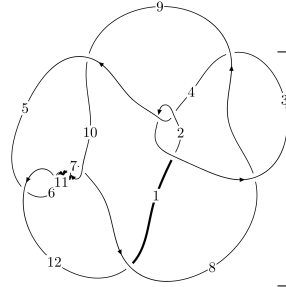
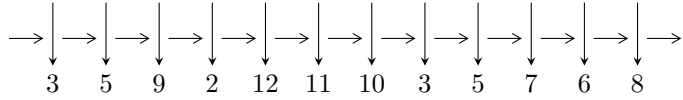


12n<sub>0251</sub> (K12n<sub>0251</sub>)



A knot diagram<sup>1</sup>

**Linearized knot diagram**



**Solving Sequence**

$$6,11 \xrightarrow{c_6} 7 \xrightarrow{c_{11}} 12 \xrightarrow{c_5} 3,5 \xrightarrow{c_2} 2 \xrightarrow{c_1} 1 \xrightarrow{c_4} 4 \xrightarrow{c_{10}} 10 \xrightarrow{c_7} 8 \xrightarrow{c_9} 9 \twoheadrightarrow c_3, c_8, c_{12}$$

**Ideals for irreducible components<sup>2</sup> of  $X_{\text{par}}$**

$$I_1^u = \langle u^{11} + 2u^{10} + 8u^9 + 13u^8 + 22u^7 + 27u^6 + 24u^5 + 19u^4 + 9u^3 + 4u^2 + b - 1, \\ u^{13} + 2u^{12} + 10u^{11} + 16u^{10} + 37u^9 + 46u^8 + 62u^7 + 57u^6 + 46u^5 + 30u^4 + 12u^3 + 7u^2 + a - u, \\ u^{14} + 2u^{13} + 11u^{12} + 18u^{11} + 46u^{10} + 60u^9 + 91u^8 + 90u^7 + 86u^6 + 60u^5 + 34u^4 + 17u^3 + 2u^2 - 1 \rangle \\ I_2^u = \langle b - u + 1, u^4 - u^3 + 4u^2 + a - 2u + 2, u^5 - u^4 + 4u^3 - 3u^2 + 3u - 1 \rangle$$

\* 2 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 19 representations.

<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$I_1^u = \langle u^{11} + 2u^{10} + \dots + b - 1, u^{13} + 2u^{12} + \dots + a - u, u^{14} + 2u^{13} + \dots + 2u^2 - 1 \rangle$$

I.

(i) Arc colorings

$$a_6 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -u \\ u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -u^{13} - 2u^{12} + \dots - 7u^2 + u \\ -u^{11} - 2u^{10} + \dots - 4u^2 + 1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} u^2 + 1 \\ -u^2 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -u^{13} - 3u^{12} + \dots - 9u^2 + 1 \\ u^{12} + 5u^{10} - 2u^9 + 3u^8 - 11u^7 - 14u^6 - 18u^5 - 16u^4 - 8u^3 - 5u^2 + 1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -u^7 - 4u^5 - 4u^3 - 2u \\ -u^9 - 5u^7 - 7u^5 - 2u^3 + u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} u^{13} + 2u^{12} + \dots + u - 1 \\ -u^{11} - 4u^9 + 2u^8 + 9u^6 + 12u^5 + 11u^4 + 6u^3 + 4u^2 + u - 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} u \\ u^3 + u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} u^2 + 1 \\ u^4 + 2u^2 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} u^7 + 4u^5 + 4u^3 + 2u \\ -u^7 - 3u^5 + u \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes

