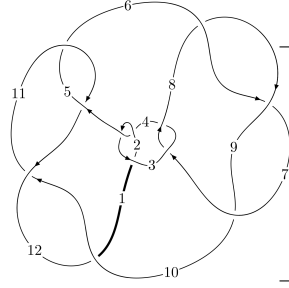
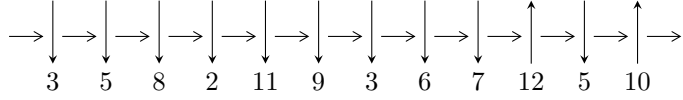


12n₀₂₂₉ (K12n₀₂₂₉)



A knot diagram¹

Linearized knot diagram



Solving Sequence

$$3,8 \xrightarrow{c_3} 4,5,11 \xrightarrow{c_5} 6 \xrightarrow{c_8} 9 \xrightarrow{c_{11}} 12 \xrightarrow{c_2} 2 \xrightarrow{c_1} 1 \xrightarrow{c_7} 7 \xrightarrow{c_{10}} 10 \longrightarrow c_4, c_6, c_9, c_{12}$$

Ideals for irreducible components² of X_{par}

$$I_1^u = \langle 4.74944 \times 10^{17} u^{17} + 1.40015 \times 10^{18} u^{16} + \dots + 6.24112 \times 10^{19} d - 1.05622 \times 10^{18}, \\ - 6.60139 \times 10^{16} u^{17} - 1.14793 \times 10^{18} u^{16} + \dots + 1.24822 \times 10^{20} c + 5.64891 \times 10^{19}, \\ - 5.68457 \times 10^{17} u^{17} - 8.64985 \times 10^{17} u^{16} + \dots + 1.24822 \times 10^{20} b - 1.55459 \times 10^{19}, \\ 2.99690 \times 10^{17} u^{17} + 2.72458 \times 10^{17} u^{16} + \dots + 2.49645 \times 10^{20} a - 2.46906 \times 10^{20}, u^{18} + 3u^{17} + \dots + 32u + \dots \rangle$$

$$I_2^u = \langle 6226u^9 a + 7765u^9 + \dots - 39596a - 22790, 19798u^9 a + 1477u^9 + \dots - 86484a - 5134, \\ 1447u^9 a + 65u^9 + \dots - 7346a - 3206, -22391u^9 a + 7563u^9 + \dots + 121770a - 50482, \\ u^{10} - u^9 - 7u^8 + 8u^7 + 13u^6 - 14u^5 - 2u^4 - 2u^3 + 13u^2 - 12u + 4 \rangle$$

$$I_1^v = \langle c, d + v, b, a - 1, v^2 - v + 1 \rangle$$

$$I_2^v = \langle a, d + v, av + c - v + 1, b - 1, v^2 - v + 1 \rangle$$

$$I_3^v = \langle a, d + 1, c + a, b - 1, v + 1 \rangle$$

$$I_4^v = \langle a, d^2 a - d^2 v - dc + dv + d - v - 1, d^2 v^2 - v^2 d - dv + v^2 + 2v + 1, \\ dca - dcv - da + dv - c^2 + cv - av + 2c - a - 1, v^2 dc - v^2 d - v^2 c + v^2 a - cv + 2av + a, \\ dav + da - dv - cv - c + v + 1, c^2 v^2 - v^2 ca + a^2 v^2 - cav - v^2 c + 2a^2 v - v^2 a + a^2 - av + v^2, b - 1 \rangle$$

* 5 irreducible components of $\dim_{\mathbb{C}} = 0$, with total 43 representations.

* 1 irreducible components of $\dim_{\mathbb{C}} = 1$

¹The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

²All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

I.

$$I_1^u = \langle 4.75 \times 10^{17}u^{17} + 1.40 \times 10^{18}u^{16} + \dots + 6.24 \times 10^{19}d - 1.06 \times 10^{18}, -6.60 \times 10^{16}u^{17} - 1.15 \times 10^{18}u^{16} + \dots + 1.25 \times 10^{20}c + 5.65 \times 10^{19}, -5.68 \times 10^{17}u^{17} - 8.65 \times 10^{17}u^{16} + \dots + 1.25 \times 10^{20}b - 1.55 \times 10^{19}, 3.00 \times 10^{17}u^{17} + 2.72 \times 10^{17}u^{16} + \dots + 2.50 \times 10^{20}a - 2.47 \times 10^{20}, u^{18} + 3u^{17} + \dots + 32u + 32 \rangle$$

