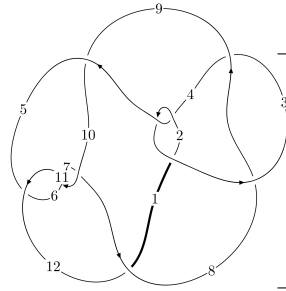
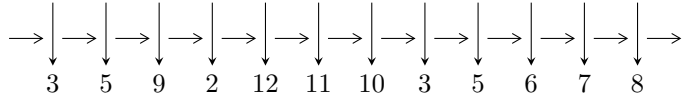


12n₀₂₄₄ (K12n₀₂₄₄)



A knot diagram¹

Linearized knot diagram



Solving Sequence

$$7,12 \xrightarrow{c_{11}} 11 \xrightarrow{c_6} 6 \xrightarrow{c_5} 3,5 \xrightarrow{c_2} 2 \xrightarrow{c_1} 1 \xrightarrow{c_4} 4 \xrightarrow{c_{10}} 10 \xrightarrow{c_7} 8 \xrightarrow{c_9} 9 \twoheadrightarrow c_3, c_8, c_{12}$$

Ideals for irreducible components² of X_{par}

$$I_1^u = \langle u^{19} + u^{18} + \dots + u^2 + b, -u^{19} - u^{18} + \dots + a - 2, u^{20} + 2u^{19} + \dots + 2u + 1 \rangle$$

$$I_2^u = \langle b - 1, u^6 - 3u^4 - u^3 + 2u^2 + a + 2u + 1, u^8 - u^7 - 3u^6 + 2u^5 + 3u^4 - 2u - 1 \rangle$$

* 2 irreducible components of $\dim_{\mathbb{C}} = 0$, with total 28 representations.

¹The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

²All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$I_1^u = \langle u^{19} + u^{18} + \dots + u^2 + b, -u^{19} - u^{18} + \dots + a - 2, u^{20} + 2u^{19} + \dots + 2u + 1 \rangle \quad \text{I.}$$

(i) Arc colorings

$$a_7 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} u \\ -u^3 + u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} u^{19} + u^{18} + \dots + 3u + 2 \\ -u^{19} - u^{18} + \dots - 8u^3 - u^2 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -u^3 + 2u \\ -u^3 + u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 2u^{19} + 2u^{18} + \dots + 6u + 3 \\ -u^{19} - u^{18} + \dots - 12u^3 + u \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -u^{12} + 5u^{10} - 9u^8 + 6u^6 - u^2 + 1 \\ u^{14} - 6u^{12} + 13u^{10} - 10u^8 - 2u^6 + 4u^4 + u^2 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -3u^{19} - 3u^{18} + \dots - 6u - 3 \\ u^{19} + u^{18} + \dots - 2u^2 - u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -u^2 + 1 \\ u^4 - 2u^2 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -u^5 + 2u^3 - u \\ u^7 - 3u^5 + 2u^3 + u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} u^{10} - 5u^8 + 8u^6 - 3u^4 - 3u^2 + 1 \\ u^{10} - 4u^8 + 5u^6 - 3u^2 \end{pmatrix}$$

(ii) Obstruction class = -1

$$\text{(iii) Cusp Shapes} = 5u^{19} + 4u^{18} - 38u^{17} - 21u^{16} + 118u^{15} + 27u^{14} - 176u^{13} + 40u^{12} + 88u^{11} - 121u^{10} + 80u^9 + 58u^8 - 89u^7 + 52u^6 - 36u^5 - 27u^4 + 46u^3 - 16u^2 + 12u - 11$$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1	$u^{20} + 39u^{19} + \dots + 18u + 1$
c_2, c_4	$u^{20} - 9u^{19} + \dots + 9u^2 - 1$
c_3, c_8	$u^{20} + u^{19} + \dots - 640u - 256$
c_5, c_7	$u^{20} - 6u^{19} + \dots + 2u - 5$
c_6, c_{10}, c_{11}	$u^{20} + 2u^{19} + \dots + 2u + 1$
c_9, c_{12}	$u^{20} - 2u^{19} + \dots + 2u + 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1	$y^{20} - 155y^{19} + \dots - 690y + 1$
c_2, c_4	$y^{20} - 39y^{19} + \dots - 18y + 1$
c_3, c_8	$y^{20} - 51y^{19} + \dots + 16384y + 65536$
c_5, c_7	$y^{20} + 6y^{19} + \dots - 194y + 25$
c_6, c_{10}, c_{11}	$y^{20} - 18y^{19} + \dots - 6y + 1$
c_9, c_{12}	$y^{20} - 42y^{19} + \dots - 6y + 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.911170 + 0.459727I$ $a = -1.34870 - 0.62192I$ $b = -2.12337 + 0.10108I$	$-17.2402 + 0.6353I$	$-16.0469 + 1.1994I$
$u = 0.911170 - 0.459727I$ $a = -1.34870 + 0.62192I$ $b = -2.12337 - 0.10108I$	$-17.2402 - 0.6353I$	$-16.0469 - 1.1994I$
$u = 0.247662 + 0.821626I$ $a = -2.43556 - 1.84521I$ $b = -2.12150 - 0.21202I$	$-15.1547 - 5.2095I$	$-13.60177 + 3.17253I$
$u = 0.247662 - 0.821626I$ $a = -2.43556 + 1.84521I$ $b = -2.12150 + 0.21202I$	$-15.1547 + 5.2095I$	$-13.60177 - 3.17253I$
$u = -1.208090 + 0.243596I$ $a = 0.570598 + 0.429334I$ $b = -0.218634 + 0.234930I$	$-1.33162 + 1.52088I$	$-9.67152 - 0.73849I$
$u = -1.208090 - 0.243596I$ $a = 0.570598 - 0.429334I$ $b = -0.218634 - 0.234930I$	$-1.33162 - 1.52088I$	$-9.67152 + 0.73849I$
$u = -0.102862 + 0.701439I$ $a = 0.082707 - 0.900739I$ $b = -0.141682 - 0.411106I$	$1.97616 + 1.89773I$	$-7.07242 - 3.81165I$
$u = -0.102862 - 0.701439I$ $a = 0.082707 + 0.900739I$ $b = -0.141682 + 0.411106I$	$1.97616 - 1.89773I$	$-7.07242 + 3.81165I$
$u = 1.312190 + 0.118081I$ $a = 0.496056 - 0.398382I$ $b = 0.691084 - 0.636911I$	$-4.98968 - 0.65533I$	$-18.6254 + 0.2318I$
$u = 1.312190 - 0.118081I$ $a = 0.496056 + 0.398382I$ $b = 0.691084 + 0.636911I$	$-4.98968 + 0.65533I$	$-18.6254 - 0.2318I$