$$= u^{13} + 2u^{12} + 11u^{11} + 18u^{10} + 45u^9 + 56u^8 + 80u^7 + 65u^6 + 50u^5 + 12u^4 - 7u^3 - 11u^2 - 9u - 14$$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1$	$u^{14} + 26u^{13} + \dots + 14u + 1$
$c_2, c_4$	$u^{14} - 6u^{13} + \dots - 2u - 1$
$c_3, c_8$	$u^{14} + u^{13} + \dots + 64u + 32$
$c_5, c_6, c_7$ $c_{10}, c_{11}$	$u^{14} - 2u^{13} + \dots + 2u^2 - 1$
$c_9, c_{12}$	$u^{14} - 2u^{13} + \dots - 2u - 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1$	$y^{14} - 86y^{13} + \dots - 730y + 1$
$c_2, c_4$	$y^{14} - 26y^{13} + \dots - 14y + 1$
$c_3, c_8$	$y^{14} - 33y^{13} + \dots - 1536y + 1024$
$c_5, c_6, c_7$ $c_{10}, c_{11}$	$y^{14} + 18y^{13} + \dots - 4y + 1$
$c_9, c_{12}$	$y^{14} - 30y^{13} + \dots - 4y + 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.550724 + 0.891947I$ $a = -0.096240 + 0.175738I$ $b = -1.07587 - 1.79627I$	$-15.0245 + 4.4031I$	$-12.54526 - 3.39165I$
$u = -0.550724 - 0.891947I$ $a = -0.096240 - 0.175738I$ $b = -1.07587 + 1.79627I$	$-15.0245 - 4.4031I$	$-12.54526 + 3.39165I$
$u = 0.190452 + 0.810025I$ $a = 0.013565 - 0.546935I$ $b = -0.396657 + 0.339392I$	$1.71814 - 1.64819I$	$-5.73834 + 4.69390I$
$u = 0.190452 - 0.810025I$ $a = 0.013565 + 0.546935I$ $b = -0.396657 - 0.339392I$	$1.71814 + 1.64819I$	$-5.73834 - 4.69390I$
$u = -0.772289$ $a = -2.27398$ $b = -0.485231$	$-17.7180$	$-15.7100$
$u = -0.241199 + 0.492313I$ $a = 0.340540 + 1.345040I$ $b = 1.022190 + 0.391429I$	$-1.48613 + 0.97077I$	$-11.76317 - 1.95166I$
$u = -0.241199 - 0.492313I$ $a = 0.340540 - 1.345040I$ $b = 1.022190 - 0.391429I$	$-1.48613 - 0.97077I$	$-11.76317 + 1.95166I$
$u = -0.04571 + 1.57188I$ $a = -1.87359 - 0.58564I$ $b = 2.33538 + 1.40783I$	$5.67567 + 1.86276I$	$-10.57290 - 1.15181I$
$u = -0.04571 - 1.57188I$ $a = -1.87359 + 0.58564I$ $b = 2.33538 - 1.40783I$	$5.67567 - 1.86276I$	$-10.57290 + 1.15181I$
$u = 0.05378 + 1.66919I$ $a = 0.834731 - 0.136645I$ $b = -1.099410 - 0.067263I$	$10.47610 - 2.59125I$	$-5.03885 + 1.58782I$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.05378 - 1.66919I$		
$a = 0.834731 + 0.136645I$	$10.47610 + 2.59125I$	$-5.03885 - 1.58782I$
$b = -1.099410 + 0.067263I$		
$u = -0.16470 + 1.67887I$		
$a = 1.88194 + 1.97217I$	$-6.19448 + 7.22352I$	$-10.76531 - 2.66085I$
$b = -2.16875 - 3.14542I$		
$u = -0.16470 - 1.67887I$		
$a = 1.88194 - 1.97217I$	$-6.19448 - 7.22352I$	$-10.76531 + 2.66085I$
$b = -2.16875 + 3.14542I$		
$u = 0.288492$		
$a = -0.927924$	$-0.575448$	$-17.4430$
$b = 0.251456$		

$$\text{II. } \Gamma_2^u = \langle b - u + 1, u^4 - u^3 + 4u^2 + a - 2u + 2, u^5 - u^4 + 4u^3 - 3u^2 + 3u - 1 \rangle$$