(i) Arc colorings

$$a_3 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -0.00120047u^{17} - 0.00109138u^{16} + \dots - 0.0893825u + 0.989028 \\ 0.00455413u^{17} + 0.00692973u^{16} + \dots + 0.245124u + 0.124544 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0.000528863u^{17} + 0.00919651u^{16} + \dots + 0.525376u - 0.452556 \\ -0.00760992u^{17} - 0.0224344u^{16} + \dots + 0.469479u + 0.0169236 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -0.00389201u^{17} - 0.00712189u^{16} + \dots + 1.21746u + 0.120580 \\ 0.00251002u^{17} + 0.00451441u^{16} + \dots + 1.02744u + 0.0384150 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0.00640203u^{17} + 0.0116363u^{16} + \dots - 0.190018u - 0.0821645 \\ 0.00251002u^{17} + 0.00451441u^{16} + \dots + 1.02744u + 0.0384150 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 0.0117438u^{17} + 0.0288644u^{16} + \dots - 0.134994u - 0.795004 \\ 0.00684312u^{17} + 0.0134766u^{16} + \dots + 0.331617u + 0.354667 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -0.00120047u^{17} - 0.00109138u^{16} + \dots - 0.0893825u + 0.989028 \\ -0.00756978u^{17} - 0.0124143u^{16} + \dots - 0.287029u - 0.204865 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -0.00877025u^{17} - 0.0135056u^{16} + \dots - 0.376412u + 0.784163 \\ -0.00756978u^{17} - 0.0124143u^{16} + \dots - 0.287029u - 0.204865 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} u \\ u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0.0131347u^{17} + 0.0229449u^{16} + \dots - 0.168830u + 0.0635675 \\ 0.00924267u^{17} + 0.0158230u^{16} + \dots + 1.04863u + 0.184147 \end{pmatrix}$$

(ii) Obstruction class = -1

$$(iii) \text{ Cusp Shapes} = -\frac{1881106086253954753}{31205580083057755580}u^{17} - \frac{5887773742508132609}{62411160166115511160}u^{16} + \dots - \frac{57261478582730965292}{7801395020764438895}u - \frac{64355080374530213256}{7801395020764438895}$$

(iv) u-Polynomials at the component

| Crossings | u-Polynomials at each crossing |
|-------------------------------|--|
| c_1 | $u^{18} + 29u^{17} + \dots + 26u + 1$ |
| c_2, c_4, c_6 c_8, c_9 | $u^{18} - 5u^{17} + \dots + 2u - 1$ |
| c_3, c_7 | $u^{18} - 3u^{17} + \dots - 32u + 32$ |
| c_5, c_{11} | $u^{18} - u^{17} + \dots + 12u + 4$ |
| c_{10}, c_{12} | $u^{18} - 5u^{17} + \dots + 136u + 16$ |

(v) Riley Polynomials at the component

| Crossings | Riley Polynomials at each crossing |
|-------------------------------|--|
| c_1 | $y^{18} - 69y^{17} + \dots - 166y + 1$ |
| c_2, c_4, c_6 c_8, c_9 | $y^{18} - 29y^{17} + \dots - 26y + 1$ |
| c_3, c_7 | $y^{18} - 15y^{17} + \dots - 2048y + 1024$ |
| c_5, c_{11} | $y^{18} + 5y^{17} + \dots - 136y + 16$ |
| c_{10}, c_{12} | $y^{18} + 17y^{17} + \dots - 38944y + 256$ |

