c_5, c_6, c_9 c_{11} | $u^{22} + 2u^{21} + \dots + 12u + 9$ |
| c_8, c_{10} | $u^{22} - 10u^{21} + \dots - 432u + 81$ |
| c_{12} | $(u^{11} + 12u^9 + 36u^7 + 2u^6 + 2u^5 + 13u^4 + 13u^3 + u^2 + 1)^2$ |

(v) Riley Polynomials at the component

| Crossings | Riley Polynomials at each crossing |
|-----------------------------|---|
| c_1 | $(y^{11} - 46y^{10} + \dots + 863y - 1)^2$ |
| c_2, c_4 | $(y^{11} - 18y^{10} + \dots + 31y - 1)^2$ |
| c_3, c_7 | $(y^{11} + 21y^{10} + \dots + 336y - 64)^2$ |
| c_5, c_6, c_9 c_{11} | $y^{22} + 10y^{21} + \dots + 432y + 81$ |
| c_8, c_{10} | $y^{22} + 2y^{21} + \dots + 12312y + 6561$ |
| c_{12} | $(y^{11} + 24y^{10} + \dots - 2y - 1)^2$ |

(vi) Complex Volumes and Cusp Shapes

| Solutions to I_3^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|---|---------------------------------------|-----------------------|
| $u = 0.545296 + 0.923005I$ $a = 0.012822 + 0.329575I$ $b = 0.622069 - 0.196649I$ | $-0.14517 - 2.25109I$ | $-0.29632 + 2.34373I$ |
| $u = 0.545296 - 0.923005I$ $a = 0.012822 - 0.329575I$ $b = 0.622069 + 0.196649I$ | $-0.14517 + 2.25109I$ | $-0.29632 - 2.34373I$ |
| $u = 0.858271 + 0.670516I$ $a = 0.369906 - 0.478944I$ $b = -1.92512 + 0.39933I$ | $-4.72798 + 1.82060I$ | $-6.54374 - 1.21714I$ |
| $u = 0.858271 - 0.670516I$ $a = 0.369906 + 0.478944I$ $b = -1.92512 - 0.39933I$ | $-4.72798 - 1.82060I$ | $-6.54374 + 1.21714I$ |
| $u = -0.240009 + 1.082970I$ $a = 0.454525 + 0.334757I$ $b = 0.515438 + 0.609605I$ | 4.11473 | $8.33208 + 0.I$ |
| $u = -0.240009 - 1.082970I$ $a = 0.454525 - 0.334757I$ $b = 0.515438 - 0.609605I$ | 4.11473 | $8.33208 + 0.I$ |
| $u = 0.705045 + 0.879700I$ $a = 0.12429 - 1.54454I$ $b = -0.016245 - 0.493238I$ | $-9.06867 - 2.70718I$ | $-3.52709 + 2.44627I$ |
| $u = 0.705045 - 0.879700I$ $a = 0.12429 + 1.54454I$ $b = -0.016245 + 0.493238I$ | $-9.06867 + 2.70718I$ | $-3.52709 - 2.44627I$ |
| $u = -0.800202 + 0.827914I$ $a = -0.14364 - 1.64878I$ $b = 0.910452 + 0.422891I$ | $-4.72798 + 1.82060I$ | $-6.54374 - 1.21714I$ |
| $u = -0.800202 - 0.827914I$ $a = -0.14364 + 1.64878I$ $b = 0.910452 - 0.422891I$ | $-4.72798 - 1.82060I$ | $-6.54374 + 1.21714I$ |