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.335820 + 0.290040I$ $a = -0.158410 + 0.393649I$ $b = -0.140101 + 0.577407I$	$-2.56262 - 5.49819I$	$-13.3788 + 5.1703I$
$u = 1.335820 - 0.290040I$ $a = -0.158410 - 0.393649I$ $b = -0.140101 - 0.577407I$	$-2.56262 + 5.49819I$	$-13.3788 - 5.1703I$
$u = -1.371860 + 0.209407I$ $a = -0.86878 - 1.49091I$ $b = 1.54182 - 0.34669I$	$-6.47245 + 3.72845I$	$-18.3956 - 2.9383I$
$u = -1.371860 - 0.209407I$ $a = -0.86878 + 1.49091I$ $b = 1.54182 + 0.34669I$	$-6.47245 - 3.72845I$	$-18.3956 + 2.9383I$
$u = -1.41274 + 0.33785I$ $a = -0.17556 + 2.27560I$ $b = -2.15361 + 0.28774I$	$19.0447 + 9.4000I$	$-17.5612 - 4.3303I$
$u = -1.41274 - 0.33785I$ $a = -0.17556 - 2.27560I$ $b = -2.15361 - 0.28774I$	$19.0447 - 9.4000I$	$-17.5612 + 4.3303I$
$u = 0.188195 + 0.497650I$ $a = 0.89217 + 2.08322I$ $b = 1.230350 + 0.275114I$	$-1.49234 - 1.05642I$	$-12.43000 + 2.14230I$
$u = 0.188195 - 0.497650I$ $a = 0.89217 - 2.08322I$ $b = 1.230350 - 0.275114I$	$-1.49234 + 1.05642I$	$-12.43000 - 2.14230I$
$u = -1.49219$ $a = 0.836574$ $b = -2.31363$	14.2449	-19.8440
$u = -0.306795$ $a = 1.05438$ $b = 0.184912$	-0.567629	-17.5890

II.

$$I_2^u = \langle b-1, u^6 - 3u^4 - u^3 + 2u^2 + a + 2u + 1, u^8 - u^7 - 3u^6 + 2u^5 + 3u^4 - 2u - 1 \rangle$$

(i) Arc colorings

$$a_7 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} u \\ -u^3 + u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -u^6 + 3u^4 + u^3 - 2u^2 - 2u - 1 \\ 1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -u^3 + 2u \\ -u^3 + u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -u^6 + 3u^4 + 2u^3 - 2u^2 - 4u - 1 \\ u^3 - u + 1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} u^3 - 2u \\ u^3 - u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -u^6 + 3u^4 + u^3 - 2u^2 - 2u - 1 \\ 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -u^2 + 1 \\ u^4 - 2u^2 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -u^5 + 2u^3 - u \\ u^7 - 3u^5 + 2u^3 + u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -u^5 + 2u^3 - u \\ u^7 - 3u^5 + 2u^3 + u \end{pmatrix}$$