(vi) Complex Volumes and Cusp Shapes

| Solutions to I_1^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|---|---------------------------------------|------------------------|
| $u = -1.078440 + 0.216619I$ $a = 0.492205 - 0.156710I$ $b = 0.844681 + 0.587317I$ $c = 1.077070 - 0.430910I$ $d = 1.068210 - 0.698024I$ | $-3.61986 - 3.92600I$ | $-13.3379 + 5.7849I$ |
| $u = -1.078440 - 0.216619I$ $a = 0.492205 + 0.156710I$ $b = 0.844681 - 0.587317I$ $c = 1.077070 + 0.430910I$ $d = 1.068210 + 0.698024I$ | $-3.61986 + 3.92600I$ | $-13.3379 - 5.7849I$ |
| $u = 0.709201 + 0.274453I$ $a = 0.515734 + 0.082365I$ $b = 0.890761 - 0.301961I$ $c = 0.436964 + 0.773316I$ $d = -0.097657 - 0.668363I$ | $-3.12578 - 1.29944I$ | $-14.10514 + 0.79844I$ |
| $u = 0.709201 - 0.274453I$ $a = 0.515734 - 0.082365I$ $b = 0.890761 + 0.301961I$ $c = 0.436964 - 0.773316I$ $d = -0.097657 + 0.668363I$ | $-3.12578 + 1.29944I$ | $-14.10514 - 0.79844I$ |
| $u = -0.610909 + 0.417338I$ $a = 0.768504 + 0.302779I$ $b = 0.126387 - 0.443779I$ $c = -0.48208 - 1.41304I$ $d = -0.884219 - 0.662050I$ | $1.20916 + 1.63680I$ | $-1.95124 - 5.83411I$ |
| $u = -0.610909 - 0.417338I$ $a = 0.768504 - 0.302779I$ $b = 0.126387 + 0.443779I$ $c = -0.48208 + 1.41304I$ $d = -0.884219 + 0.662050I$ | $1.20916 - 1.63680I$ | $-1.95124 + 5.83411I$ |

| Solutions to I_1^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|---|---------------------------------------|------------------------|
| $u = 0.555399$ $a = 0.739573$ $b = 0.352132$ $c = -0.371975$ $d = 0.206595$ | -0.726383 | -14.1310 |
| $u = -0.072203 + 0.503217I$ $a = 1.330050 + 0.161709I$ $b = -0.259101 - 0.090079I$ $c = -0.46842 + 1.35904I$ $d = 0.650071 + 0.333845I$ | $-0.39079 - 2.25423I$ | $-1.75748 + 3.62098I$ |
| $u = -0.072203 - 0.503217I$ $a = 1.330050 - 0.161709I$ $b = -0.259101 + 0.090079I$ $c = -0.46842 - 1.35904I$ $d = 0.650071 - 0.333845I$ | $-0.39079 + 2.25423I$ | $-1.75748 - 3.62098I$ |
| $u = -1.83506 + 0.34828I$ $a = -1.318640 - 0.296832I$ $b = -1.72178 + 0.16248I$ $c = 0.10743 + 1.64261I$ $d = 0.76923 + 2.97688I$ | $-11.72250 + 5.21750I$ | $-12.21552 - 2.94469I$ |
| $u = -1.83506 - 0.34828I$ $a = -1.318640 + 0.296832I$ $b = -1.72178 - 0.16248I$ $c = 0.10743 - 1.64261I$ $d = 0.76923 - 2.97688I$ | $-11.72250 - 5.21750I$ | $-12.21552 + 2.94469I$ |
| $u = -1.70473 + 1.04671I$ $a = -0.961354 - 0.702659I$ $b = -1.67800 + 0.49555I$ $c = -0.21746 - 1.42452I$ $d = -1.86176 - 2.20079I$ | $19.5607 + 13.8899I$ | $-13.2954 - 6.2001I$ |

| Solutions to I_1^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|---|---------------------------------------|------------------------|
| $u = -1.70473 - 1.04671I$ $a = -0.961354 + 0.702659I$ $b = -1.67800 - 0.49555I$ $c = -0.21746 + 1.42452I$ $d = -1.86176 + 2.20079I$ | $19.5607 - 13.8899I$ | $-13.2954 + 6.2001I$ |
| $u = -0.16477 + 2.05598I$ $a = 0.354039 - 0.009486I$ $b = 1.82253 + 0.07562I$ $c = -0.653183 - 0.249237I$ $d = -0.62005 + 1.30187I$ | $-15.4858 - 3.5329I$ | $-13.90580 + 2.19457I$ |
| $u = -0.16477 - 2.05598I$ $a = 0.354039 + 0.009486I$ $b = 1.82253 - 0.07562I$ $c = -0.653183 + 0.249237I$ $d = -0.62005 - 1.30187I$ | $-15.4858 + 3.5329I$ | $-13.90580 - 2.19457I$ |
| $u = 2.12691$ $a = -1.17023$ $b = -1.85453$ $c = 0.262059$ $d = -0.557378$ | -16.6053 | -15.4680 |
| $u = 1.91575 + 0.96837I$ $a = -0.965214 + 0.561225I$ $b = -1.77427 - 0.45020I$ $c = -0.245361 + 0.187449I$ $d = 0.651569 - 0.121506I$ | $18.1284 - 6.9769I$ | $-14.6320 + 1.8700I$ |
| $u = 1.91575 - 0.96837I$ $a = -0.965214 - 0.561225I$ $b = -1.77427 + 0.45020I$ $c = -0.245361 - 0.187449I$ $d = 0.651569 + 0.121506I$ | $18.1284 + 6.9769I$ | $-14.6320 - 1.8700I$ |

