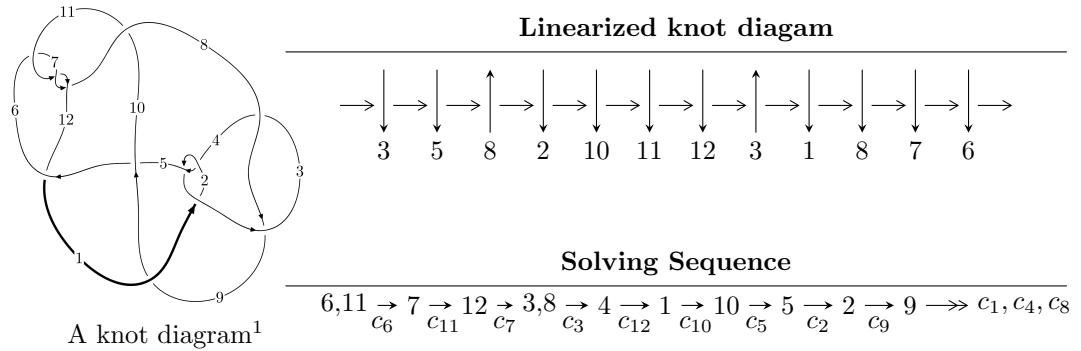


$12n_{0240}$  ( $K12n_{0240}$ )



Ideals for irreducible components<sup>2</sup> of  $X_{\text{par}}$

$$I_1^u = \langle -u^{45} + u^{44} + \dots + b + 2u, -2u^{45} + 2u^{44} + \dots + a + 8u, u^{46} - 2u^{45} + \dots + u + 1 \rangle$$

$$I_2^u = \langle u^3 + b - u + 1, u^6 - 3u^4 + 2u^2 + a + 1, u^8 + u^7 - 3u^6 - 2u^5 + 3u^4 + 2u - 1 \rangle$$

\* 2 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 54 representations.

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<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/math/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$I_1^u = \langle -u^{45} + u^{44} + \cdots + b + 2u, -2u^{45} + 2u^{44} + \cdots + a + 8u, u^{46} - 2u^{45} + \cdots + u + 1 \rangle^{\text{I.}}$$

(i) **Arc colorings**

$$a_6 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -u \\ -u^3 + u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 2u^{45} - 2u^{44} + \cdots + 10u^2 - 8u \\ u^{45} - u^{44} + \cdots + 5u^2 - 2u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -u^2 + 1 \\ -u^4 + 2u^2 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 4u^{45} - 4u^{44} + \cdots - 10u - 1 \\ u^{45} - u^{44} + \cdots + 4u^2 - 3u \end{pmatrix}$$

$$a_1 = \begin{pmatrix} u^3 - 2u \\ -u^3 + u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} u^5 - 2u^3 + u \\ u^7 - 3u^5 + 2u^3 + u \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -u^{12} + 5u^{10} - 9u^8 + 6u^6 - u^2 + 1 \\ -u^{14} + 6u^{12} - 13u^{10} + 10u^8 + 2u^6 - 4u^4 - u^2 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} u^{45} - u^{44} + \cdots - 8u + 1 \\ u^{45} - u^{44} + \cdots + 5u^2 - u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} u^{13} - 6u^{11} + 13u^9 - 10u^7 - 2u^5 + 4u^3 + u \\ -u^{13} + 5u^{11} - 9u^9 + 6u^7 - u^3 + u \end{pmatrix}$$