(i) Arc colorings

$$a_6 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -u \\ u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -u^4 + u^3 - 4u^2 + 2u - 2 \\ u - 1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} u^2 + 1 \\ -u^2 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -u^4 + u^3 - 5u^2 + 2u - 3 \\ u^2 + u - 1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -u^2 - 1 \\ u^2 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -u^4 + u^3 - 4u^2 + 2u - 2 \\ u - 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} u \\ u^3 + u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} u^2 + 1 \\ u^4 + 2u^2 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} u^2 + 1 \\ u^4 + 2u^2 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes =  $-3u^4 + 3u^3 - 12u^2 + 10u - 19$

(iv) **u**-Polynomials at the component

Crossings	<b>u</b> -Polynomials at each crossing
$c_1, c_2$	$(u - 1)^5$
$c_3, c_8$	$u^5$
$c_4$	$(u + 1)^5$
$c_5, c_6, c_7$	$u^5 - u^4 + 4u^3 - 3u^2 + 3u - 1$
$c_9, c_{12}$	$u^5 + u^4 - u^2 + u + 1$
$c_{10}, c_{11}$	$u^5 + u^4 + 4u^3 + 3u^2 + 3u + 1$



(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_4$	$(y - 1)^5$
$c_3, c_8$	$y^5$
$c_5, c_6, c_7$ $c_{10}, c_{11}$	$y^5 + 7y^4 + 16y^3 + 13y^2 + 3y - 1$
$c_9, c_{12}$	$y^5 - y^4 + 4y^3 - 3y^2 + 3y - 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.233677 + 0.885557I$ $a = 0.487744 + 0.170166I$ $b = -0.766323 + 0.885557I$	$0.17487 - 2.21397I$	$-10.60206 + 4.05273I$
$u = 0.233677 - 0.885557I$ $a = 0.487744 - 0.170166I$ $b = -0.766323 - 0.885557I$	$0.17487 + 2.21397I$	$-10.60206 - 4.05273I$
$u = 0.416284$ $a = -1.81849$ $b = -0.583716$	$-2.52712$	$-16.7900$
$u = 0.05818 + 1.69128I$ $a = 0.92150 - 1.10071I$ $b = -0.94182 + 1.69128I$	$9.31336 - 3.33174I$	$-10.00277 + 3.46299I$
$u = 0.05818 - 1.69128I$ $a = 0.92150 + 1.10071I$ $b = -0.94182 - 1.69128I$	$9.31336 + 3.33174I$	$-10.00277 - 3.46299I$

### III. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1$	$((u - 1)^5)(u^{14} + 26u^{13} + \dots + 14u + 1)$
$c_2$	$((u - 1)^5)(u^{14} - 6u^{13} + \dots - 2u - 1)$
$c_3, c_8$	$u^5(u^{14} + u^{13} + \dots + 64u + 32)$
$c_4$	$((u + 1)^5)(u^{14} - 6u^{13} + \dots - 2u - 1)$
$c_5, c_6, c_7$	$(u^5 - u^4 + 4u^3 - 3u^2 + 3u - 1)(u^{14} - 2u^{13} + \dots + 2u^2 - 1)$
$c_9, c_{12}$	$(u^5 + u^4 - u^2 + u + 1)(u^{14} - 2u^{13} + \dots - 2u - 1)$
$c_{10}, c_{11}$	$(u^5 + u^4 + 4u^3 + 3u^2 + 3u + 1)(u^{14} - 2u^{13} + \dots + 2u^2 - 1)$

#### IV. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1$	$((y - 1)^5)(y^{14} - 86y^{13} + \dots - 730y + 1)$
$c_2, c_4$	$((y - 1)^5)(y^{14} - 26y^{13} + \dots - 14y + 1)$
$c_3, c_8$	$y^5(y^{14} - 33y^{13} + \dots - 1536y + 1024)$
$c_5, c_6, c_7$ $c_{10}, c_{11}$	$(y^5 + 7y^4 + 16y^3 + 13y^2 + 3y - 1)(y^{14} + 18y^{13} + \dots - 4y + 1)$
$c_9, c_{12}$	$(y^5 - y^4 + 4y^3 - 3y^2 + 3y - 1)(y^{14} - 30y^{13} + \dots - 4y + 1)$