II. $I_2^u = \langle 6226au^9 + 7765u^9 + \dots - 3.96 \times 10^4 a - 2.28 \times 10^4, 1.98 \times 10^4 au^9 + 1477u^9 + \dots - 8.65 \times 10^4 a - 5134, 1447au^9 + 65u^9 + \dots - 7346a - 3206, -2.24 \times 10^4 au^9 + 7563u^9 + \dots + 1.22 \times 10^5 a - 5.05 \times 10^4, u^{10} - u^9 + \dots - 12u + 4 \rangle$

(i) Arc colorings

$$\begin{aligned}
a_3 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\
a_8 &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\
a_4 &= \begin{pmatrix} 1 \\ u^2 \end{pmatrix} \\
a_5 &= \begin{pmatrix} a \\ -0.422112au^9 - 0.0189615u^9 + \dots + 2.14294a + 0.935239 \end{pmatrix} \\
a_{11} &= \begin{pmatrix} -1.44384au^9 - 0.107716u^9 + \dots + 6.30718a + 0.374417 \\ -0.908110au^9 - 1.13258u^9 + \dots + 5.77538a + 3.32410 \end{pmatrix} \\
a_6 &= \begin{pmatrix} \frac{3673}{6856}u^9 a + \frac{1}{4}u^9 + \dots - \frac{1823}{3428}a - 3 \\ 1.03574u^9 - 0.613623u^8 + \dots + 10.7148u - 6.53180 \end{pmatrix} \\
a_9 &= \begin{pmatrix} -0.535735au^9 + 0.785735u^9 + \dots + 0.531797a - 3.53180 \\ 1.03574u^9 - 0.613623u^8 + \dots + 10.7148u - 6.53180 \end{pmatrix} \\
a_{12} &= \begin{pmatrix} -0.663652au^9 - 0.107716u^9 + \dots + 2.73337a + 0.374417 \\ -0.682614au^9 - 0.637544u^9 + \dots + 3.66861a + 1.89177 \end{pmatrix} \\
a_2 &= \begin{pmatrix} a \\ 0.422112au^9 + 0.0189615u^9 + \dots - 2.14294a - 0.935239 \end{pmatrix} \\
a_1 &= \begin{pmatrix} 0.422112au^9 + 0.0189615u^9 + \dots - 1.14294a - 0.935239 \\ 0.422112au^9 + 0.0189615u^9 + \dots - 2.14294a - 0.935239 \end{pmatrix} \\
a_7 &= \begin{pmatrix} u \\ u \end{pmatrix} \\
a_{10} &= \begin{pmatrix} -0.681009au^9 + 0.785735u^9 + \dots + 2.22025a - 3.53180 \\ -0.145274au^9 + 1.03574u^9 + \dots + 1.68845a - 6.53180 \end{pmatrix}
\end{aligned}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes

$$= -\frac{3875}{1714}u^9 + \frac{183}{1714}u^8 + \frac{26957}{1714}u^7 - \frac{2248}{857}u^6 - \frac{51811}{1714}u^5 - \frac{541}{857}u^4 + \frac{185}{857}u^3 + \frac{9943}{857}u^2 - \frac{27495}{1714}u - \frac{882}{857}$$

(iv) u-Polynomials at the component

| Crossings | u-Polynomials at each crossing |
|-------------------------------|---|
| c_1 | $u^{20} + 19u^{19} + \dots - 1248u + 256$ |
| c_2, c_4, c_6 c_8, c_9 | $u^{20} - 3u^{19} + \dots + 8u + 16$ |
| c_3, c_7 | $(u^{10} + u^9 - 7u^8 - 8u^7 + 13u^6 + 14u^5 - 2u^4 + 2u^3 + 13u^2 + 12u + 4)^2$ |
| c_5, c_{11} | $(u^{10} - 2u^9 + 3u^8 - 2u^7 + 4u^6 - 3u^5 + 3u^4 + 3u^2 - u + 1)^2$ |
| c_{10}, c_{12} | $(u^{10} - 2u^9 + 9u^8 - 14u^7 + 28u^6 - 31u^5 + 35u^4 - 20u^3 + 15u^2 - 5u + 1)^2$ |