| Solutions to I_3^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|--|---------------------------------------|-----------------------|
| $u = 0.047914 + 1.160270I$ $a = 2.24792 - 1.55926I$ $b = 1.93663 - 2.04614I$ | $1.59514 + 0.83621I$ | $-6.12521 - 2.51411I$ |
| $u = 0.047914 - 1.160270I$ $a = 2.24792 + 1.55926I$ $b = 1.93663 + 2.04614I$ | $1.59514 - 0.83621I$ | $-6.12521 + 2.51411I$ |
| $u = 1.089810 + 0.428144I$ $a = -0.395831 + 0.234267I$ $b = 2.55516 - 0.12719I$ | $-16.0296 + 6.7782I$ | $-6.17368 - 2.81310I$ |
| $u = 1.089810 - 0.428144I$ $a = -0.395831 - 0.234267I$ $b = 2.55516 + 0.12719I$ | $-16.0296 - 6.7782I$ | $-6.17368 + 2.81310I$ |
| $u = -0.703030 + 0.415587I$ $a = 0.495039 + 0.546851I$ $b = -0.195521 - 0.253083I$ | $-0.14517 - 2.25109I$ | $-0.29632 + 2.34373I$ |
| $u = -0.703030 - 0.415587I$ $a = 0.495039 - 0.546851I$ $b = -0.195521 + 0.253083I$ | $-0.14517 + 2.25109I$ | $-0.29632 - 2.34373I$ |
| $u = 0.190193 + 0.774835I$ $a = -2.15826 + 2.04536I$ $b = -1.52590 + 1.49076I$ | $1.59514 - 0.83621I$ | $-6.12521 + 2.51411I$ |
| $u = 0.190193 - 0.774835I$ $a = -2.15826 - 2.04536I$ $b = -1.52590 - 1.49076I$ | $1.59514 + 0.83621I$ | $-6.12521 - 2.51411I$ |
| $u = -0.804264 + 1.135210I$ $a = -0.80264 + 1.70705I$ $b = -1.69330 - 0.63124I$ | $-16.0296 + 6.7782I$ | $-6.17368 - 2.81310I$ |
| $u = -0.804264 - 1.135210I$ $a = -0.80264 - 1.70705I$ $b = -1.69330 + 0.63124I$ | $-16.0296 - 6.7782I$ | $-6.17368 + 2.81310I$ |

| Solutions to I_3^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|---------------------------|---------------------------------------|-----------------------|
| $u = 0.11097 + 1.44346I$ | | |
| $a = -2.20412 + 0.05114I$ | $-9.06867 + 2.70718I$ | $-3.52709 - 2.44627I$ |
| $b = -2.68367 + 0.72362I$ | | |
| $u = 0.11097 - 1.44346I$ | | |
| $a = -2.20412 - 0.05114I$ | $-9.06867 - 2.70718I$ | $-3.52709 + 2.44627I$ |
| $b = -2.68367 - 0.72362I$ | | |

$$\text{IV. } I_4^u = \langle u^5 + u^4 + u^3 + 2u^2 + b + u + 1, u^5 + u^4 + u^3 + u^2 + a + u, u^6 + u^5 + 2u^4 + 2u^3 + 2u^2 + 2u + 1 \rangle$$

(i) Arc colorings

$$a_6 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -u^5 - u^4 - u^3 - u^2 - u \\ -u^5 - u^4 - u^3 - 2u^2 - u - 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -u \\ u^3 + u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -u^5 - u^4 - u^3 - u^2 - u - 1 \\ -u^5 - u^4 - u^3 - u^2 - u - 1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -1 \\ u^2 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -u^5 - u^4 - u^3 - u^2 - u \\ -u^5 - u^4 - u^3 - 2u^2 - u - 1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -u^3 \\ u^5 + u^3 + u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -u^3 \\ u^5 + u^3 + u \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -u^5 - u^4 - 2u^3 - 2u^2 - 2u - 2 \\ u^5 + 2u^3 + u^2 + u + 1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -u^4 - u^2 - u - 1 \\ u^5 + 2u^3 + u^2 + u + 1 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = $u^5 + 5u^3 + u^2 + 5u - 2$

(iv) u-Polynomials at the component

| Crossings | u-Polynomials at each crossing |
|---------------|---|
| c_1, c_2 | $(u - 1)^6$ |
| c_3, c_7 | u^6 |
| c_4 | $(u + 1)^6$ |
| c_5, c_6 | $u^6 + u^5 + 2u^4 + 2u^3 + 2u^2 + 2u + 1$ |
| c_8, c_{10} | $u^6 + 3u^5 + 4u^4 + 2u^3 + 1$ |
| c_9, c_{11} | $u^6 - u^5 + 2u^4 - 2u^3 + 2u^2 - 2u + 1$ |
| c_{12} | $(u^3 - u^2 + 1)^2$ |

(v) Riley Polynomials at the component

| Crossings | Riley Polynomials at each crossing |
|-----------------------------|--------------------------------------|
| c_1, c_2, c_4 | $(y - 1)^6$ |
| c_3, c_7 | y^6 |
| c_5, c_6, c_9 c_{11} | $y^6 + 3y^5 + 4y^4 + 2y^3 + 1$ |
| c_8, c_{10} | $y^6 - y^5 + 4y^4 - 2y^3 + 8y^2 + 1$ |
| c_{12} | $(y^3 - y^2 + 2y - 1)^2$ |