(ii) **Obstruction class** = -1

(iii) **Cusp Shapes** =  $-3u^{45} + 56u^{43} + \cdots - 5u - 1$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1$	$u^{46} + 11u^{45} + \cdots + 25u + 1$
$c_2, c_4$	$u^{46} - 9u^{45} + \cdots - 9u + 1$
$c_3, c_8$	$u^{46} + u^{45} + \cdots + 1152u + 256$
$c_5$	$u^{46} - 2u^{45} + \cdots + 2660u + 1960$
$c_6, c_7, c_{11}$	$u^{46} + 2u^{45} + \cdots - u + 1$
$c_9$	$u^{46} + 2u^{45} + \cdots + 7u + 1$
$c_{10}, c_{12}$	$u^{46} - 6u^{45} + \cdots - 73u + 17$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1$	$y^{46} + 57y^{45} + \cdots - 21y + 1$
$c_2, c_4$	$y^{46} - 11y^{45} + \cdots - 25y + 1$
$c_3, c_8$	$y^{46} - 51y^{45} + \cdots - 1490944y + 65536$
$c_5$	$y^{46} + 18y^{45} + \cdots - 21367920y + 3841600$
$c_6, c_7, c_{11}$	$y^{46} - 38y^{45} + \cdots - 17y + 1$
$c_9$	$y^{46} + 54y^{45} + \cdots - 17y + 1$
$c_{10}, c_{12}$	$y^{46} + 34y^{45} + \cdots - 5737y + 289$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.088878 + 0.844041I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = 3.37742 - 1.22551I$	$11.39320 + 1.80249I$	$-2.43037 - 0.91952I$
$b = -2.98228 + 0.61868I$		
$u = -0.088878 - 0.844041I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = 3.37742 + 1.22551I$	$11.39320 - 1.80249I$	$-2.43037 + 0.91952I$
$b = -2.98228 - 0.61868I$		
$u = -0.116026 + 0.837306I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = -3.46305 + 1.35399I$	$10.46260 + 9.14915I$	$-3.66280 - 5.53840I$
$b = 3.14660 - 0.77902I$		
$u = -0.116026 - 0.837306I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = -3.46305 - 1.35399I$	$10.46260 - 9.14915I$	$-3.66280 + 5.53840I$
$b = 3.14660 + 0.77902I$		
$u = 1.141830 + 0.219995I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = -0.660574 + 0.098342I$	$-1.38478 - 0.54129I$	$-5.73844 + 0.I$
$b = -0.127713 - 0.217138I$		
$u = 1.141830 - 0.219995I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = -0.660574 - 0.098342I$	$-1.38478 + 0.54129I$	$-5.73844 + 0.I$
$b = -0.127713 + 0.217138I$		
$u = 0.058004 + 0.794656I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = 1.48803 - 0.66681I$	$3.97447 - 2.81253I$	$-2.78364 + 4.01547I$
$b = -1.176270 + 0.234722I$		
$u = 0.058004 - 0.794656I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = 1.48803 + 0.66681I$	$3.97447 + 2.81253I$	$-2.78364 - 4.01547I$
$b = -1.176270 - 0.234722I$		
$u = -1.139460 + 0.393221I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = -1.60826 + 1.63861I$	$7.33193 - 4.71190I$	$-6.52326 + 0.I$
$b = 2.48711 + 1.35446I$		
$u = -1.139460 - 0.393221I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = -1.60826 - 1.63861I$	$7.33193 + 4.71190I$	$-6.52326 + 0.I$
$b = 2.48711 - 1.35446I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.175260 + 0.396885I$		
$a = 1.58950 - 1.52874I$	$8.06092 + 2.65955I$	0
$b = -2.60724 - 1.21777I$		
$u = -1.175260 - 0.396885I$		
$a = 1.58950 + 1.52874I$	$8.06092 - 2.65955I$	0
$b = -2.60724 + 1.21777I$		
$u = -0.027447 + 0.752835I$		
$a = -2.58406 - 0.48560I$	$1.16885 + 1.15848I$	$-5.01072 + 0.12391I$
$b = 1.92495 + 0.96879I$		
$u = -0.027447 - 0.752835I$		
$a = -2.58406 + 0.48560I$	$1.16885 - 1.15848I$	$-5.01072 - 0.12391I$
$b = 1.92495 - 0.96879I$		
$u = 0.135112 + 0.737338I$		
$a = -0.263549 - 0.833035I$	$1.53760 - 3.03900I$	$-1.98360 + 5.04098I$
$b = 0.030415 + 0.576766I$		
$u = 0.135112 - 0.737338I$		
$a = -0.263549 + 0.833035I$	$1.53760 + 3.03900I$	$-1.98360 - 5.04098I$