(v) Riley Polynomials at the component

| Crossings | Riley Polynomials at each crossing |
|-------------------------------|---|
| c_1 | $y^{20} - 39y^{19} + \dots - 4268544y + 65536$ |
| c_2, c_4, c_6 c_8, c_9 | $y^{20} - 19y^{19} + \dots + 1248y + 256$ |
| c_3, c_7 | $(y^{10} - 15y^9 + \dots - 40y + 16)^2$ |
| c_5, c_{11} | $(y^{10} + 2y^9 + 9y^8 + 14y^7 + 28y^6 + 31y^5 + 35y^4 + 20y^3 + 15y^2 + 5y + 1)^2$ |
| c_{10}, c_{12} | $(y^{10} + 14y^9 + \dots + 5y + 1)^2$ |

(vi) Complex Volumes and Cusp Shapes

| Solutions to I_2^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|--|---------------------------------------|------------------------|
| $u = -0.620250 + 0.748934I$ $a = 0.448932 - 0.060647I$ $b = 1.187590 + 0.295523I$ $c = -0.036785 + 1.027380I$ $d = 0.50487 + 1.48189I$ | $-4.43566 + 1.46073I$ | $-14.6593 - 3.2864I$ |
| $u = -0.620250 + 0.748934I$ $a = -0.77388 - 2.52919I$ $b = -1.110620 + 0.361536I$ $c = -0.84252 + 1.37187I$ $d = 0.746622 + 0.664780I$ | $-4.43566 + 1.46073I$ | $-14.6593 - 3.2864I$ |
| $u = -0.620250 - 0.748934I$ $a = 0.448932 + 0.060647I$ $b = 1.187590 - 0.295523I$ $c = -0.036785 - 1.027380I$ $d = 0.50487 - 1.48189I$ | $-4.43566 - 1.46073I$ | $-14.6593 + 3.2864I$ |
| $u = -0.620250 - 0.748934I$ $a = -0.77388 + 2.52919I$ $b = -1.110620 - 0.361536I$ $c = -0.84252 - 1.37187I$ $d = 0.746622 - 0.664780I$ | $-4.43566 - 1.46073I$ | $-14.6593 + 3.2864I$ |
| $u = 0.793271 + 0.121626I$ $a = 0.549929 + 0.112131I$ $b = 0.745831 - 0.355977I$ $c = -0.79610 - 1.70490I$ $d = -2.03769 - 3.21838I$ | $-2.87696 + 2.81207I$ | $-12.88002 - 4.64391I$ |
| $u = 0.793271 + 0.121626I$ $a = -4.13892 + 0.99173I$ $b = -1.228490 - 0.054749I$ $c = 3.11748 + 3.57912I$ $d = 0.42416 + 1.44928I$ | $-2.87696 + 2.81207I$ | $-12.88002 - 4.64391I$ |

| Solutions to I_2^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|---|---------------------------------------|------------------------|
| $u = 0.793271 - 0.121626I$ $a = 0.549929 - 0.112131I$ $b = 0.745831 + 0.355977I$ $c = -0.79610 + 1.70490I$ $d = -2.03769 + 3.21838I$ | $-2.87696 - 2.81207I$ | $-12.88002 + 4.64391I$ |
| $u = 0.793271 - 0.121626I$ $a = -4.13892 - 0.99173I$ $b = -1.228490 + 0.054749I$ $c = 3.11748 - 3.57912I$ $d = 0.42416 - 1.44928I$ | $-2.87696 - 2.81207I$ | $-12.88002 + 4.64391I$ |
| $u = 0.413972 + 0.524496I$ $a = 0.920372 - 0.380673I$ $b = -0.072202 + 0.383745I$ $c = -1.62004 + 0.89776I$ $d = -0.357634 - 0.319019I$ | $-1.39065 + 0.79591I$ | $-7.22040 + 0.81155I$ |
| $u = 0.413972 + 0.524496I$ $a = 0.475648 + 0.039205I$ $b = 1.088210 - 0.172121I$ $c = 0.706375 - 0.124338I$ $d = 1.141520 + 0.478061I$ | $-1.39065 + 0.79591I$ | $-7.22040 + 0.81155I$ |
| $u = 0.413972 - 0.524496I$ $a = 0.920372 + 0.380673I$ $b = -0.072202 - 0.383745I$ $c = -1.62004 - 0.89776I$ $d = -0.357634 + 0.319019I$ | $-1.39065 - 0.79591I$ | $-7.22040 - 0.81155I$ |
| $u = 0.413972 - 0.524496I$ $a = 0.475648 - 0.039205I$ $b = 1.088210 + 0.172121I$ $c = 0.706375 + 0.124338I$ $d = 1.141520 - 0.478061I$ | $-1.39065 - 0.79591I$ | $-7.22040 - 0.81155I$ |