(ii) Obstruction class = 1

$$\text{(iii) Cusp Shapes} = -u^7 - 2u^6 + 2u^5 + 8u^4 + 3u^3 - 7u^2 - 8u - 19$$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1, c_2	$(u - 1)^8$
c_3, c_8	u^8
c_4	$(u + 1)^8$
c_5, c_7	$u^8 - 3u^7 + 7u^6 - 10u^5 + 11u^4 - 10u^3 + 6u^2 - 4u + 1$
c_6	$u^8 + u^7 - 3u^6 - 2u^5 + 3u^4 + 2u - 1$
c_9, c_{12}	$u^8 + u^7 - u^6 - 2u^5 + u^4 + 2u^3 - 2u - 1$
c_{10}, c_{11}	$u^8 - u^7 - 3u^6 + 2u^5 + 3u^4 - 2u - 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1, c_2, c_4	$(y - 1)^8$
c_3, c_8	y^8
c_5, c_7	$y^8 + 5y^7 + 11y^6 + 6y^5 - 17y^4 - 34y^3 - 22y^2 - 4y + 1$
c_6, c_{10}, c_{11}	$y^8 - 7y^7 + 19y^6 - 22y^5 + 3y^4 + 14y^3 - 6y^2 - 4y + 1$
c_9, c_{12}	$y^8 - 3y^7 + 7y^6 - 10y^5 + 11y^4 - 10y^3 + 6y^2 - 4y + 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to I_2^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.180120 + 0.268597I$ $a = 0.646194 - 0.127698I$ $b = 1.00000$	$-2.68559 + 1.13123I$	$-15.9046 - 0.8051I$
$u = -1.180120 - 0.268597I$ $a = 0.646194 + 0.127698I$ $b = 1.00000$	$-2.68559 - 1.13123I$	$-15.9046 + 0.8051I$
$u = -0.108090 + 0.747508I$ $a = 1.43073 - 0.89199I$ $b = 1.00000$	$0.51448 + 2.57849I$	$-11.78039 - 3.88175I$
$u = -0.108090 - 0.747508I$ $a = 1.43073 + 0.89199I$ $b = 1.00000$	$0.51448 - 2.57849I$	$-11.78039 + 3.88175I$
$u = 1.37100$ $a = -0.966009$ $b = 1.00000$	-8.14766	-19.8290
$u = 1.334530 + 0.318930I$ $a = 0.142888 + 1.323540I$ $b = 1.00000$	$-4.02461 - 6.44354I$	$-16.5091 + 6.0410I$
$u = 1.334530 - 0.318930I$ $a = 0.142888 - 1.323540I$ $b = 1.00000$	$-4.02461 + 6.44354I$	$-16.5091 - 6.0410I$
$u = -0.463640$ $a = -0.473616$ $b = 1.00000$	-2.48997	-16.7830

III. u-Polynomials

Crossings	u-Polynomials at each crossing
c_1	$((u-1)^8)(u^{20} + 39u^{19} + \dots + 18u + 1)$
c_2	$((u-1)^8)(u^{20} - 9u^{19} + \dots + 9u^2 - 1)$
c_3, c_8	$u^8(u^{20} + u^{19} + \dots - 640u - 256)$
c_4	$((u+1)^8)(u^{20} - 9u^{19} + \dots + 9u^2 - 1)$
c_5, c_7	$(u^8 - 3u^7 + 7u^6 - 10u^5 + 11u^4 - 10u^3 + 6u^2 - 4u + 1)$ $\cdot (u^{20} - 6u^{19} + \dots + 2u - 5)$
c_6	$(u^8 + u^7 - 3u^6 - 2u^5 + 3u^4 + 2u - 1)(u^{20} + 2u^{19} + \dots + 2u + 1)$
c_9, c_{12}	$(u^8 + u^7 + \dots - 2u - 1)(u^{20} - 2u^{19} + \dots + 2u + 1)$
c_{10}, c_{11}	$(u^8 - u^7 - 3u^6 + 2u^5 + 3u^4 - 2u - 1)(u^{20} + 2u^{19} + \dots + 2u + 1)$

IV. Riley Polynomials

Crossings	Riley Polynomials at each crossing
c_1	$((y - 1)^8)(y^{20} - 155y^{19} + \dots - 690y + 1)$
c_2, c_4	$((y - 1)^8)(y^{20} - 39y^{19} + \dots - 18y + 1)$
c_3, c_8	$y^8(y^{20} - 51y^{19} + \dots + 16384y + 65536)$
c_5, c_7	$(y^8 + 5y^7 + 11y^6 + 6y^5 - 17y^4 - 34y^3 - 22y^2 - 4y + 1)$ $\cdot (y^{20} + 6y^{19} + \dots - 194y + 25)$
c_6, c_{10}, c_{11}	$(y^8 - 7y^7 + 19y^6 - 22y^5 + 3y^4 + 14y^3 - 6y^2 - 4y + 1)$ $\cdot (y^{20} - 18y^{19} + \dots - 6y + 1)$
c_9, c_{12}	$(y^8 - 3y^7 + 7y^6 - 10y^5 + 11y^4 - 10y^3 + 6y^2 - 4y + 1)$ $\cdot (y^{20} - 42y^{19} + \dots - 6y + 1)$