$b = 0.030415 - 0.576766I$		
$u = 1.215480 + 0.337571I$		
$a = 0.103389 + 1.085520I$	$0.425497 - 1.277230I$	0
$b = -0.822594 + 0.083089I$		
$u = 1.215480 - 0.337571I$		
$a = 0.103389 - 1.085520I$	$0.425497 + 1.277230I$	0
$b = -0.822594 - 0.083089I$		
$u = -1.259210 + 0.309211I$		
$a = -0.456708 + 1.219730I$	$-2.63767 + 2.66589I$	0
$b = 2.37986 - 0.29804I$		
$u = -1.259210 - 0.309211I$		
$a = -0.456708 - 1.219730I$	$-2.63767 - 2.66589I$	0
$b = 2.37986 + 0.29804I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.308600 + 0.052486I$		
$a = 0.039504 + 0.254143I$	$-5.32887 + 1.91338I$	0
$b = 0.45316 - 1.39921I$		
$u = -1.308600 - 0.052486I$		
$a = 0.039504 - 0.254143I$	$-5.32887 - 1.91338I$	0
$b = 0.45316 + 1.39921I$		
$u = 1.31477$		
$a = 1.61451$	-6.82836	-12.1040
$b = 0.0640641$		
$u = -0.494895 + 0.460674I$		
$a = 0.357271 - 1.172810I$	$5.38865 + 5.18412I$	$-6.71823 - 6.02395I$
$b = 0.450500 - 0.532533I$		
$u = -0.494895 - 0.460674I$		
$a = 0.357271 + 1.172810I$	$5.38865 - 5.18412I$	$-6.71823 + 6.02395I$
$b = 0.450500 + 0.532533I$		
$u = 1.291940 + 0.323151I$		
$a = -1.15932 - 1.41965I$	-2.95162 - 5.04688I	0
$b = 1.49071 - 1.53239I$		
$u = 1.291940 - 0.323151I$		
$a = -1.15932 + 1.41965I$	-2.95162 + 5.04688I	0
$b = 1.49071 + 1.53239I$		
$u = -0.418017 + 0.505684I$		
$a = -0.149306 + 0.739200I$	$5.63155 - 1.66298I$	$-5.86083 - 1.14993I$
$b = -0.653704 + 0.563087I$		
$u = -0.418017 - 0.505684I$		
$a = -0.149306 - 0.739200I$	$5.63155 + 1.66298I$	$-5.86083 + 1.14993I$
$b = -0.653704 - 0.563087I$		
$u = -1.307310 + 0.347945I$		
$a = 0.790380 - 0.475352I$	-0.29502 + 6.93232I	0
$b = -1.45484 - 0.59474I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.307310 - 0.347945I$		
$a = 0.790380 + 0.475352I$	$-0.29502 - 6.93232I$	0
$b = -1.45484 + 0.59474I$		
$u = 1.366120 + 0.148240I$		
$a = -0.533420 - 0.484870I$	$0.048597 - 0.512586I$	0
$b = -0.989531 + 0.198012I$		
$u = 1.366120 - 0.148240I$		
$a = -0.533420 + 0.484870I$	$0.048597 + 0.512586I$	0
$b = -0.989531 - 0.198012I$		
$u = -1.345150 + 0.312918I$		
$a = 0.253414 + 0.362467I$	$-3.12507 + 6.85143I$	0
$b = 0.191334 - 0.810458I$		
$u = -1.345150 - 0.312918I$		
$a = 0.253414 - 0.362467I$	$-3.12507 - 6.85143I$	0
$b = 0.191334 + 0.810458I$		
$u = 1.329650 + 0.375534I$		
$a = 0.49137 + 2.28669I$	$6.94740 - 6.18607I$	0
$b = -3.08691 - 0.08101I$		
$u = 1.329650 - 0.375534I$		
$a = 0.49137 - 2.28669I$	$6.94740 + 6.18607I$	0
$b = -3.08691 + 0.08101I$		
$u = -1.38696$		
$a = -0.181617$	$-7.20797$	0
$b = 0.699740$		
$u = 1.345460 + 0.367374I$		
$a = -0.43223 - 2.36028I$	$5.8692 - 13.4842I$	0
$b = 3.46843 + 0.20726I$		
$u = 1.345460 - 0.367374I$		
$a = -0.43223 + 2.36028I$	$5.8692 + 13.4842I$	0
$b = 3.46843 - 0.20726I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.390620 + 0.107679I$		
$a = 0.514855 + 0.841670I$	$-0.55483 - 6.96949I$	0
$b = 0.807363 - 0.612141I$		
$u = 1.390620 - 0.107679I$		
$a = 0.514855 - 0.841670I$	$-0.55483 + 6.96949I$	0
$b = 0.807363 + 0.612141I$		
$u = 0.582853$		
$a = -0.782593$	-1.21098	-7.83090
$b = 0.178233$		
$u = 0.282232 + 0.263140I$		
$a = -0.99274 - 1.11009I$	$-0.549820 - 0.931505I$	$-8.30910 + 7.33237I$
$b = 0.157868 + 0.383616I$		
$u = 0.282232 - 0.263140I$		
$a = -0.99274 + 1.11009I$	$-0.549820 + 0.931505I$	$-8.30910 - 7.33237I$
$b = 0.157868 - 0.383616I$		
$u = -0.263046$		
$a = 2.94586$	-2.04174	0.290920
$b = 0.883552$		