| Solutions to I_2^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|---|---------------------------------------|------------------------|
| $u = 1.88200 + 0.46774I$ $a = -1.236340 + 0.360963I$ $b = -1.74531 - 0.21760I$ $c = -0.930133 + 0.846762I$ $d = -1.17593 + 1.51598I$ | $-12.6890 - 7.4068I$ | $-12.74326 + 4.41038I$ |
| $u = 1.88200 + 0.46774I$ $a = 0.385819 - 0.297883I$ $b = 0.623883 + 1.253760I$ $c = 0.399930 - 0.904911I$ $d = 2.14658 - 1.15854I$ | $-12.6890 - 7.4068I$ | $-12.74326 + 4.41038I$ |
| $u = 1.88200 - 0.46774I$ $a = -1.236340 - 0.360963I$ $b = -1.74531 + 0.21760I$ $c = -0.930133 - 0.846762I$ $d = -1.17593 - 1.51598I$ | $-12.6890 + 7.4068I$ | $-12.74326 - 4.41038I$ |
| $u = 1.88200 - 0.46774I$ $a = 0.385819 + 0.297883I$ $b = 0.623883 - 1.253760I$ $c = 0.399930 + 0.904911I$ $d = 2.14658 + 1.15854I$ | $-12.6890 + 7.4068I$ | $-12.74326 - 4.41038I$ |
| $u = -1.96899 + 0.18613I$ $a = -1.262570 - 0.138704I$ $b = -1.78259 + 0.08597I$ $c = -0.815769 + 0.005529I$ $d = -0.287282 + 0.794814I$ | $-13.15130 + 0.50253I$ | $-13.49701 + 0.08773I$ |
| $u = -1.96899 + 0.18613I$ $a = 0.381016 + 0.259317I$ $b = 0.79370 - 1.22078I$ $c = -0.182431 + 0.386420I$ $d = -1.60521 + 0.16272I$ | $-13.15130 + 0.50253I$ | $-13.49701 + 0.08773I$ |

| Solutions to I_2^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|-----------------------------|---------------------------------------|------------------------|
| $u = -1.96899 - 0.18613I$ | $-13.15130 - 0.50253I$ | $-13.49701 - 0.08773I$ |
| $a = -1.262570 + 0.138704I$ | | |
| $b = -1.78259 - 0.08597I$ | | |
| $c = -0.815769 - 0.005529I$ | | |
| $d = -0.287282 - 0.794814I$ | | |
| $u = -1.96899 - 0.18613I$ | $-13.15130 - 0.50253I$ | $-13.49701 - 0.08773I$ |
| $a = 0.381016 - 0.259317I$ | | |
| $b = 0.79370 + 1.22078I$ | | |
| $c = -0.182431 - 0.386420I$ | | |
| $d = -1.60521 - 0.16272I$ | | |

$$\text{III. } I_1^v = \langle c, d + v, b, a - 1, v^2 - v + 1 \rangle$$

(i) Arc colorings

$$a_3 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} v \\ 0 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0 \\ -v \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 1 \\ v - 1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} v - 1 \\ -v + 1 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} v \\ -v \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} v \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -1 \\ -v + 1 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = $4v - 11$

(iv) u-Polynomials at the component

| Crossings | u-Polynomials at each crossing |
|-------------------------------|--------------------------------|
| c_1, c_2, c_3 c_4, c_7 | u^2 |
| c_5, c_{10} | $u^2 + u + 1$ |
| c_6 | $(u - 1)^2$ |
| c_8, c_9 | $(u + 1)^2$ |
| c_{11}, c_{12} | $u^2 - u + 1$ |