(vi) Complex Volumes and Cusp Shapes

| Solutions to I_4^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|--|---------------------------------------|-------------------------|
| $u = 0.498832 + 1.001300I$ $a = 0.767394 + 0.943705I$ $b = 0.521167 - 0.055259I$ | $-1.37919 - 2.82812I$ | $-5.84740 + 3.54173I$ |
| $u = 0.498832 - 1.001300I$ $a = 0.767394 - 0.943705I$ $b = 0.521167 + 0.055259I$ | $-1.37919 + 2.82812I$ | $-5.84740 - 3.54173I$ |
| $u = -0.284920 + 1.115140I$ $a = 1.37744 - 1.47725I$ $b = 1.53980 - 0.84179I$ | 2.75839 | $-6 - 1.305207 + 0.10I$ |
| $u = -0.284920 - 1.115140I$ $a = 1.37744 + 1.47725I$ $b = 1.53980 + 0.84179I$ | 2.75839 | $-6 - 1.305207 + 0.10I$ |
| $u = -0.713912 + 0.305839I$ $a = 0.355167 - 0.198843I$ $b = -1.060970 + 0.237841I$ | $-1.37919 - 2.82812I$ | $-5.84740 + 3.54173I$ |
| $u = -0.713912 - 0.305839I$ $a = 0.355167 + 0.198843I$ $b = -1.060970 - 0.237841I$ | $-1.37919 + 2.82812I$ | $-5.84740 - 3.54173I$ |

$$\mathbf{V. } I_5^u = \langle au + 5b - 3a + u - 3, a^2 + au + 5u - 4, u^2 + 1 \rangle$$

(i) Arc colorings

$$a_6 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} a \\ -\frac{1}{5}au + \frac{3}{5}a - \frac{1}{5}u + \frac{3}{5} \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -u \\ 0 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -\frac{1}{5}au + \frac{3}{5}a - \frac{1}{5}u + \frac{3}{5} \\ -\frac{2}{5}au + \frac{1}{5}a - \frac{2}{5}u + \frac{6}{5} \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -\frac{2}{5}au - \frac{4}{5}a - \frac{7}{5}u + \frac{16}{5} \\ -\frac{1}{5}au - \frac{2}{5}a - \frac{6}{5}u + \frac{8}{5} \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -u + 2 \\ \frac{1}{5}au + \frac{2}{5}a - \frac{4}{5}u + \frac{2}{5} \end{pmatrix}$$

$$a_8 = \begin{pmatrix} u \\ u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} \frac{2}{5}au - \frac{1}{5}a - \frac{8}{5}u - \frac{6}{5} \\ -1 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -\frac{1}{5}au - \frac{2}{5}a - \frac{6}{5}u + \frac{8}{5} \\ -u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -\frac{1}{5}au - \frac{2}{5}a - \frac{11}{5}u + \frac{8}{5} \\ -u \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = 0

(iv) u-Polynomials at the component

| Crossings | u-Polynomials at each crossing |
|-----------------------------|--------------------------------|
| c_1 | $(u^2 - 3u + 1)^2$ |
| c_2 | $(u^2 + u - 1)^2$ |
| c_3, c_7 | $u^4 + 3u^2 + 1$ |
| c_4 | $(u^2 - u - 1)^2$ |
| c_5, c_6, c_9 c_{11} | $(u^2 + 1)^2$ |
| c_8, c_{10} | $(u + 1)^4$ |
| c_{12} | $u^4 + 7u^2 + 1$ |

(v) Riley Polynomials at the component

| Crossings | Riley Polynomials at each crossing |
|-----------------------------|------------------------------------|
| c_1 | $(y^2 - 7y + 1)^2$ |
| c_2, c_4 | $(y^2 - 3y + 1)^2$ |
| c_3, c_7 | $(y^2 + 3y + 1)^2$ |
| c_5, c_6, c_9 c_{11} | $(y + 1)^4$ |
| c_8, c_{10} | $(y - 1)^4$ |
| c_{12} | $(y^2 + 7y + 1)^2$ |