### II.

$$I_2^u = \langle u^3 + b - u + 1, \ u^6 - 3u^4 + 2u^2 + a + 1, \ u^8 + u^7 - 3u^6 - 2u^5 + 3u^4 + 2u - 1 \rangle$$

(i) **Arc colorings**

$$a_6 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -u \\ -u^3 + u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -u^6 + 3u^4 - 2u^2 - 1 \\ -u^3 + u - 1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -u^2 + 1 \\ -u^4 + 2u^2 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -u^6 + 3u^4 - 2u^2 - 1 \\ -u^3 + u - 1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} u^3 - 2u \\ -u^3 + u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} u^5 - 2u^3 + u \\ u^7 - 3u^5 + 2u^3 + u \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -u^3 + 2u \\ u^3 - u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -u^6 + 3u^4 + u^3 - 2u^2 - 2u - 1 \\ -2u^3 + 2u - 1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -u^2 + 1 \\ -u^4 + 2u^2 \end{pmatrix}$$

(ii) **Obstruction class = 1**

(iii) **Cusp Shapes** =  $-u^7 - 6u^6 + 2u^5 + 16u^4 - 5u^3 - 9u^2 + 8u - 21$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_2$	$(u - 1)^8$
$c_3, c_8$	$u^8$
$c_4$	$(u + 1)^8$
$c_5, c_9$	$u^8 - u^7 - u^6 + 2u^5 + u^4 - 2u^3 + 2u - 1$
$c_6, c_7$	$u^8 + u^7 - 3u^6 - 2u^5 + 3u^4 + 2u - 1$
$c_{10}, c_{12}$	$u^8 + 3u^7 + 7u^6 + 10u^5 + 11u^4 + 10u^3 + 6u^2 + 4u + 1$
$c_{11}$	$u^8 - u^7 - 3u^6 + 2u^5 + 3u^4 - 2u - 1$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_4$	$(y - 1)^8$
$c_3, c_8$	$y^8$
$c_5, c_9$	$y^8 - 3y^7 + 7y^6 - 10y^5 + 11y^4 - 10y^3 + 6y^2 - 4y + 1$
$c_6, c_7, c_{11}$	$y^8 - 7y^7 + 19y^6 - 22y^5 + 3y^4 + 14y^3 - 6y^2 - 4y + 1$
$c_{10}, c_{12}$	$y^8 + 5y^7 + 11y^6 + 6y^5 - 17y^4 - 34y^3 - 22y^2 - 4y + 1$