(v) Riley Polynomials at the component

| Crossings | Riley Polynomials at each crossing |
|-----------------------------------|------------------------------------|
| c_1, c_2, c_3 c_4, c_7 | y^2 |
| c_5, c_{10}, c_{11} c_{12} | $y^2 + y + 1$ |
| c_6, c_8, c_9 | $(y - 1)^2$ |

(vi) Complex Volumes and Cusp Shapes

| Solutions to I_1^v | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|--|---------------------------------------|-----------------------|
| $v = 0.500000 + 0.866025I$ $a = 1.00000$ $b = 0$ $c = 0$ $d = -0.500000 - 0.866025I$ | $-1.64493 - 2.02988I$ | $-9.00000 + 3.46410I$ |
| $v = 0.500000 - 0.866025I$ $a = 1.00000$ $b = 0$ $c = 0$ $d = -0.500000 + 0.866025I$ | $-1.64493 + 2.02988I$ | $-9.00000 - 3.46410I$ |

$$\text{IV. } I_2^v = \langle a, d + v, av + c - v + 1, b - 1, v^2 - v + 1 \rangle$$

(i) Arc colorings

$$a_3 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} v \\ 0 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} v - 1 \\ -v \end{pmatrix}$$

$$a_6 = \begin{pmatrix} v \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} v \\ 0 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} v - 1 \\ -1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} v \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} v \\ 0 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = $-4v - 7$

(iv) u-Polynomials at the component

| Crossings | u-Polynomials at each crossing |
|-------------------------------|--------------------------------|
| c_1, c_2 | $(u - 1)^2$ |
| c_3, c_6, c_7 c_8, c_9 | u^2 |
| c_4 | $(u + 1)^2$ |
| c_5, c_{12} | $u^2 - u + 1$ |
| c_{10}, c_{11} | $u^2 + u + 1$ |

(v) Riley Polynomials at the component

| Crossings | Riley Polynomials at each crossing |
|-----------------------------------|------------------------------------|
| c_1, c_2, c_4 | $(y - 1)^2$ |
| c_3, c_6, c_7 c_8, c_9 | y^2 |
| c_5, c_{10}, c_{11} c_{12} | $y^2 + y + 1$ |

(vi) Complex Volumes and Cusp Shapes

| Solutions to I_2^v | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|-----------------------------|---------------------------------------|-----------------------|
| $v = 0.500000 + 0.866025I$ | $-1.64493 + 2.02988I$ | $-9.00000 - 3.46410I$ |
| $a = 0$ | | |
| $b = 1.00000$ | | |
| $c = -0.500000 + 0.866025I$ | | |
| $d = -0.500000 - 0.866025I$ | | |
| $v = 0.500000 - 0.866025I$ | $-1.64493 - 2.02988I$ | $-9.00000 + 3.46410I$ |
| $a = 0$ | | |
| $b = 1.00000$ | | |
| $c = -0.500000 - 0.866025I$ | | |
| $d = -0.500000 + 0.866025I$ | | |

$$\mathbf{V. } I_3^v = \langle a, d + 1, c + a, b - 1, v + 1 \rangle$$

(i) Arc colorings

$$a_3 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -1 \\ -1 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = -12

(iv) **u**-Polynomials at the component

| Crossings | u -Polynomials at each crossing |
|---|--|
| c_1, c_2, c_6 | $u - 1$ |
| c_3, c_5, c_7 c_{10}, c_{11}, c_{12} | u |
| c_4, c_8, c_9 | $u + 1$ |

(v) Riley Polynomials at the component

| Crossings | Riley Polynomials at each crossing |
|---|------------------------------------|
| c_1, c_2, c_4 c_6, c_8, c_9 | $y - 1$ |
| c_3, c_5, c_7 c_{10}, c_{11}, c_{12} | y |

(vi) Complex Volumes and Cusp Shapes

| Solutions to I_3^v | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|----------------------|---------------------------------------|------------|
| $v = -1.00000$ | | |
| $a = 0$ | | |
| $b = 1.00000$ | -3.28987 | -12.0000 |
| $c = 0$ | | |
| $d = -1.00000$ | | |

VI.

$$I_4^v = \langle a, -d^2v + dv + \dots + d - 1, d^2v^2 - dv^2 + \dots + 2v + 1, -cdv + dv + \dots - a - 1, cdv^2 - dv^2 + \dots + 2av + a, adv - dv + \dots - c + 1, c^2v^2 - acv^2 + \dots - av + a^2, b - 1 \rangle$$

(i) Arc colorings

$$a_3 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} v \\ 0 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} c \\ d \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -c + 1 \\ -dc + 1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} c + v - 1 \\ dc - 1 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} c \\ d + c \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} v \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} c - 1 \\ dc - 1 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes = $d^2c - d^2 - 2dc + v^2 + 4c - 15$

(iv) u-Polynomials at the component : It cannot be defined for a positive dimension component.