(vi) Complex Volumes and Cusp Shapes

| Solutions to I_5^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|--|---------------------------------------|------------|
| $u = 1.000000I$ $a = -2.23607 + 0.61803I$ $b = -0.618034 + 0.618034I$ | -5.59278 | 0 |
| $u = 1.000000I$ $a = 2.23607 - 1.61803I$ $b = 1.61803 - 1.61803I$ | 2.30291 | 0 |
| $u = -1.000000I$ $a = -2.23607 - 0.61803I$ $b = -0.618034 - 0.618034I$ | -5.59278 | 0 |
| $u = -1.000000I$ $a = 2.23607 + 1.61803I$ $b = 1.61803 + 1.61803I$ | 2.30291 | 0 |

VI. u-Polynomials

| Crossings | u-Polynomials at each crossing |
|---------------|---|
| c_1 | $((u-1)^{10}(u^2-3u+1)^2(u^{11}+18u^{10}+\dots+31u+1)^2 \cdot (u^{17}+25u^{16}+\dots-31u+16)$ |
| c_2 | $(u-1)^{10}(u^2+u-1)^2 \cdot (u^{11}-4u^{10}-u^9+17u^8+u^7-40u^6+3u^5+37u^4-3u^3-9u^2+7u-1)^2 \cdot (u^{17}-5u^{16}+\dots-u+4)$ |
| c_3, c_7 | $u^{10}(u^4+3u^2+1)(u^{11}+u^{10}+\dots-4u+8)^2 \cdot (u^{17}-3u^{16}+\dots+176u+64)$ |
| c_4 | $(u+1)^{10}(u^2-u-1)^2 \cdot (u^{11}-4u^{10}-u^9+17u^8+u^7-40u^6+3u^5+37u^4-3u^3-9u^2+7u-1)^2 \cdot (u^{17}-5u^{16}+\dots-u+4)$ |
| c_5, c_6 | $(u^2+1)^2(u^4+u^2-u+1)(u^6+u^5+2u^4+2u^3+2u^2+2u+1) \cdot (u^{17}+3u^{15}+\dots+11u^3-1)(u^{22}+2u^{21}+\dots+12u+9)$ |
| c_8, c_{10} | $(u+1)^4(u^4+2u^3+3u^2+u+1)(u^6+3u^5+4u^4+2u^3+1) \cdot (u^{17}-6u^{16}+\dots-6u^2+1)(u^{22}-10u^{21}+\dots-432u+81)$ |
| c_9, c_{11} | $(u^2+1)^2(u^4+u^2+u+1)(u^6-u^5+2u^4-2u^3+2u^2-2u+1) \cdot (u^{17}+3u^{15}+\dots+11u^3-1)(u^{22}+2u^{21}+\dots+12u+9)$ |
| c_{12} | $(u^3-u^2+1)^2(u^4+7u^2+1)(u^4+3u^3+4u^2+3u+2) \cdot (u^{11}+12u^9+36u^7+2u^6+2u^5+13u^4+13u^3+u^2+1)^2 \cdot (u^{17}+19u^{15}+\dots-5u^2+4)$ |

VII. Riley Polynomials

| Crossings | Riley Polynomials at each crossing |
|-----------------------------|---|
| c_1 | $((y-1)^{10})(y^2-7y+1)^2(y^{11}-46y^{10}+\dots+863y-1)^2$ $\cdot (y^{17}-61y^{16}+\dots-15103y-256)$ |
| c_2, c_4 | $((y-1)^{10})(y^2-3y+1)^2(y^{11}-18y^{10}+\dots+31y-1)^2$ $\cdot (y^{17}-25y^{16}+\dots-31y-16)$ |
| c_3, c_7 | $y^{10}(y^2+3y+1)^2(y^{11}+21y^{10}+\dots+336y-64)^2$ $\cdot (y^{17}+27y^{16}+\dots+4352y-4096)$ |
| c_5, c_6, c_9 c_{11} | $(y+1)^4(y^4+2y^3+3y^2+y+1)(y^6+3y^5+4y^4+2y^3+1)$ $\cdot (y^{17}+6y^{16}+\dots+6y^2-1)(y^{22}+10y^{21}+\dots+432y+81)$ |
| c_8, c_{10} | $(y-1)^4(y^4+2y^3+7y^2+5y+1)(y^6-y^5+4y^4-2y^3+8y^2+1)$ $\cdot (y^{17}+18y^{16}+\dots+12y-1)(y^{22}+2y^{21}+\dots+12312y+6561)$ |
| c_{12} | $(y^2+7y+1)^2(y^3-y^2+2y-1)^2(y^4-y^3+2y^2+7y+4)$ $\cdot ((y^{11}+24y^{10}+\dots-2y-1)^2)(y^{17}+38y^{16}+\dots+40y-16)$ |