**(vi) Complex Volumes and Cusp Shapes**

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.180120 + 0.268597I$ $a = -0.325934 + 0.693334I$ $b = -1.20799 - 0.83423I$	$-2.68559 - 1.13123I$	$-10.92586 + 0.21647I$
$u = 1.180120 - 0.268597I$ $a = -0.325934 - 0.693334I$ $b = -1.20799 + 0.83423I$	$-2.68559 + 1.13123I$	$-10.92586 - 0.21647I$
$u = 0.108090 + 0.747508I$ $a = 1.03462 - 0.99451I$ $b = -0.711982 + 1.138990I$	$0.51448 - 2.57849I$	$-8.77377 + 3.25417I$
$u = 0.108090 - 0.747508I$ $a = 1.03462 + 0.99451I$ $b = -0.711982 - 1.138990I$	$0.51448 + 2.57849I$	$-8.77377 - 3.25417I$
$u = -1.37100$ $a = -0.801005$ $b = 0.205997$	$-8.14766$	$-19.8990$
$u = -1.334530 + 0.318930I$ $a = 0.842429 - 0.289836I$ $b = -0.365014 - 1.352640I$	$-4.02461 + 6.44354I$	$-14.3478 - 4.5473I$
$u = -1.334530 - 0.318930I$ $a = 0.842429 + 0.289836I$ $b = -0.365014 + 1.352640I$	$-4.02461 - 6.44354I$	$-14.3478 + 4.5473I$
$u = 0.463640$ $a = -1.30123$ $b = -0.636025$	$-2.48997$	$-19.0060$

### III. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1$	$((u - 1)^8)(u^{46} + 11u^{45} + \cdots + 25u + 1)$
$c_2$	$((u - 1)^8)(u^{46} - 9u^{45} + \cdots - 9u + 1)$
$c_3, c_8$	$u^8(u^{46} + u^{45} + \cdots + 1152u + 256)$
$c_4$	$((u + 1)^8)(u^{46} - 9u^{45} + \cdots - 9u + 1)$
$c_5$	$(u^8 - u^7 - u^6 + 2u^5 + u^4 - 2u^3 + 2u - 1) \cdot (u^{46} - 2u^{45} + \cdots + 2660u + 1960)$
$c_6, c_7$	$(u^8 + u^7 - 3u^6 - 2u^5 + 3u^4 + 2u - 1)(u^{46} + 2u^{45} + \cdots - u + 1)$
$c_9$	$(u^8 - u^7 + \cdots + 2u - 1)(u^{46} + 2u^{45} + \cdots + 7u + 1)$
$c_{10}, c_{12}$	$(u^8 + 3u^7 + 7u^6 + 10u^5 + 11u^4 + 10u^3 + 6u^2 + 4u + 1) \cdot (u^{46} - 6u^{45} + \cdots - 73u + 17)$
$c_{11}$	$(u^8 - u^7 - 3u^6 + 2u^5 + 3u^4 - 2u - 1)(u^{46} + 2u^{45} + \cdots - u + 1)$

#### IV. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1$	$((y - 1)^8)(y^{46} + 57y^{45} + \dots - 21y + 1)$
$c_2, c_4$	$((y - 1)^8)(y^{46} - 11y^{45} + \dots - 25y + 1)$
$c_3, c_8$	$y^8(y^{46} - 51y^{45} + \dots - 1490944y + 65536)$
$c_5$	$(y^8 - 3y^7 + 7y^6 - 10y^5 + 11y^4 - 10y^3 + 6y^2 - 4y + 1) \cdot (y^{46} + 18y^{45} + \dots - 21367920y + 3841600)$
$c_6, c_7, c_{11}$	$(y^8 - 7y^7 + 19y^6 - 22y^5 + 3y^4 + 14y^3 - 6y^2 - 4y + 1) \cdot (y^{46} - 38y^{45} + \dots - 17y + 1)$
$c_9$	$(y^8 - 3y^7 + 7y^6 - 10y^5 + 11y^4 - 10y^3 + 6y^2 - 4y + 1) \cdot (y^{46} + 54y^{45} + \dots - 17y + 1)$
$c_{10}, c_{12}$	$(y^8 + 5y^7 + 11y^6 + 6y^5 - 17y^4 - 34y^3 - 22y^2 - 4y + 1) \cdot (y^{46} + 34y^{45} + \dots - 5737y + 289)$