(v) Riley Polynomials at the component : It cannot be defined for a positive dimension component.

(iv) Complex Volumes and Cusp Shapes

| Solution to I_4^v | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|---------------------|---------------------------------------|------------------------|
| $v = \dots$ | | |
| $a = \dots$ | | |
| $b = \dots$ | $-3.28987 + 2.02988I$ | $-12.35599 + 3.42923I$ |
| $c = \dots$ | | |
| $d = \dots$ | | |

VII. u-Polynomials

| Crossings | u-Polynomials at each crossing |
|-----------------|---|
| c_1 | $u^2(u-1)^3(u^{18} + 29u^{17} + \dots + 26u + 1)$ $\cdot (u^{20} + 19u^{19} + \dots - 1248u + 256)$ |
| c_2, c_6 | $u^2(u-1)^3(u^{18} - 5u^{17} + \dots + 2u - 1)(u^{20} - 3u^{19} + \dots + 8u + 16)$ |
| c_3, c_7 | $u^5(u^{10} + u^9 + \dots + 12u + 4)^2$ $\cdot (u^{18} - 3u^{17} + \dots - 32u + 32)$ |
| c_4, c_8, c_9 | $u^2(u+1)^3(u^{18} - 5u^{17} + \dots + 2u - 1)(u^{20} - 3u^{19} + \dots + 8u + 16)$ |
| c_5, c_{11} | $u(u^2 - u + 1)(u^2 + u + 1)$ $\cdot (u^{10} - 2u^9 + 3u^8 - 2u^7 + 4u^6 - 3u^5 + 3u^4 + 3u^2 - u + 1)^2$ $\cdot (u^{18} - u^{17} + \dots + 12u + 4)$ |
| c_{10} | $u(u^2 + u + 1)^2$ $\cdot (u^{10} - 2u^9 + 9u^8 - 14u^7 + 28u^6 - 31u^5 + 35u^4 - 20u^3 + 15u^2 - 5u + 1)^2$ $\cdot (u^{18} - 5u^{17} + \dots + 136u + 16)$ |
| c_{12} | $u(u^2 - u + 1)^2$ $\cdot (u^{10} - 2u^9 + 9u^8 - 14u^7 + 28u^6 - 31u^5 + 35u^4 - 20u^3 + 15u^2 - 5u + 1)^2$ $\cdot (u^{18} - 5u^{17} + \dots + 136u + 16)$ |

VIII. Riley Polynomials

| Crossings | Riley Polynomials at each crossing |
|-------------------------------|---|
| c_1 | $y^2(y-1)^3(y^{18} - 69y^{17} + \dots - 166y + 1)$ $\cdot (y^{20} - 39y^{19} + \dots - 4268544y + 65536)$ |
| c_2, c_4, c_6 c_8, c_9 | $y^2(y-1)^3(y^{18} - 29y^{17} + \dots - 26y + 1)$ $\cdot (y^{20} - 19y^{19} + \dots + 1248y + 256)$ |
| c_3, c_7 | $y^5(y^{10} - 15y^9 + \dots - 40y + 16)^2(y^{18} - 15y^{17} + \dots - 2048y + 1024)$ |
| c_5, c_{11} | $y(y^2 + y + 1)^2$ $\cdot (y^{10} + 2y^9 + 9y^8 + 14y^7 + 28y^6 + 31y^5 + 35y^4 + 20y^3 + 15y^2 + 5y + 1)^2$ $\cdot (y^{18} + 5y^{17} + \dots - 136y + 16)$ |
| c_{10}, c_{12} | $y(y^2 + y + 1)^2(y^{10} + 14y^9 + \dots + 5y + 1)^2$ $\cdot (y^{18} + 17y^{17} + \dots - 38944y + 256)$ |